

# Quantum Information and Quantum Materials

Alexander (Lex) Kemper

 Department of Physics  
North Carolina State University  
<https://go.ncsu.edu/kemper-lab>

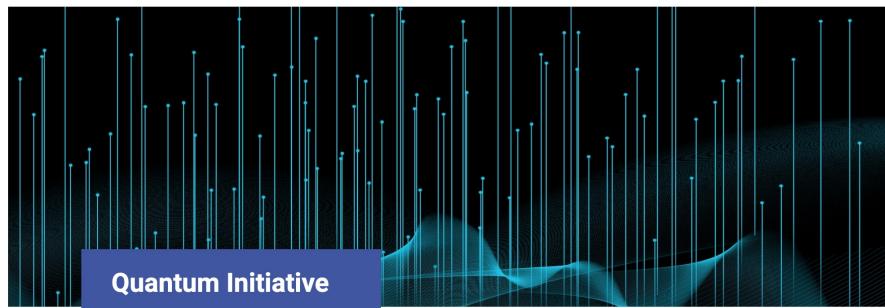
SEQC  
10/30/2024



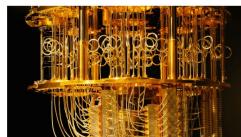


## Quantum Initiative

Quantum Initiative   Quantum Computing   Quantum Materials   Quantum Networking   Events   Get Connected   News



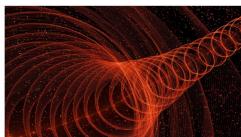
### Quantum Initiative



#### Quantum Computing

Quantum computers are incredibly powerful machines that take a new approach to processing information using the principles of quantum mechanics.

[Read more →](#)



#### Quantum Materials

NC State faculty is working to expand our knowledge of how materials behave and can be manipulated at the micro level for useful application in the field of quantum.

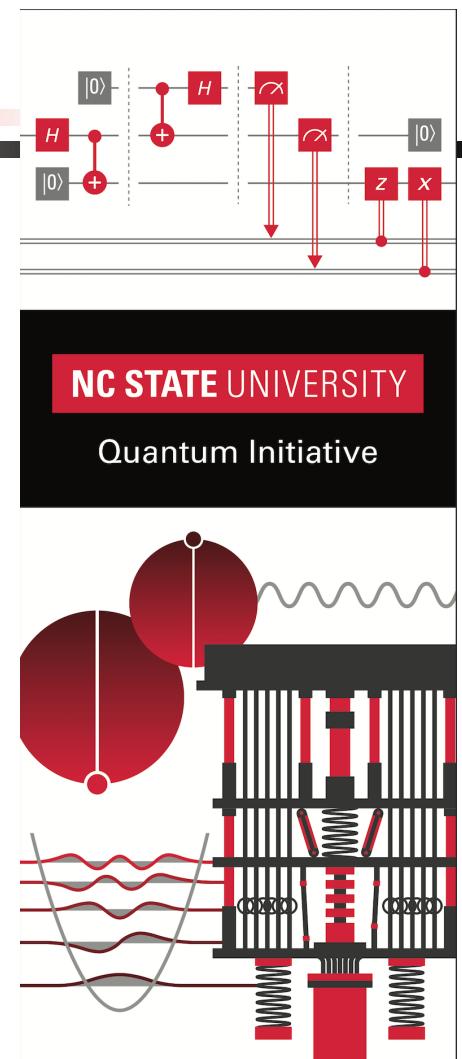
[Read more →](#)



#### Quantum Networking

As quantum computing technology moves past infancy and into application, NC State is working on the ways this delicate information can be securely exchanged between quantum platforms.

[Read more →](#)



NC STATE UNIVERSITY  
Quantum Initiative

<https://quantum.ncsu.edu/>

## **Quantum Computing**

Algorithms  
Error mitigation/correction  
System software  
Applications

## **Quantum Networking**

Single-photon emitters/detectors  
Distributed entanglement  
Networking protocols  
Distributed quantum computing

## **Education**

Courses – within and across disciplines  
Certificates, Degree programs  
Seminars, Workshops, Conferences  
Student engagement, clubs

## **Quantum Materials**

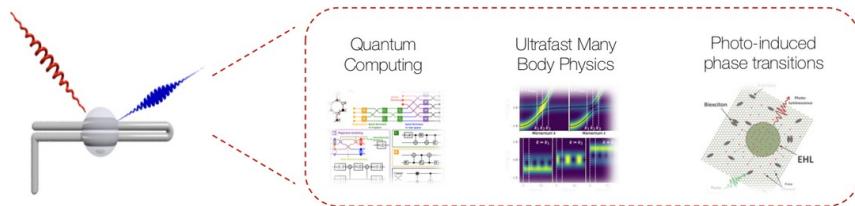
Perovskites  
Organic LEDs  
Quantum dots  
Novel superconductors

## **Industry Engagement**

IBM QIC  
SBIR/STTR  
Short courses, invited speakers  
QED-C

# **NC Quantum Institute**

<https://quantum.ncsu.edu/>



## Kemper Lab

*Quantum materials in and out of equilibrium.*

### Collaborations with:

- Bojko Bakalov (NCSU Math)
- Marco Cerezo, Martin de la Rocca (LANL)
- Jim Freericks (Georgetown)
- Daan Camps, Roel van Beeumen, Bert de Jong, Akhil Francis (LBNL)
- Thomas Steckmann (UMD)
- Yan Wang, Eugene Dumitrescu (ORNL)
- Emanuel Gull (U. Michigan)
- Itay Hen (U. Southern California)

### Current members



Alexander (Lex)  
Kemper  
Principal investigator



Anjali Agrawal  
Graduate Researcher



Heba Labib  
Graduate Researcher



Norman Hogan  
Graduate Researcher



Ethan Blair  
Undergraduate  
Researcher



Arvin Kushwaha  
Undergraduate  
Researcher



Omar Alsheikh  
Graduate Researcher

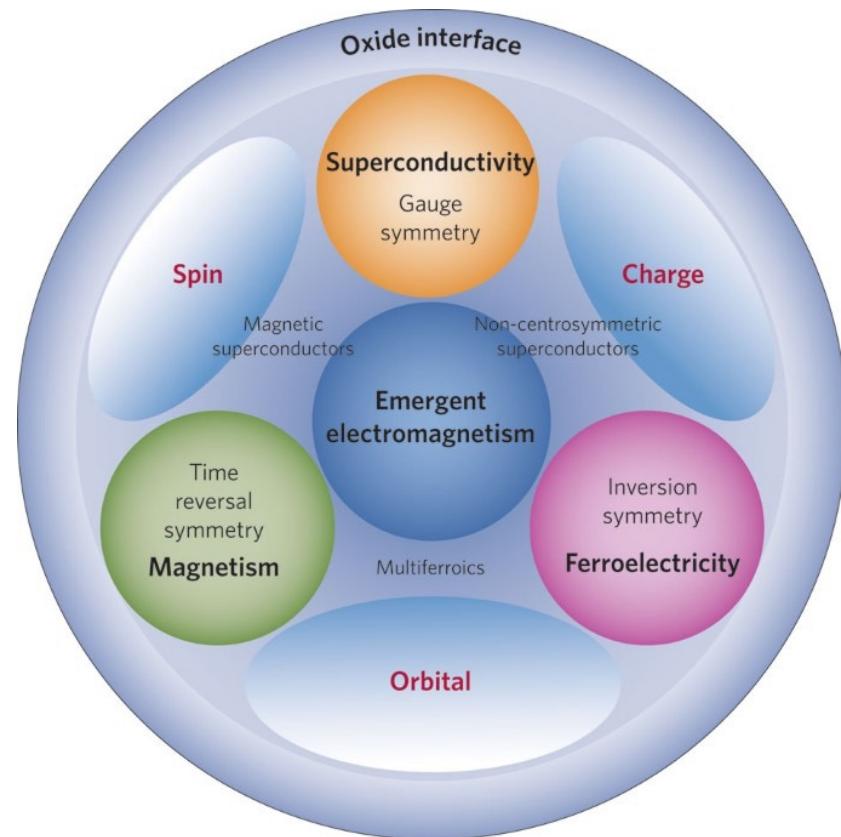


Goksu Toga  
Postdoctoral Researcher



Your Name  
New lab member

# Quantum Information and Quantum Materials

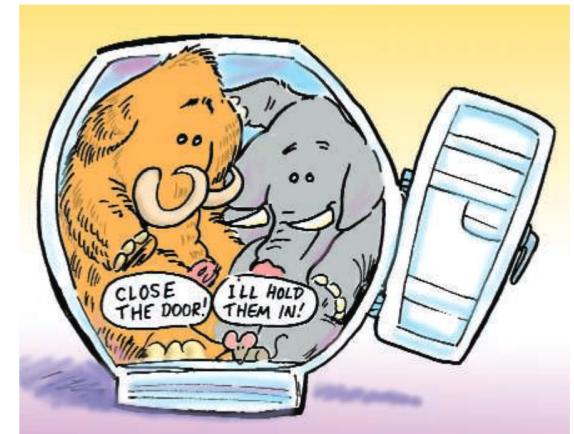


## PHYSICS

# Is There Glue in Cuprate Superconductors?

Philip W. Anderson

Many theories about electron pairing in cuprate superconductors may be on the wrong track.



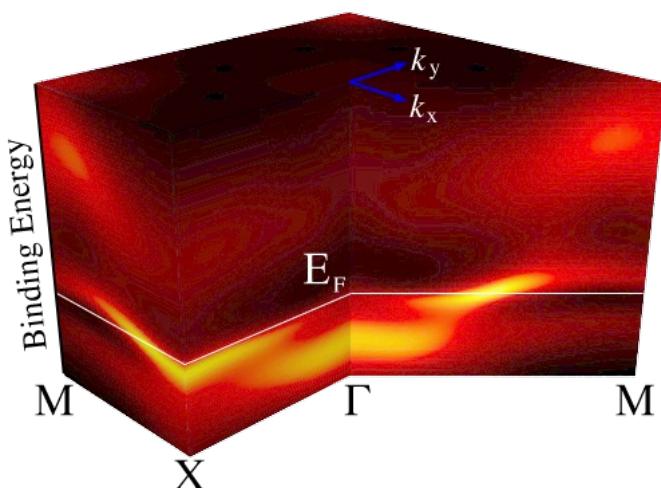
"We have a mammoth and an elephant in our refrigerator—do we care much if there is also a mouse?"

Q: What do you do with a quantum state once you've prepared one?

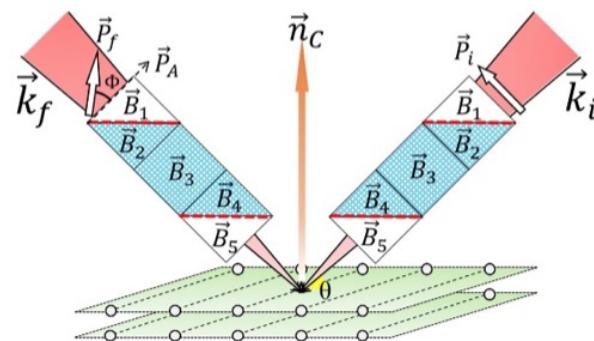
**A: You measure its excitations.**

# Measuring Excitations

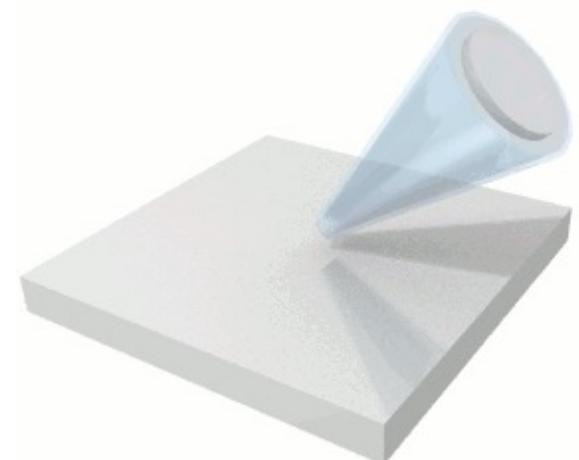
Figures courtesy of  
Devereaux/Shen group  
and ORNL



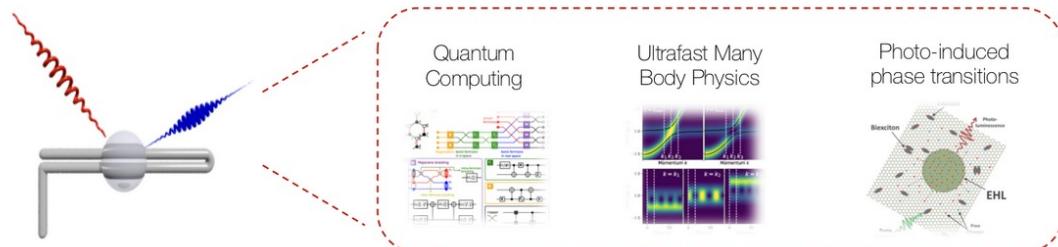
Angle-resolved Photoemission  
(ARPES)



Neutron Scattering



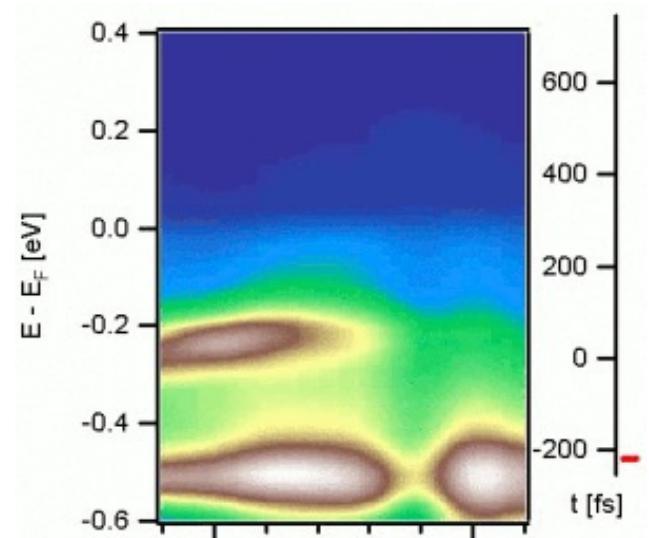
Time-resolved ARPES



## Kemper Lab

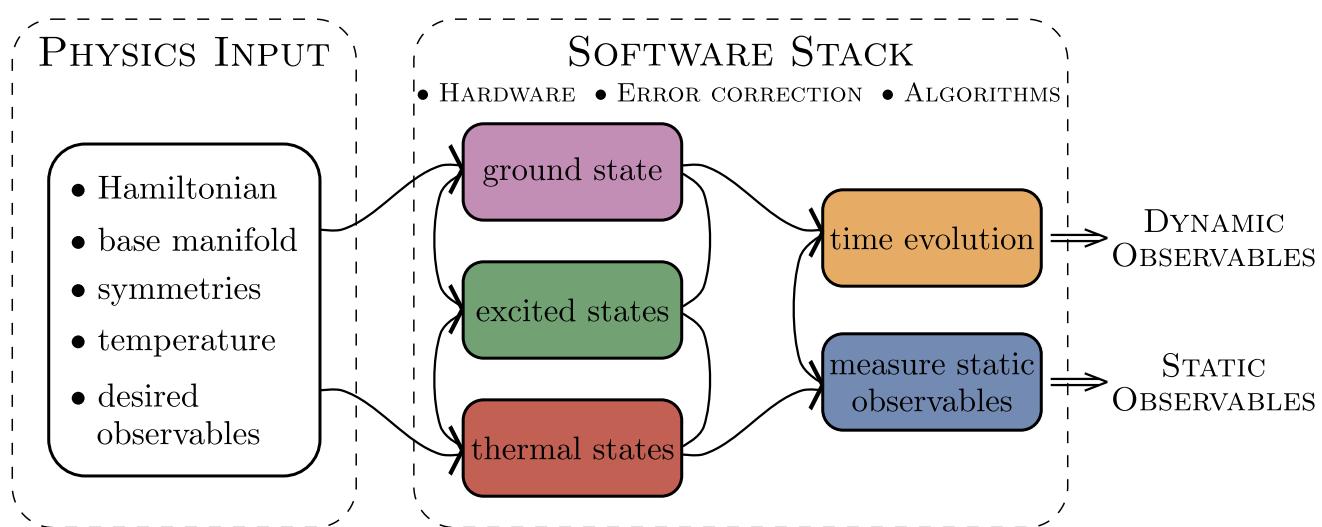
*Quantum materials in and out of equilibrium.*

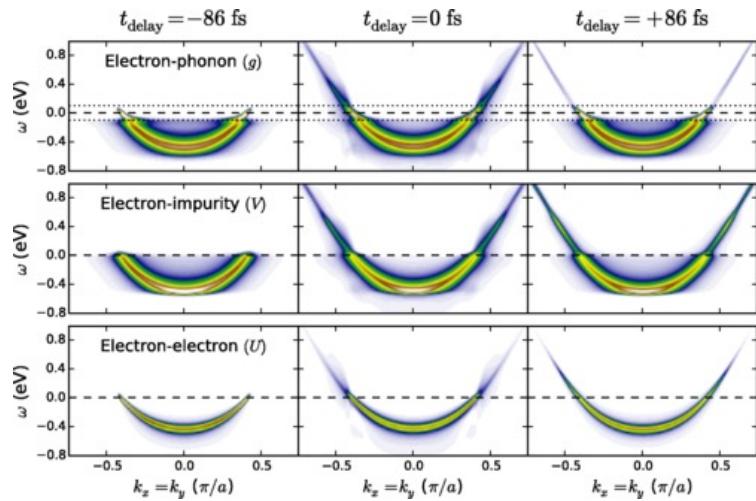
### Time-resolved experiments



Shen group (Stanford)

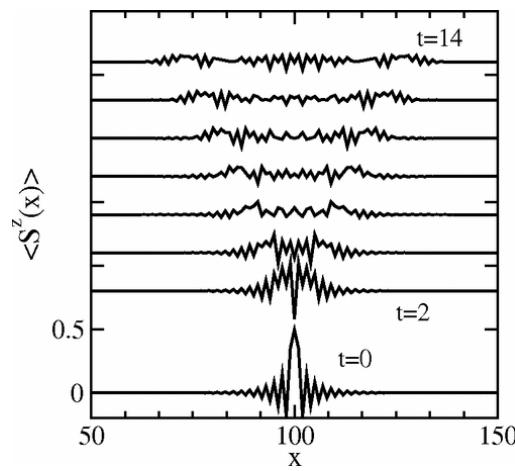
# A-Z quantum simulation





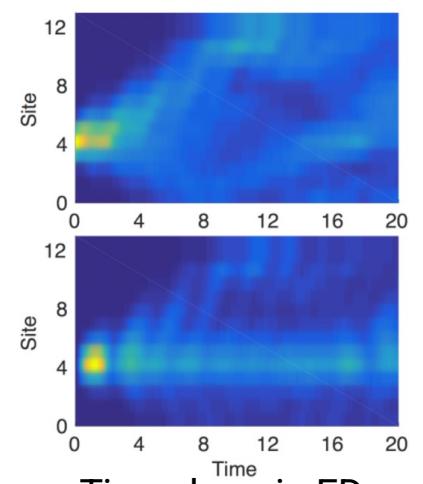
Non-Equilibrium Green's functions

*Phys. Rev. X 8, 041009 (2018)*



Time domain DMRG

*Phys. Rev. Lett. 93, 076401 (2004)*

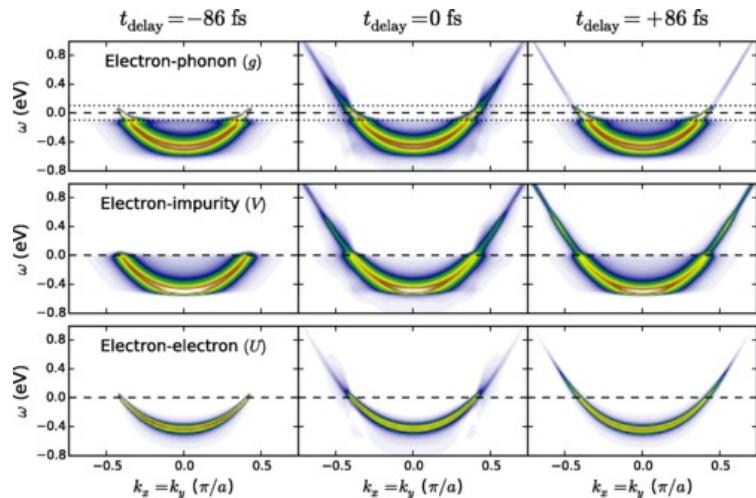


Time domain ED

Johnston & Kemper, unpublished

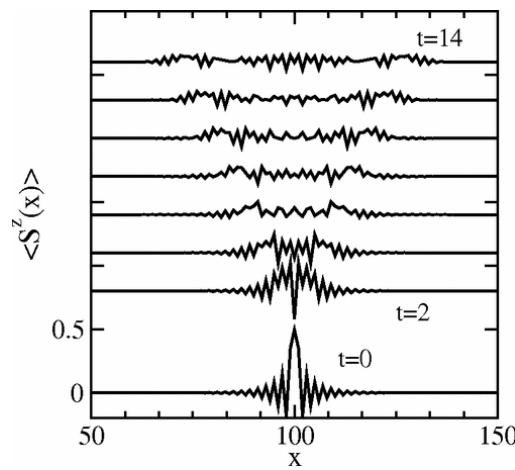


All these techniques eventually reach a barrier.

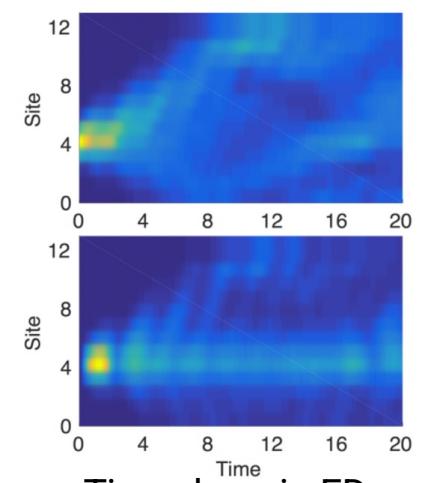


Non-Equilibrium Green's functions

*Phys. Rev. X 8, 041009 (2018)*

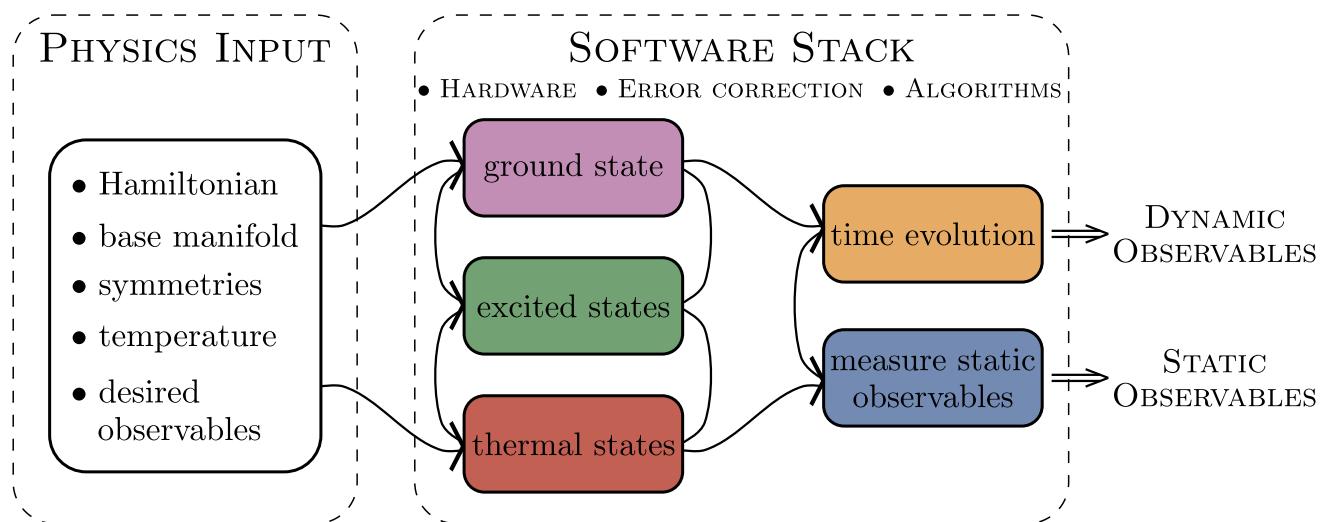


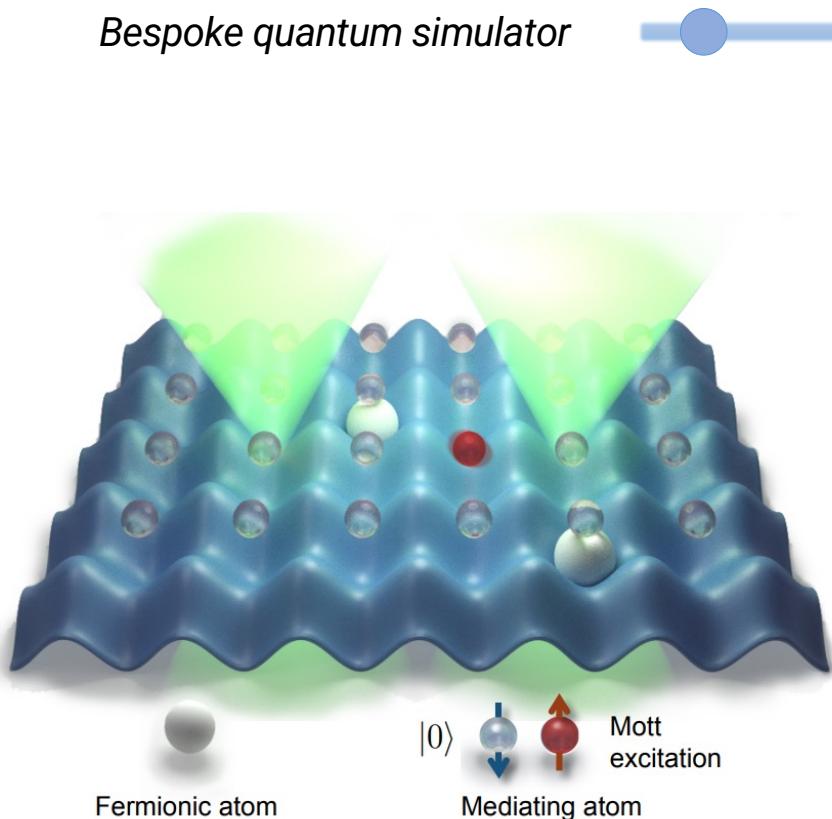
*Phys. Rev. Lett. 93, 076401 (2004)*



Johnston & Kemper, unpublished

# A-Z quantum simulation





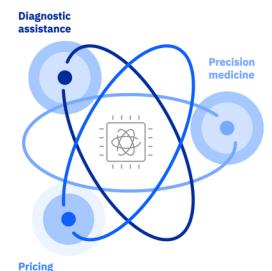
Bespoke quantum simulator

Digital algorithms

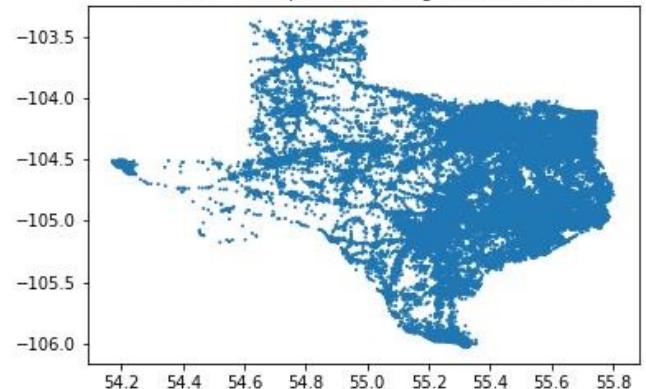


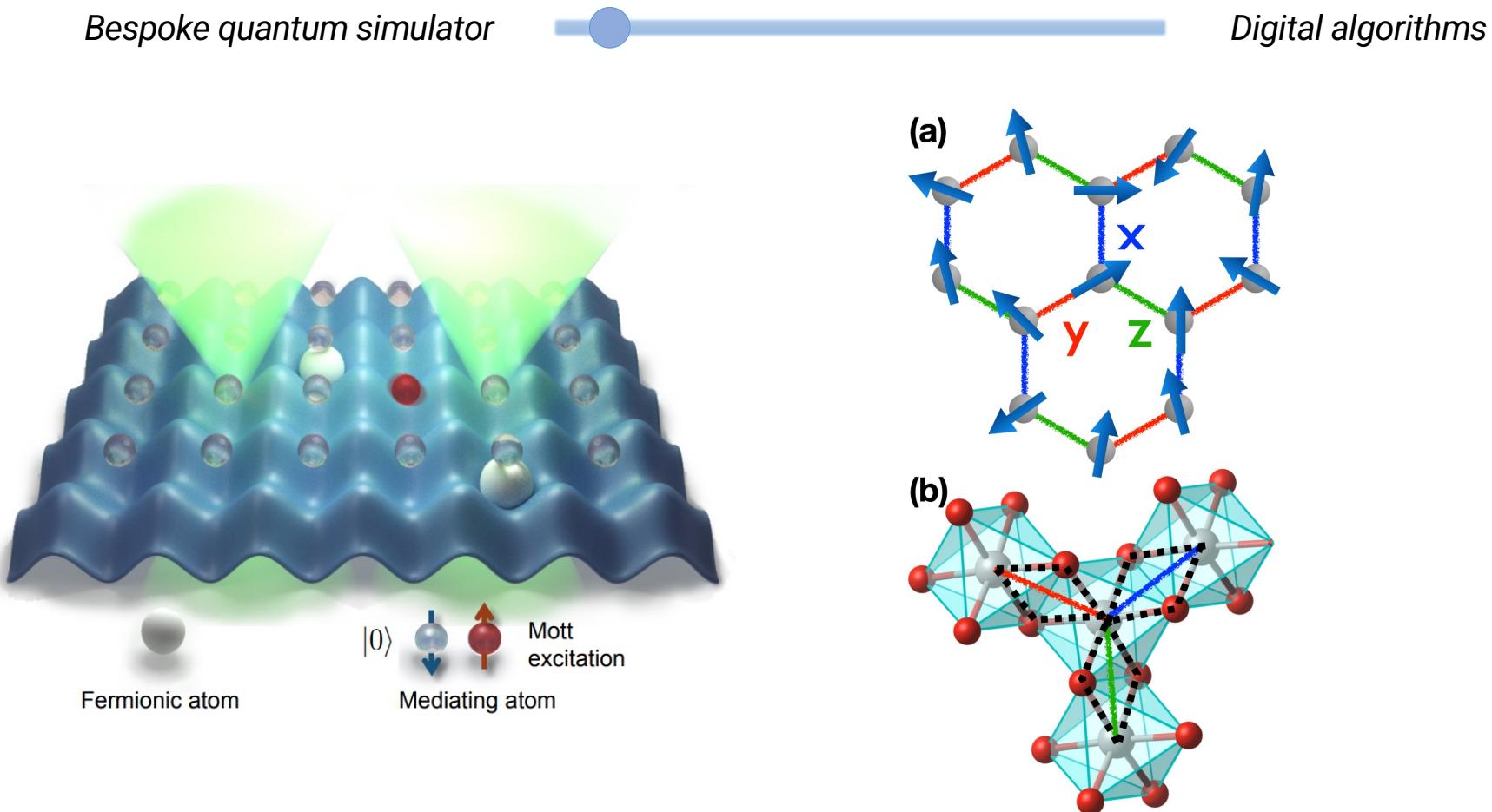
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**Figure 1**  
Quantum computers may enable three key healthcare use cases that reinforce each other in a virtuous cycle. For instance, accurate diagnoses enable precise treatments, as well as a better reflection of patient risks in pricing models.

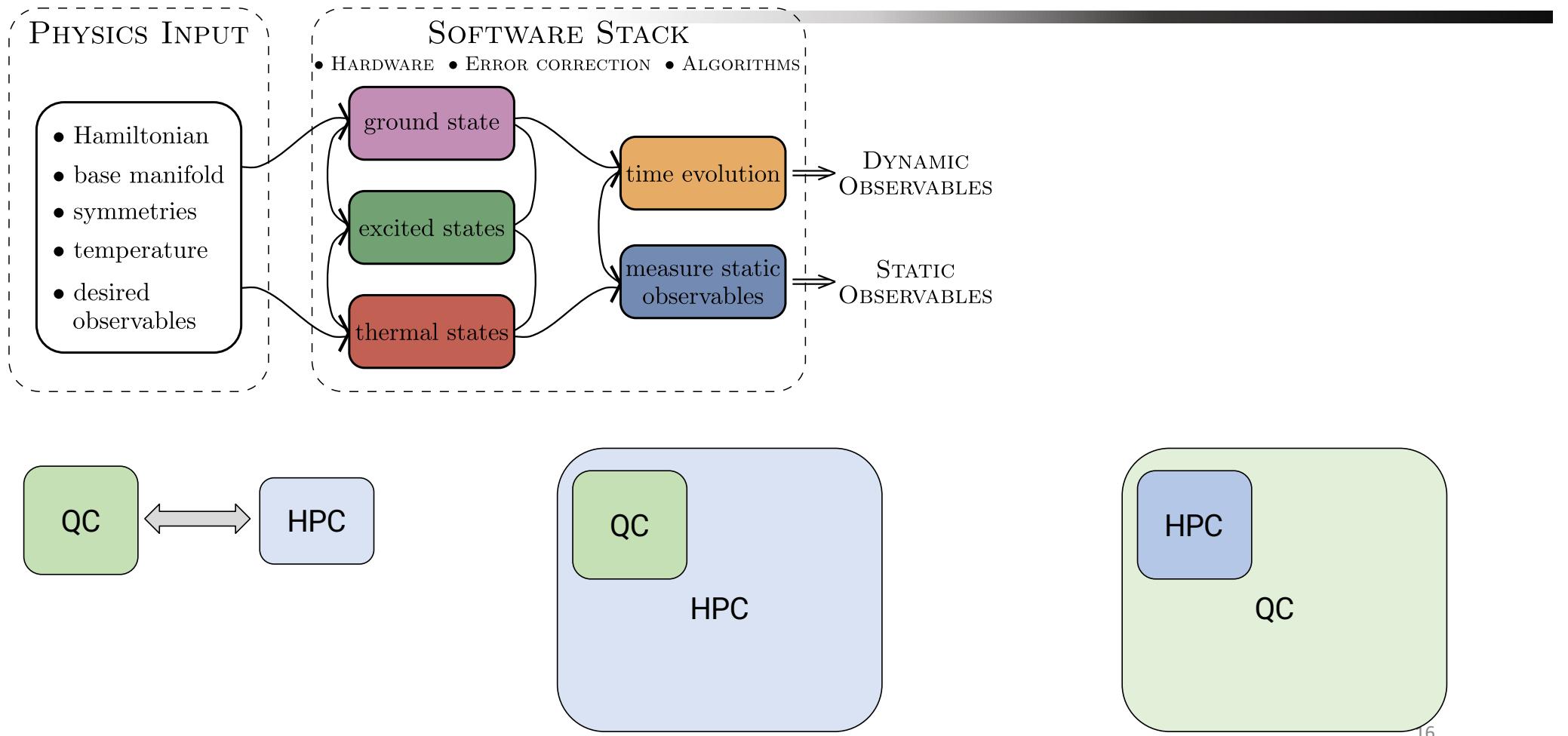


(Centers of) Required Coverage Areas in Texas

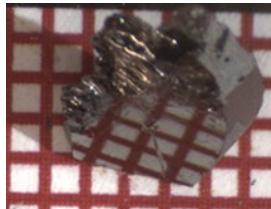




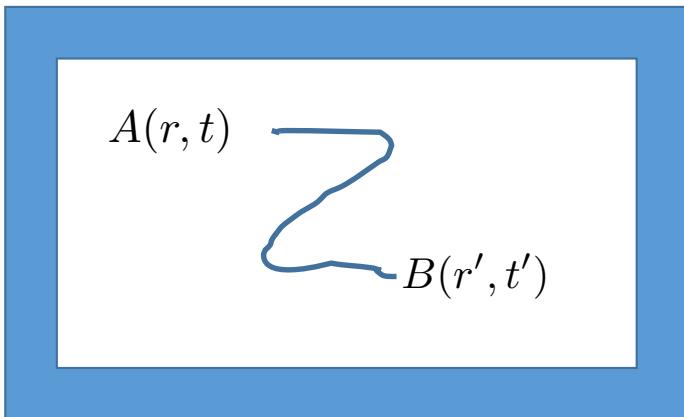
# A-Z quantum simulation



# Correlation functions



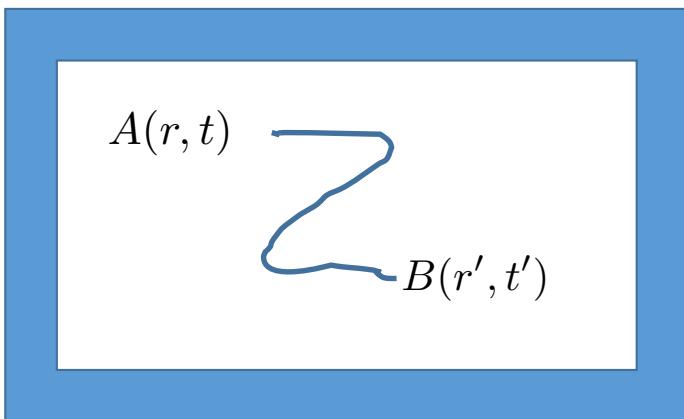
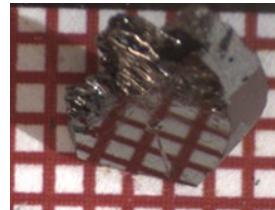
$$\langle A(r, t)B(r', t') \rangle$$



*Given some (observable) operator  $B$  at  $(r', t')$ , what is the likelihood of some (observable) operator  $A$  at  $(r, t)$ ?*

*Optical conductivity,  $\gamma$ /X-ray scattering, photoemission, neutron scattering, Raman, IR absorption, etc.*

# Correlation functions



$e^{iE_0 t} \langle \phi_0 | B e^{-i\mathcal{H}t} A | \phi_0 \rangle$

Interfere with ground state

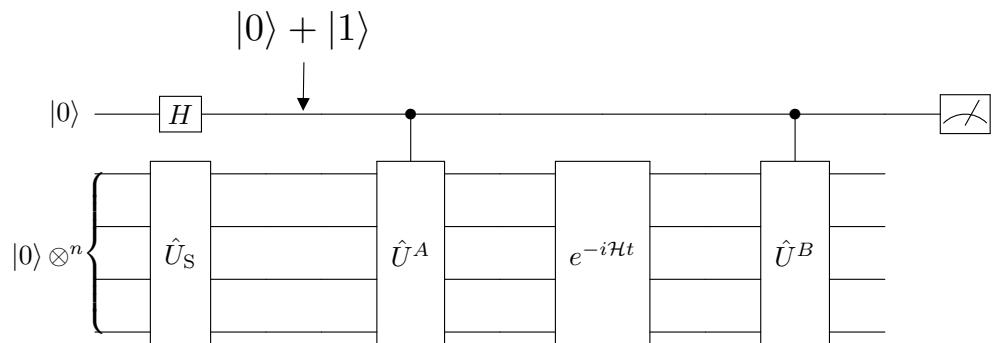
Complete expectation value

Time evolve

Apply excitation B

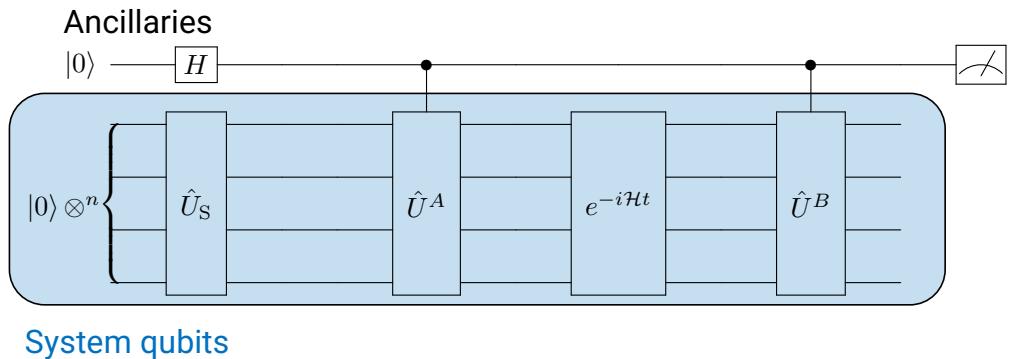
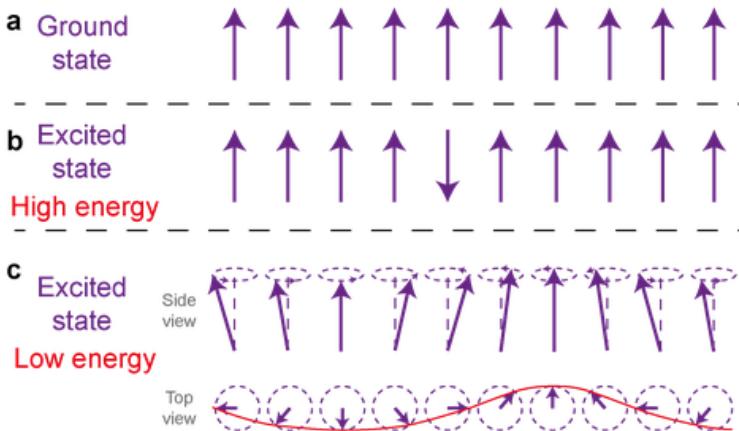
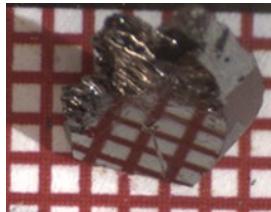
Apply excitation A

Prepare state of interest

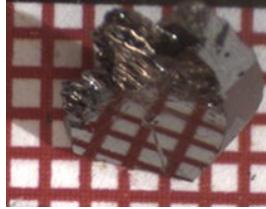


Somma, Simulating physical phenomena by quantum networks (2002)

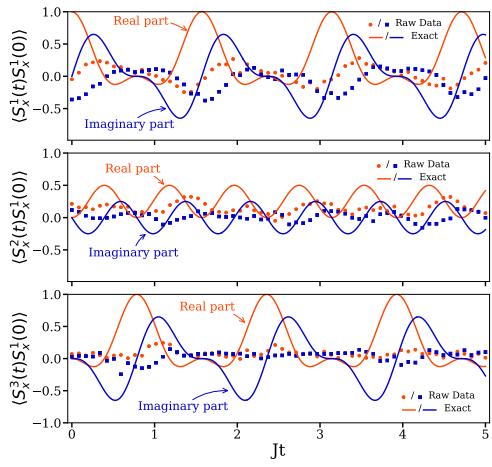
# Correlation functions



# Correlation functions

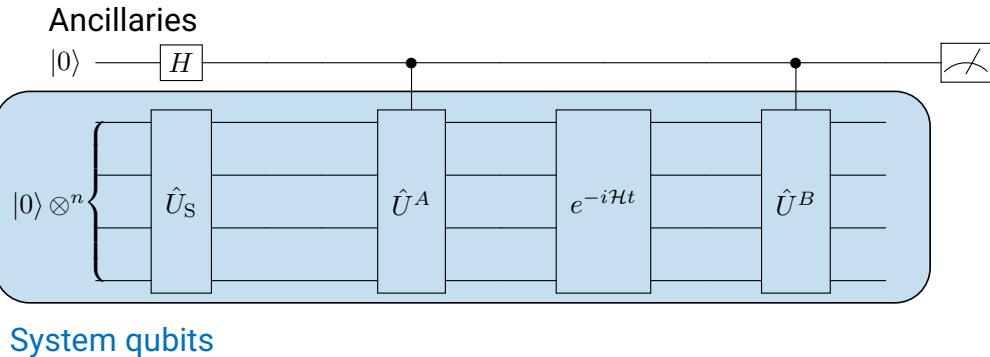


Raw data (2019)

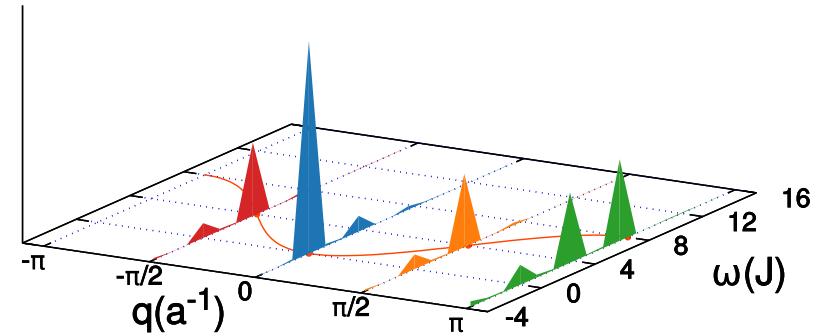


$$\langle A(r, t)B(r', t') \rangle$$

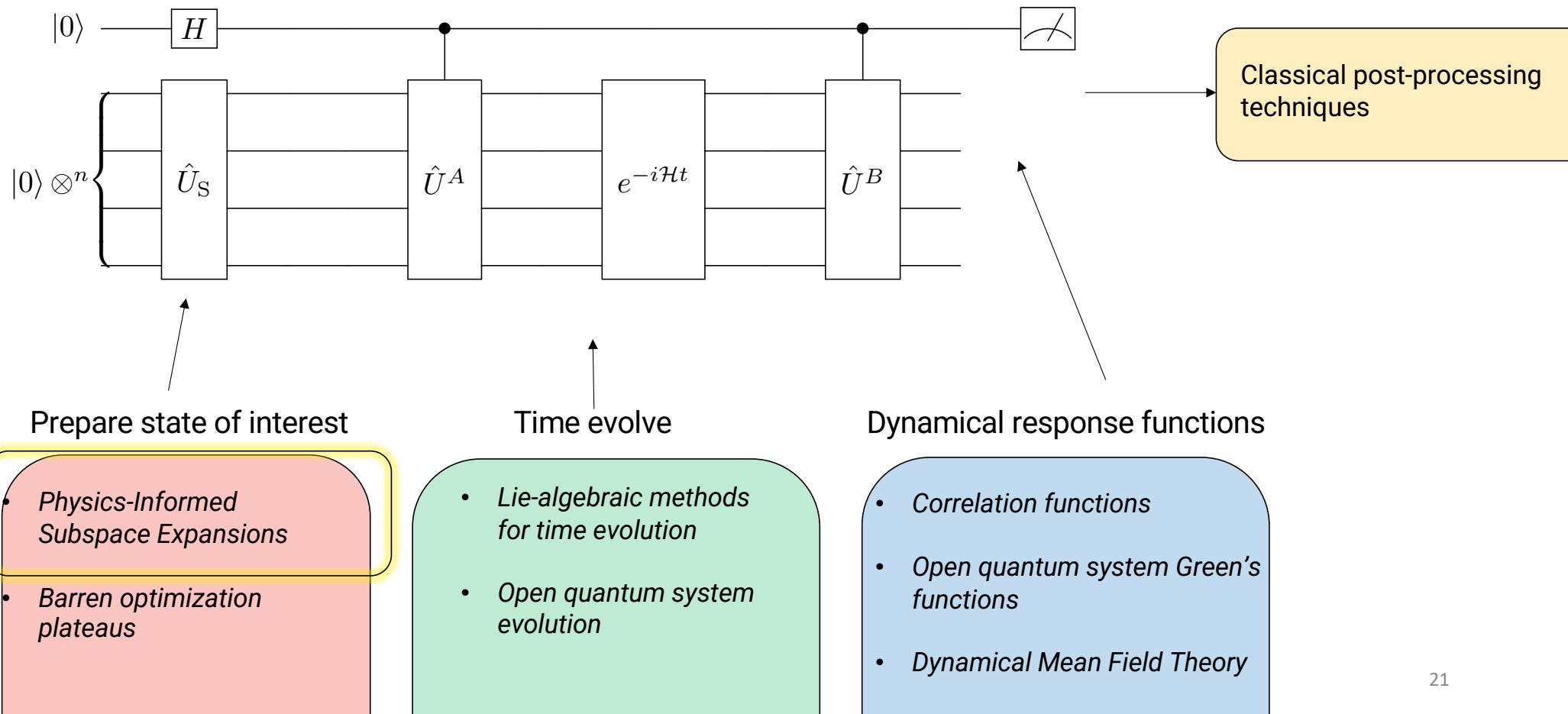
Error mitigation



$|S(q, \omega)|^2$ : PaS



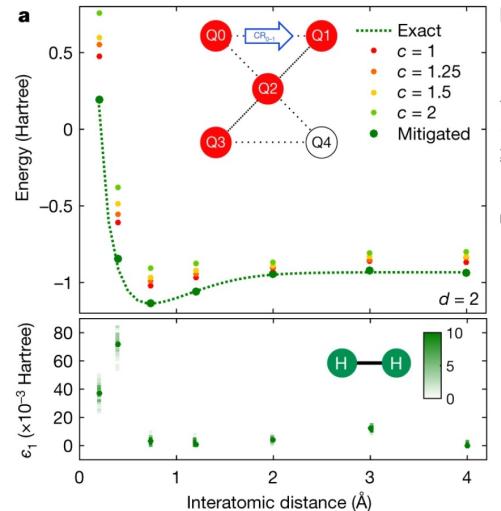
# A-Z quantum simulation



# A-Z quantum simulation

$|0\rangle$

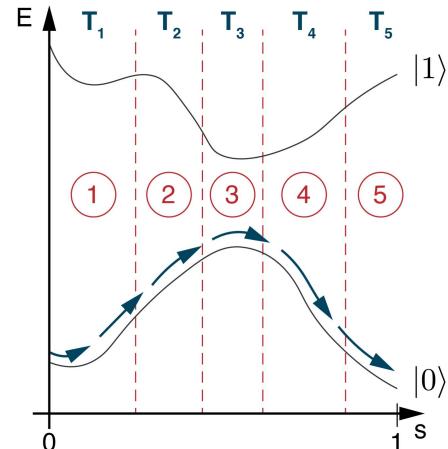
## Variational Quantum Eigensolver



[ Kandala, Abhinav, et.al., *Nature* 549, no. 7671 (2017): 242-246. ]

## Barren Plateau

## Adiabatic State Preparation

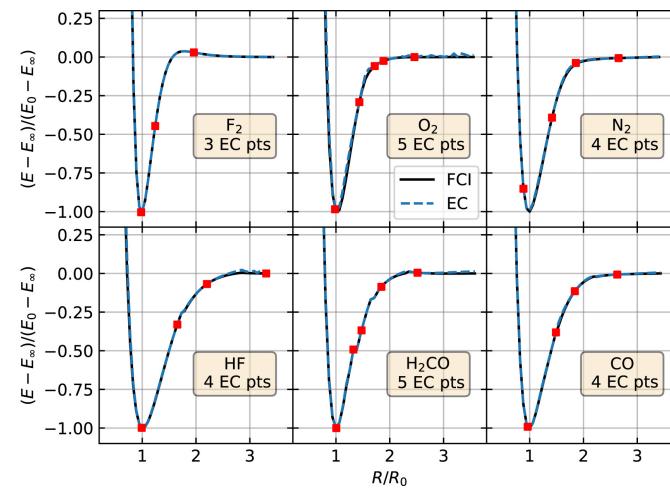
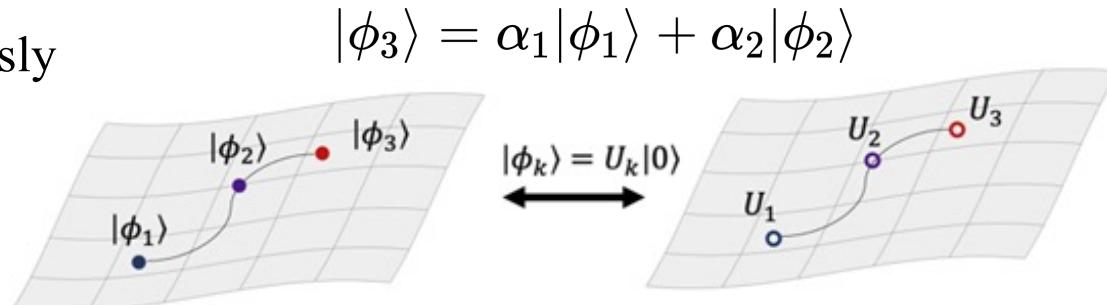
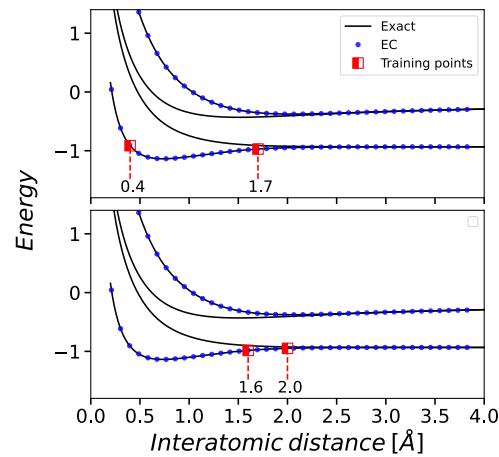


[ Schiffer, Benjamin F., et.al., *PRX Quantum* 3, no. 2 (2022): 020347 ]

## Larger depth circuits

## A-Z quantum simulation

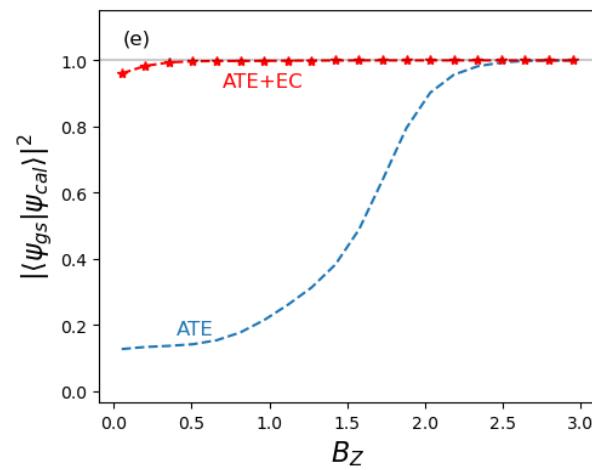
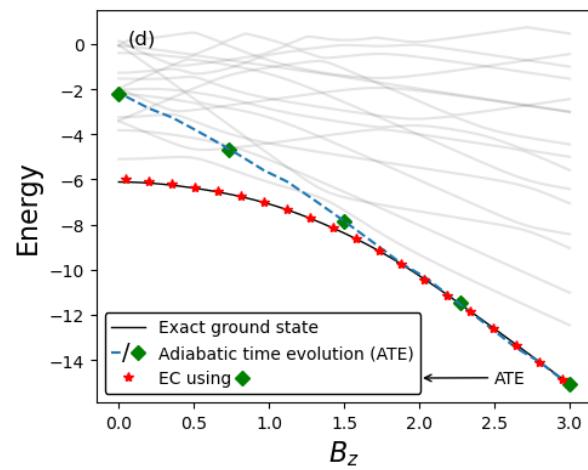
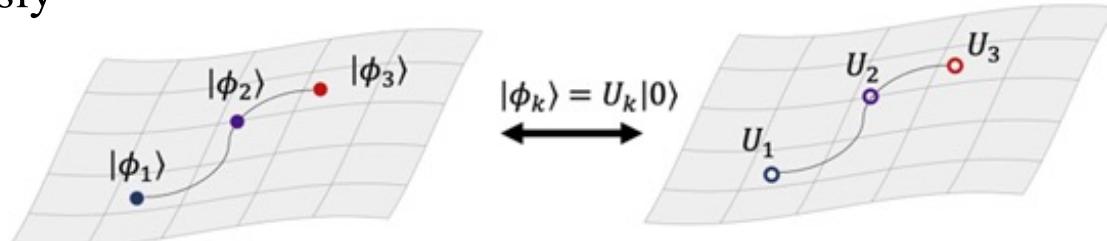
- Ground state varies continuously in a parameter space and is spanned by a few low energy state vectors.



# A-Z quantum simulation

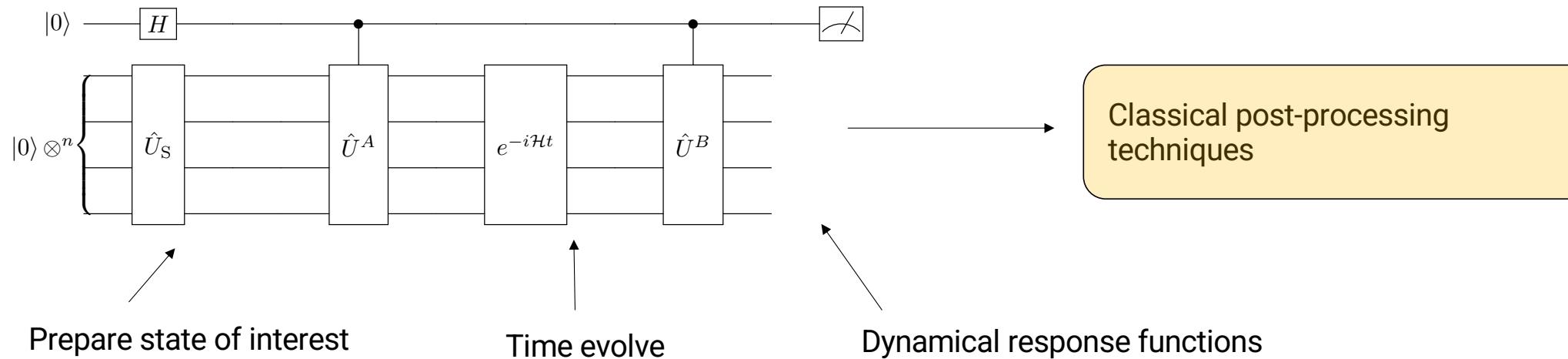
- Ground state varies continuously in a parameter space and is spanned by a few low energy state vectors.

$$|\phi_3\rangle = \alpha_1|\phi_1\rangle + \alpha_2|\phi_2\rangle$$



Agrawal, arXiv:2406.17037

# A-Z quantum simulation



- Physics-Informed Subspace Expansions
- Barren optimization plateaus

- Lie-algebraic methods for time evolution
- Open quantum system evolution

- Correlation functions
- Open quantum system Green's functions
- Dynamical Mean Field Theory

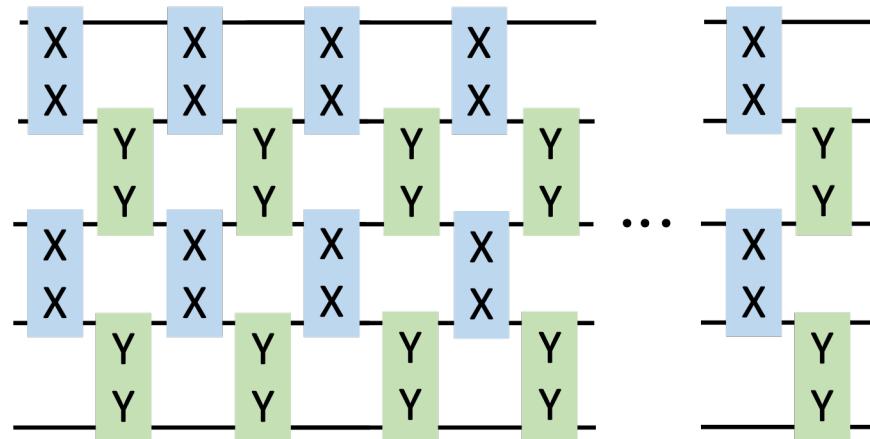
# A-Z quantum simulation

$|0\rangle$

**Exact simulation of a time independent spin Hamiltonian:**

$$\mathcal{H} = \sum_j h_j \sigma^j$$

$U(t) =$



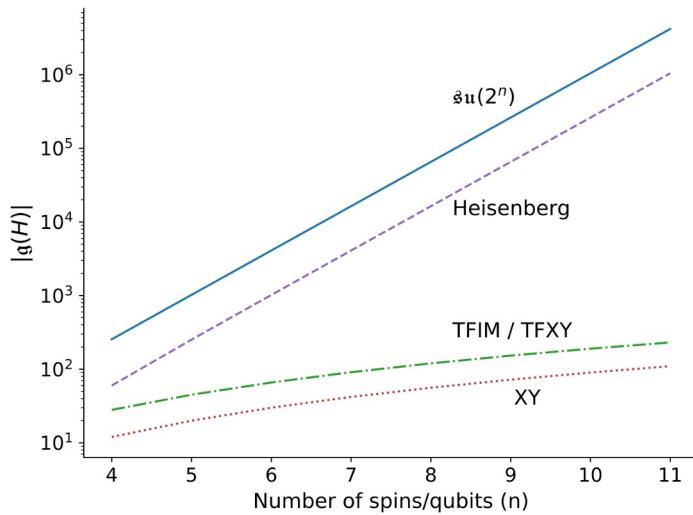
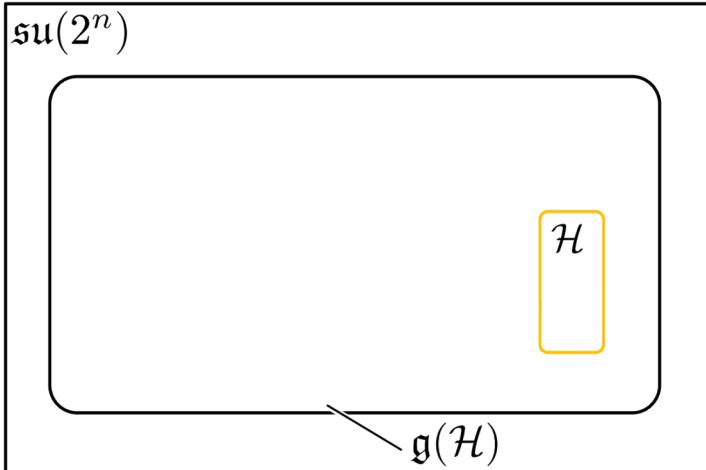
## A-Z quantum simulation

 $|0\rangle$  $|0\rangle$ **Exact simulation of a time independent spin Hamiltonian:**

$$\mathcal{H} = \sum_j h_j \sigma^j$$

$$U(t) = e^{-it\mathcal{H}} = \prod_{\substack{\bar{\sigma}^i \in \mathfrak{su}(2^n) \\ \bar{\sigma}^i \in \mathfrak{g}(\mathcal{H})}} e^{i\kappa_i \bar{\sigma}^i}$$

$$\text{DLA} := \text{span}\{[a_{i_1}, [a_{i_2}, [\cdots [a_{i_r}, a_j] \cdots]]]\}$$



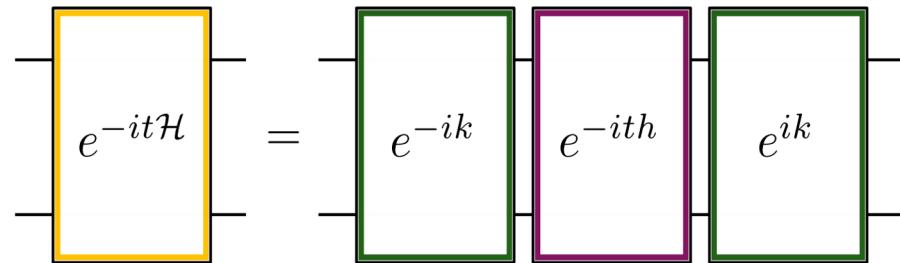
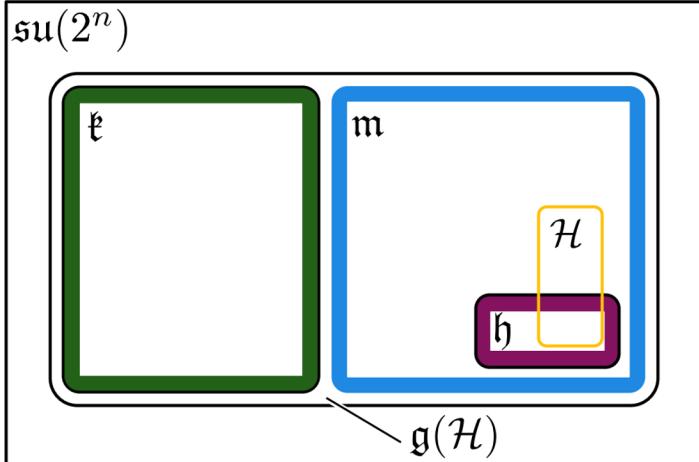
## A-Z quantum simulation

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$$\text{DLA} := \text{span}\{[a_{i_1}, [a_{i_2}, [\cdots [a_{i_r}, a_j] \cdots]]]\}$$

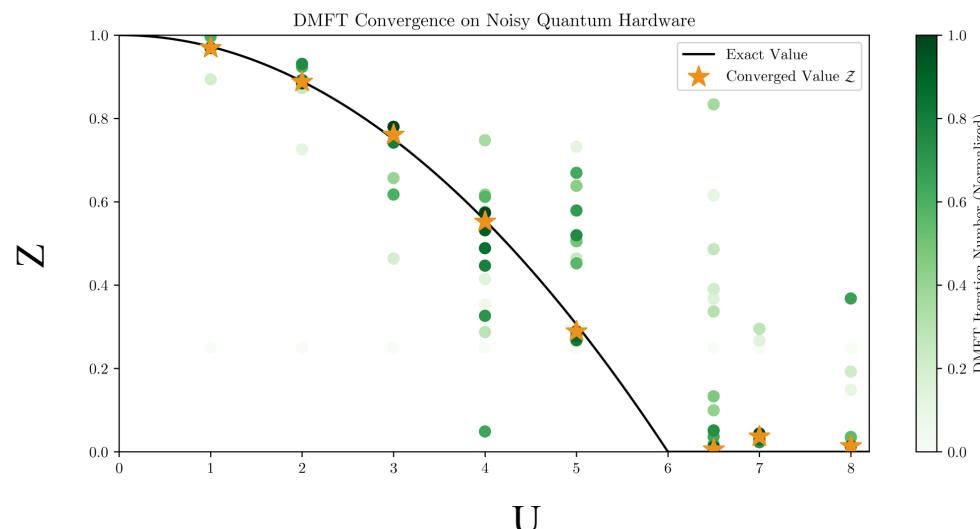
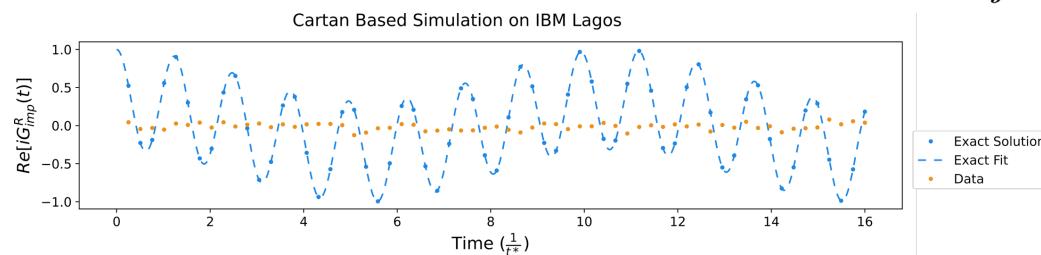


E. Kökcü et al., Phys. Rev. Lett. (2022)

# A-Z quantum simulation

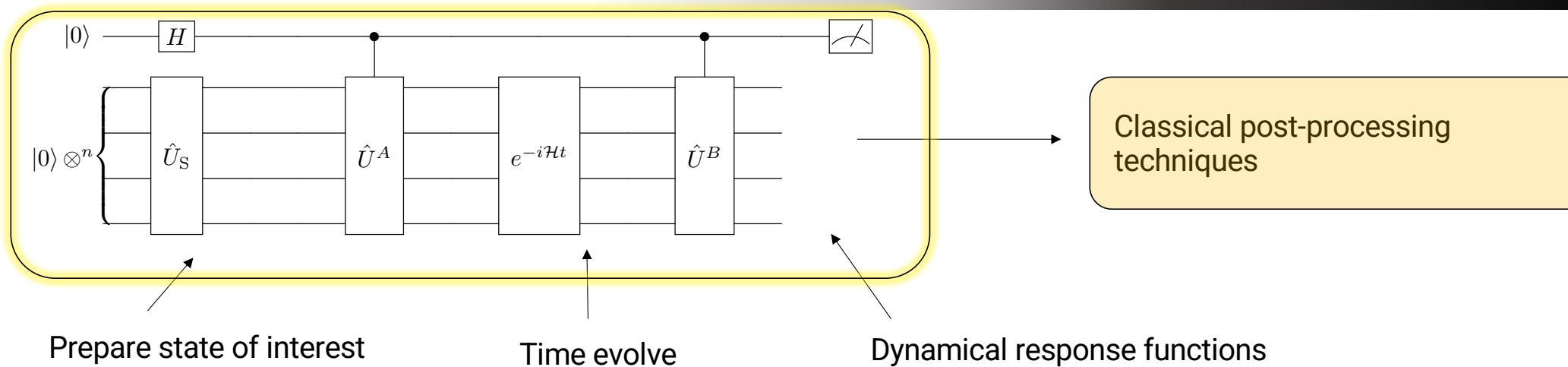
$|0\rangle$

**Exact simulation of a time independent spin Hamiltonian:**  $\mathcal{H} = \sum_j h_j \sigma^j$



T. Steckmann et al., PRR (2023) 29

# A-Z quantum simulation

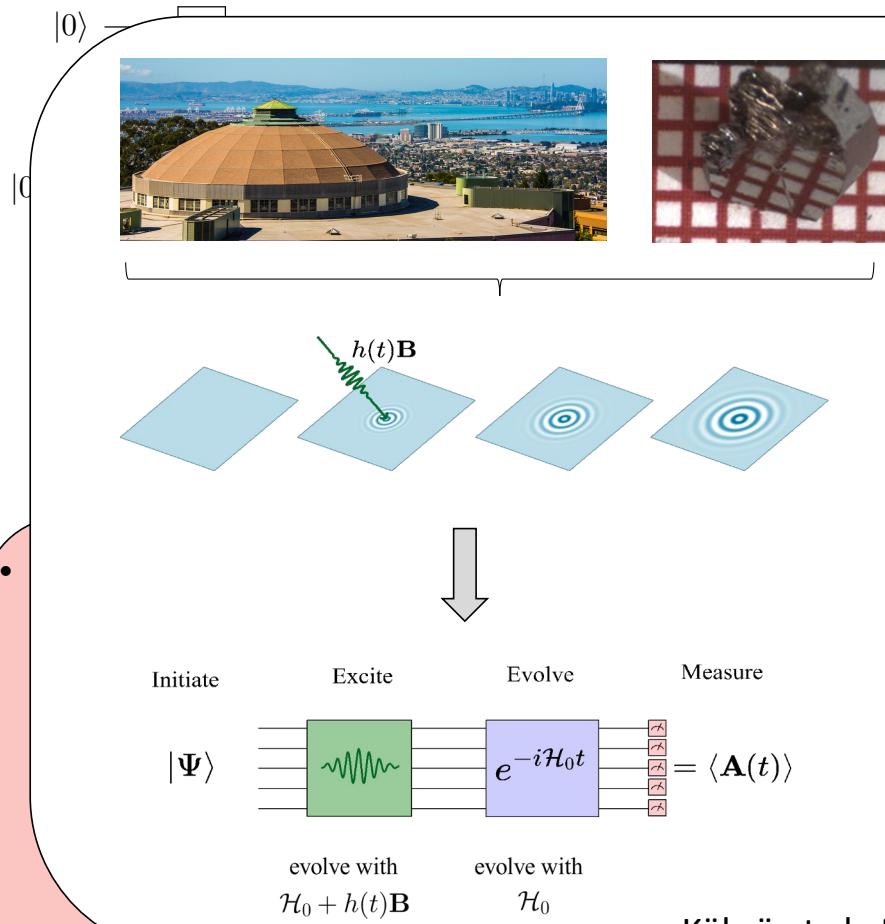


- *Physics-Informed Subspace Expansions*
- *Barren optimization plateaus*

- *Lie-algebraic methods for time evolution*
- *Open quantum system evolution*

- *Correlation functions*
- *Open quantum system Green's functions*
- *Dynamical Mean Field Theory*

# A-Z quantum simulation



A linear response framework for simulating bosonic and fermionic correlation functions illustrated on quantum computers

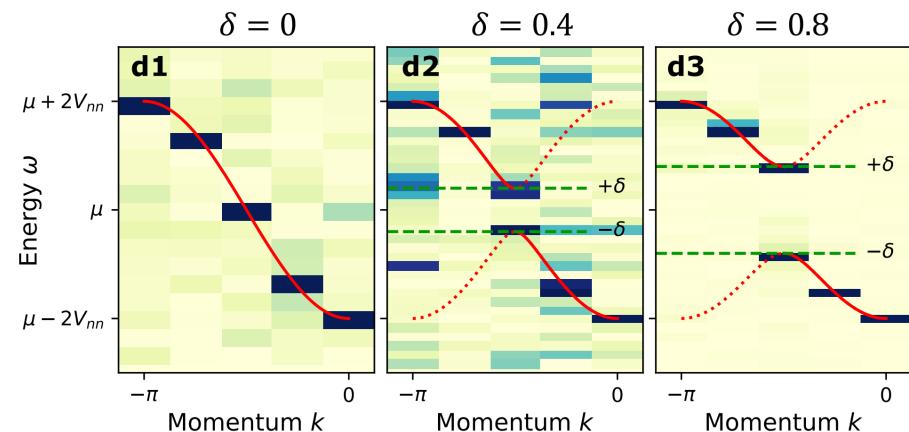
Efekan Kökcü ,<sup>1</sup> Heba A. Labib ,<sup>1</sup> J. K. Freericks ,<sup>2</sup> and A. F. Kemper ,<sup>1,\*</sup>

<sup>1</sup>Department of Physics, North Carolina State University, Raleigh, North Carolina 27695, USA

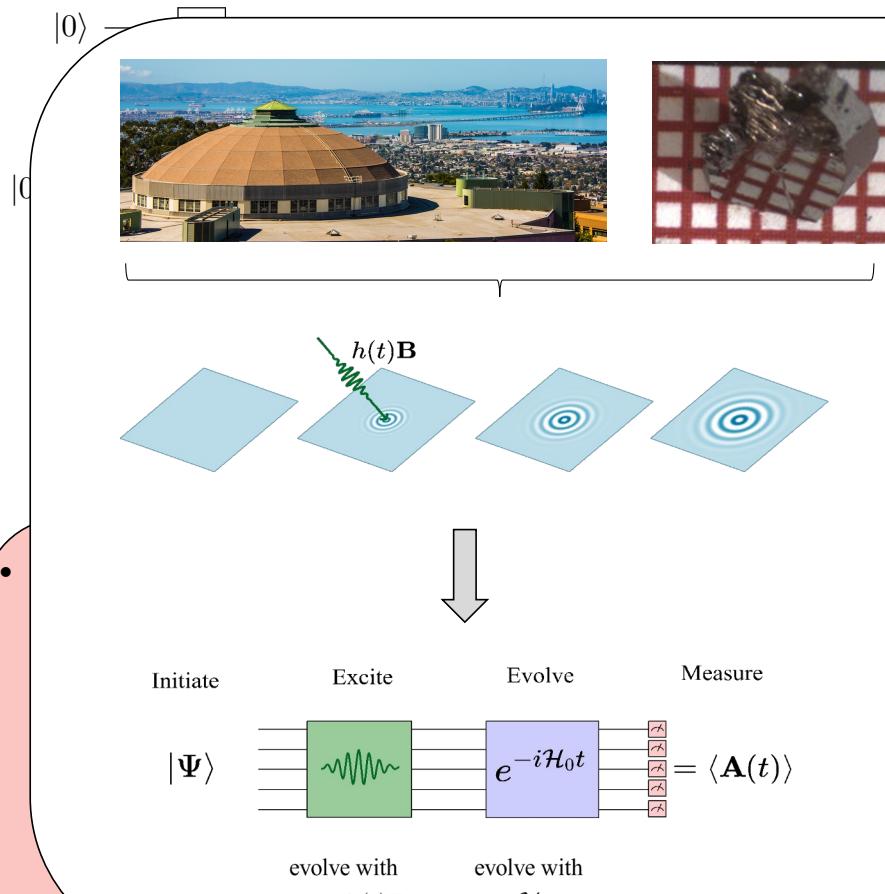
<sup>2</sup>Department of Physics, Georgetown University, 37th and O Sts. NW, Washington, DC 20057 USA

(Dated: February 22, 2023)

1. Make the excitation part of the quantum simulation
2. Post-process the data to get the response functions



# A-Z quantum simulation



A linear response framework for simulating bosonic and fermionic correlation functions illustrated on quantum computers

Efekan Kökcü ,<sup>1</sup> Heba A. Labib ,<sup>1</sup> J. K. Freericks ,<sup>2</sup> and A. F. Kemper ,<sup>1,\*</sup>

<sup>1</sup>Department of Physics, North Carolina State University, Raleigh, North Carolina 27695, USA

<sup>2</sup>Department of Physics, Georgetown University, 37th and O Sts. NW, Washington, DC 20057 USA

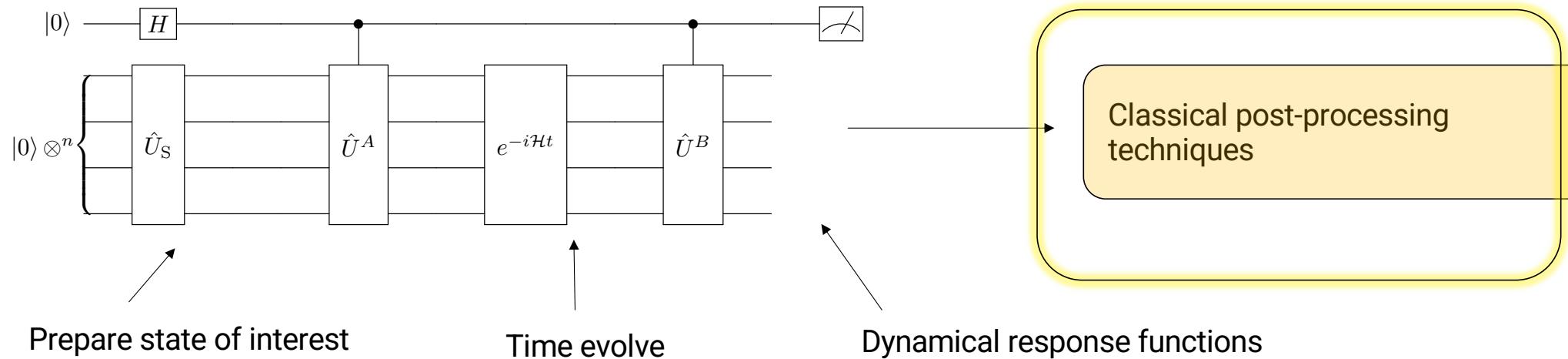
(Dated: February 22, 2023)

## Benefits

- Any operator A,B you desire (as long as it is Hermitian\*)
- No ancillas/controlled operations needed
- Many correlation functions at the same time
- Less post-processing (less noise)
- Frequency/momentum selective

Kökcü et al., Nat. Comm. 2024

# A-Z quantum simulation



- *Physics-Informed Subspace Expansions*
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## A-Z quantum simulation

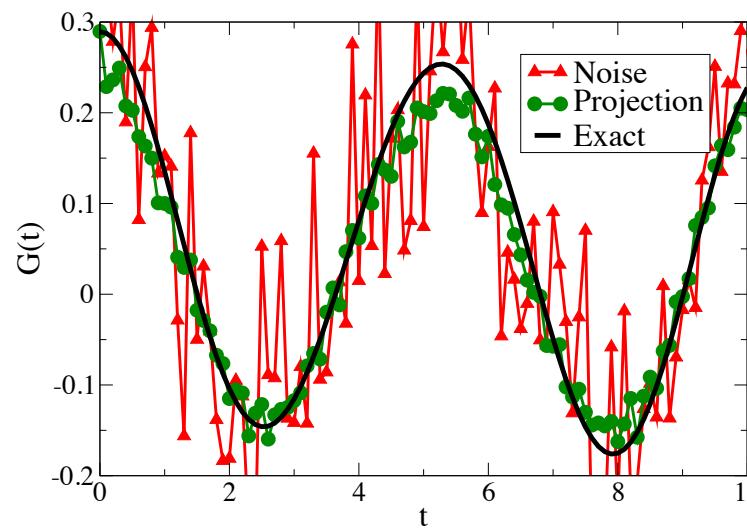
- It turns out that these are positive semi-definite (PSD) functions:

$$G_{AA}(t - t') = \text{Tr} [\rho A(t)^\dagger A(t')]$$

- Then this is a PSD matrix:

$$\underline{G} = \begin{pmatrix} f_0 & f_1 & f_2 & \cdots & f_n \\ f_1^* & f_0 & f_1 & \cdots & f_{n-1} \\ f_2^* & f_1^* & f_0 & \cdots & f_{n-2} \\ \vdots & & \ddots & & \vdots \\ f_n^* & f_{n-1}^* & f_{n-2}^* & \cdots & f_0 \end{pmatrix}$$

where  $G_{AA}(t_i - t_j) \rightarrow f_{i-j}$



# A-Z quantum simulation

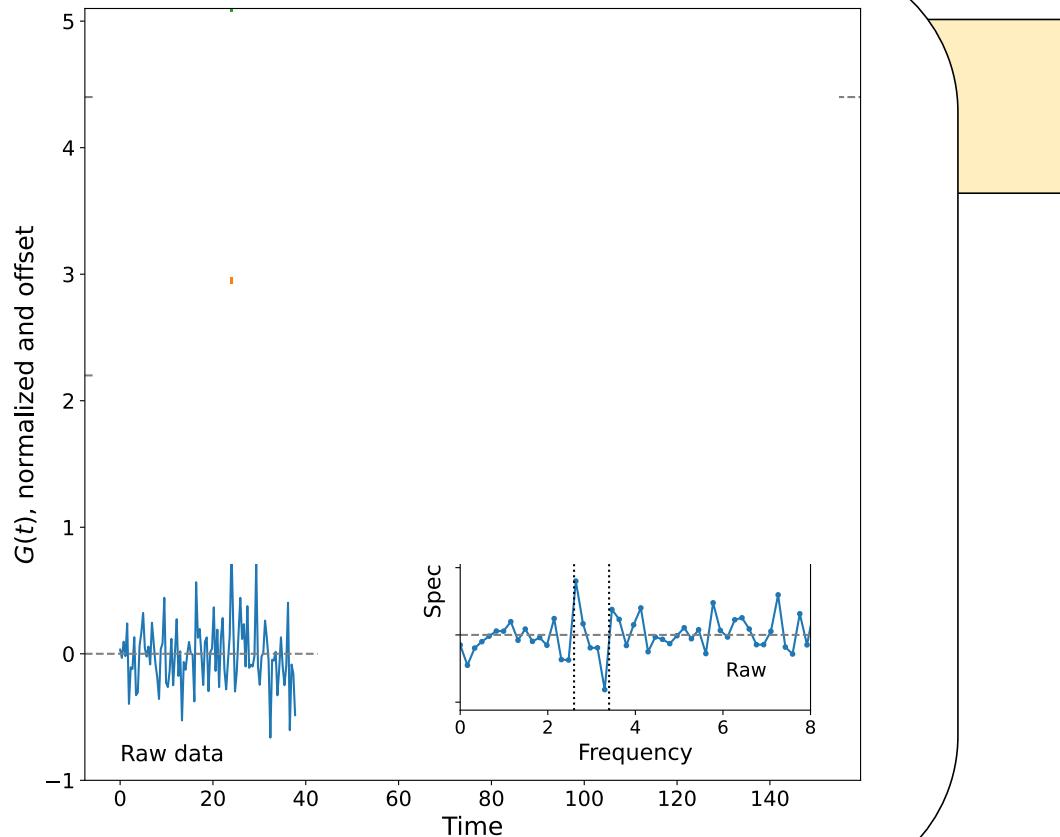
- It turns out that these are positive semi-definite (PSD) functions:

$$G_{AA}(t - t') = \text{Tr} [\rho A(t)^\dagger A(t')]$$

- Then this is a PSD matrix:

$$\underline{G} = \begin{pmatrix} f_0 & f_1 & f_2 & \cdots & f_n \\ f_1^* & f_0 & f_1 & \cdots & f_{n-1} \\ f_2^* & f_1^* & f_0 & \cdots & f_{n-2} \\ \vdots & & \ddots & & \vdots \\ f_n^* & f_{n-1}^* & f_{n-2}^* & \cdots & f_0 \end{pmatrix}$$

where  $G_{AA}(t_i - t_j) \rightarrow f_{i-j}$



## A-Z quantum simulation

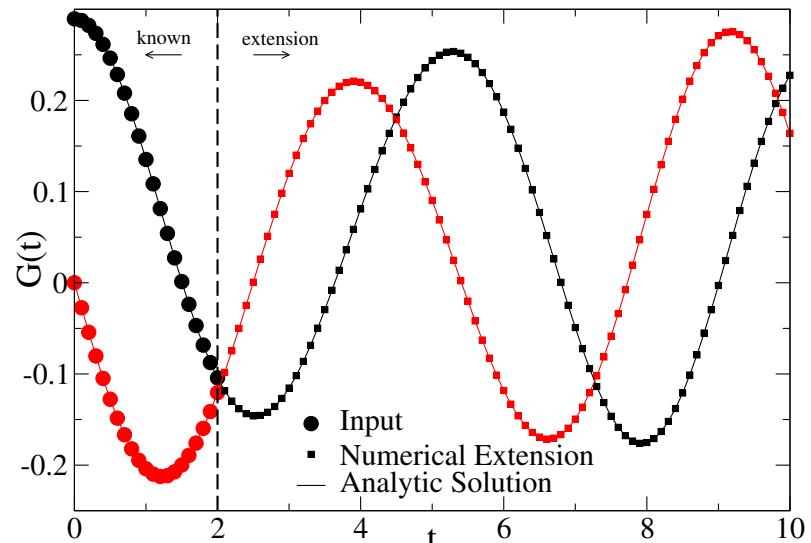
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# A-Z quantum simulation

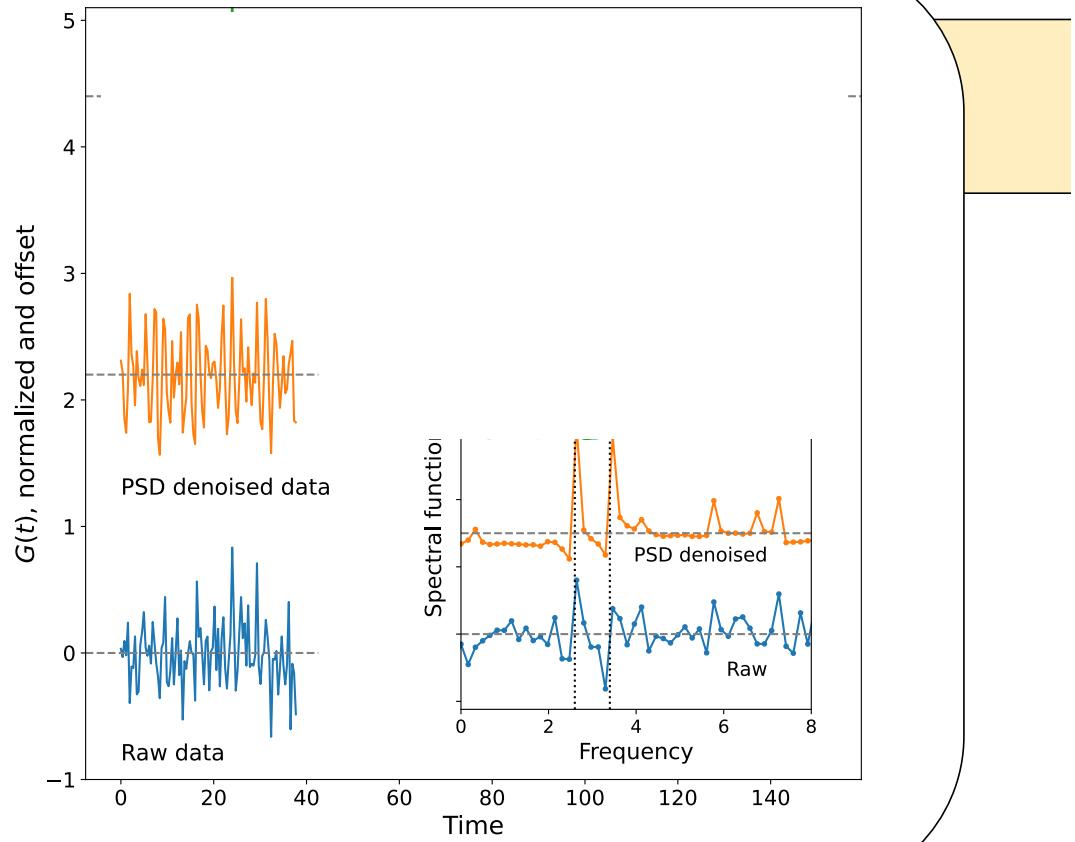
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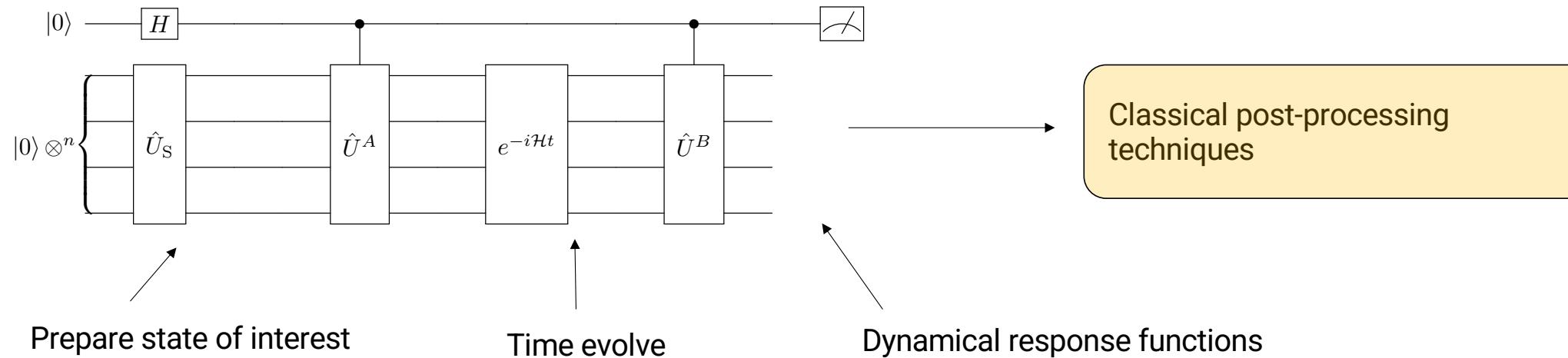
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# A-Z quantum simulation



- Physics-Informed Subspace Expansions
- Barren optimization plateaus

- Lie-algebraic methods for time evolution
- Open quantum system evolution

- Correlation functions
- Open quantum system Green's functions
- Dynamical Mean Field Theory