

Quantum algorithms for dynamics and dynamical observables

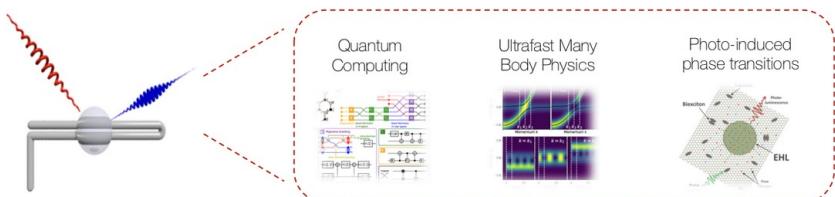
Alexander (Lex) Kemper



Department of Physics
North Carolina State University
<https://go.ncsu.edu/kemper-lab>

IPAM Quantum Algorithms
10/05/2023





Kemper Lab

Quantum materials in and out of equilibrium.

Collaborations with:

- Bojko Bakalov (NCSU)
- Marco Cerezo, Martin de la Rocca (LANL)
- Jim Freericks (Georgetown)
- Daan Camps, Roel van Beeumen, Bert de Jong, Akhil Francis (LBNL)
- Thomas Steckmann (UMD)
- Yan Wang, Eugene Dumitrescu (ORNL)

Current members



Alexander (Lex)
Kemper
Principal investigator



Efekan Kökçü
Graduate Researcher



Anjali Agrawal
Graduate Researcher



Heba Labib
Graduate Researcher



Jack Howard
Undergraduate
Researcher



Natalia Wilson
Undergraduate
Researcher



Daniel Brandon
Undergraduate
Researcher



Sarah Klas
Undergraduate
Researcher



Norman Hogan
Graduate Researcher



Ethan Blair
Undergraduate
Researcher

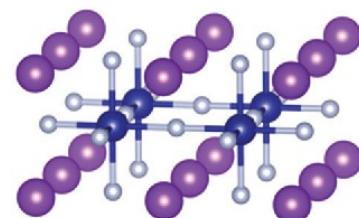


Your Name
New lab member

A Tale of Two Transitions

Ising Magnet

Rb_2CoF_4



$$\mathcal{H} = -J \sum_i \sigma_i^z \sigma_{i+1}^z + h_x \sum_i$$

Ferromagnetic

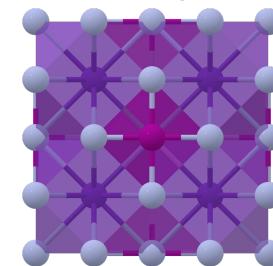


Antiferromagnetic



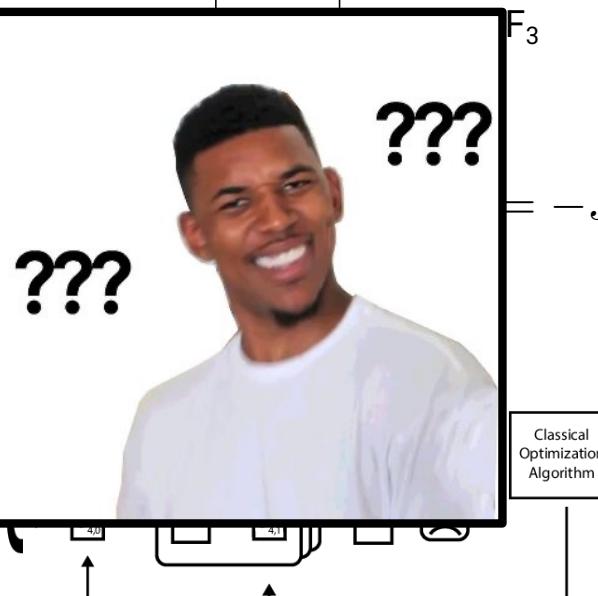
[10.1039/c6cp02362b](https://doi.org/10.1039/c6cp02362b)

Heisenberg Magnet



F_3

$$= -J \sum_i \vec{\sigma}_i \cdot \vec{\sigma}_{i+1} + h_x \sum_i \sigma_i^x$$



[Optimization of the Variational Quantum Eigensolver for Quantum Chemistry Applications](#)

Ferromagnetic



Antiferromagnetic



Materials project

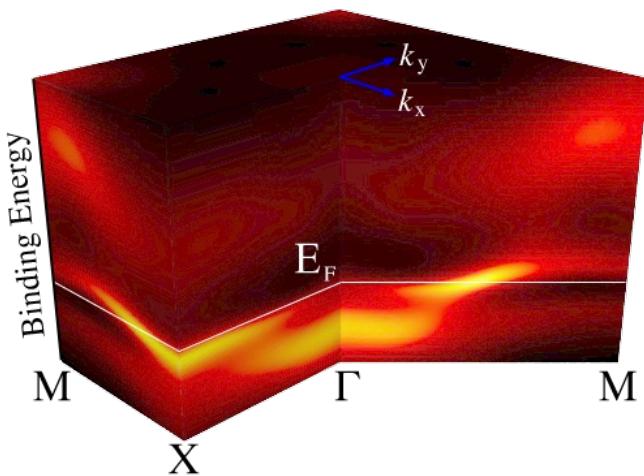
3

Q: What do you do with a quantum state once you've prepared one?

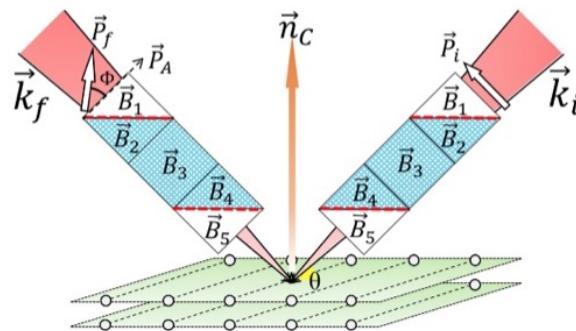
A: You measure its excitations.

Measuring Excitations

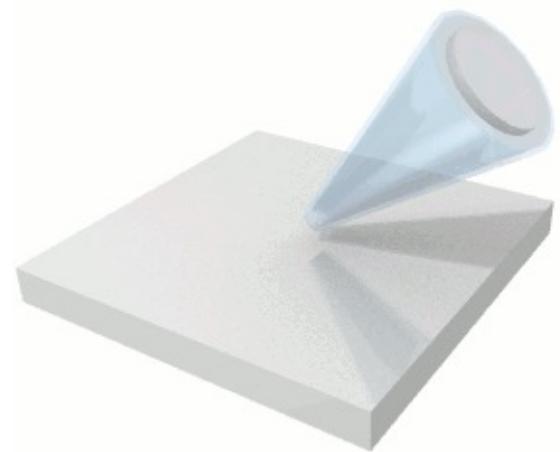
Figures courtesy of
Devereaux/Shen group
and ORNL



Angle-resolved Photoemission
(ARPES)

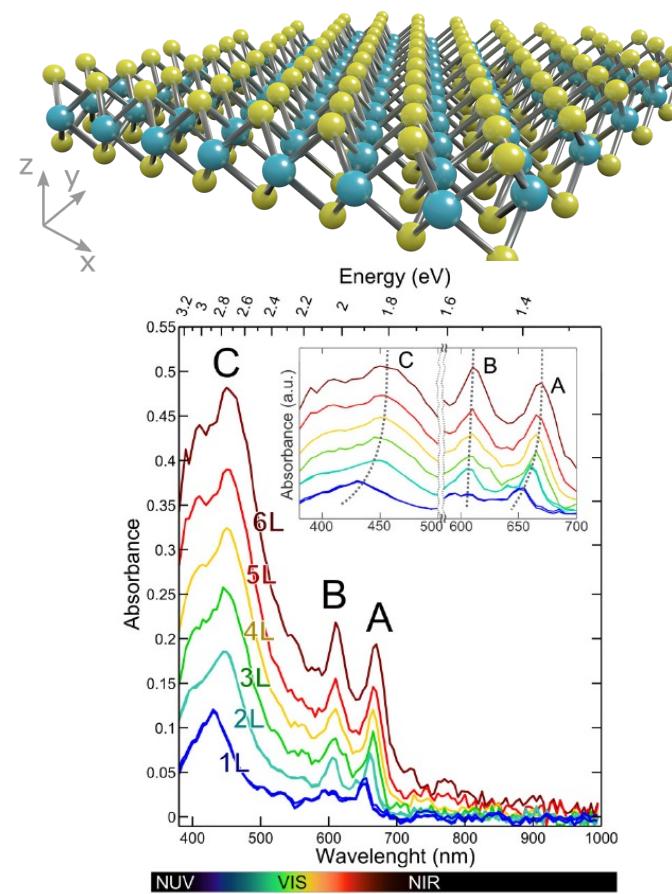
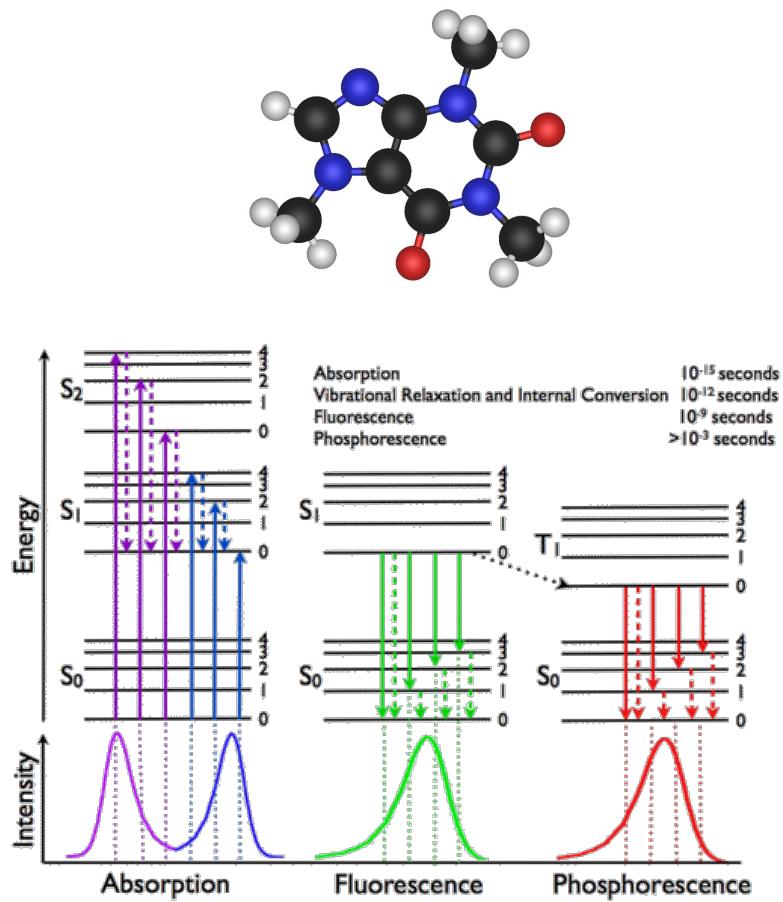


Neutron Scattering



Time-resolved ARPES

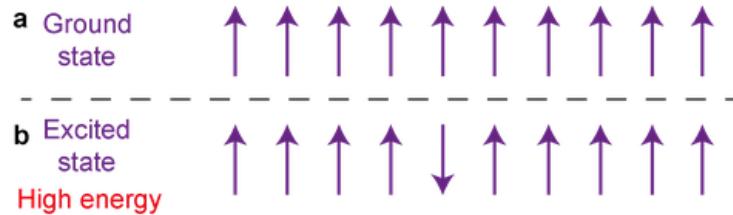
Measuring Excitations



Measuring Excitations

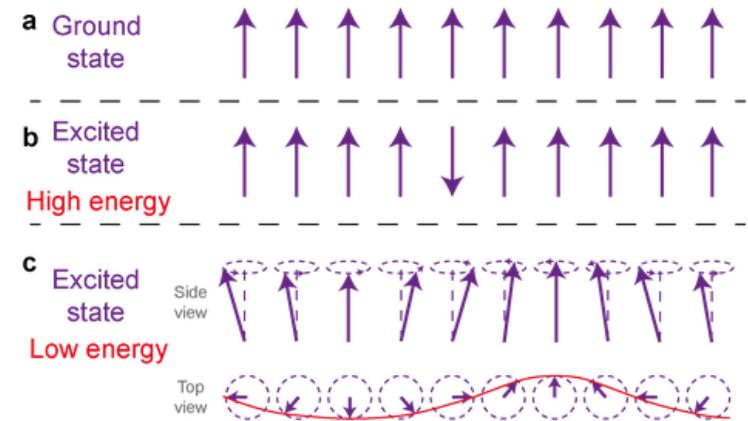
Ising Model

$$\mathcal{H} = -J \sum_i \sigma_i^z \sigma_{i+1}^z + h_x \sum_i \sigma_i^x$$

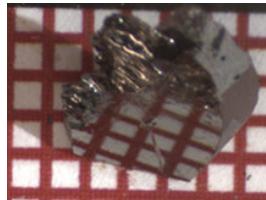


Heisenberg model

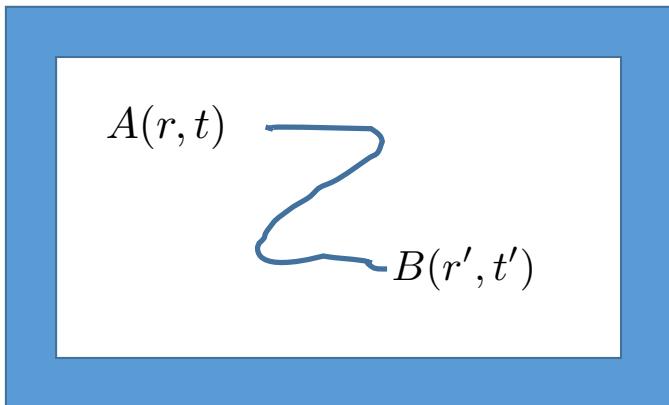
$$\mathcal{H} = -J \sum_i \vec{\sigma}_i \cdot \vec{\sigma}_{i+1} + h_x \sum_i \sigma_i^x$$



Correlation functions



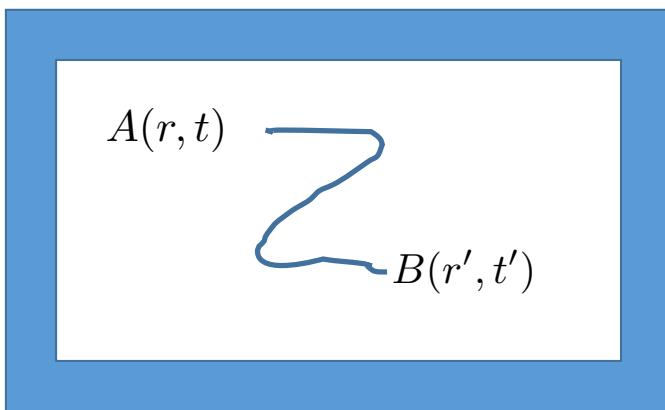
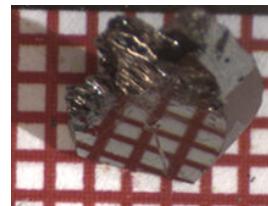
$$\langle A(r, t)B(r', t') \rangle$$



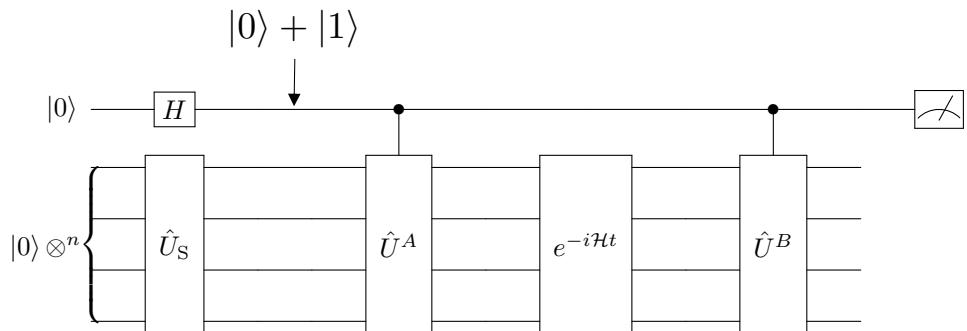
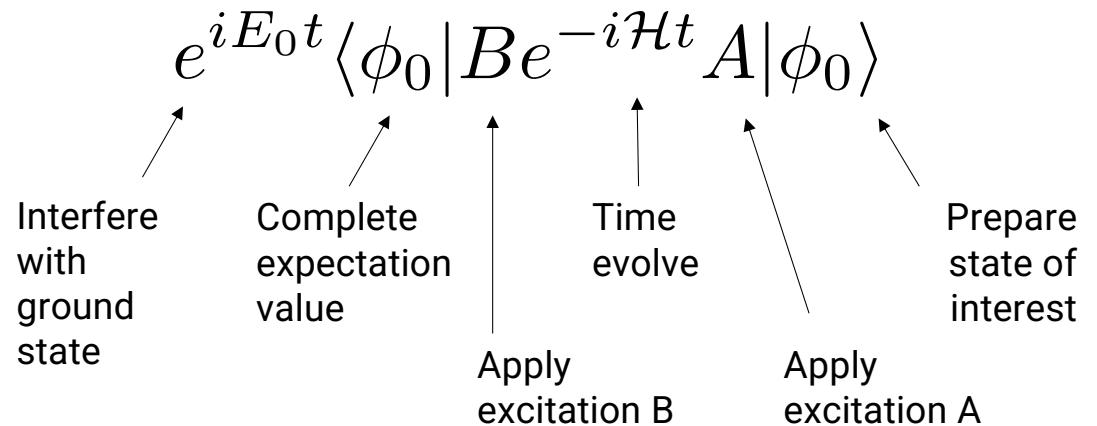
Given some (observable) operator B at (r',t'), what is the likelihood of some (observable) operator A at (r,t)?

Optical conductivity, γ /X-ray scattering, photoemission, neutron scattering, Raman, IR absorption, etc.

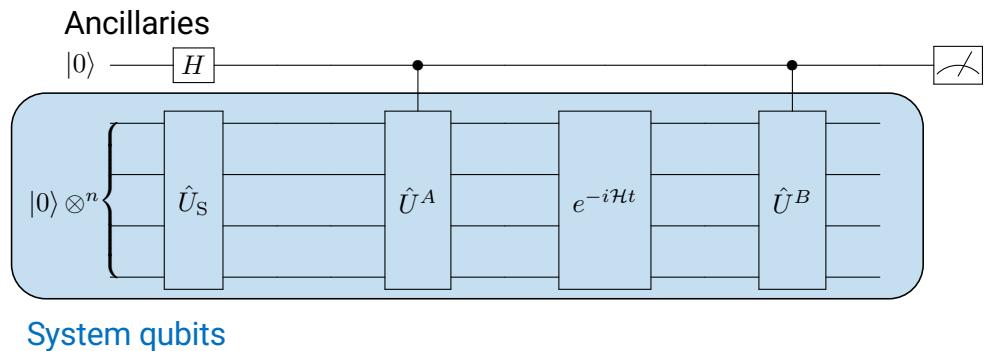
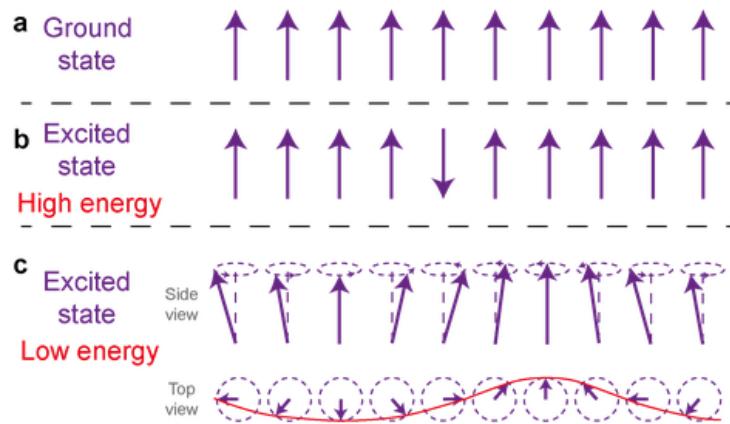
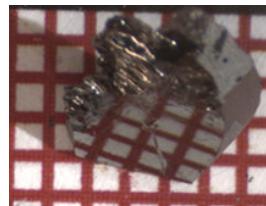
Correlation functions



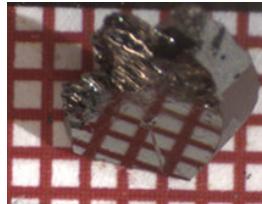
Somma, Simulating physical phenomena by quantum networks (2002)



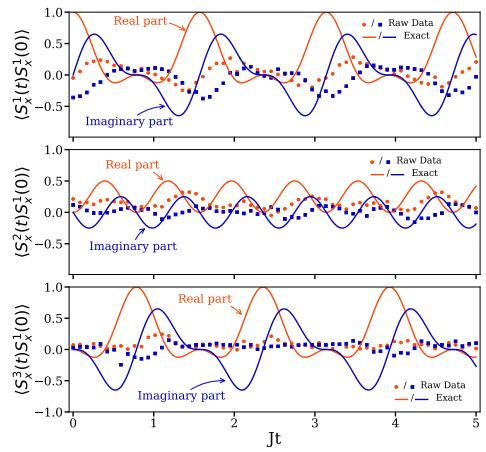
Correlation functions



Correlation functions

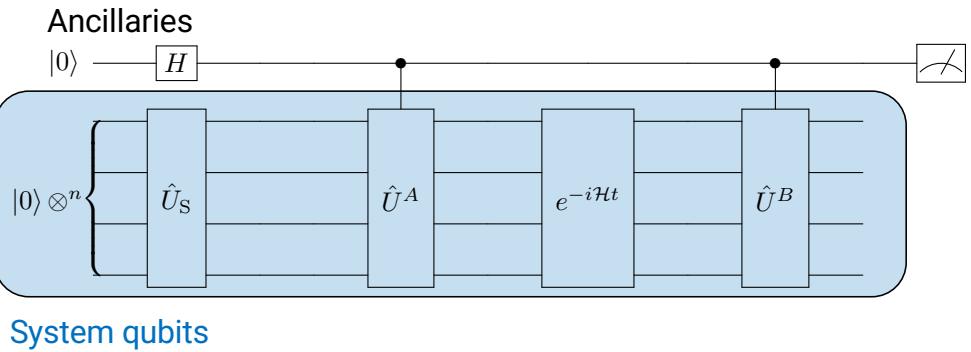
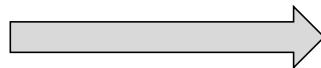


Raw data (2019)

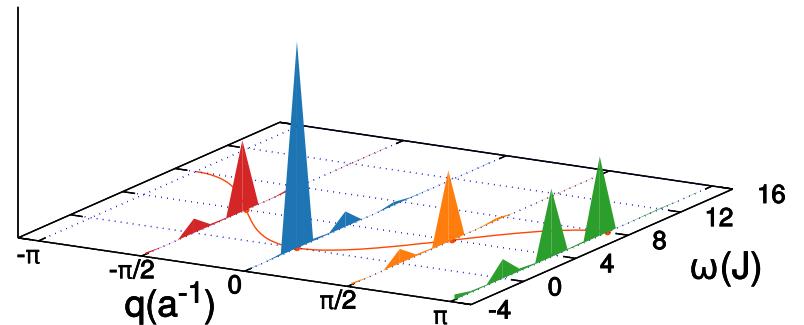


$$\langle A(r, t)B(r', t') \rangle$$

Error mitigation

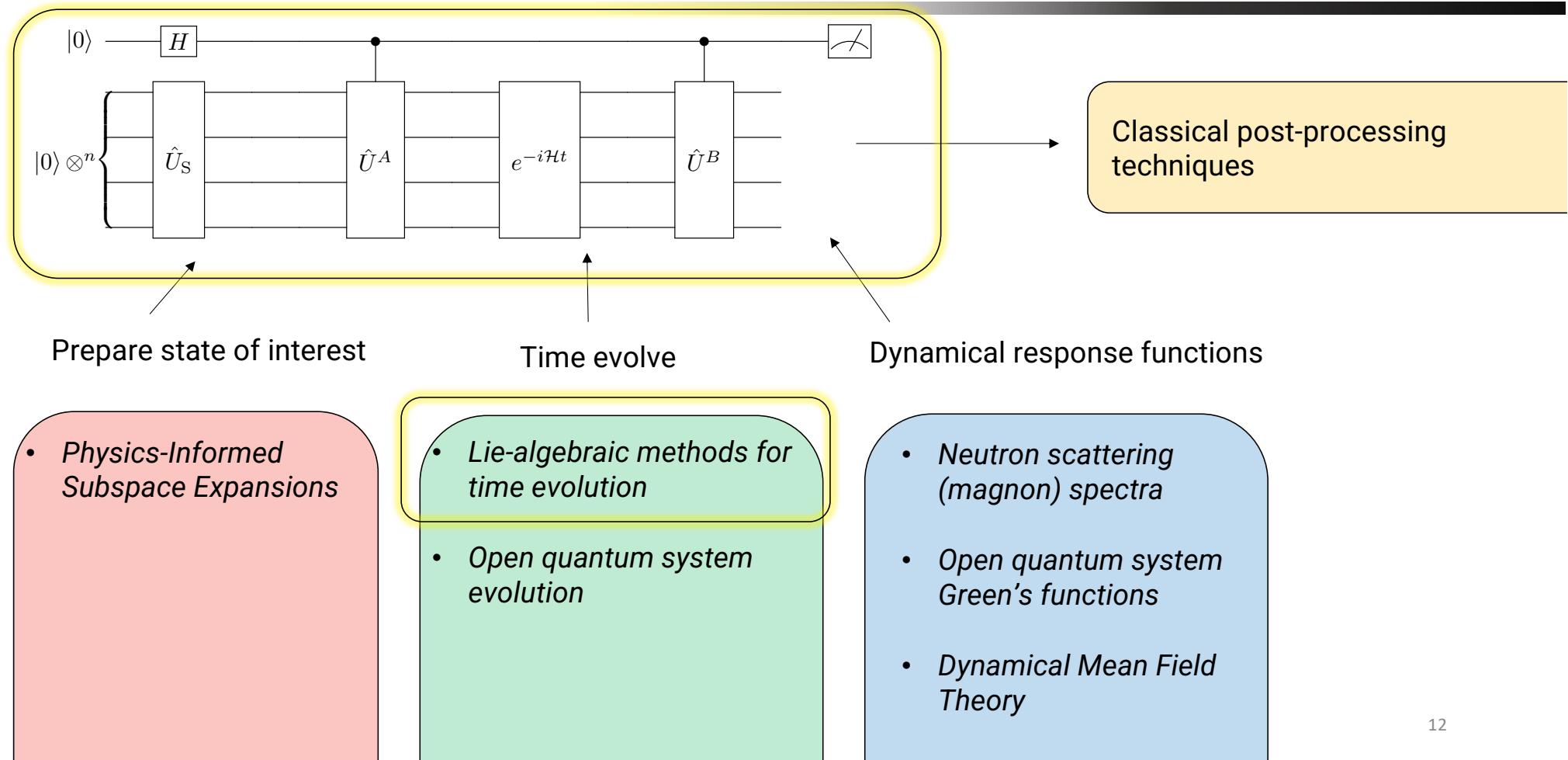


$|\mathbf{S}(\mathbf{q}, \omega)|^2$: PaS



11

A-Z quantum simulation



(A few) Quantum Algorithm(s) for correlation functions

Robust measurements of n-point correlation functions of driven-dissipative quantum systems on a digital quantum computer

Lorenzo Del Re^{1,2}, Brian Rost,¹ Michael Foss-Feig,³ A. F. Kemper,⁴ and J. K. Freericks¹

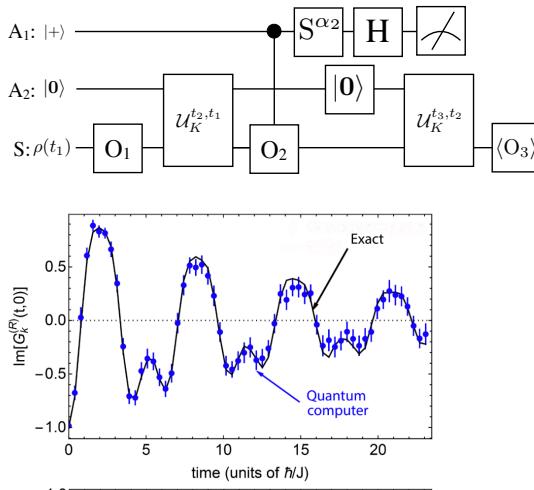
¹Department of Physics, Georgetown University, 37th and O St NW, Washington, DC 20057, USA

²Max Planck Institute for Solid State Research, D-70569 Stuttgart, Germany

³Quantinuum, 303 S. Technology Ct, Broomfield, Colorado 80021, USA

⁴Department of Physics, North Carolina State University, Raleigh, North Carolina 27695, USA

(Dated: April 27, 2022)



(Anti-)Commutators, open/dissipative

L. Del Re, B. Rost, M. Foss-Feig, AFK, J.K. Freericks
2204.12400

Quantum Computed Green's Functions using a Cumulant Expansion of the Lanczos Method

Gabriel Greene-Diniz,^{1,*} David Zsolt Manrique,¹ Kentaro Yamamoto,² Evgeny Plekhanov,¹ Nathan Fitzpatrick,¹ Michal Krompiec,¹ Rei Sakuma,³ and David Muñoz Ramo⁴

¹Quantinuum, Terrington House, 13-15 Hills Road, Cambridge CB2 1NL, UK

²Quantinuum K.K., Otemachi Financial City Grand Cube 3F, 1-9-2 Otemachi, Chiyoda-ku, Tokyo, Japan

³Materials Informatics Initiative, RD Technology & Digital Transformation Center, JSR Corporation, 3-103-9, Tonomachi, Kawasaki-ku, Kawasaki, 210-0821, Kanagawa, Japan.

(Dated: September 19, 2023)

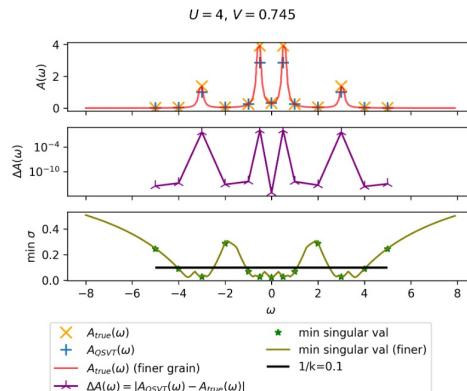
Calculating the Single-Particle Many-body Green's Functions via the Quantum Singular Value Transform Algorithm

Alexis Ralli,^{1,2,*} Gabriel Greene-Diniz,¹ David Muñoz Ramo,¹ and Nathan Fitzpatrick^{1,†}

¹Quantinuum, Terrington House, 13-15 Hills Road, Cambridge CB2 1NL, United Kingdom

²Centre for Computational Science, Department of Chemistry, University College London, WC1H 0AJ, United Kingdom

(Dated: July 26, 2023)



PRL 111, 147205 (2013)

PHYSICAL REVIEW LETTERS

week ending

4 OCTOBER 2013

Probing Real-Space and Time-Resolved Correlation Functions with Many-Body Ramsey Interferometry

Michael Knap,^{1,2,*} Adrian Kantian,³ Thierry Giannouchi,³ Immanuel Bloch,^{4,5} Mikhail D. Lukin,¹ and Eugene Demler¹

¹Department of Physics, Harvard University, Cambridge, Massachusetts 02138, USA

²ITAMP, Harvard-Smithsonian Center for Astrophysics, Cambridge, Massachusetts 02138, USA

³DPMC-MaNEP, University of Geneva, 24 Quai Ernest-Ansermet CH-1211 Geneva, Switzerland

⁴Max-Planck-Institut für Quantenoptik, Hans-Kopfermann-Strasse 1, 85748 Garching, Germany

⁵Fakultät für Physik, Ludwig-Maximilians-Universität München, 80799 München, Germany

(Received 2 July 2013; revised manuscript received 18 September 2013; published 4 October 2013)

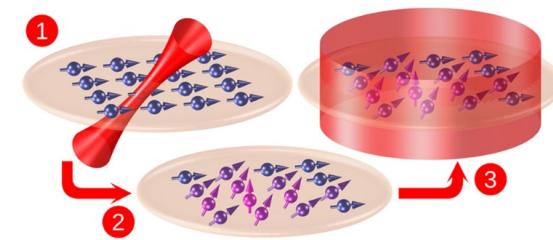
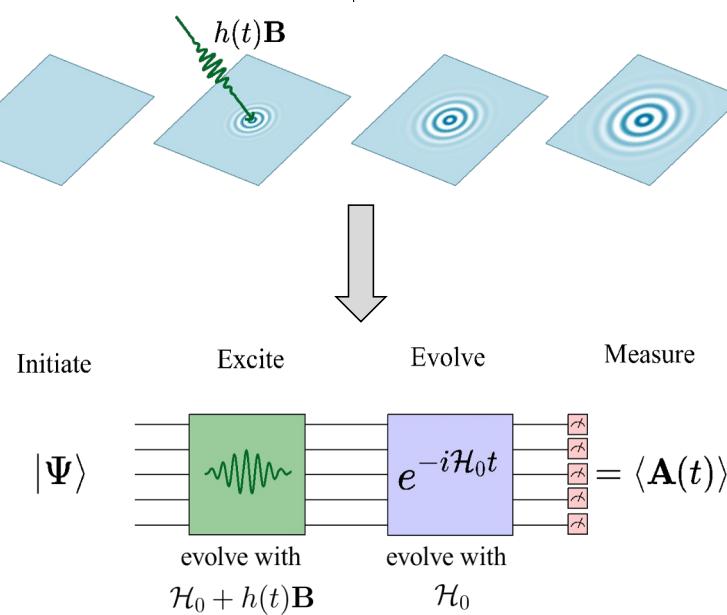


FIG. 1 (color online). Many-body Ramsey interferometry consists of the following steps: (1) A spin system prepared in its ground state is locally excited by $\pi/2$ rotation; (2) the system evolves in time; (3) a global $\pi/2$ rotation is applied, followed by the measurement of the spin state. This protocol provides the dynamic many-body Green's function.

Commutators

10.1103/PhysRevLett.111.147205

Linear Response



A linear response framework for simulating bosonic and fermionic correlation functions illustrated on quantum computers

Efekan Kökcü ,¹ Heba A. Labib ,¹ J. K. Freericks ,² and A. F. Kemper ,^{1,*}

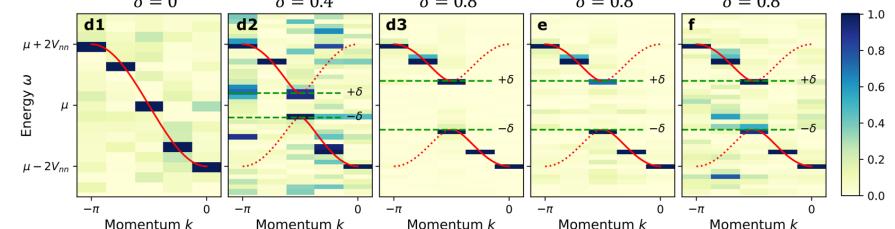
¹Department of Physics, North Carolina State University, Raleigh, North Carolina 27695, USA

²Department of Physics, Georgetown University, 37th and O Sts. NW, Washington, DC 20057 USA

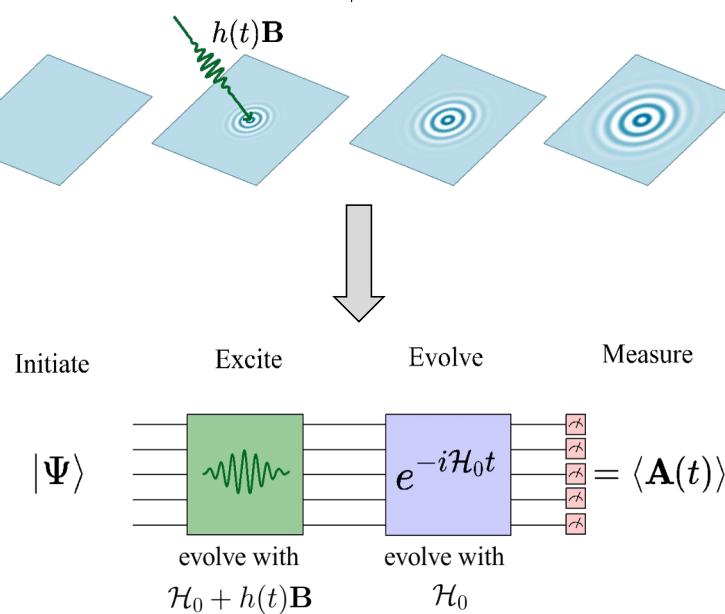
(Dated: February 22, 2023)

1. Make the excitation part of the quantum simulation
2. Post-process the data to get the response functions

$$\left. \frac{\delta A(t)}{\delta h(t')} \right|_{h=0} = -i\theta(t-t') \langle \psi_0 | [\mathbf{A}(t), \mathbf{B}(t')] | \psi_0 \rangle$$



Linear Response



A linear response framework for simulating bosonic and fermionic correlation functions illustrated on quantum computers

Efekan Kökcü¹, Heba A. Labib¹, J. K. Freericks², and A. F. Kemper^{1,*}

¹Department of Physics, North Carolina State University, Raleigh, North Carolina 27695, USA

²Department of Physics, Georgetown University, 37th and O Sts. NW, Washington, DC 20057 USA

(Dated: February 22, 2023)

Benefits

- Any operator A,B you desire (as long as it is Hermitian*)
- No ancillas/controlled operations needed
- Many correlation functions at the same time
- Less post-processing (less noise)
- Frequency/momentum selective

Some Mathematics...

The time evolution operator satisfies

$$i\partial_t U(t) = V(t)U(t)$$

Which is formally solved by

$$U(t) = \mathcal{T} \exp \left(-i \int_{-\infty}^t V(\bar{t}) d\bar{t} \right)$$

Or approximately(for small V) by

$$U(t) \approx 1 - i \int_{-\infty}^t V(\bar{t}) d\bar{t}$$

Thus the wave function is given by

$$|\psi(t)\rangle \approx |\psi_0\rangle - i \int_{-\infty}^t V(\bar{t}) |\psi_0\rangle d\bar{t}$$

We now pick an operator **A** to evaluate

$$\langle \psi(t) | \mathbf{A}(t) | \psi(t) \rangle = \langle \psi_0 | \mathbf{A}(t) | \psi_0 \rangle = \\ -i \int_{-\infty}^t \langle \psi_0 | [\mathbf{A}(t), \mathbf{V}(\bar{t})] | \psi_0 \rangle d\bar{t}$$

Putting the time dependence outside via $\mathbf{V}(t) = h(t)\mathbf{B}$

$$\delta A(t) = -i \int_{-\infty}^t \langle [\mathbf{A}(t), \mathbf{B}] \rangle h(\bar{t}) d\bar{t}$$

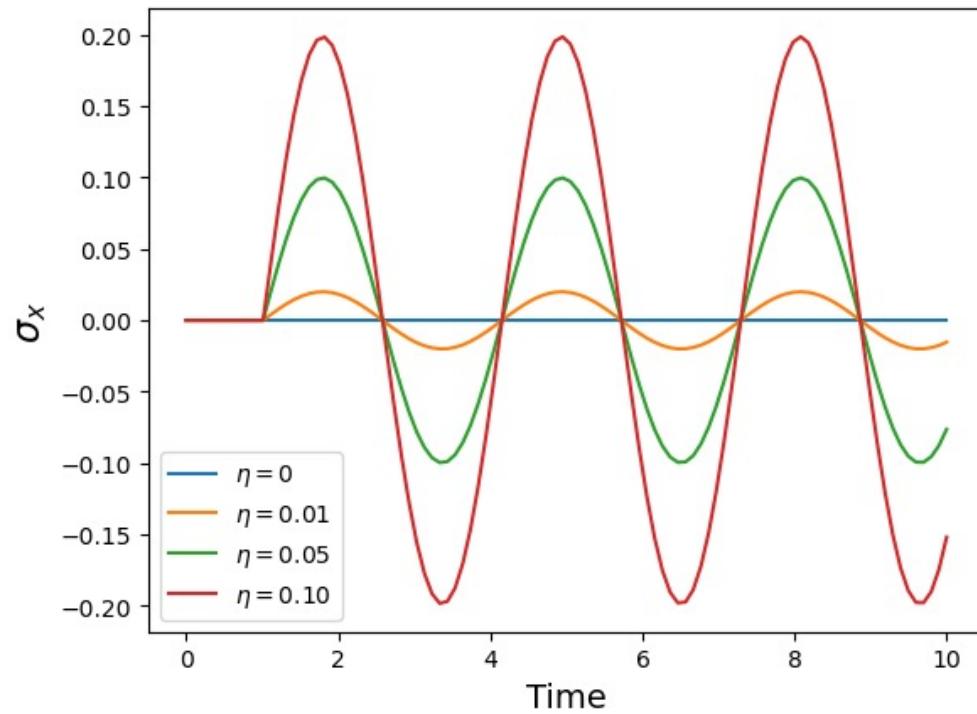
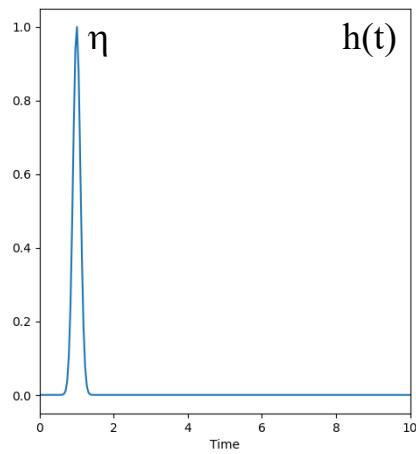
$$\delta A(t) = \int_{-\infty}^{\infty} \chi^R(t, \bar{t}) h(\bar{t}) d\bar{t}$$

Linear Response

A simple example: single spin with energy level difference = 2

$$\mathbf{H}_0 = \sigma^z$$

$$\mathbf{A} = \mathbf{B} = \sigma^x$$

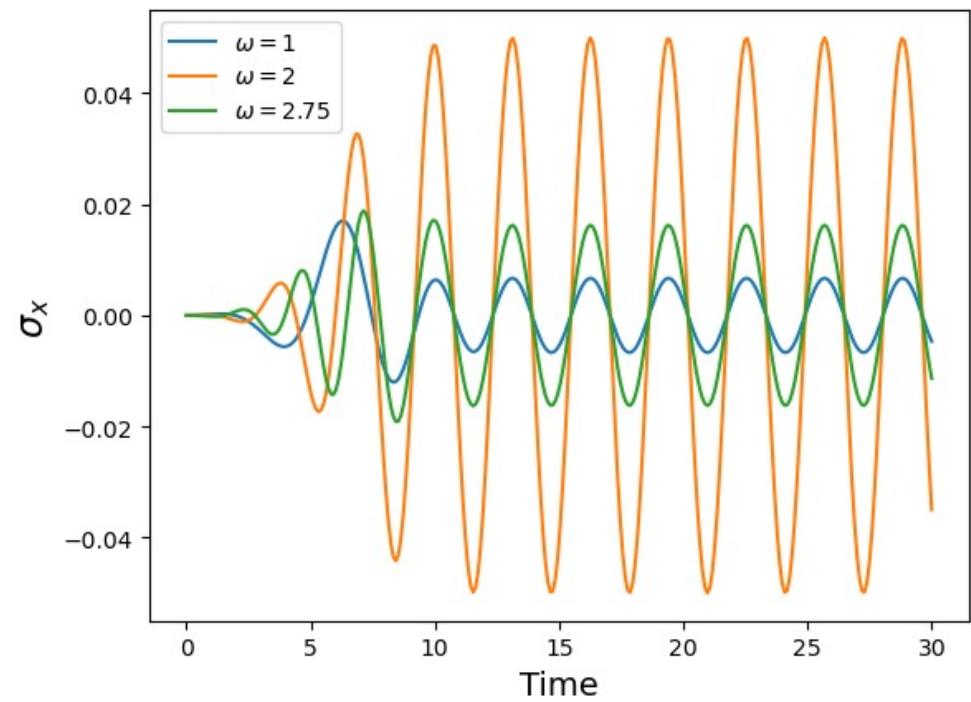
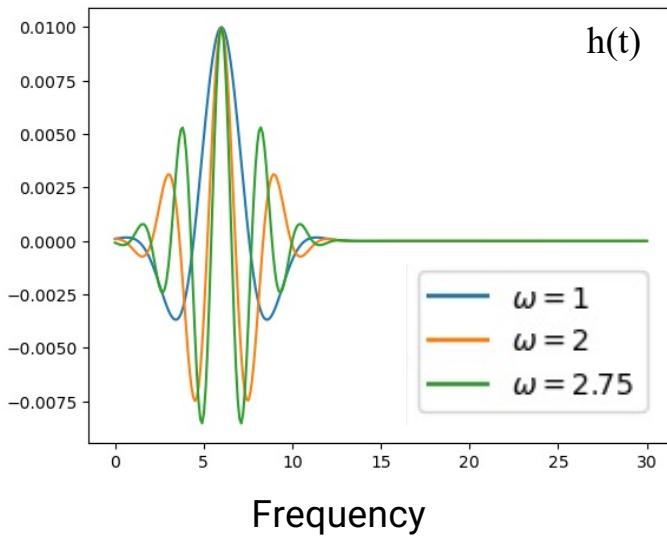


Linear Response

A simple example: single spin with energy level difference = 2

$$\mathbf{H}_0 = \sigma^z$$

$$\mathbf{A} = \mathbf{B} = \sigma^x$$

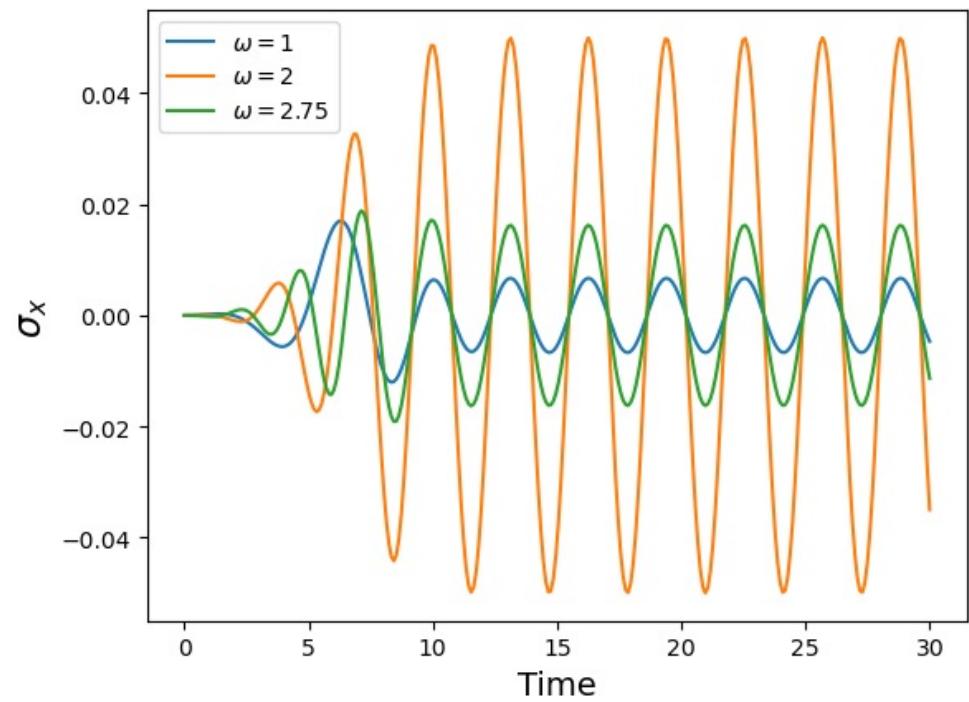
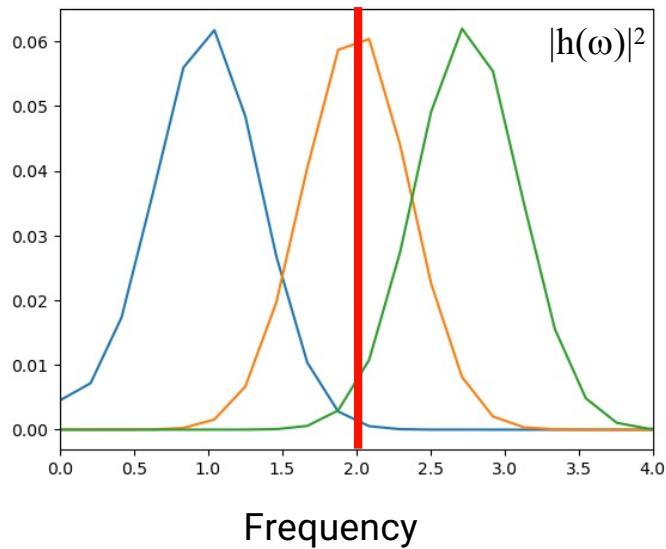


Linear Response

A simple example: single spin with energy level difference = 2

$$\mathbf{H}_0 = \sigma^z$$

$$\mathbf{A} = \mathbf{B} = \sigma^x$$



Fermionic Linear Response

$$\frac{\delta A(t)}{\delta h(t')} \Big|_{h=0} = -i\theta(t-t') \langle \psi_0 | [\mathbf{A}(t), \mathbf{B}(t')] | \psi_0 \rangle$$

Notice this is a commutator...

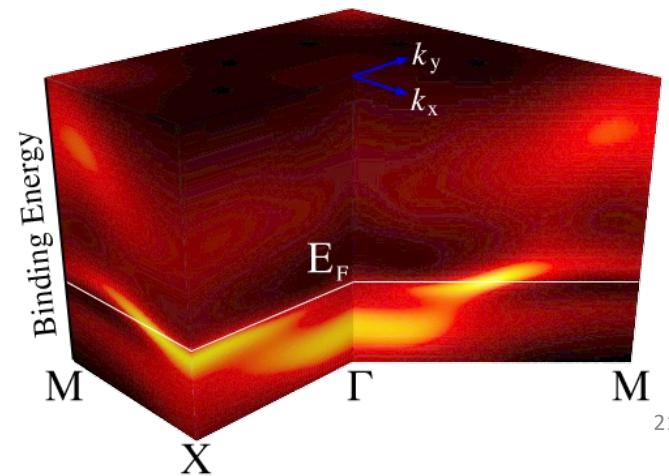
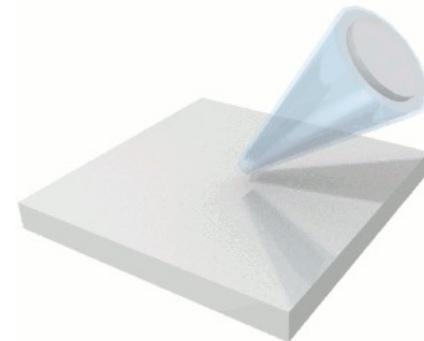
... we might also want to have an anti-commuter

$$G(t, t') = -i\theta(t-t') \langle \psi_0 | \{ \mathbf{A}(t), \mathbf{B}(t') \} | \psi_0 \rangle$$

Why?

$$G^R(r_i, t; r_j, t') = -i\theta(t-t') \langle \psi_0 | \{ c_i(t), c_j^\dagger(t') \} | \psi_0 \rangle$$

Fermionic creation/
annihilation operators



Option 1: Auxiliary operator

$$\frac{\delta A(t)}{\delta h(t')} \Big|_{h=0} = -i\theta(t-t')\langle\psi_0|[\mathbf{A}(t), \mathbf{B}(t')]\rangle|\psi_0\rangle$$

Find an operator \mathbf{P} such that:

$$\{\mathbf{B}(t), \mathbf{P}\} = 0$$

$$[\mathcal{H}_0, \mathbf{P}] = 0$$

$$\mathbf{P}|\psi_0\rangle = s|\psi_0\rangle$$

Then:

$$\begin{aligned} G(t, t') &= -i\theta(t-t')\langle\psi_0|\{\mathbf{A}(t), \mathbf{B}(t')\}|\psi_0\rangle \\ &= \frac{i}{s}\theta(t-t')\langle\psi_0|[\mathbf{A}(t)\mathbf{P}(t), \mathbf{B}(t')]\rangle|\psi_0\rangle \end{aligned}$$

Example: parity

$$\mathbf{P} = Z_1 Z_2 \dots Z_n$$

Option 2: Post-selection

Fermionic Linear Response

Option 1: Auxiliary operator

$$\frac{\delta A(t)}{\delta h(t')} \Big|_{h=0} = -i\theta(t-t')\langle\psi_0|[\mathbf{A}(t), \mathbf{B}(t')]\rangle\psi_0$$

Find an operator \mathbf{P} such that:

$$\{\mathbf{B}(t), \mathbf{P}\} = 0$$

$$[\mathcal{H}_0, \mathbf{P}] = 0$$

$$\mathbf{P}|\psi_0\rangle = s|\psi_0\rangle$$

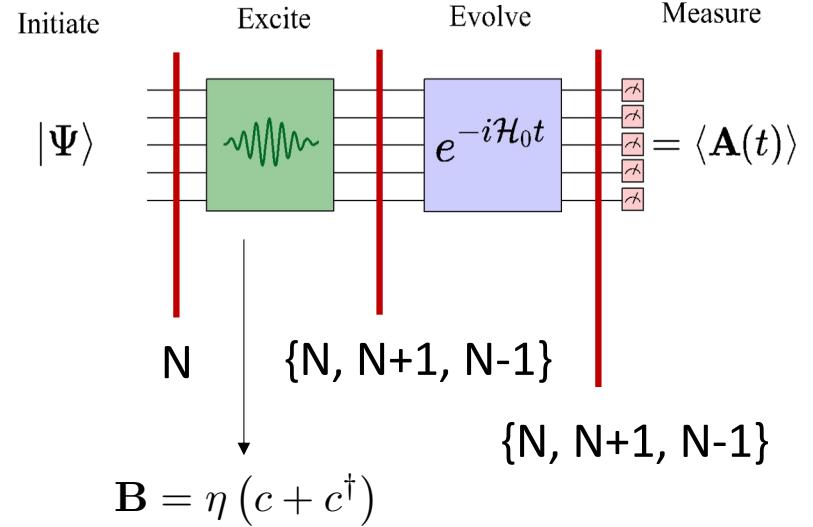
Then:

$$\begin{aligned} G(t, t') &= -i\theta(t-t')\langle\psi_0|\{\mathbf{A}(t), \mathbf{B}(t')\}|\psi_0\rangle \\ &= \frac{i}{s}\theta(t-t')\langle\psi_0|[\mathbf{A}(t)\mathbf{P}(t), \mathbf{B}(t')]\rangle\psi_0 \end{aligned}$$

Example: parity

$$\mathbf{P} = Z_1 Z_2 \dots Z_n$$

Option 2: Post-selection



Post-selection on particle number gives us

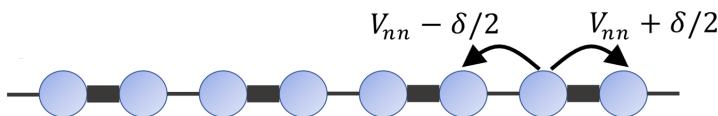
$$G_{ij}^<(t) = i \langle\psi_0|c_j^\dagger(0)c_i(t)|\psi_0\rangle$$

$$G_{ij}^>(t) = -i \langle\psi_0|c_i(t)c_j^\dagger(0)|\psi_0\rangle$$

Linear Response -> Green's function

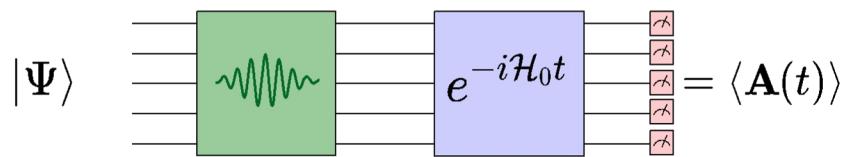
2302.10219

Su-Schrieffer-Heeger model for polyacetylene

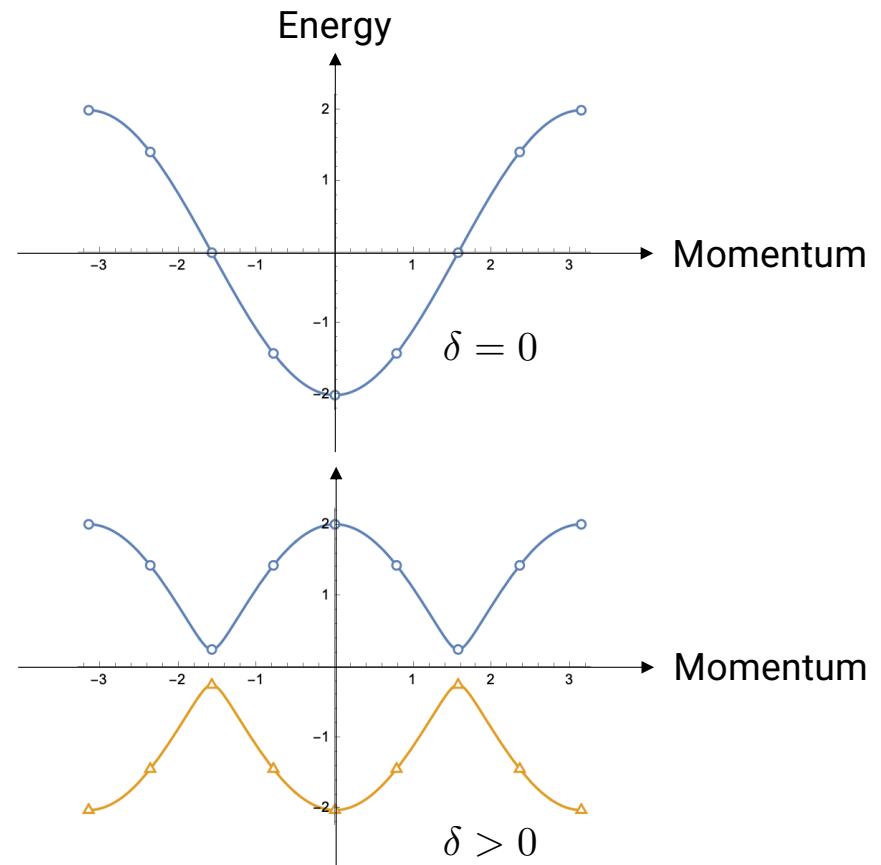


$$\mathcal{H}_0 = - \sum_{\langle i,j \rangle} \left[V_{nn} + (-1)^i \delta/2 \right] c_i^\dagger c_j - \mu \sum_i c_i^\dagger c_i$$

Initiate Excite Evolve Measure



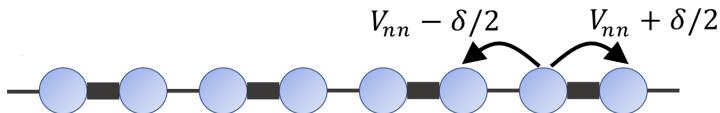
$$G^R(r_i, t; r_j, t') = -i\theta(t - t') \langle \psi_0 | \{c_i(t), c_j^\dagger(t')\} | \psi_0 \rangle$$



Linear Response -> Green's function

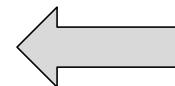
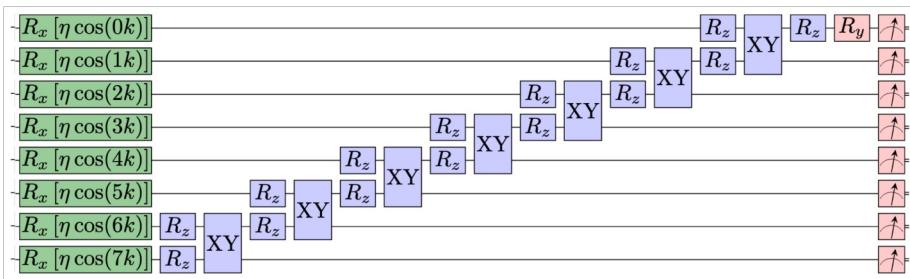
2302.10219

Su-Schrieffer-Heeger model for polyacetylene



$$\mathcal{H}_0 = - \sum_{\langle i,j \rangle} \left[V_{nn} + (-1)^i \delta/2 \right] c_i^\dagger c_j - \mu \sum_i c_i^\dagger c_i$$

Compressed circuit run on *ibm_auckland*



$$\mathbf{B} = \sum_i 2 \cos(kr_i) \left[c_i + c_i^\dagger \right]$$

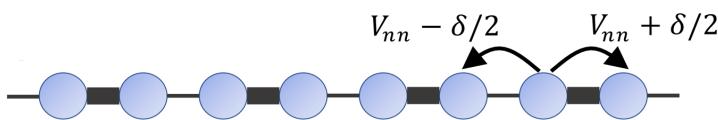
Choose **B** to create a momentum eigenstate

$$G_k^R(t) = -i\theta(t) \langle \psi_0 | \{c_k(t), c_k^\dagger(0)\} | \psi_0 \rangle$$

Linear Response -> Green's function

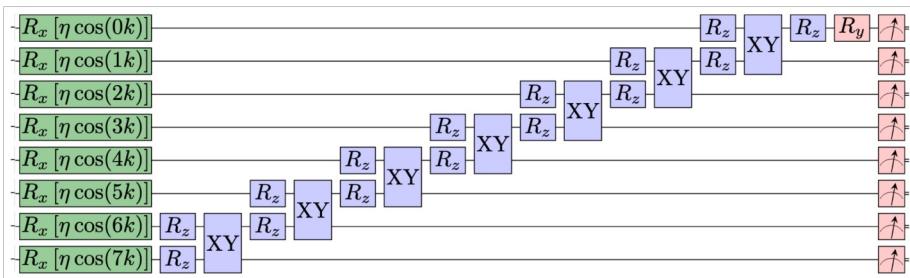
2302.10219

Su-Schrieffer-Heeger model for polyacetylene



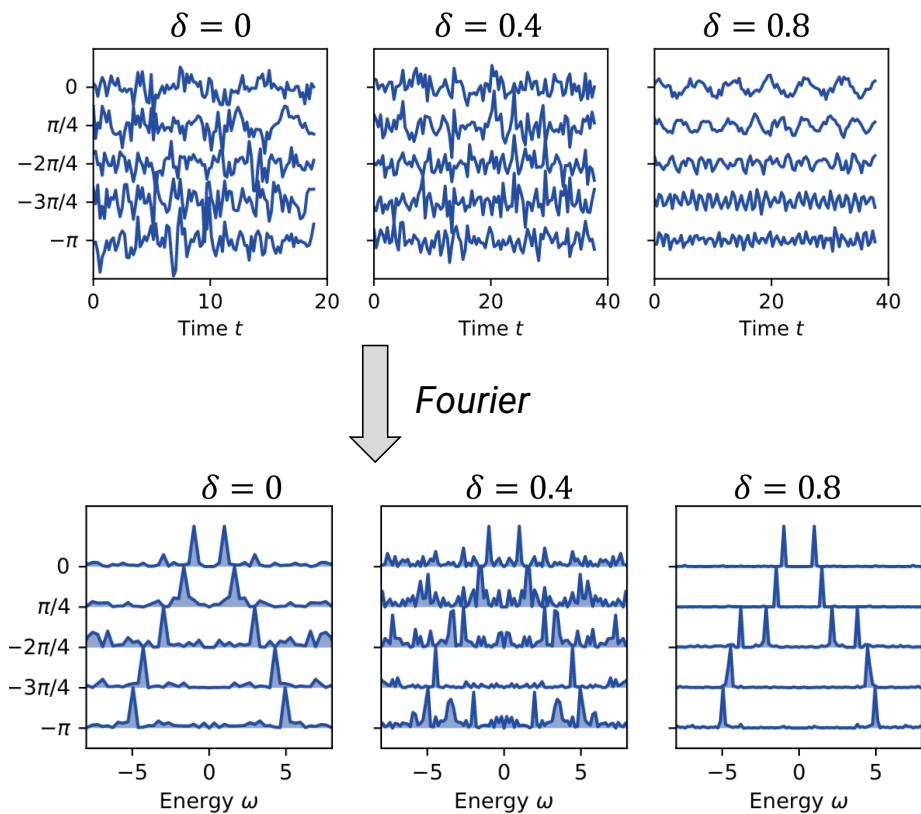
$$\mathcal{H}_0 = - \sum_{\langle i,j \rangle} \left[V_{nn} + (-1)^i \delta/2 \right] c_i^\dagger c_j - \mu \sum_i c_i^\dagger c_i$$

Compressed circuit run on *ibm_auckland*



Choose **B** to create a momentum eigenstate

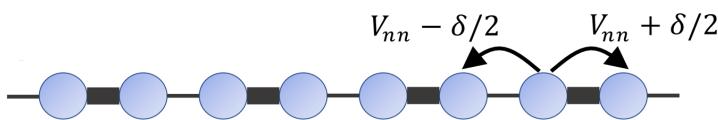
$$G_k^R(t) = -i\theta(t) \langle \psi_0 | \{c_k(t), c_k^\dagger(0)\} | \psi_0 \rangle$$



Linear Response -> Green's function

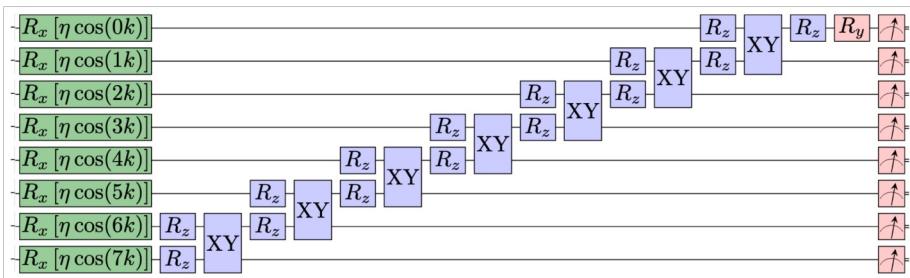
2302.10219

Su-Schrieffer-Heeger model for polyacetylene



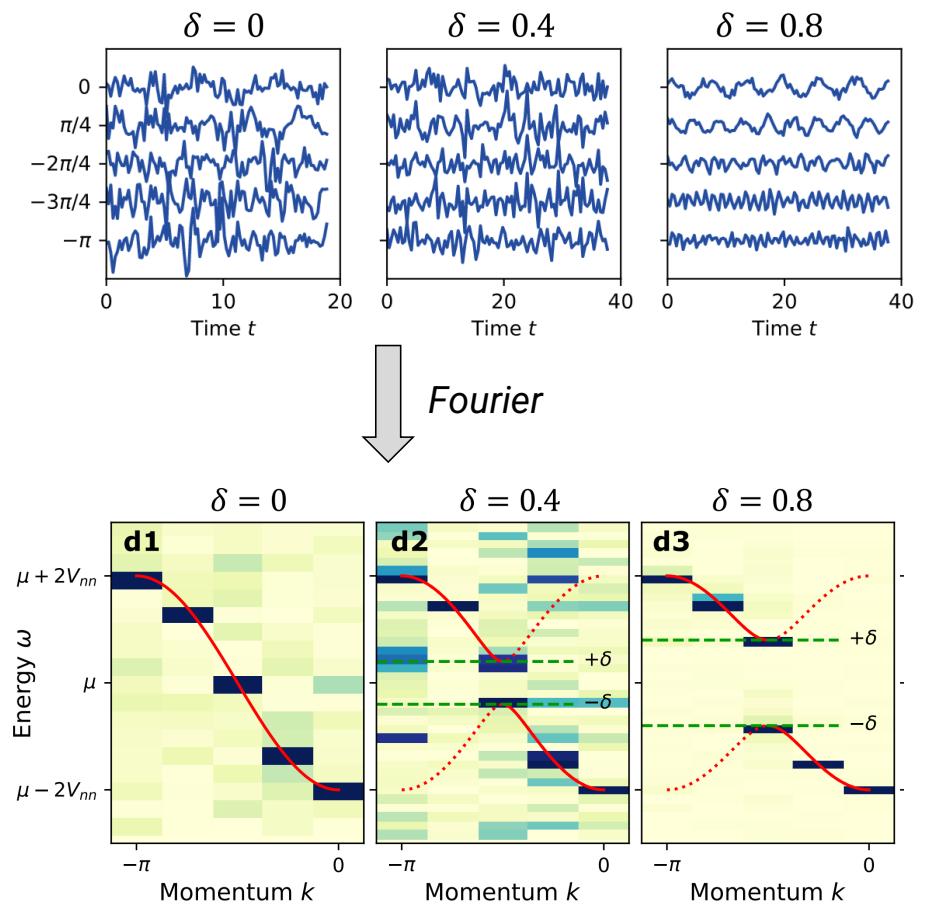
$$\mathcal{H}_0 = - \sum_{\langle i,j \rangle} \left[V_{nn} + (-1)^i \delta/2 \right] c_i^\dagger c_j - \mu \sum_i c_i^\dagger c_i$$

Compressed circuit run on *ibm_auckland*



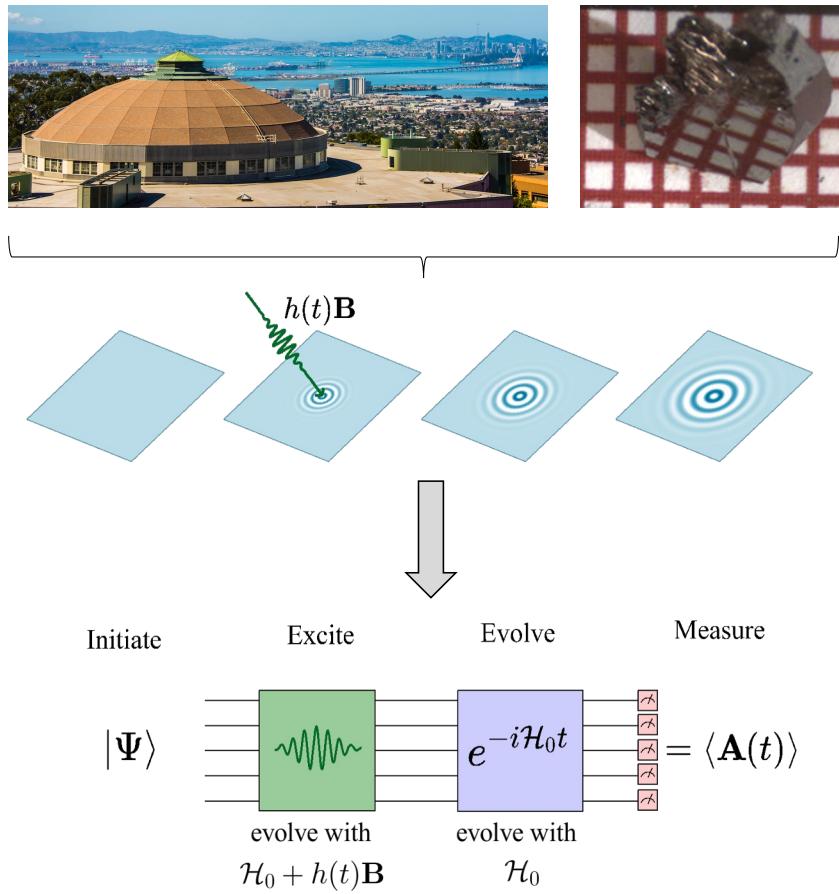
Choose **B** to create a momentum eigenstate

$$G_k^R(t) = -i\theta(t)\langle\psi_0|\{c_k(t), c_k^\dagger(0)\}|\psi_0\rangle$$

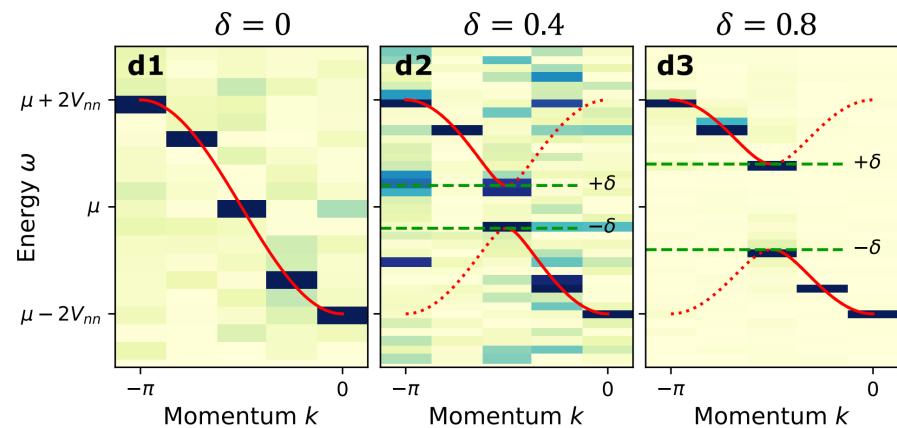


Linear Response

Digital version of
this talk



- Ancilla free
- Momentum and frequency selectivity
- Both bosonic and fermionic correlators
- More noise robust compared to existing methods

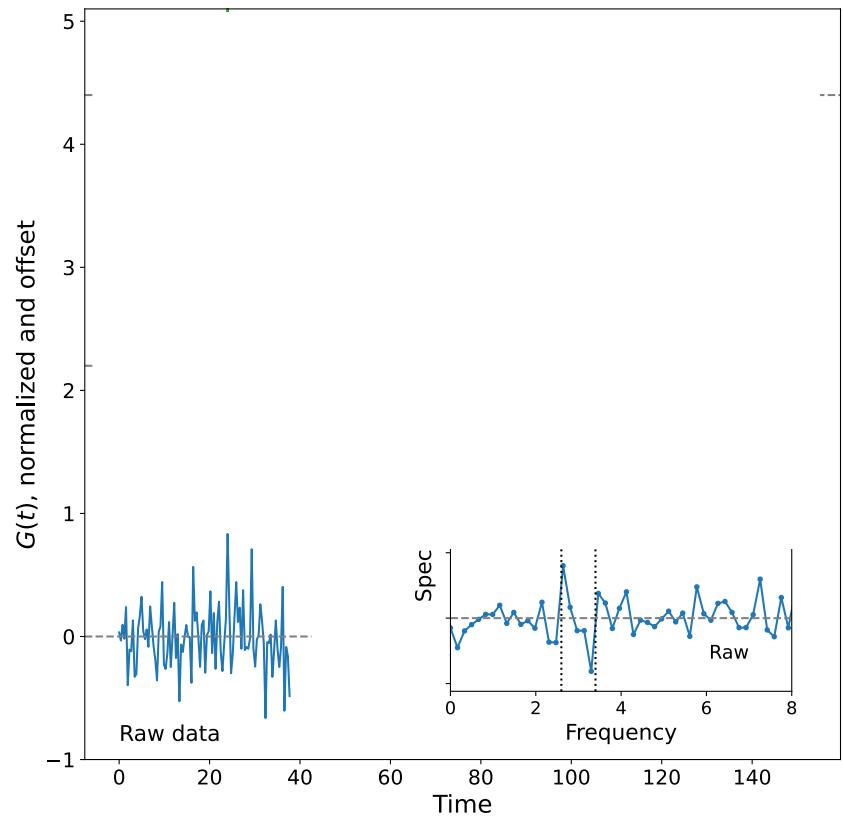


E. Kökcü, H. Labib, J.K. Freericks, AFK., arXiv:2302.10219

Further improvements via mathematics

- It turns out that these are positive semi-definite functions:

$$\langle A^\dagger(t)A(t') \rangle$$

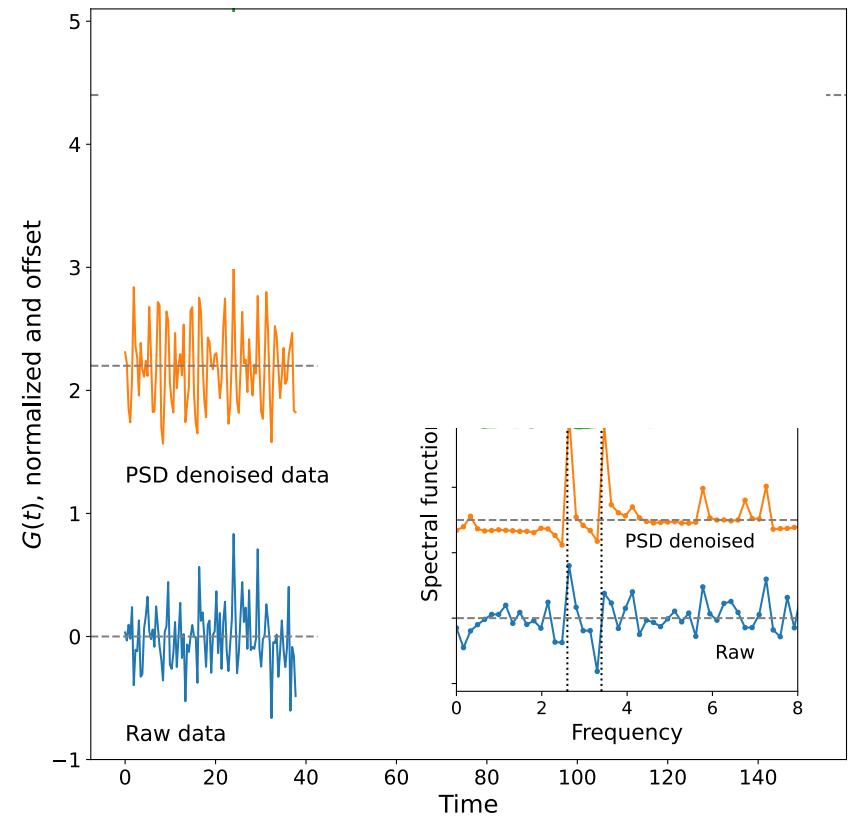


Further improvements via mathematics

- It turns out that these are positive semi-definite functions:

$$\langle A^\dagger(t)A(t') \rangle$$

- We can project the noisy data onto the nearest PSD function

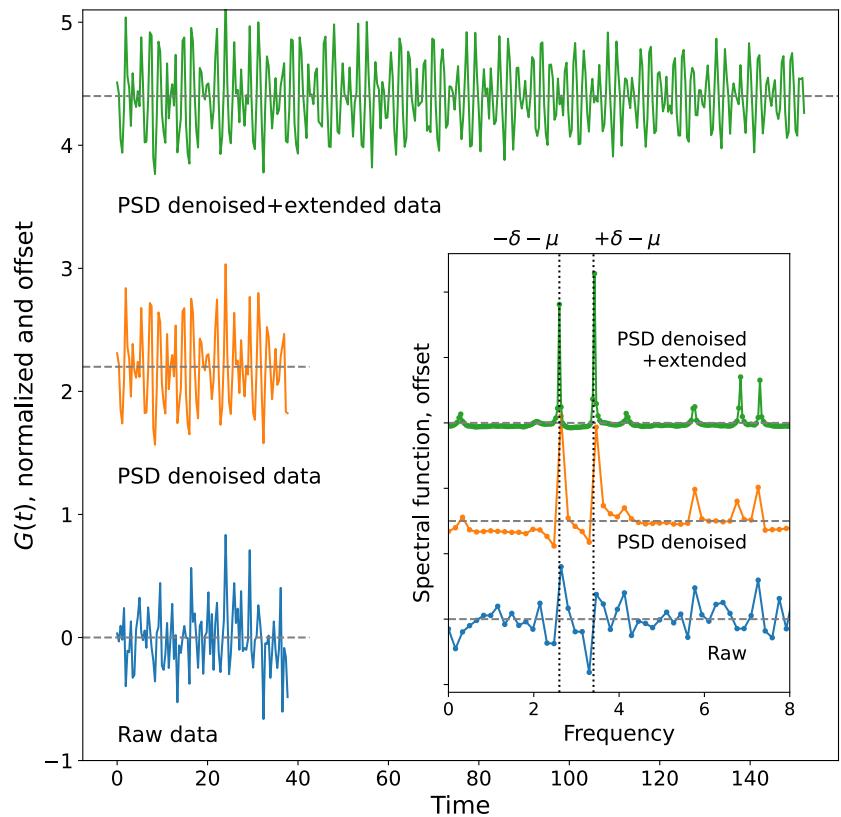


Further improvements via mathematics

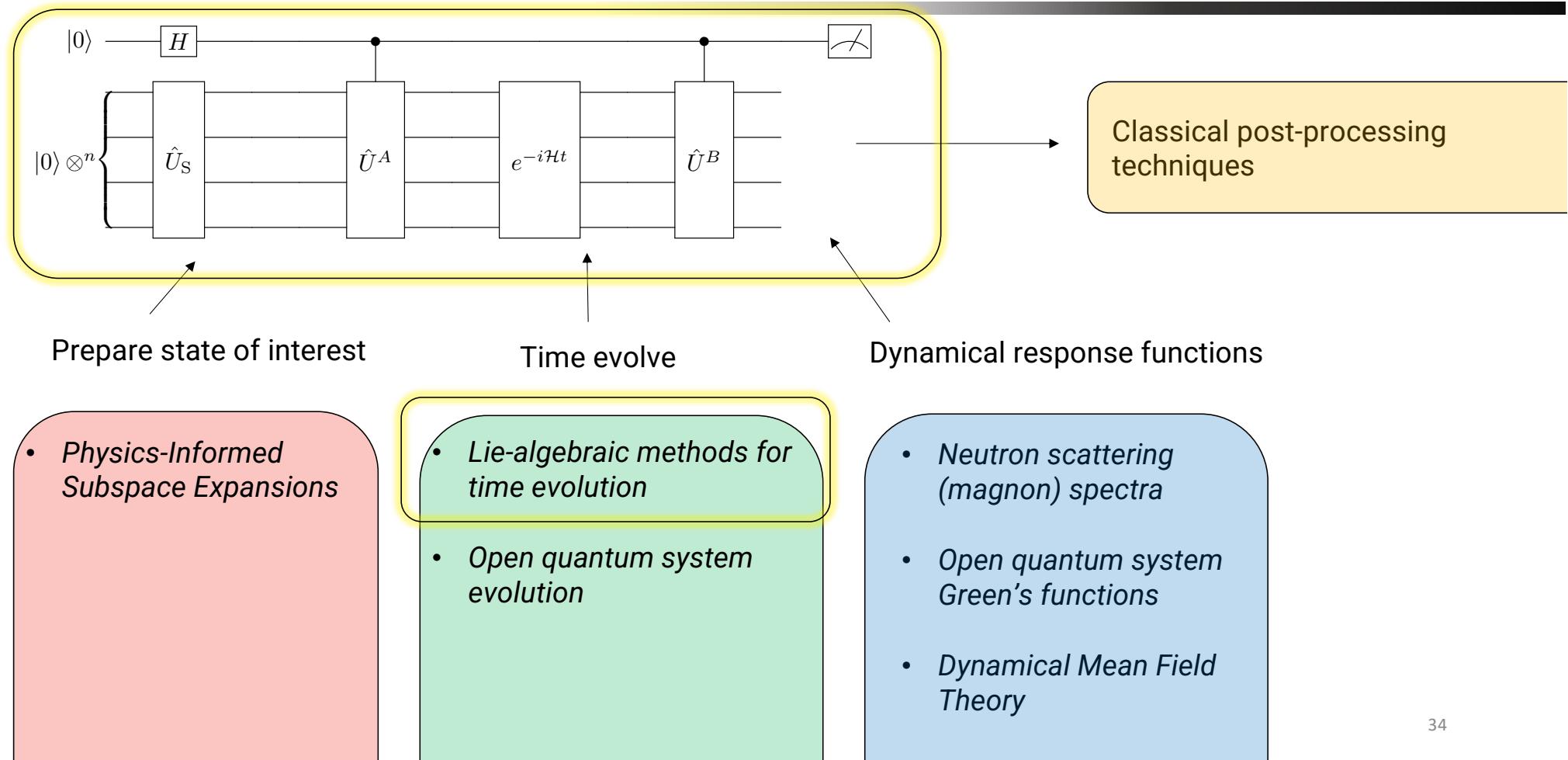
- It turns out that these are positive semi-definite functions:

$$\langle A^\dagger(t)A(t') \rangle$$

- We can project the noisy data onto the nearest PSD function
- Given sufficiently dense data, a unique extension exists* and we can extend the data to longer times

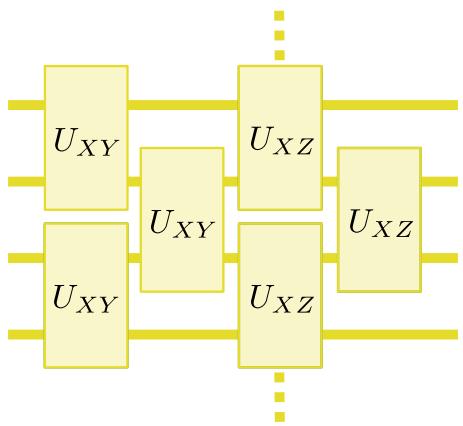


A-Z quantum simulation

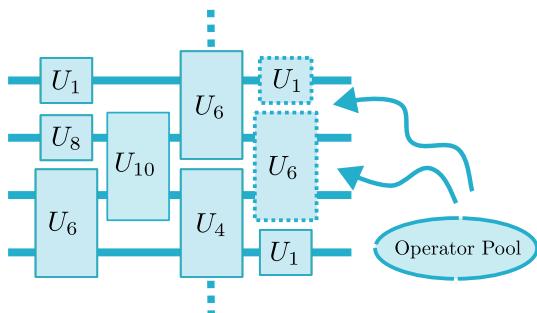


Lie algebraic methods for quantum computing

Time evolution



Variational ansätze



Dynamical Lie algebras

Given a set of operators a_i (either in the operator pool or Hamiltonian)

Their Dynamical Lie Algebra expresses all the operators that can be generated by this set

$$\text{DLA} := \text{span}\left\{ [a_{i_1}, [a_{i_2}, [\cdots [a_{i_r}, a_j] \cdots]]] \right\}$$

Cartan decomposition for exact time evolution

Kökcü, PRL 2022

Circuit compression

Kökcü, PRA 2022

Camps, SIMAX 2022

Kökcü, arXiv:2303.09538

Unified Framework for Barren plateaus in VQA

Ragone, arXiv:2309.09342

Complete (DLA) classification of 1-d nearest neighbor spin models

Wiersema, arXiv:2309.05690

Unitary Synthesis: Cartan Decomposition

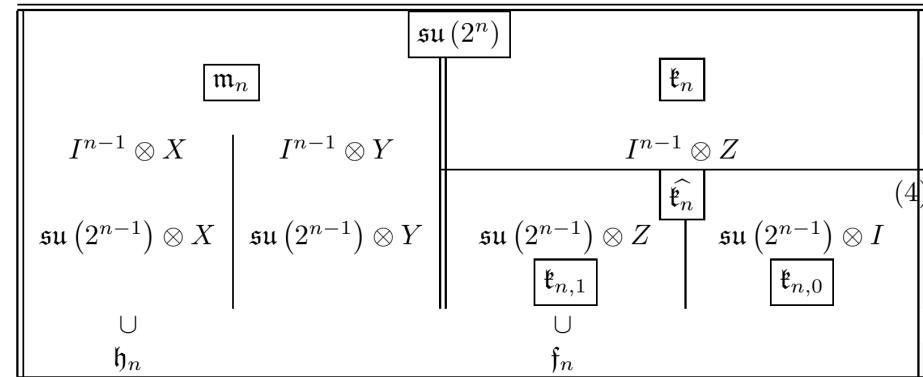
- Cartan decomposition found its application in generic unitary synthesis for quantum circuits (*, **)

$$\mathfrak{g} = \mathfrak{m} \oplus \mathfrak{k}$$

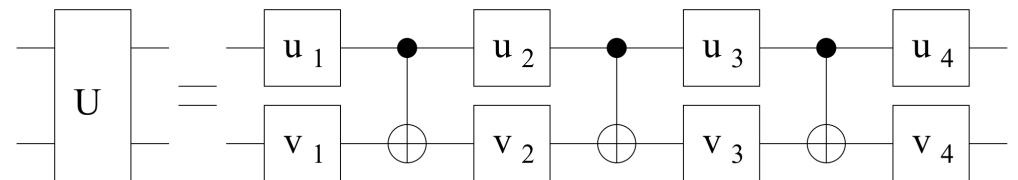
$$[\mathfrak{k}, \mathfrak{k}] \subset \mathfrak{k}$$

$$[\mathfrak{m}, \mathfrak{k}] = \mathfrak{m}$$

$$[\mathfrak{m}, \mathfrak{m}] \subset \mathfrak{k}.$$



$$I^{n-1} = I^{\otimes(n-1)} = \underbrace{I \otimes \dots \otimes I}_{n-1}$$



(*) N. Khaneja and S. J. Glaser, Chemical Physics 267, 11 (2001).

(**) H. N. Sa Earp and J. K. Pachos, Journal of Mathematical Physics 46, 082108 (2005), doi.org/10.1063/1.2008210.

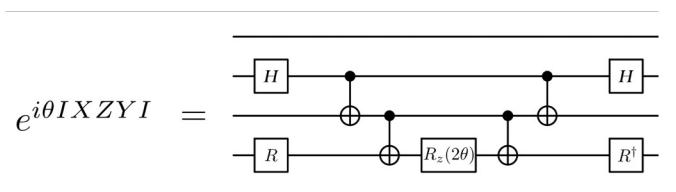
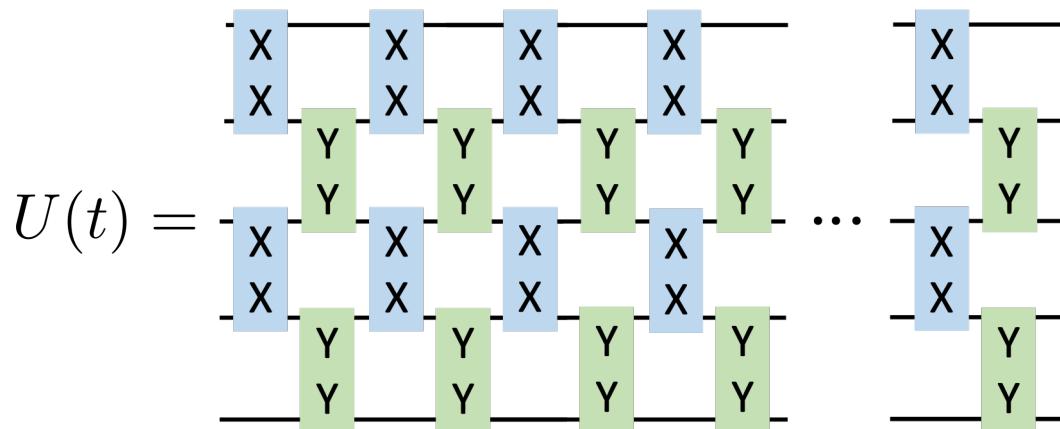
(***) G. Vidal and C. M. Dawson, Physical Review A 69, 010301 (2004).

Main Problem

Exact simulation of a time independent spin Hamiltonian: $\mathcal{H} = \sum_j h_j \sigma^j$

$$\mathcal{H} = a XXIII + b IYYII + c IIXXI + d IIIYY$$

$$U(\epsilon) = e^{-i\epsilon\mathcal{H}} = e^{-i\epsilon a} XXIII e^{-i\epsilon b} IYYII e^{-i\epsilon c} IIXXI e^{-i\epsilon d} IIIYY + O(\epsilon^2)$$

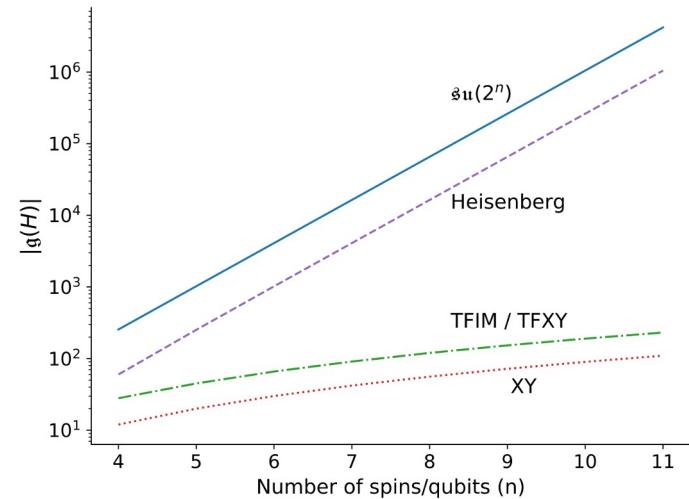
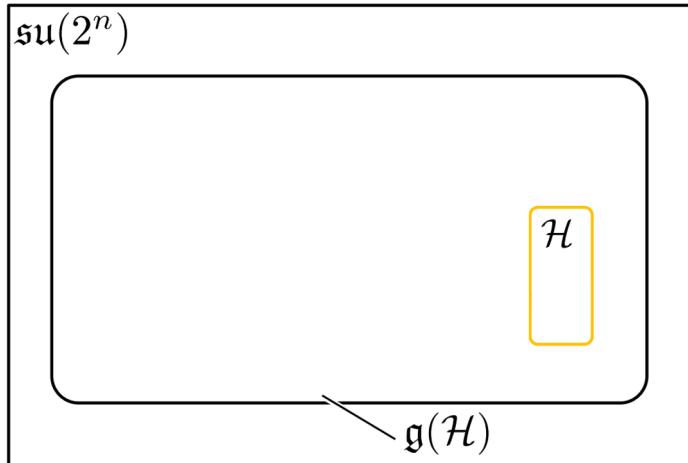


Main Problem

Exact simulation of a time independent spin Hamiltonian: $\mathcal{H} = \sum_j h_j \sigma^j$

$$U(t) = e^{-it\mathcal{H}} = \prod_{\substack{\bar{\sigma}^i \in \mathfrak{su}(2^n) \\ \bar{\sigma}^i \in \mathfrak{g}(\mathcal{H})}} e^{i\kappa_i \bar{\sigma}^i}$$

$$\text{DLA} := \text{span}\{[a_{i_1}, [a_{i_2}, [\cdots [a_{i_r}, a_j] \cdots]]]\}$$



Cartan Decomposition and KHK Theorem

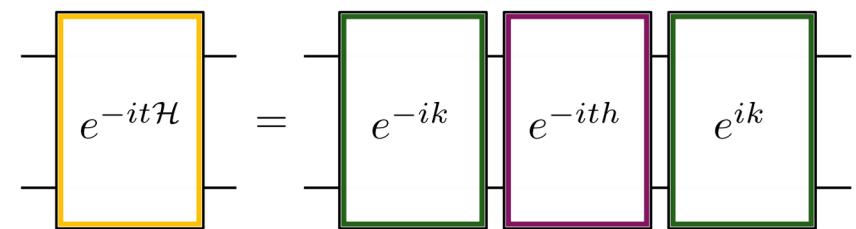
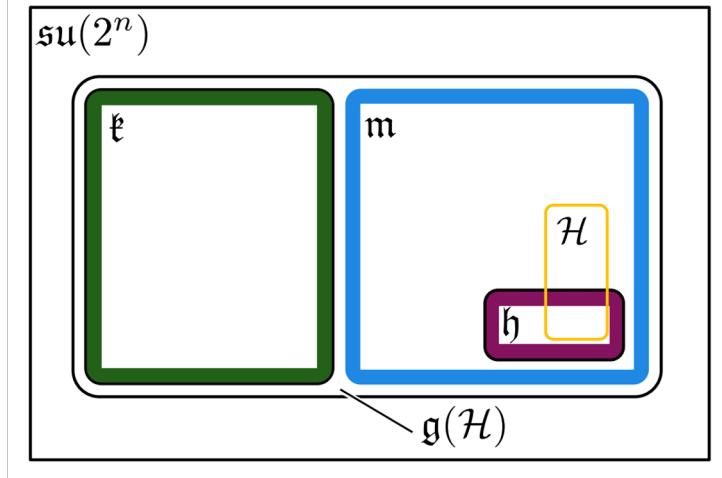
Definition 1 Consider a compact semi-simple Lie subgroup $G \subset SU(2^n)$, which has a corresponding Lie subalgebra \mathfrak{g} . A **Cartan decomposition** on \mathfrak{g} is defined as an orthogonal split $\mathfrak{g} = \mathfrak{k} \oplus \mathfrak{m}$ satisfying

$$[\mathfrak{k}, \mathfrak{k}] \subset \mathfrak{k} \quad [\mathfrak{m}, \mathfrak{m}] \subset \mathfrak{k} \quad [\mathfrak{k}, \mathfrak{m}] = \mathfrak{m} \quad (4)$$

and is referred as $(\mathfrak{g}, \mathfrak{k})$. **Cartan subalgebra** of this decomposition is defined as one of the maximal Abelian subalgebras of \mathfrak{m} , and denoted as \mathfrak{h} .

Theorem 1 Given a Cartan decomposition $\mathfrak{g} = \mathfrak{k} \oplus \mathfrak{m}$, for any element $\mathcal{H} \in \mathfrak{m}$ there exist a $K \in e^{\mathfrak{k}}$ and $h \in \mathfrak{h}$ such that

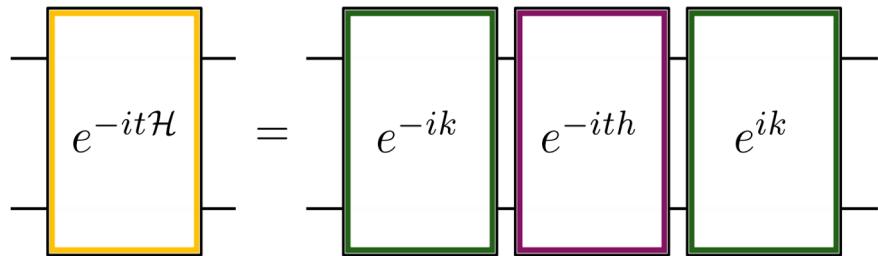
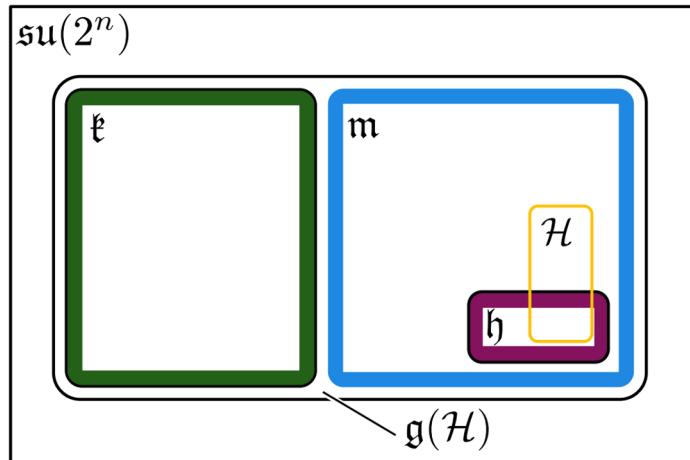
$$\mathcal{H} = KhK^\dagger \quad (5)$$



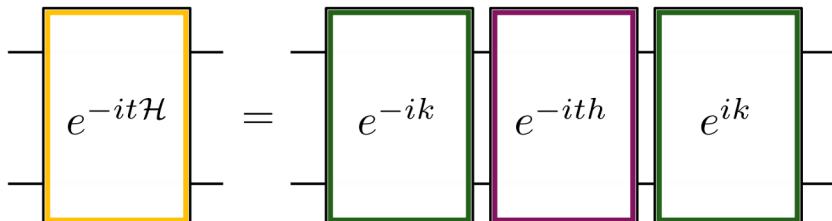
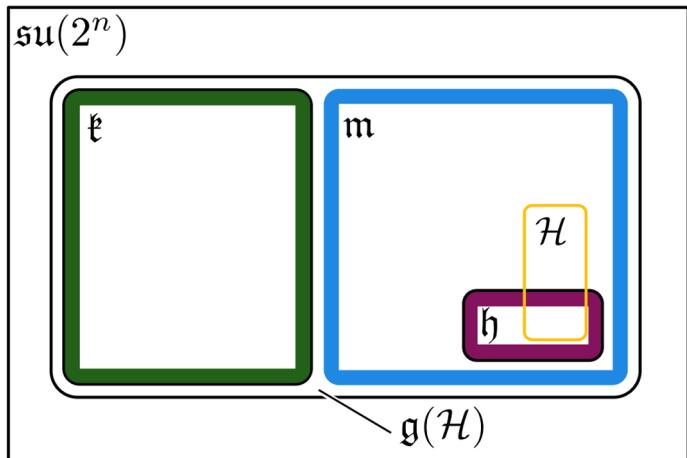
Main Problem

Exact simulation of a time independent spin Hamiltonian: $\mathcal{H} = \sum_j h_j \sigma^j$

$$U(t) = e^{-it\mathcal{H}} = \prod_{\substack{\bar{\sigma}^i \in \mathfrak{su}(2^n) \\ \bar{\sigma}^i \in \mathfrak{g}(\mathcal{H})}} e^{i\kappa_i \bar{\sigma}^i}$$



Cartan Decomposition and KHK Theorem



$$U(t) = e^{-it\mathcal{H}} = \prod_{\substack{\bar{\sigma}^i \in \mathfrak{su}(2^n) \\ \bar{\sigma}^i \in \mathfrak{g}(\mathcal{H})}} e^{i\kappa_i \bar{\sigma}^i}$$

Have $H \in \mathfrak{m}$, and consider the following function

$$f(K) = \langle KvK^\dagger H \rangle$$

where

$$K = e^{\theta_1 k_1} e^{\theta_2 k_2} \dots e^{\theta_{n_k} k_{n_k}}$$

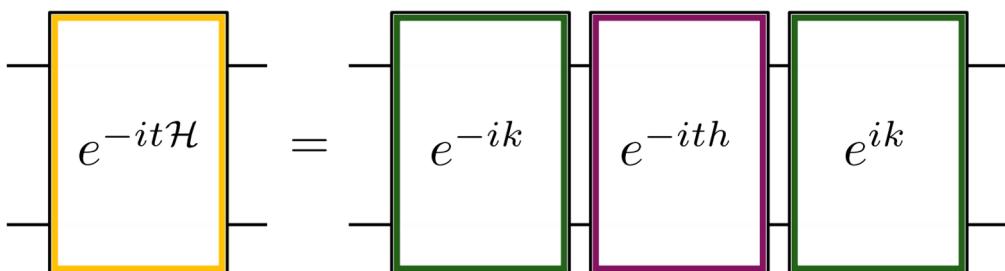
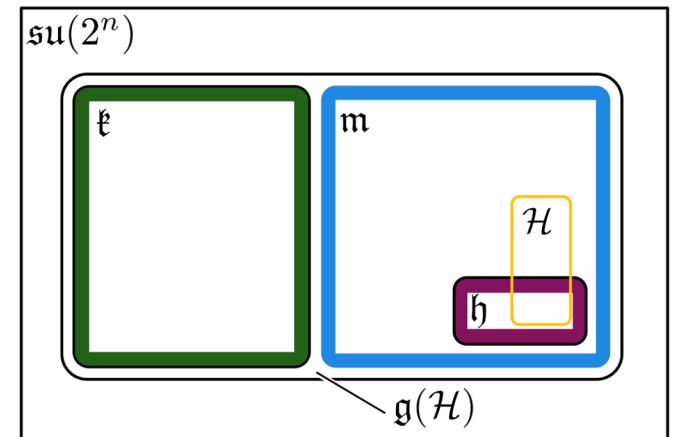
$$v = h_1 + \pi h_2 + \pi^2 h_3 + \dots + \pi^{n_h-1} h_{n_h}$$

Then for any local minimum or maximum of the function f denoted by K_0 will satisfy

$$K_0^\dagger H K_0 \in \mathfrak{h}$$

Algorithm

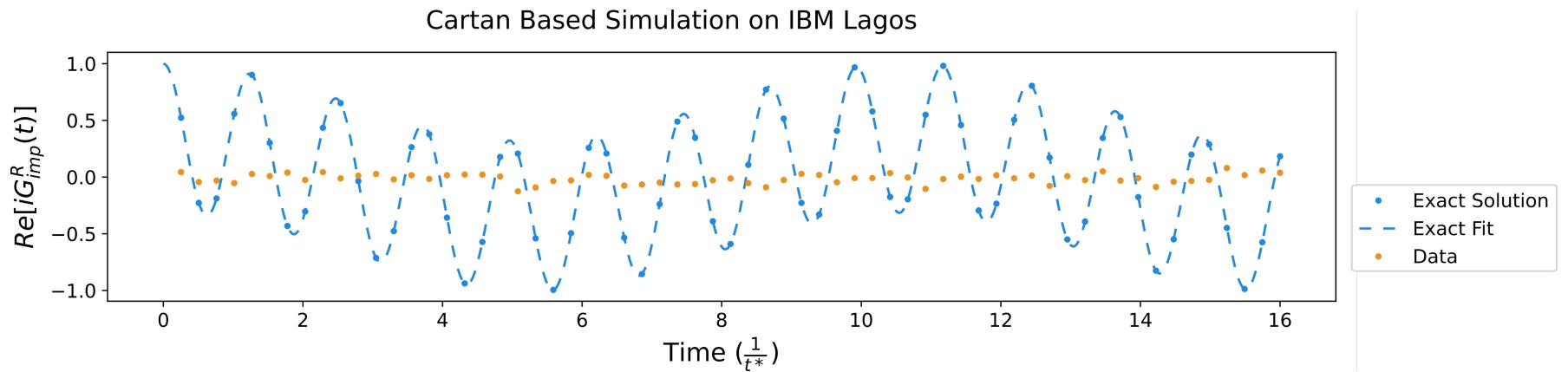
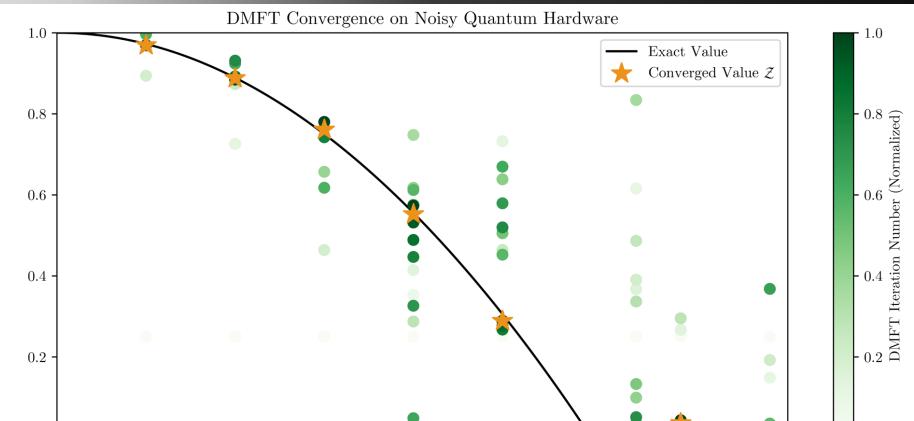
- 1) Generate Hamiltonian algebra $\mathfrak{g}(H)$
- 2) Find a Cartan decomposition where H is in \mathfrak{m}
- 3) Obtain parameters via **local** minimum of $f(K)$
- 4) Build the circuit using K and h
- 5) Then simulate for any t



$$f(K) = \langle KvK^\dagger, \mathcal{H} \rangle$$

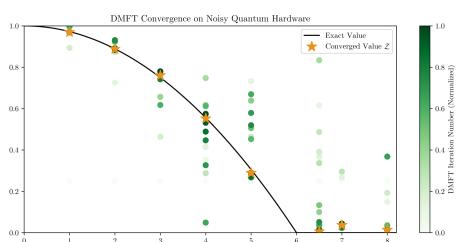
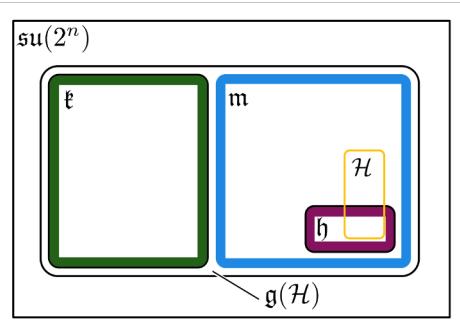
Cartan Decomposition

- $O(n^2)$ circuit for TFIM, TFXY, XY
- Applicable for any model
- Optimize only once for any time t
- Obtained 1st ever self-consistent DMFT Hubbard phase diagram on IBM QC.



2 Algebraic methods for circuit compression

Cartan Decomposition



- Produces exact, fixed depth time evolution unitaries for any model.
- Produces unitaries for linear combinations of (anti)-Hermitian operators (UCC factors).
- We have code available!
<https://github.com/kemperlab/cartan-quantum-synthesizer>

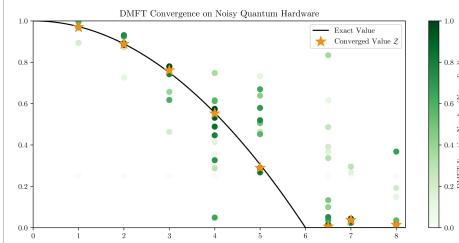
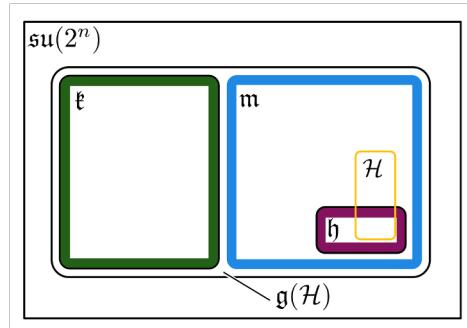
Kökcü PRL (2022), Steckmann PRR (2023)

Algebraic Compression

Kökcü PRA (2021), Camp SIMAX 2022, Kökcü arXiv:2303.09538

2 Algebraic methods for circuit generation

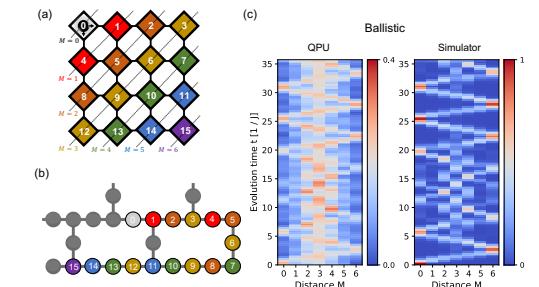
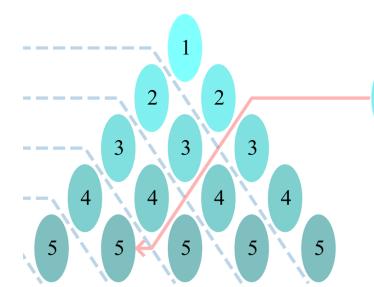
Cartan Decomposition



- Produces exact, fixed depth time evolution unitaries for any model.
- Produces unitaries for linear combinations of (anti)-Hermitian operators (UCC factors).
- We have code available!
<https://github.com/kemperlab/cartan-quantum-synthesizer>

Kökcü PRL (2022), Steckmann PRR (2023)

Algebraic Compression

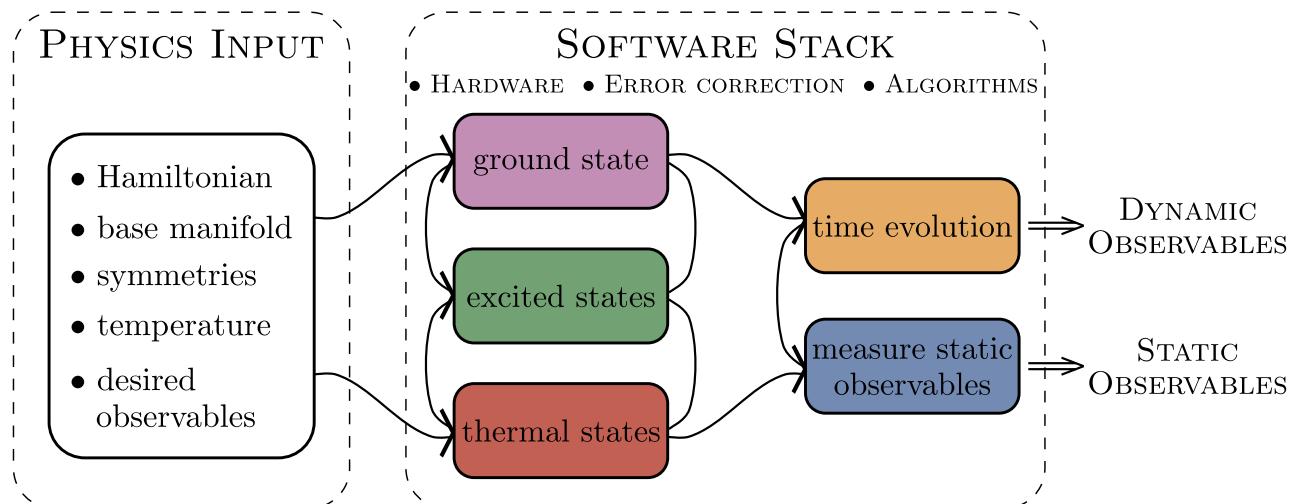


- Compressed Trotter circuits down to a shallow fixed depth circuit for 1-D nearest neighbor TFXY, TFIM, XY and Kitaev models.
- Based on 3 easy to check, local properties.
- We have code available! Check F3C, F3C++ and F3Cpy at <https://github.com/QuantumComputingLab>

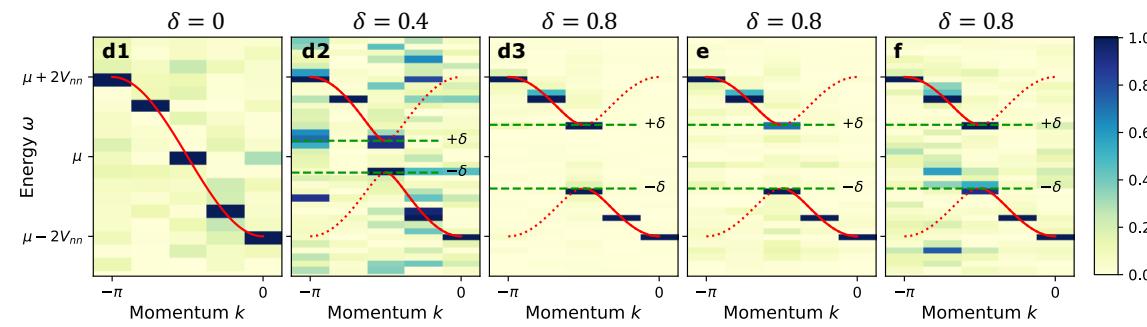
Kökcü PRA (2021), Camp SIMAX 2022, Kökcü arXiv:2303.09538

Quantum Matter meets Quantum Computing

Digital version of
this talk



<https://go.ncsu.edu/kemper-lab>



- Experimental relevance:
Measuring correlation functions
- Measuring exact integer Chern numbers for topological states
- Open quantum evolution and fixed points (1000 Trotter steps)
- Time evolution via Lie algebraic decomposition and compression
- Thermodynamics via Lee-Yang Zeros
- Physics-Informed Subspace Expansions