

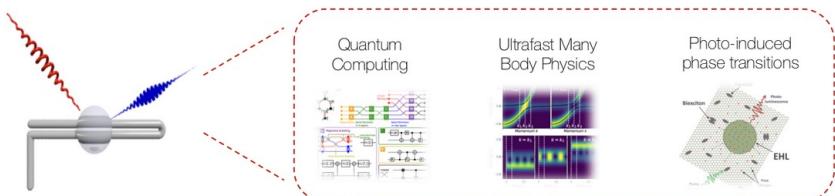
Quantum Information meets Quantum Matter

Alexander (Lex) Kemper

 Department of Physics
North Carolina State University
<https://go.ncsu.edu/kemper-lab>

UNC Chapel Hill Colloquium
11/20/2023





Kemper Lab

Quantum materials in and out of equilibrium.

Collaborations with:

- Bojko Bakalov (NCSU)
- Marco Cerezo, Martin de la Rocca (LANL)
- Jim Freericks (Georgetown)
- Daan Camps, Roel van Beeumen, Bert de Jong, Akhil Francis (LBNL)
- Thomas Steckmann (UMD)
- Yan Wang, Eugene Dumitrescu (ORNL)

Current members



Alexander (Lex)
Kemper
Principal investigator



Efekan Kökçü
Graduate Researcher



Anjali Agrawal
Graduate Researcher



Heba Labib
Graduate Researcher



Jack Howard
Undergraduate
Researcher



Natalia Wilson
Undergraduate
Researcher



Daniel Brandon
Undergraduate
Researcher



Sarah Klas
Undergraduate
Researcher



Norman Hogan
Graduate Researcher



Ethan Blair
Undergraduate
Researcher



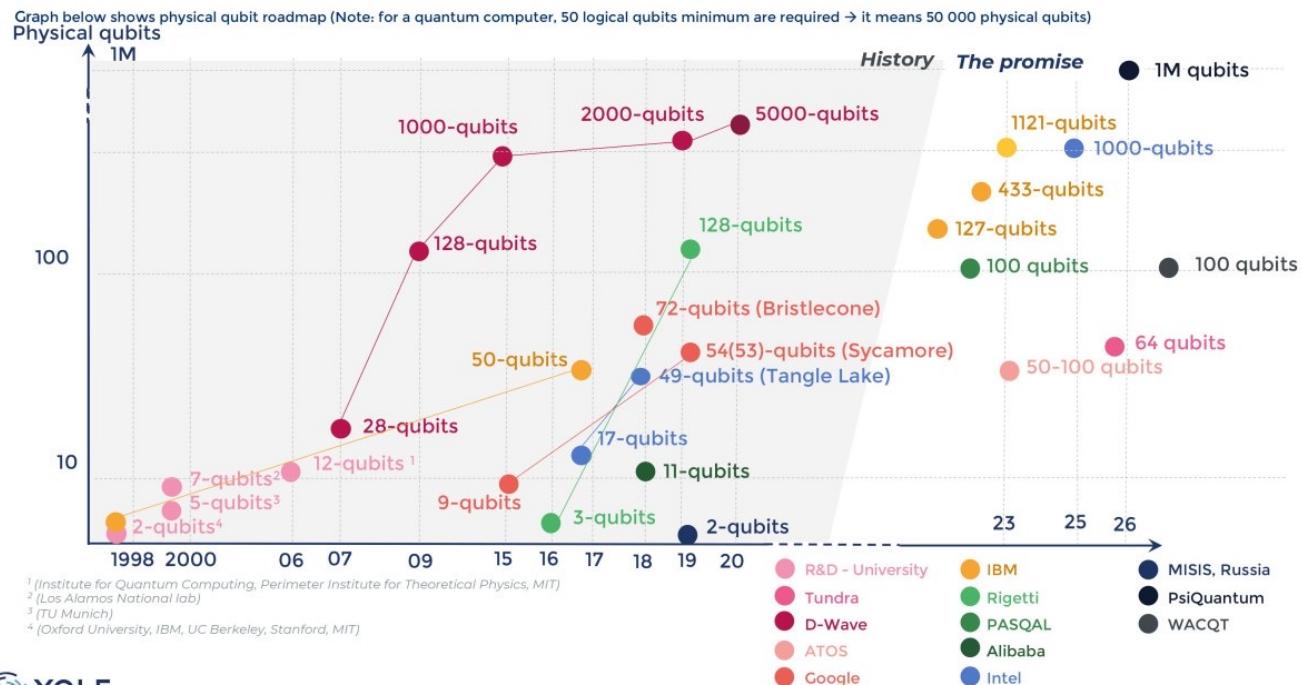
Your Name
New lab member

Brief outline

- Quantum Matter meets Quantum Computing
- Response functions
 - Why we care
 - How do find them
- A different paradigm: Making the experiment part of the simulation via linear response
- Beyond Quantum Simulation

PHYSICAL QUBIT ROADMAP FOR QUANTUM COMPUTER – HISTORY AND FUTURE

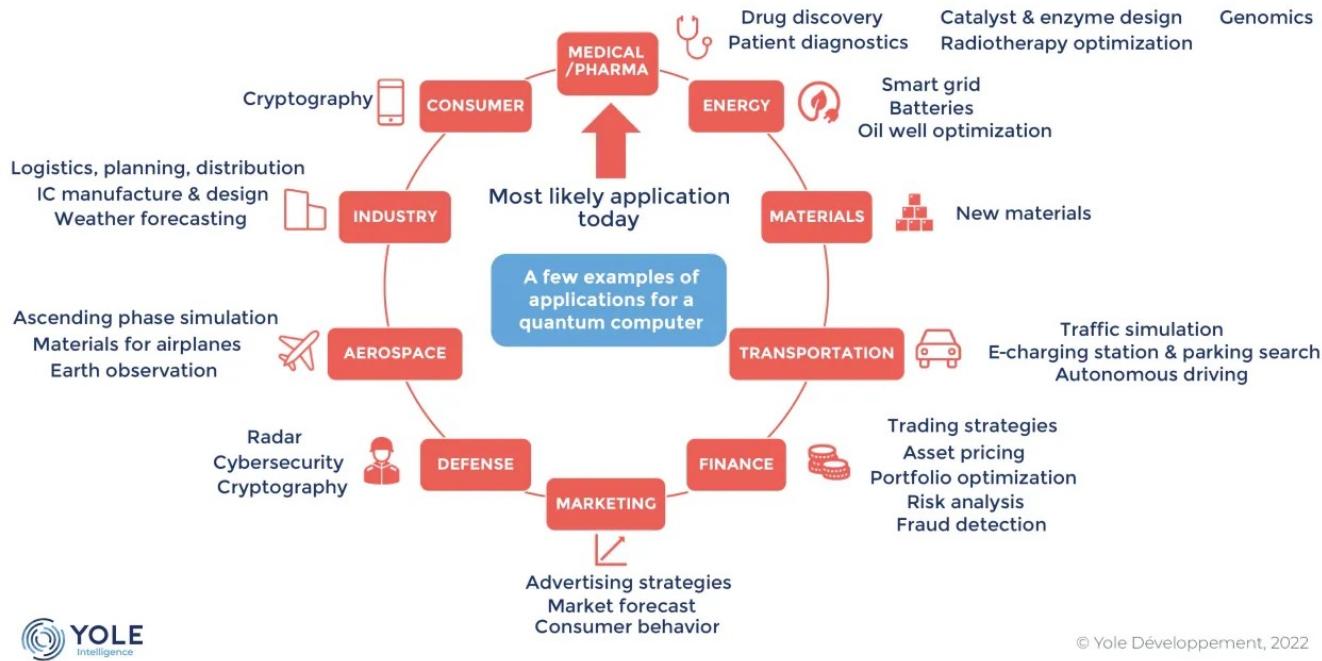
Source: Quantum Technologies report, Yole Développement, 2021



© Yole Développement, 2022

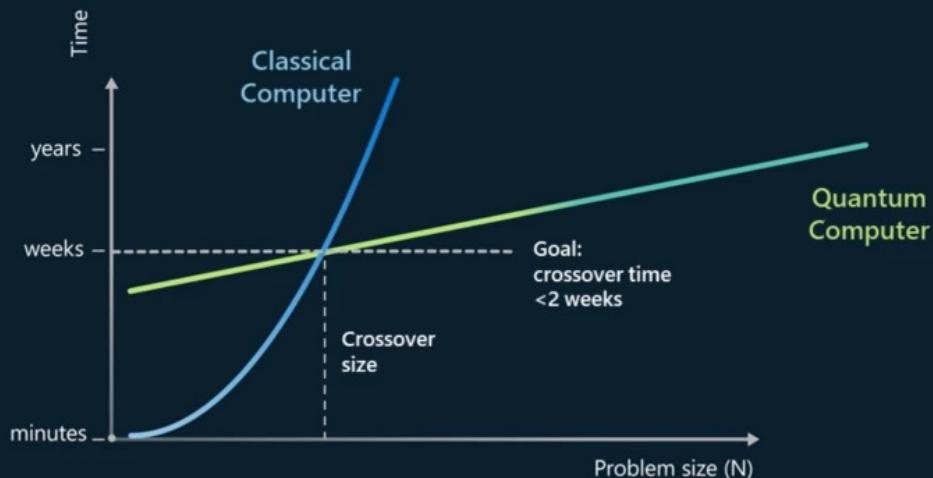
QUANTUM COMPUTING – MULTIPLE COMPLEX PROBLEMS IN MULTIPLE MARKETS

Source: Quantum Technologies report, Yole Développement, 2021

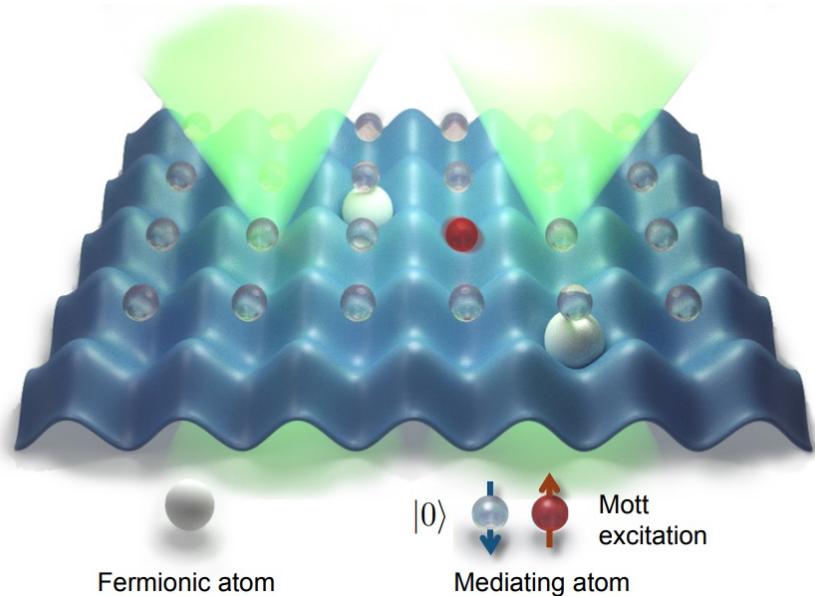




Achieving practical quantum advantage



Bespoke quantum simulator

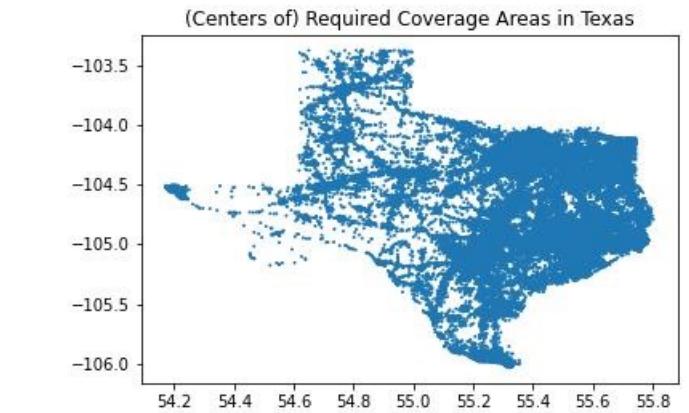
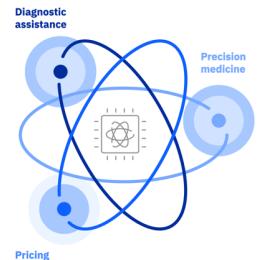


Digital algorithms

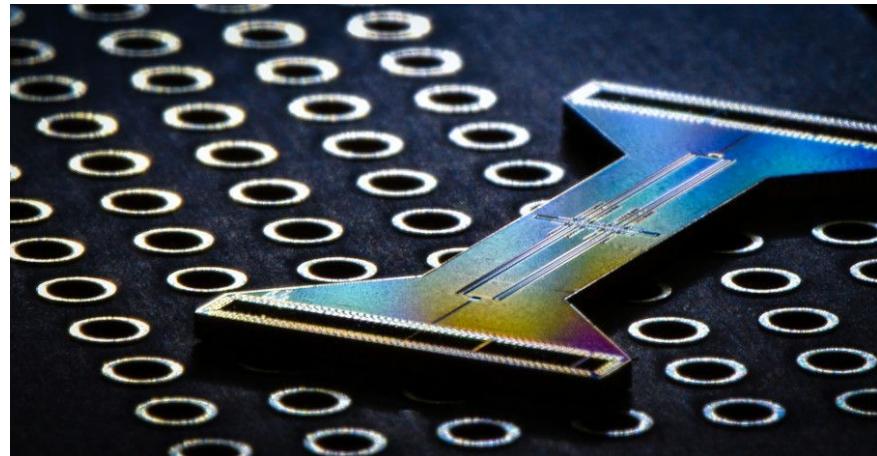


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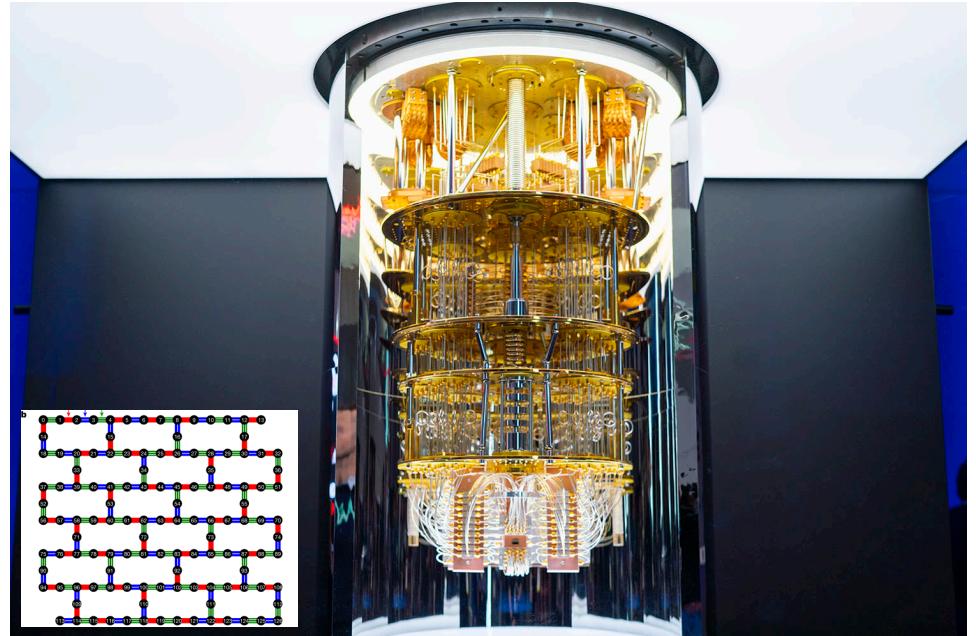
Figure 1
Quantum computers may enable three key healthcare use cases that reinforce each other in a virtuous cycle. For instance, accurate diagnoses enable precise treatments, as well as a better reflection of patient risks in pricing models.



Bespoke quantum simulator



Digital algorithms



Simulating Physics with Computers

Richard P. Feynman

Department of Physics, California Institute of Technology, Pasadena, California 91107

Received May 7, 1981

1. Can classical physics be simulated by a classical computer?
2. Can quantum physics be simulated by a classical computer?
3. Can physics be simulated by a quantum computer?
4. Can a quantum simulation be universal?

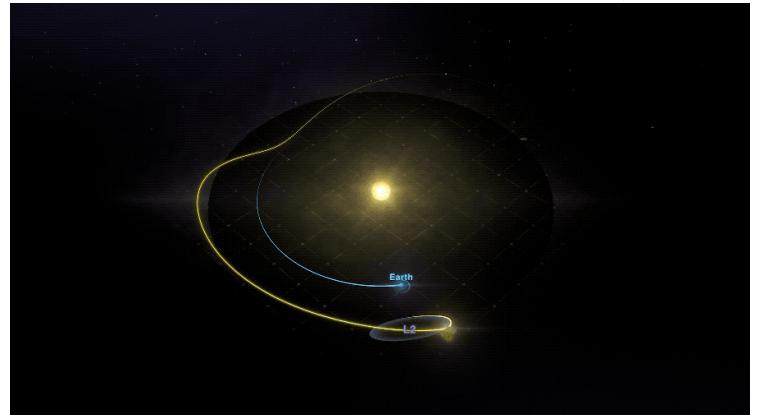
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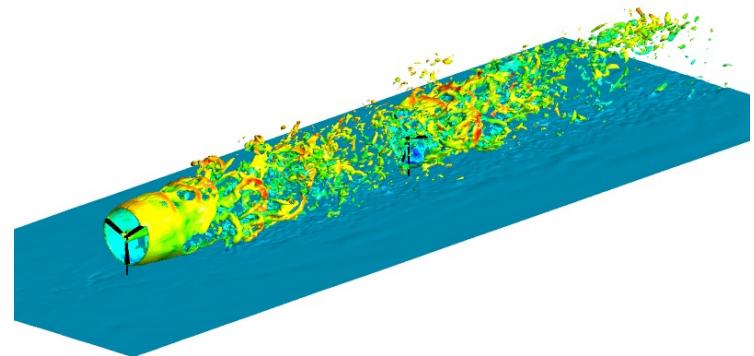
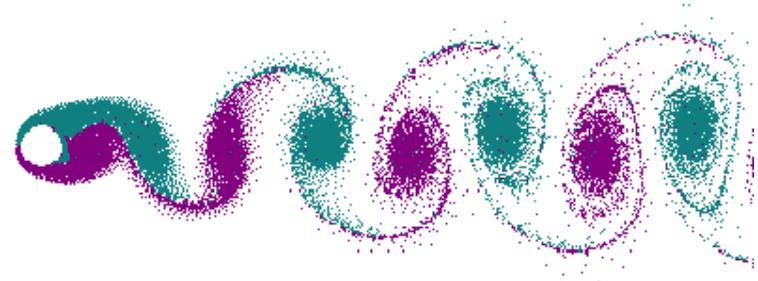
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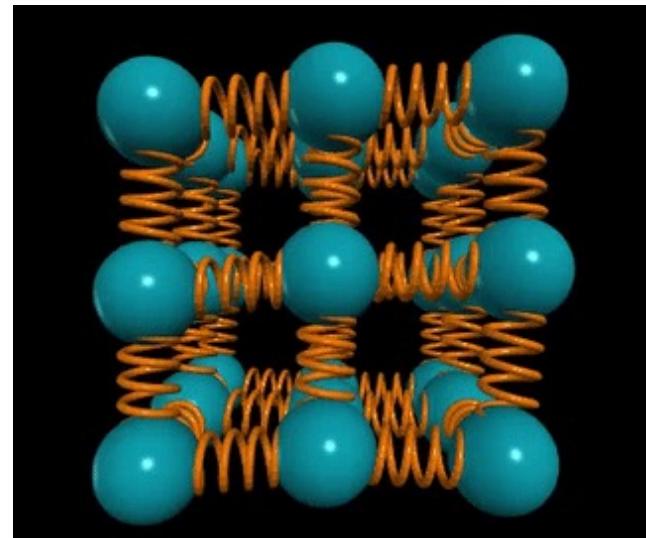
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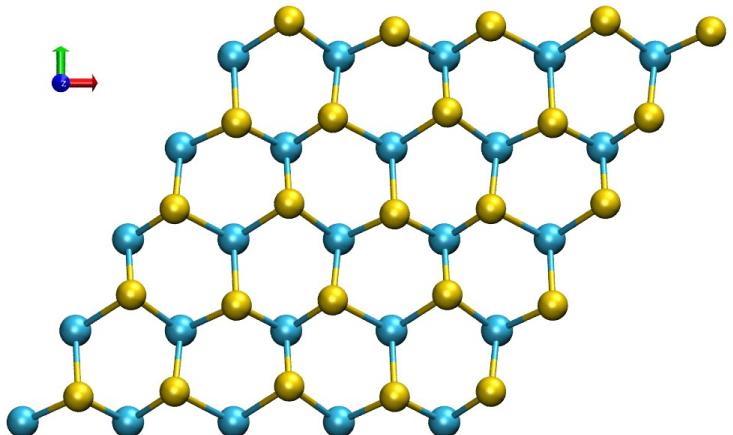
RESEARCH

TOPOLOGICAL MATTER

Observation of chiral phonons

Hanyu Zhu,^{1,2} Jun Yi,¹ Ming-Yang Li,³ Jun Xiao,¹ Lifan Zhang,⁴ Chih-Wen Yang,³
Robert A. Kaindl,² Lain-Jong Li,³ Yuan Wang,^{1,2*} Xiang Zhang^{1,2*}

DOI: [10.1126/science.aar2711](https://doi.org/10.1126/science.aar2711)



Simulating Physics with Computers

Richard P. Feynman

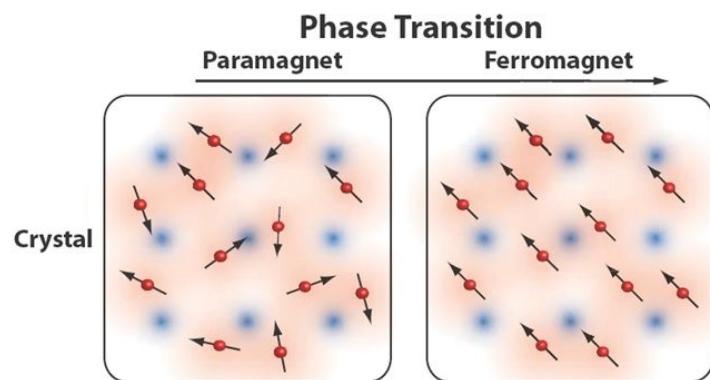
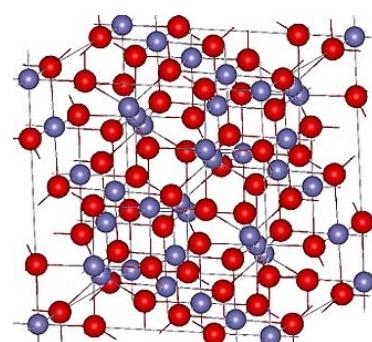
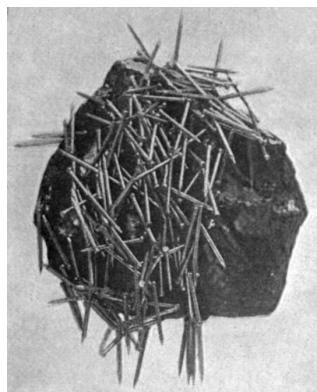
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Magnetite $[\text{Fe}^{2+}(\text{Fe}^{3+})_2(\text{O}^{2-})_4]$

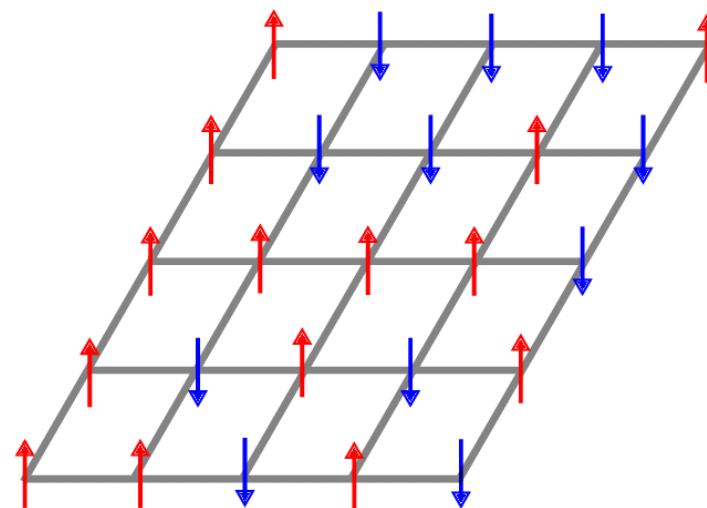


[Published: February 1925](#)

Beitrag zur Theorie des Ferromagnetismus

[Ernst Ising](#)

[Zeitschrift für Physik](#) 31, 253–258 (1925) | [Cite this article](#)



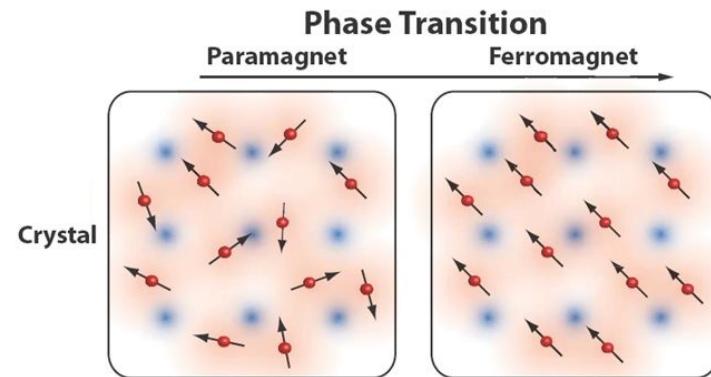
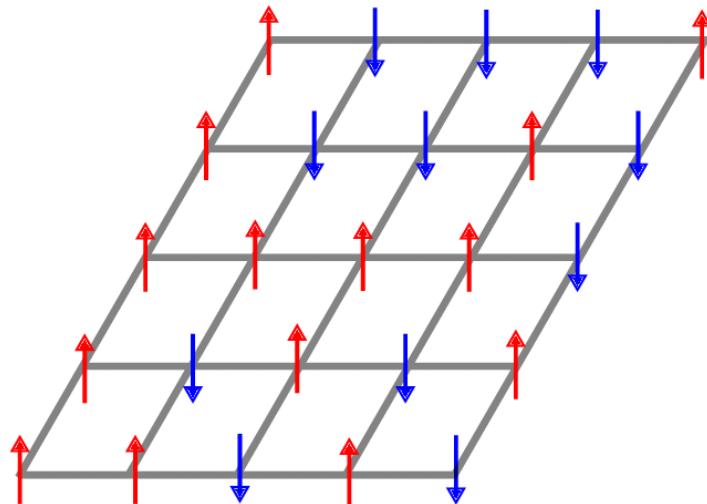
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50 spins = ? states

- a) 1,000 – 10,000
- b) 10,000 – 1,000,000
- c) 1,000,000 – 1,000,000,000
- d) More than 1,000,000,000

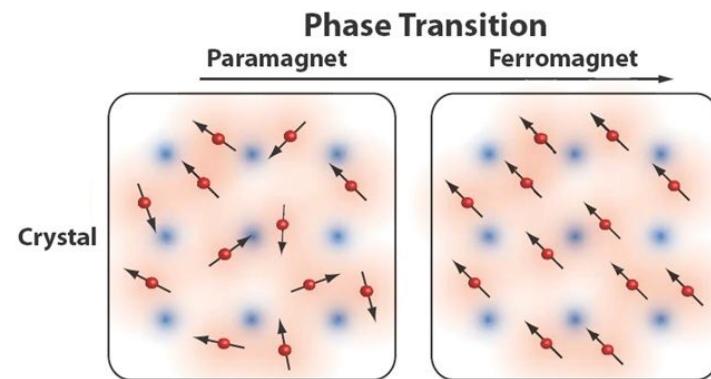
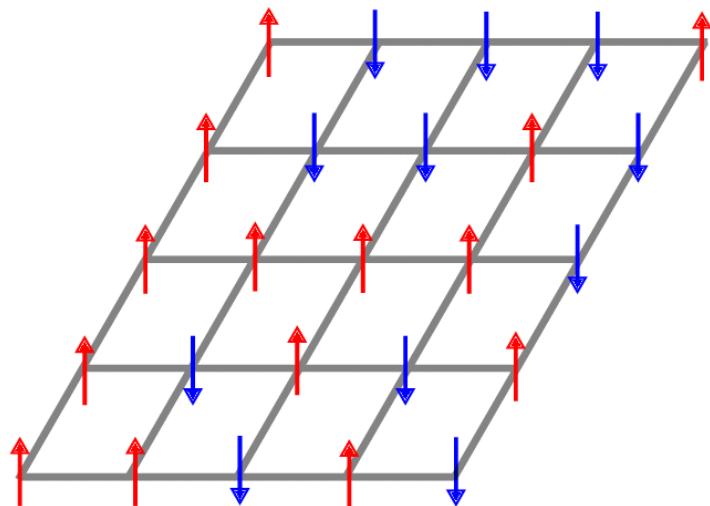
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50 spins = 1,125,899,906,842,624 states

18 Petabytes of memory

10^{23} atoms



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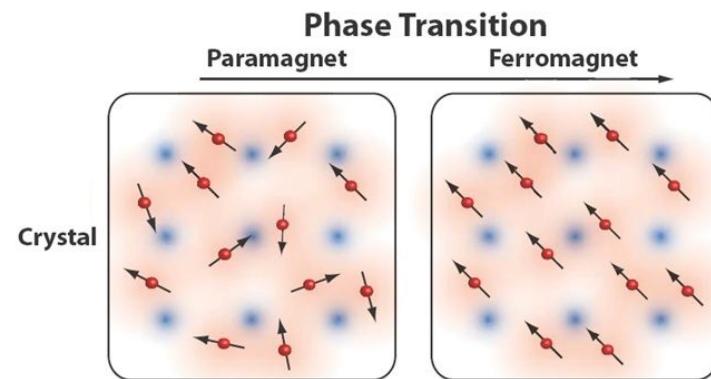
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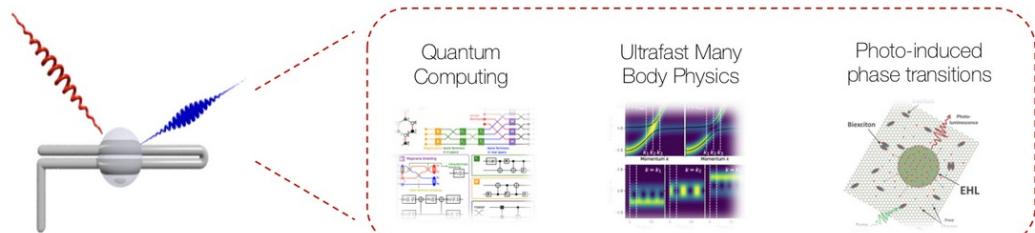
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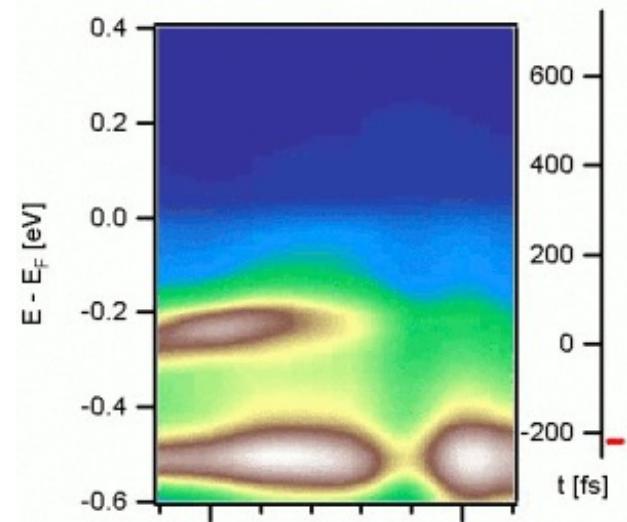
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Kemper Lab

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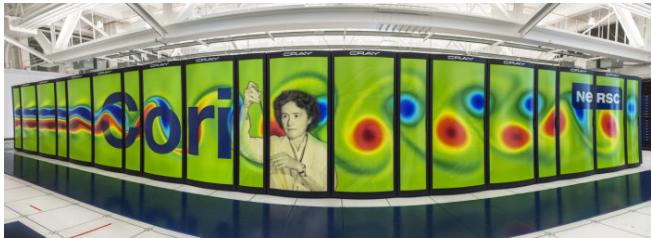
Time-resolved experiments



Shen group (Stanford)

20

2. Can quantum physics be simulated by a classical computer?



Density functional theory/GW
 Exact diagonalization
 Quantum Monte Carlo
 Non-equilibrium Green's functions
 Matrix Product States
 Tensor Networks

-
-
-

NERSC Applications

several popular applications. Note that the Perlmutter software stack is still being built out; some applications are available at this time. For Perlmutter, these tables indicate applications that are available (as of 06/01/2023).

Density functional theory

Application	Perlmutter GPU	Perlmutter CPU
BerkeleyGW	3.x	3.x
CP2K	2022.1 (docker)	2022.1 (docker)
SIESTA	-	4.0.2 (spack)
Quantum ESPRESSO	7.x	7.x
VASP	6.x	5.4, 6.x
Wannier90	3.1.0	-

Molecular dynamics

Application	Perlmutter GPU	Perlmutter CPU
AMBER	20	20
Ab initio	-	-
Gromacs	2022.3	2021.5-plumed
LAMMPS	2022.11.03	2022.11.03
NAMD	2.15a2	2.15a2

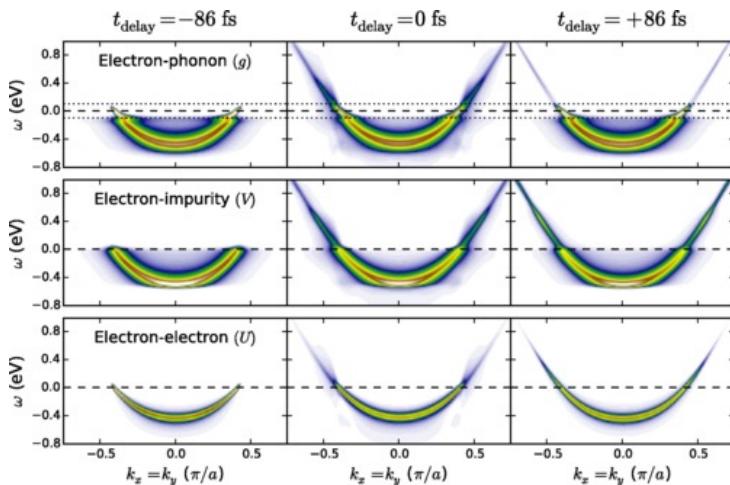
Chemistry applications

Application	Perlmutter GPU	Perlmutter CPU
PyTorch	-	-
TensorBoard	-	-
Benchmarks	-	-
Distributed training	-	-
Hyperparameter optimization	-	-

Table of contents

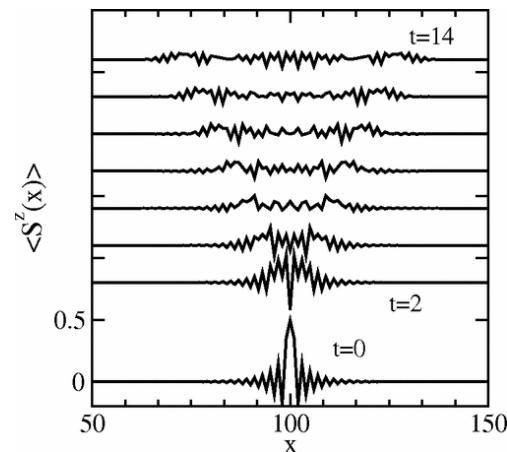
- Popular applications
- Density functional theory
- Molecular dynamics
- Chemistry applications
- Mathematical environments
- Visualization

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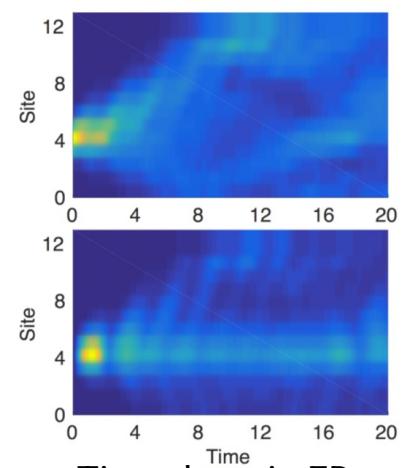


Non-Equilibrium Green's functions

Phys. Rev. X 8, 041009 (2018)



Time domain DMRG
Phys. Rev. Lett. 93, 076401 (2004)

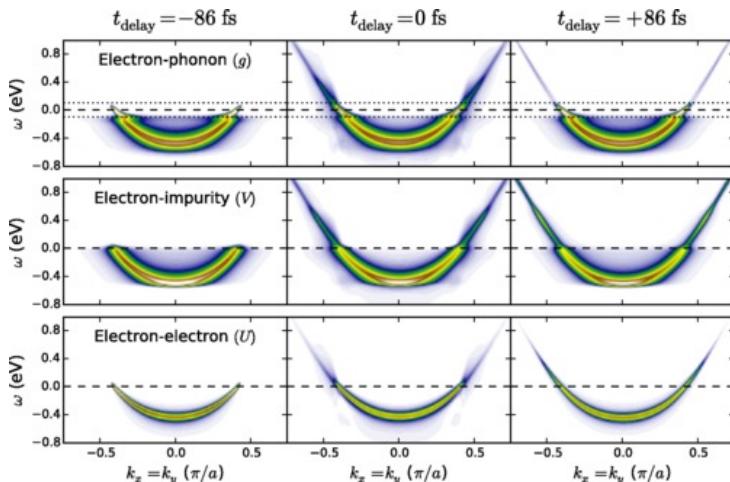


Time domain ED
Johnston & Kemper, unpublished

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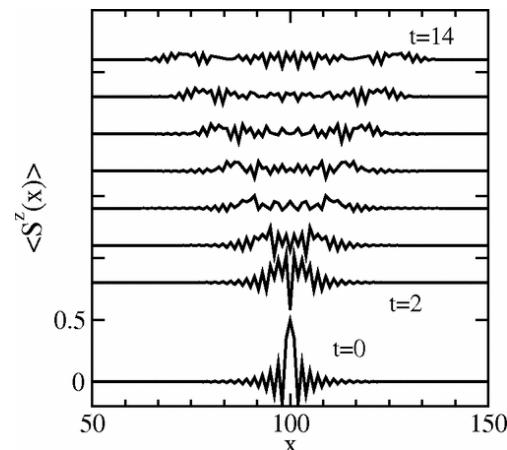


All these techniques eventually reach a barrier.

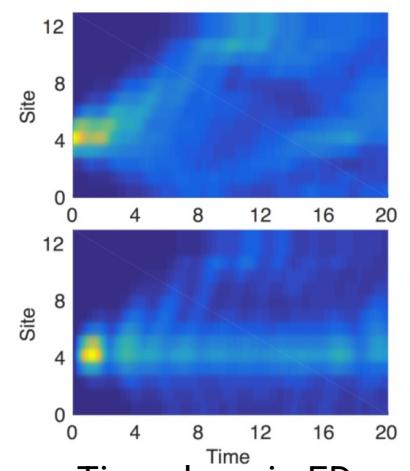


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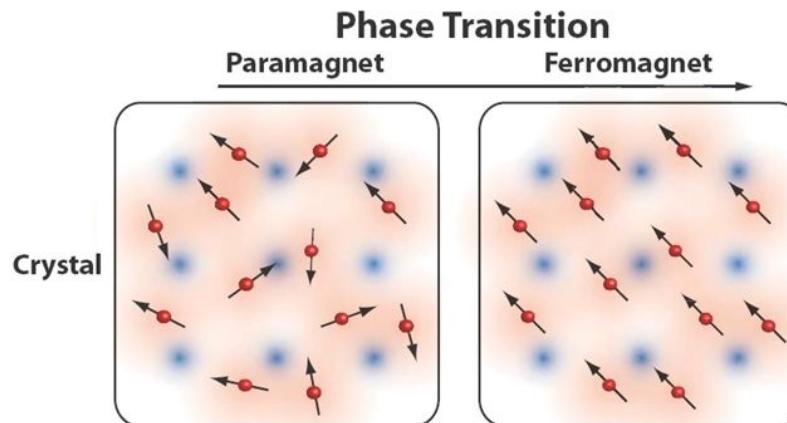
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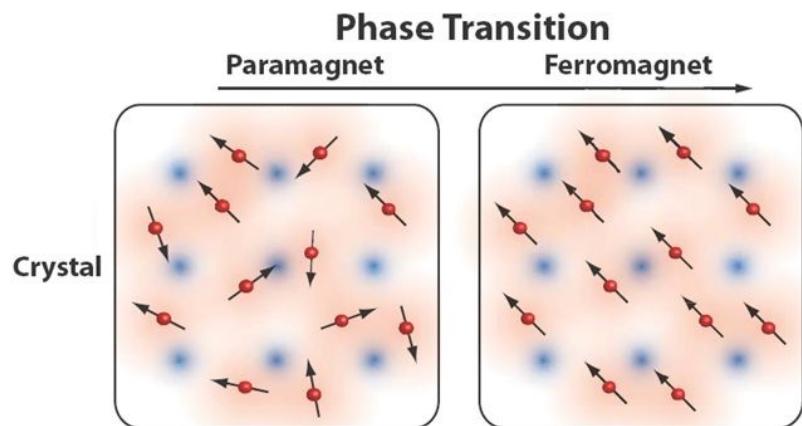
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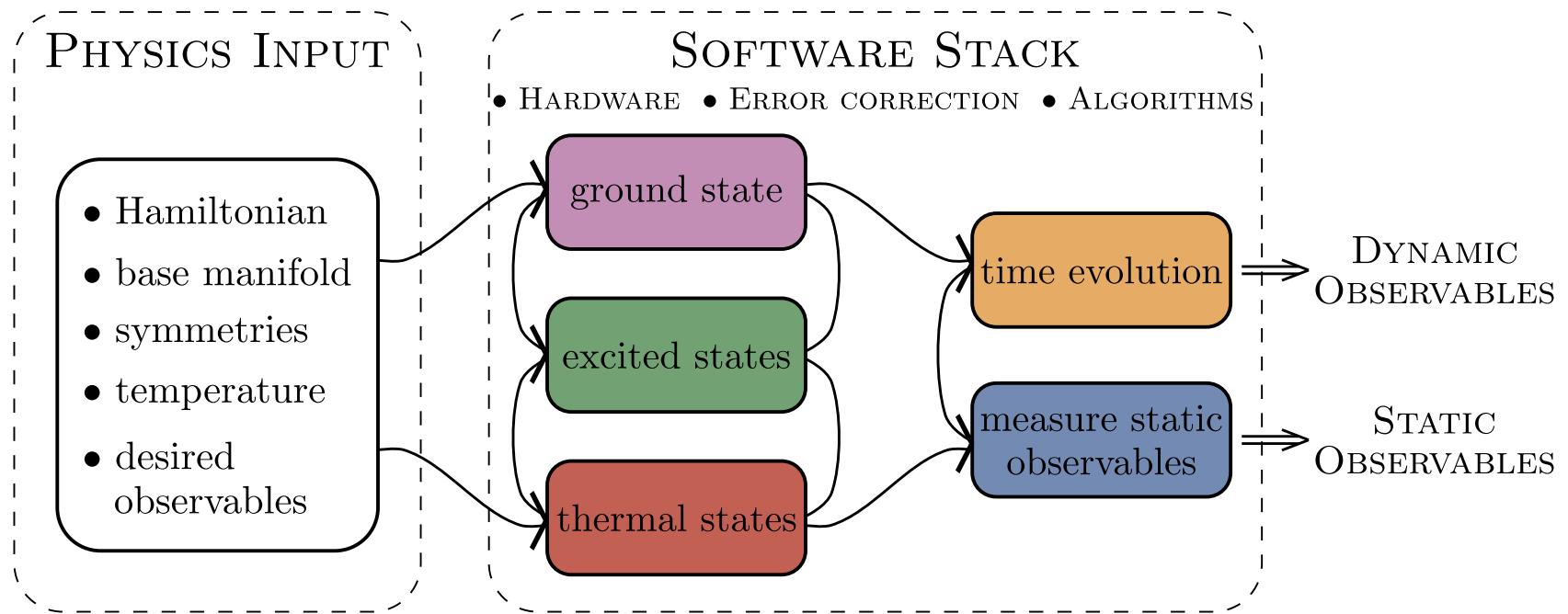
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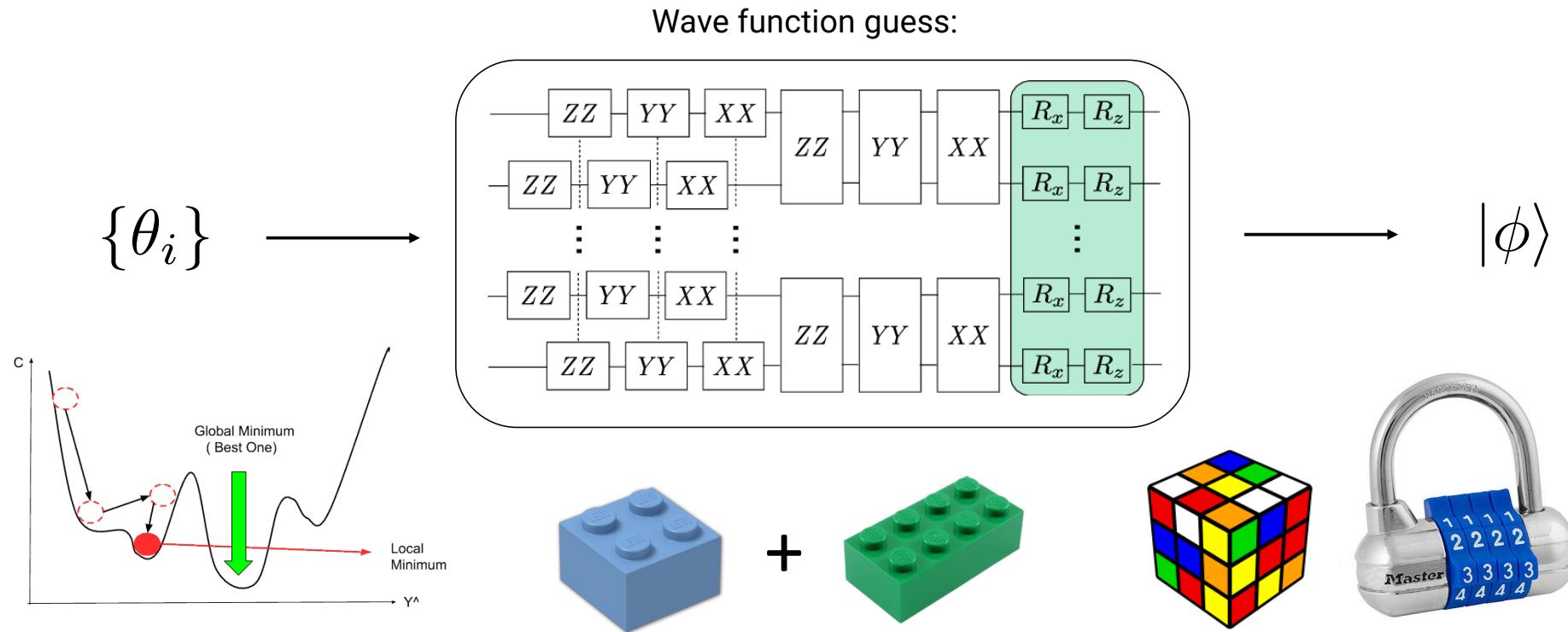
50 spins = 50 qubits

Quantum Matter meets Quantum Computing

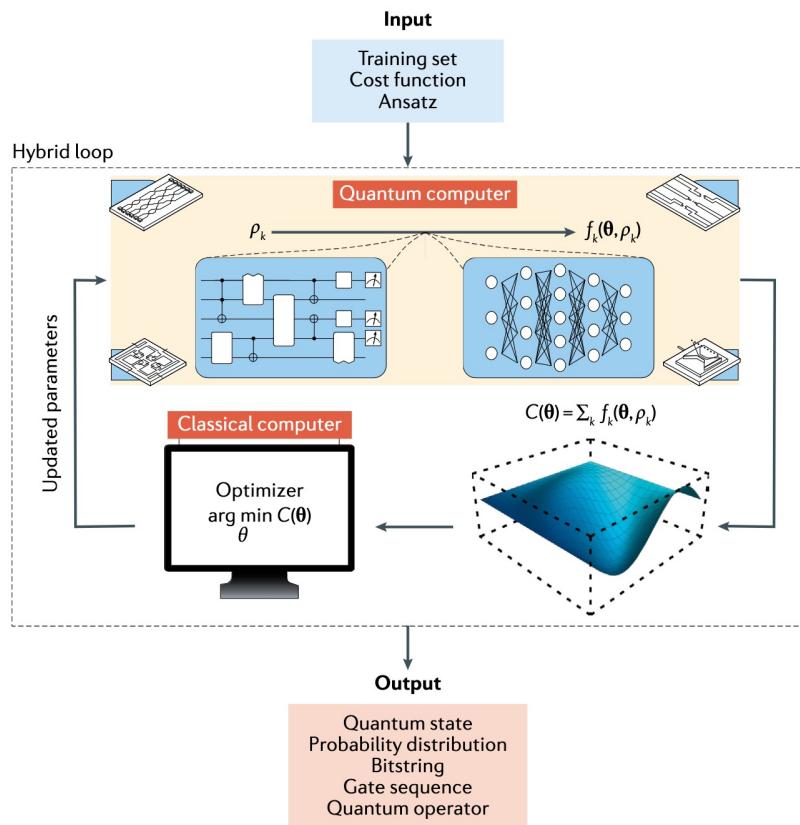


3. Can quantum physics be simulated by a quantum computer?

Variational Principle: $E_{\text{ground}} \leq \langle \phi | H | \phi \rangle$



3. Can quantum physics be simulated by a quantum computer?

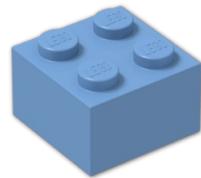
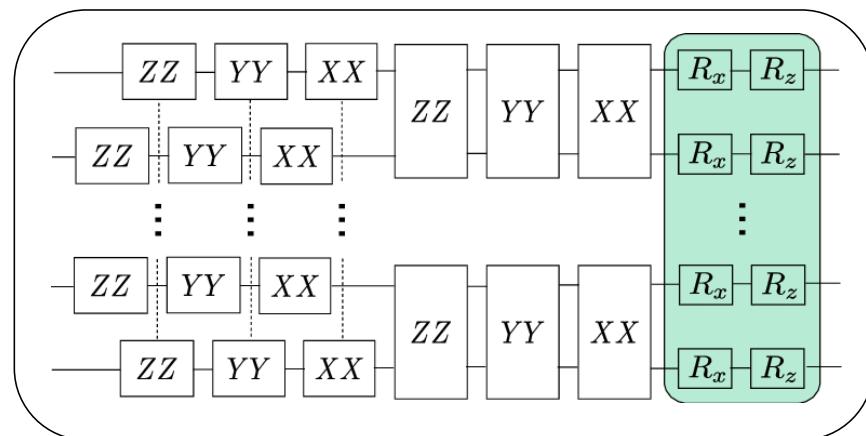


Cost function: Energy of the molecular configuration



10.1038/nature23879

Wave function guess:



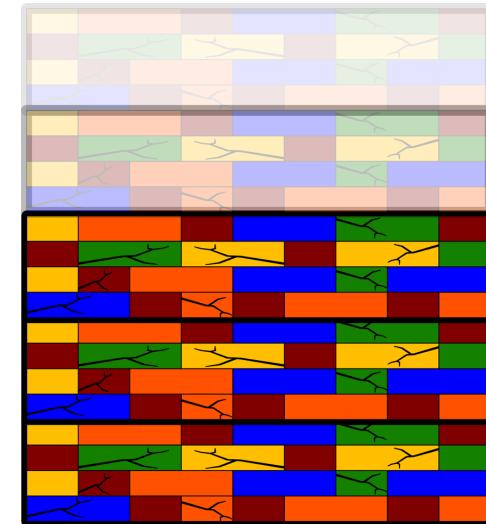
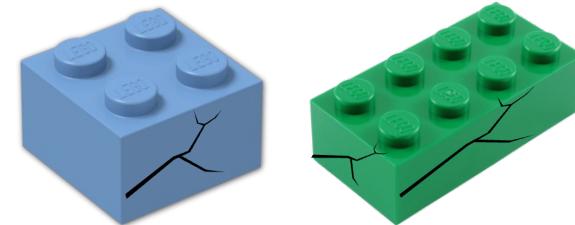
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Single Qubit Gates

Two Qubit Gate

*Actual Gates



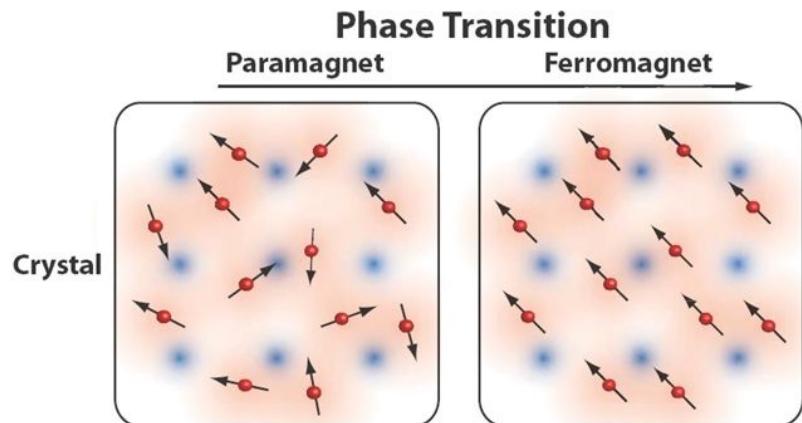
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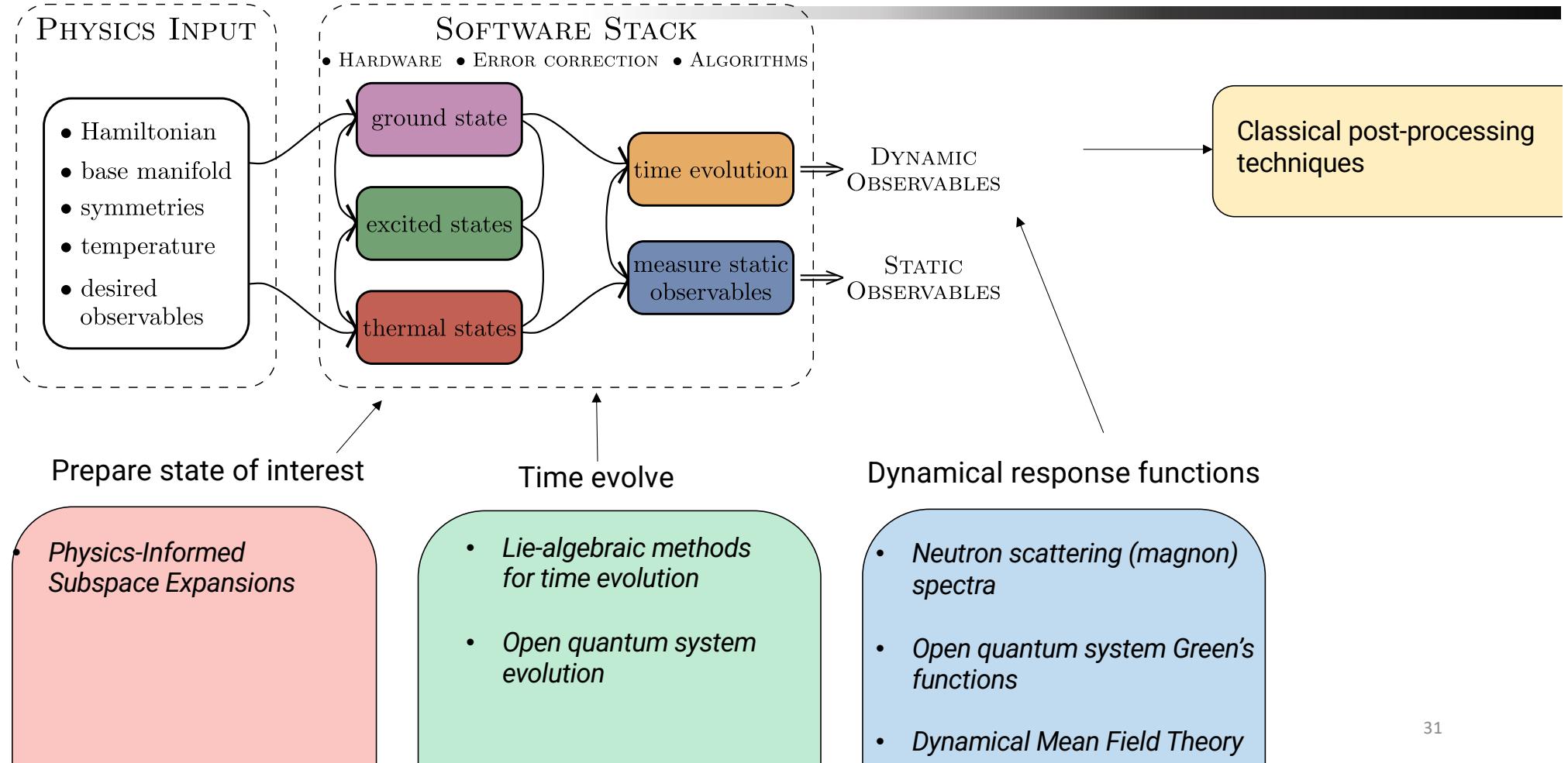
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50 spins = 50 qubits

A-Z quantum simulation



Q: What do you do with a quantum state once you've prepared one?

Ising Model

794

Brazilian Journal of Physics, vol. 30, no. 4, December, 2000

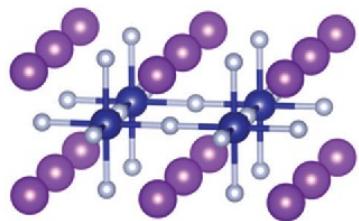
The Ising Model and Real Magnetic Materials

W. P. Wolf

*Yale University, Department of Applied Physics,
P.O. Box 208284, New Haven, Connecticut 06520-8284, U.S.A.*

Received on 3 August, 2000

The factors that make certain magnetic materials behave similarly to corresponding Ising models are reviewed. Examples of extensively studied materials include $\text{Dy}(\text{C}_2\text{H}_5\text{SO}_4)_3 \cdot 9\text{H}_2\text{O}$ (DyES), $\text{Dy}_3\text{Al}_5\text{O}_{12}$ (DyAlG), DyPO_4 , $\text{Dy}_2\text{Tl}_2\text{O}_7$, LiTbF_4 , K_2CoF_4 , and Rb_2CoF_4 . Various comparisons between theory and experiment for these materials are examined. The agreement is found to be generally very good, even when there are clear differences between the ideal Ising model and the real materials. In a number of experiments behavior has been observed that requires extensions of the usual Ising model. These include the effects of long range magnetic dipole interactions, competing interaction effects in field-induced phase transitions, induced staggered field effects and frustration effects, and dynamic effects. The results show that the Ising model and real magnetic materials have provided an unusually rich and productive field for the interaction between theory and experiment over the past 40 years.



[10.1039/c6cp02362b](https://doi.org/10.1039/c6cp02362b)

Heisenberg model

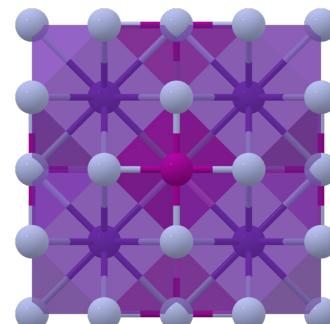
PHYSICAL REVIEW B

covering condensed matter and materials physics

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Critical behavior of the three-dimensional Heisenberg antiferromagnet RbMnF_3

R. Coldea, R. A. Cowley, T. G. Perring, D. F. McMorrow, and B. Roessli
Phys. Rev. B **57**, 5281 – Published 1 March 1998

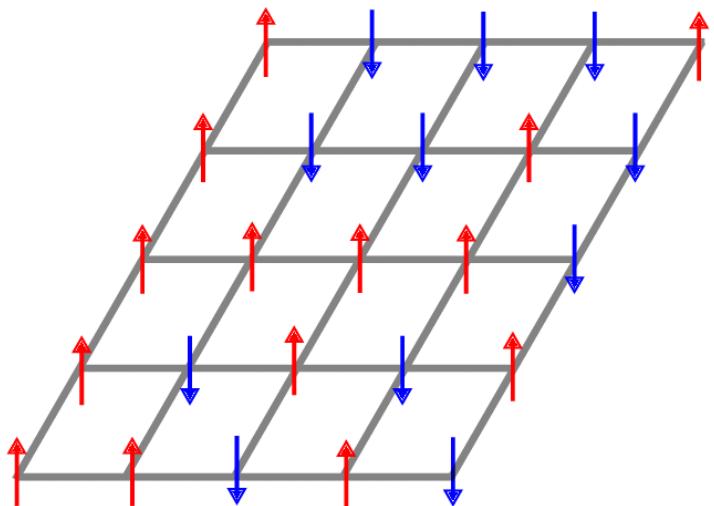


Materials project

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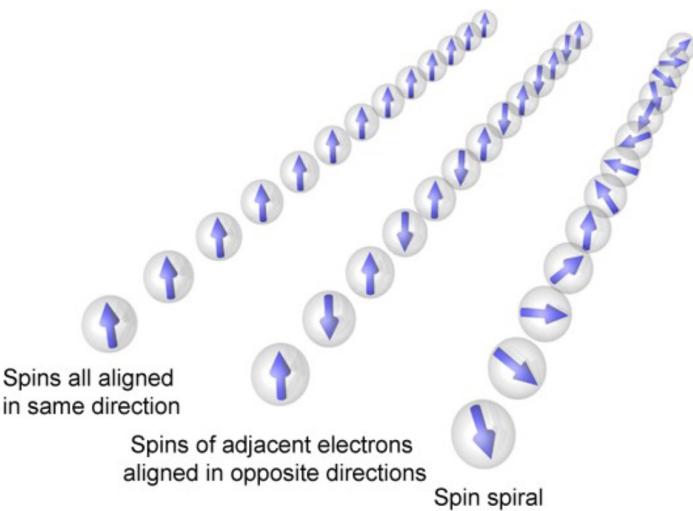
Ising Model

$$\mathcal{H} = -J \sum_i \sigma_i^z \sigma_{i+1}^z + h_x \sum_i \sigma_i^x$$



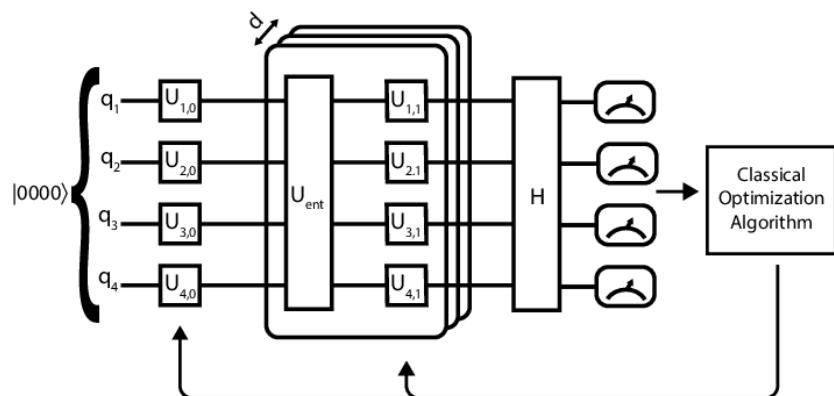
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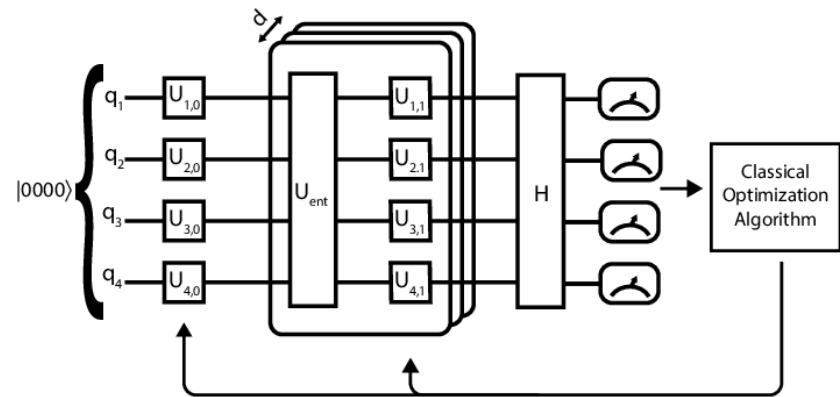
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[Optimization of the Variational Quantum Eigensolver for Quantum Chemistry Applications](#)

Heisenberg model

$$\mathcal{H} = -J \sum_i \vec{\sigma}_i \cdot \vec{\sigma}_{i+1} + h_x \sum_i \sigma_i^x$$



Ising Model

$$\mathcal{H} = -J \sum_i \sigma_i^z \sigma_{i+1}^z + h_x \sum_i \sigma_i^x$$

Ferromagnetic



Antiferromagnetic



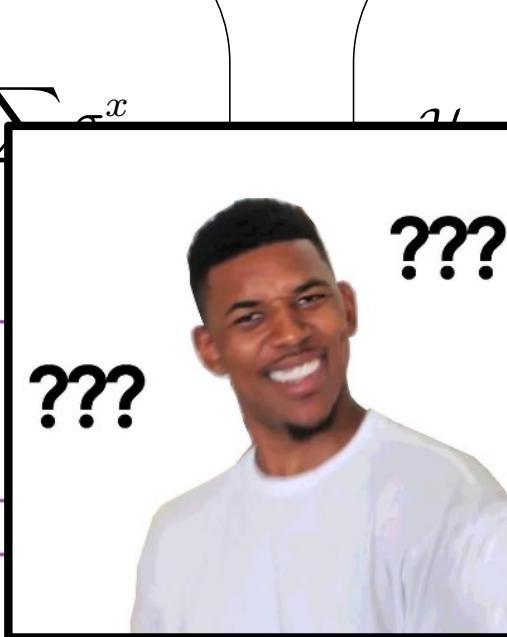
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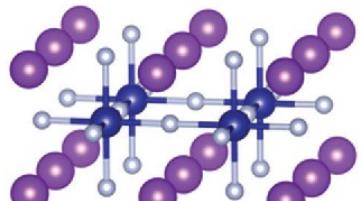
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P.O. Box 208284, New Haven, Connecticut 06520-8284, U.S.A.*

Received on 3 August, 2000

The factors that make certain magnetic materials behave similarly to corresponding Ising models are reviewed. Examples of extensively studied materials include $\text{Dy}(\text{C}_2\text{H}_5\text{SO}_4)_3$, $\text{Dy}_3\text{Al}_5\text{O}_{12}$ (DyAl₅G), DyPO_4 , $\text{Dy}_2\text{Tl}_2\text{O}_7$, LiTbF_4 , K_2CoF_4 , and Rb_2CoF_4 . Variations between theory and experiment for these materials are examined. The agreement is generally very good, even when there are clear differences between the ideal Ising model and the real materials. In a number of experiments behavior has been observed that requires extensions of the usual Ising model. These include the effects of long range magnetic dipole interactions, interaction effects in field-induced phase transitions, induced staggered field effects, and dynamic effects. The results show that the Ising model and real magnetic materials provided an unusually rich and productive field for the interaction between theory and experiment over the past 40 years.



[10.1039/c6cp02362b](https://doi.org/10.1039/c6cp02362b)

Heisenberg model

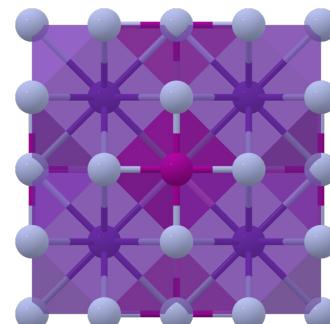
PHYSICAL REVIEW B

condensed matter and materials physics

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al behavior of the three-dimensional Heisenberg ferromagnet RbMnF_3

a, R. A. Cowley, T. G. Perring, D. F. McMorrow, and B. Roessli
Phys. Rev. B **57**, 5281 – Published 1 March 1998



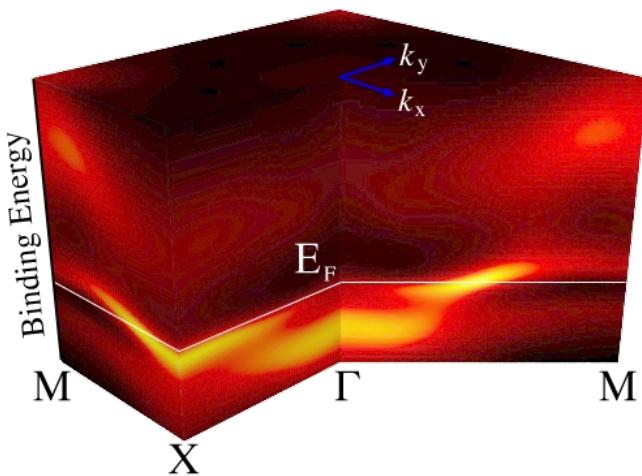
Materials project

Q: What do you do with a quantum state once you've prepared one?

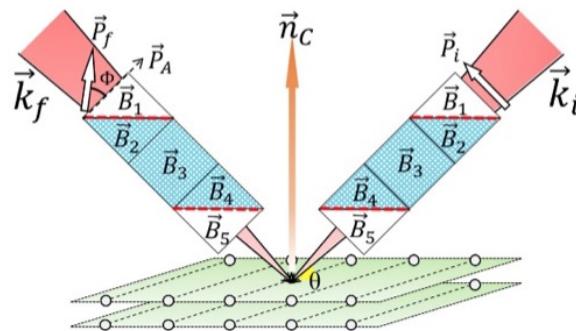
A: You measure its excitations.

Measuring Excitations

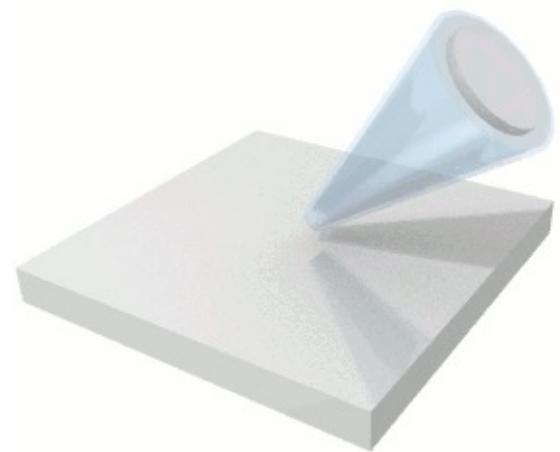
Figures courtesy of
Devereaux/Shen group
and ORNL



Angle-resolved Photoemission
(ARPES)

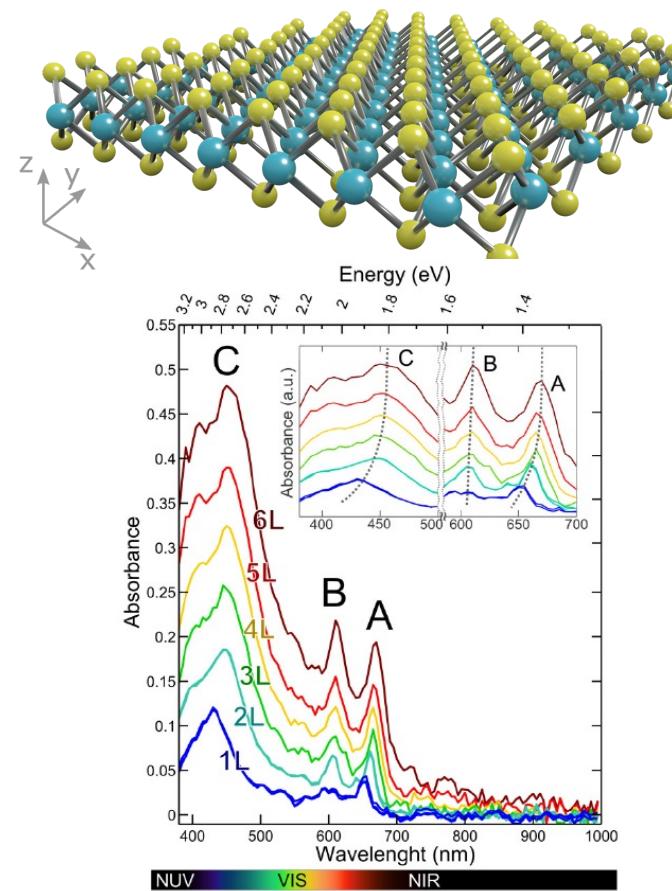
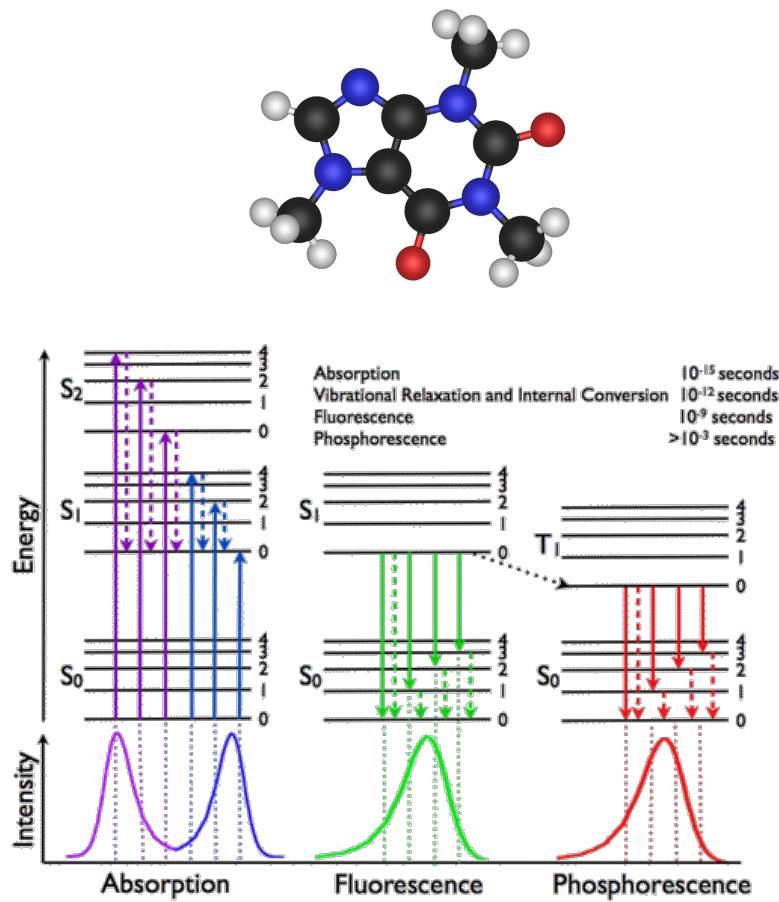


Neutron Scattering



Time-resolved ARPES

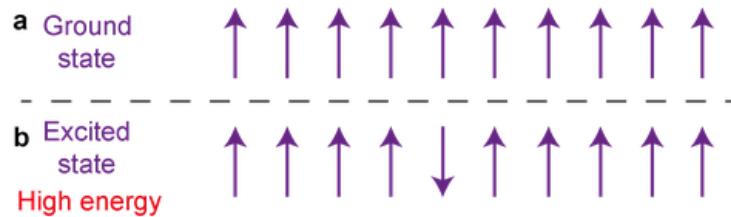
Measuring Excitations



Measuring Excitations

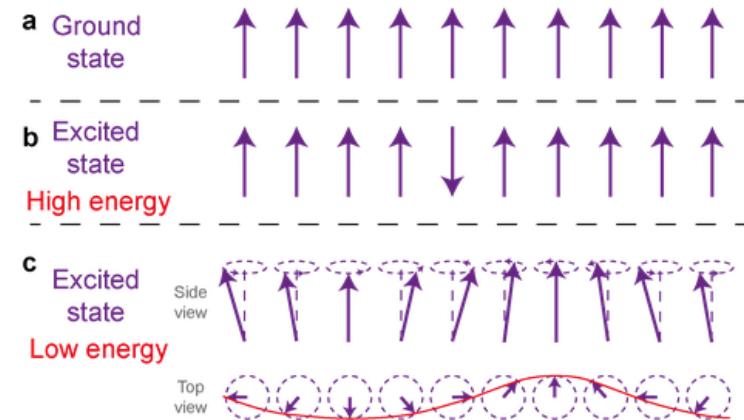
Ising Model

$$\mathcal{H} = -J \sum_i \sigma_i^z \sigma_{i+1}^z + h_x \sum_i \sigma_i^x$$

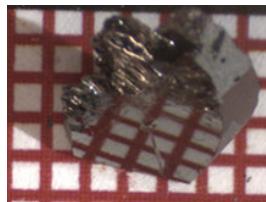


Heisenberg model

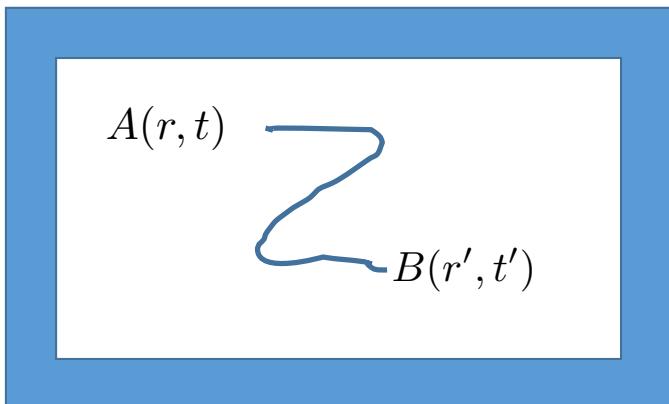
$$\mathcal{H} = -J \sum_i \vec{\sigma}_i \cdot \vec{\sigma}_{i+1} + h_x \sum_i \sigma_i^x$$



Quantum Computer = Quantum Simulator



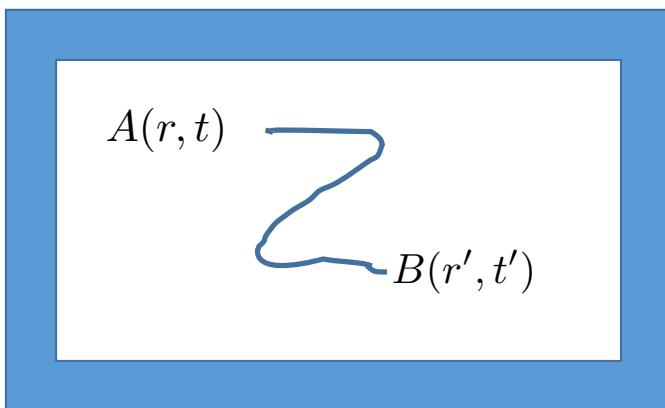
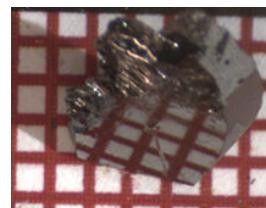
$$\langle A(r, t)B(r', t') \rangle$$



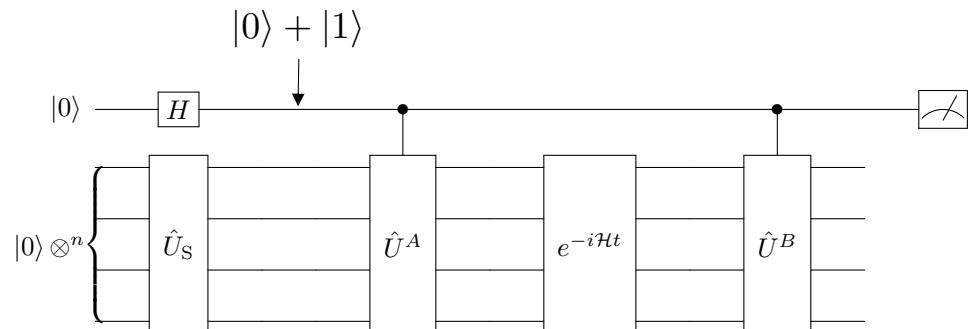
Given some (observable) operator B at (r', t') , what is the likelihood of some (observable) operator A at (r, t) ?

Optical conductivity, X-ray scattering, photoemission, etc.

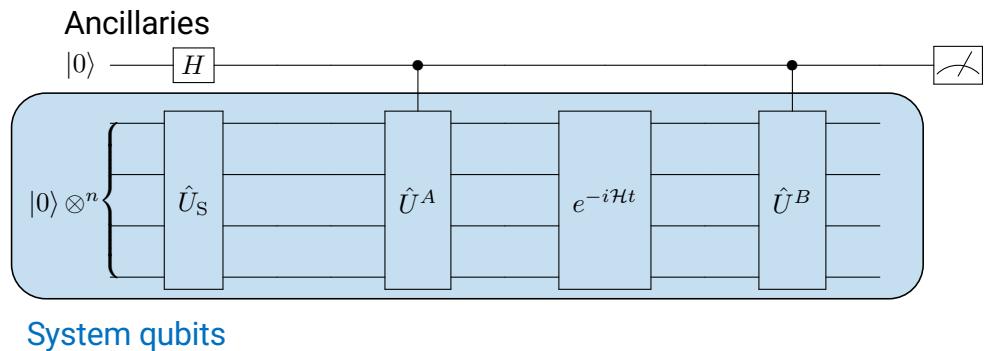
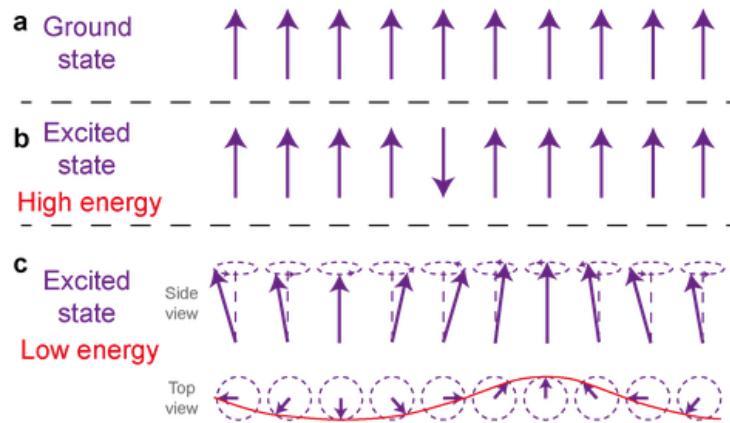
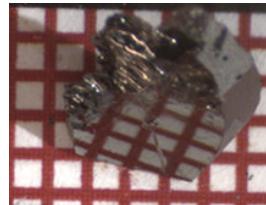
Quantum Computer = Quantum Simulator



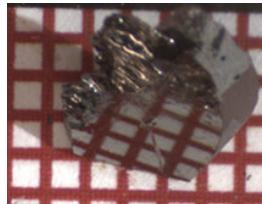
$e^{iE_0 t} \langle \phi_0 | B e^{-i\mathcal{H}t} A | \phi_0 \rangle$
 Interfere with ground state
 Complete expectation value
 Time evolve
 Apply excitation B
 Apply excitation A
 Prepare state of interest



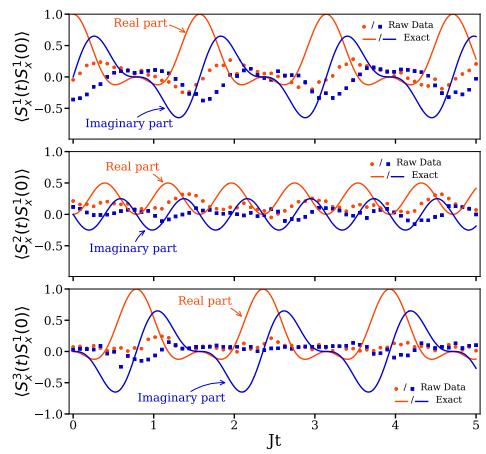
Correlation functions



Correlation functions

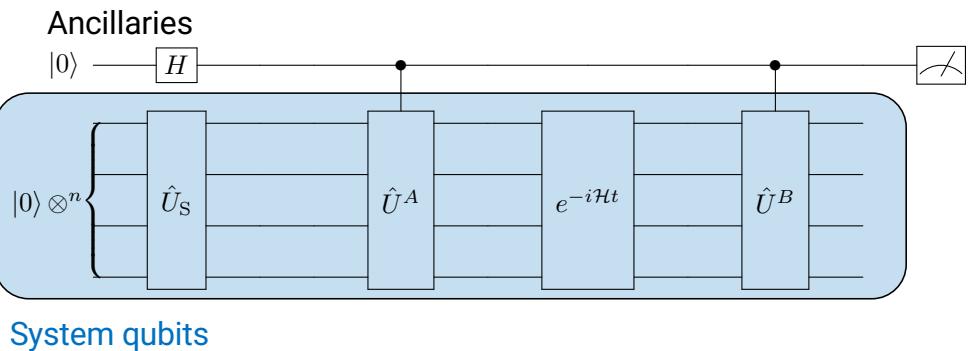
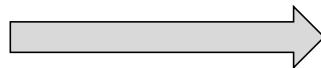


Raw data (2019)

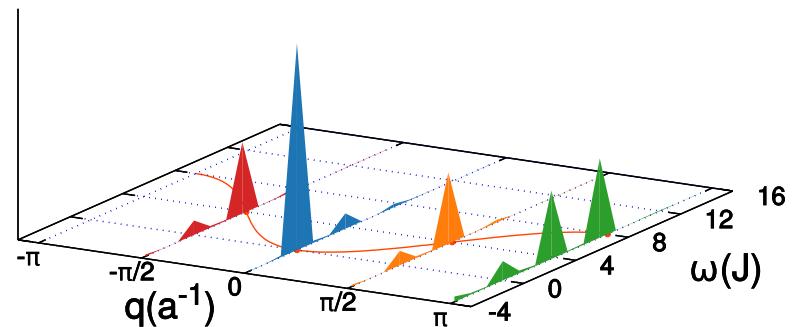


$$\langle A(r, t)B(r', t') \rangle$$

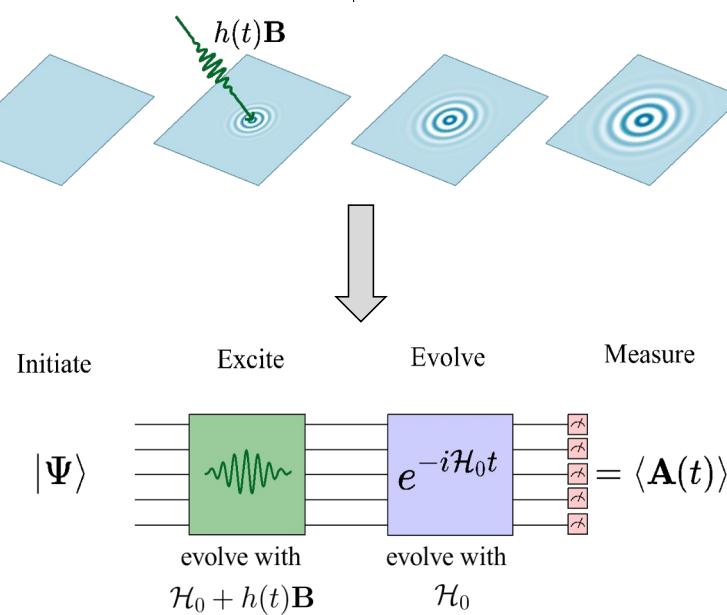
Error mitigation



$|\mathbf{S}(\mathbf{q}, \omega)|^2$: PaS



Linear Response



A linear response framework for simulating bosonic and fermionic correlation functions illustrated on quantum computers

Efekan Kökcü ,¹ Heba A. Labib ,¹ J. K. Freericks ,² and A. F. Kemper ,^{1,*}

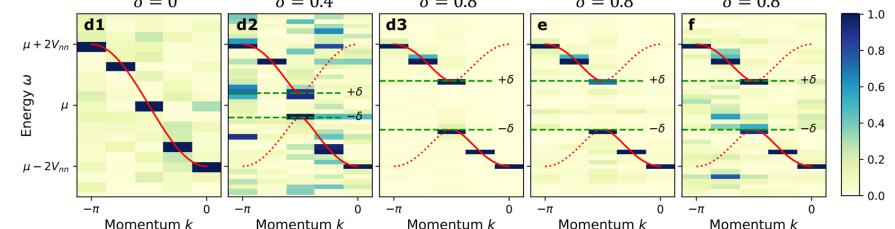
¹Department of Physics, North Carolina State University, Raleigh, North Carolina 27695, USA

²Department of Physics, Georgetown University, 37th and O Sts. NW, Washington, DC 20057 USA

(Dated: February 22, 2023)

1. Make the excitation part of the quantum simulation
2. Post-process the data to get the response functions

$$\left. \frac{\delta A(t)}{\delta h(t')} \right|_{h=0} = -i\theta(t-t') \langle \psi_0 | [\mathbf{A}(t), \mathbf{B}(t')] | \psi_0 \rangle$$

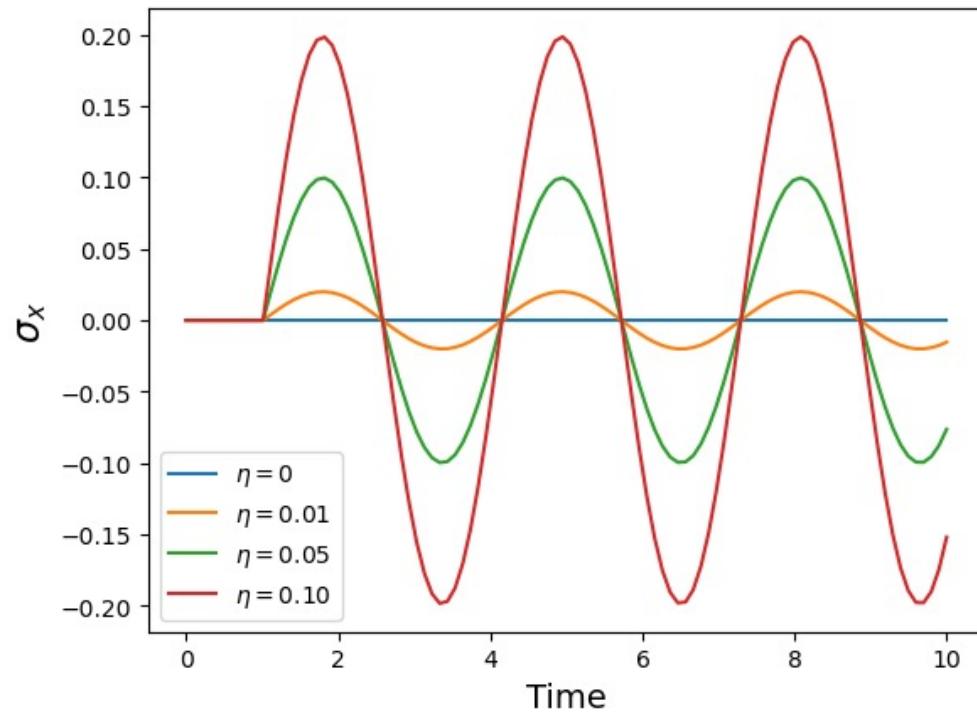
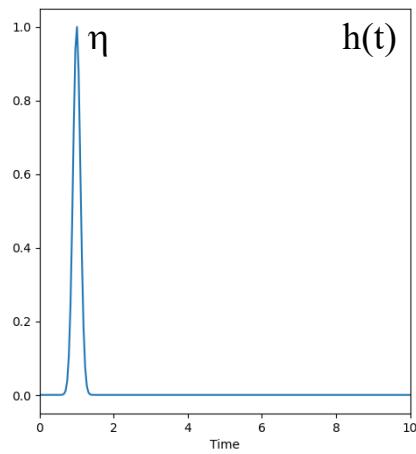


Linear Response

A simple example: single spin with energy level difference = 2

$$\mathbf{H}_0 = \sigma^z$$

$$\mathbf{A} = \mathbf{B} = \sigma^x$$

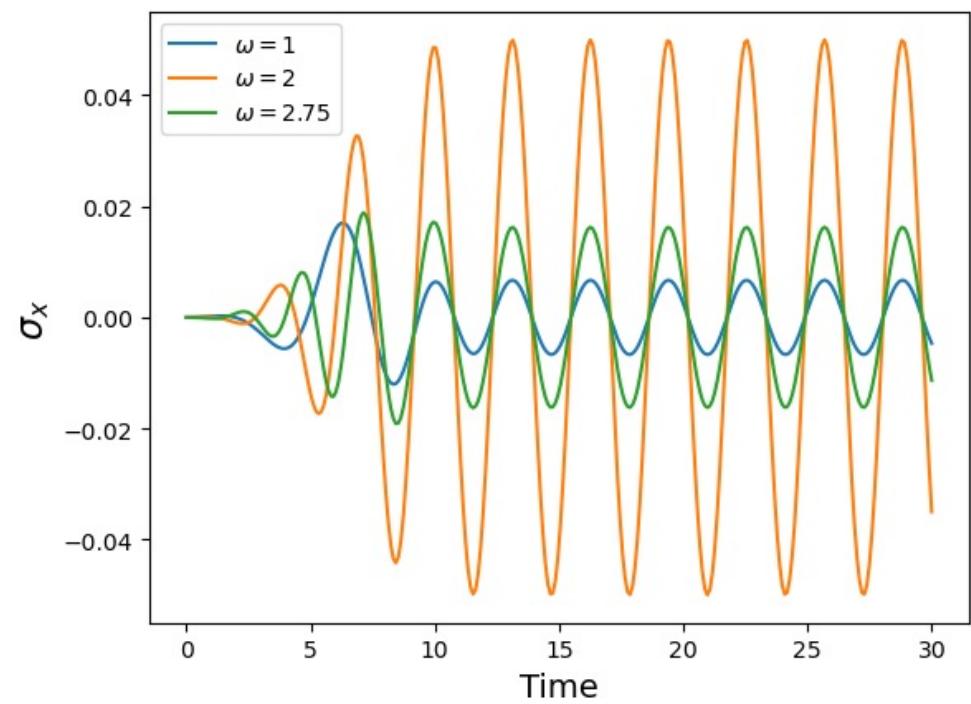
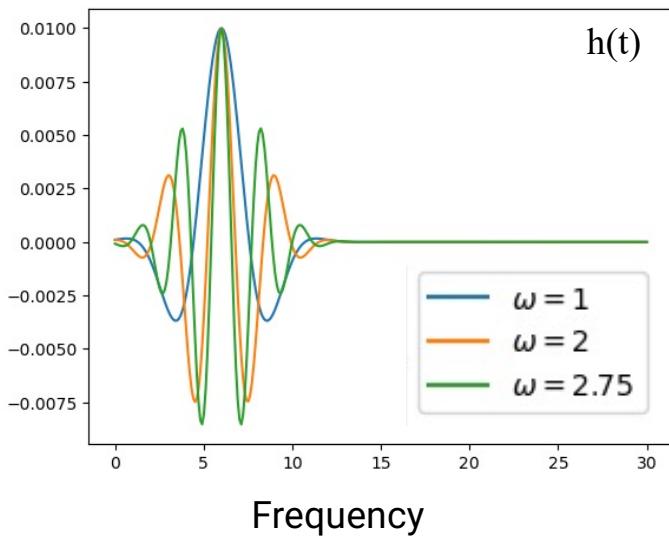


Linear Response

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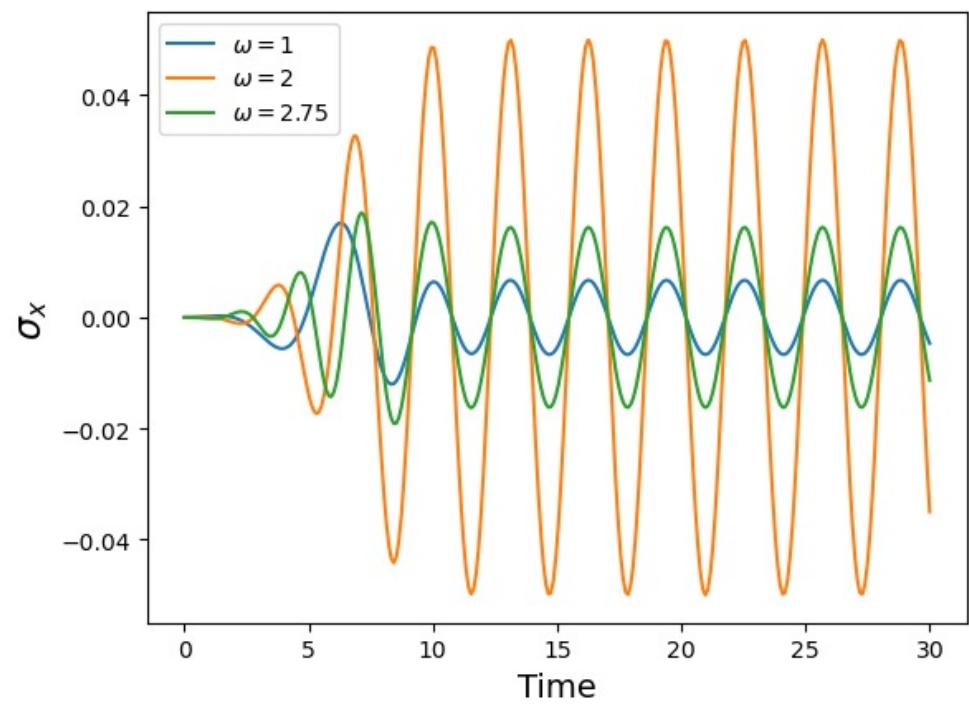
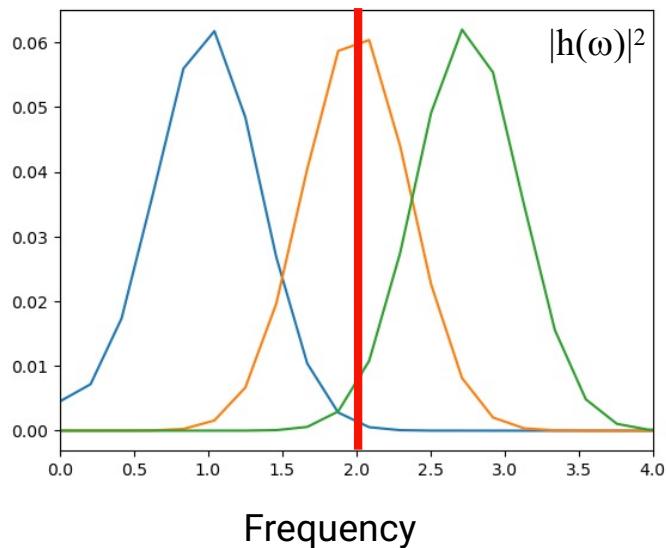


Linear Response

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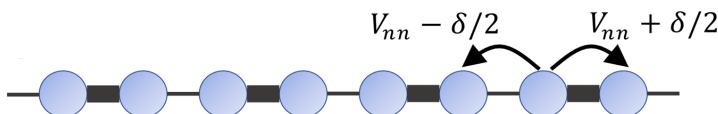
$$\mathbf{A} = \mathbf{B} = \sigma^x$$



Linear Response -> Green's function

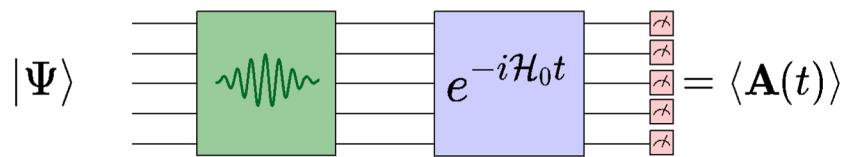
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Su-Schrieffer-Heeger model for polyacetylene

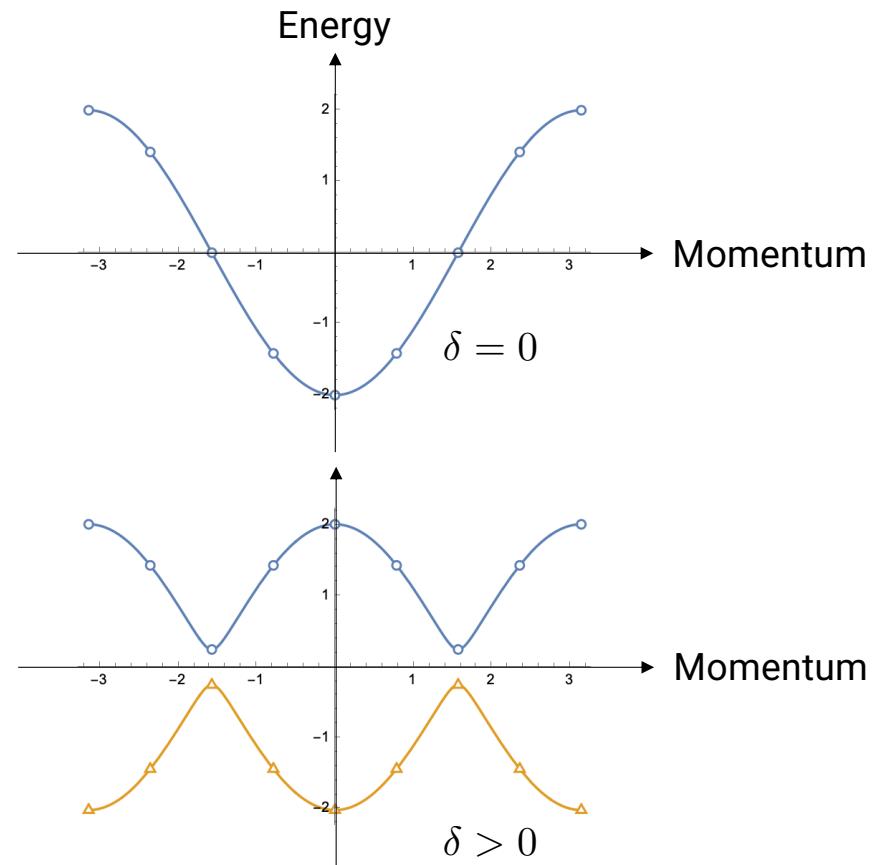


$$\mathcal{H}_0 = - \sum_{\langle i,j \rangle} \left[V_{nn} + (-1)^i \delta/2 \right] c_i^\dagger c_j - \mu \sum_i c_i^\dagger c_i$$

Initiate Excite Evolve Measure



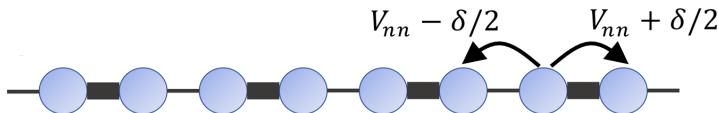
$$G^R(r_i, t; r_j, t') = -i\theta(t - t') \langle \psi_0 | \{c_i(t), c_j^\dagger(t')\} | \psi_0 \rangle$$



Linear Response -> Green's function

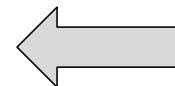
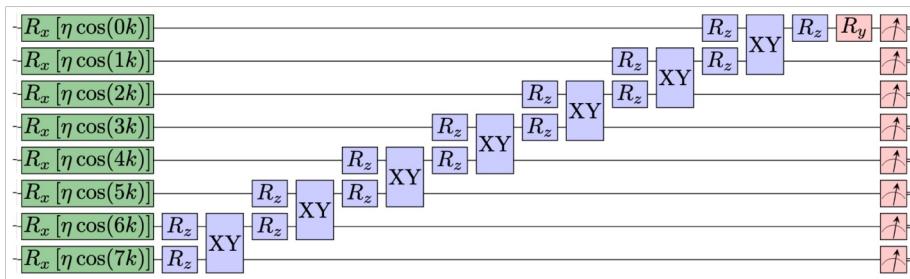
2302.10219

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Compressed circuit run on *ibm_auckland*



$$\mathbf{B} = \sum_i 2 \cos(kr_i) \left[c_i + c_i^\dagger \right]$$

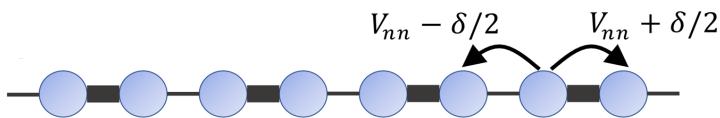
Choose \mathbf{B} to create a momentum eigenstate

$$G_k^R(t) = -i\theta(t) \langle \psi_0 | \{c_k(t), c_k^\dagger(0)\} | \psi_0 \rangle$$

Linear Response -> Green's function

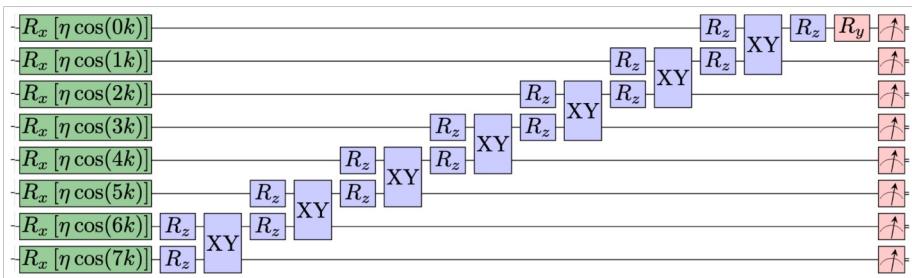
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Su-Schrieffer-Heeger model for polyacetylene



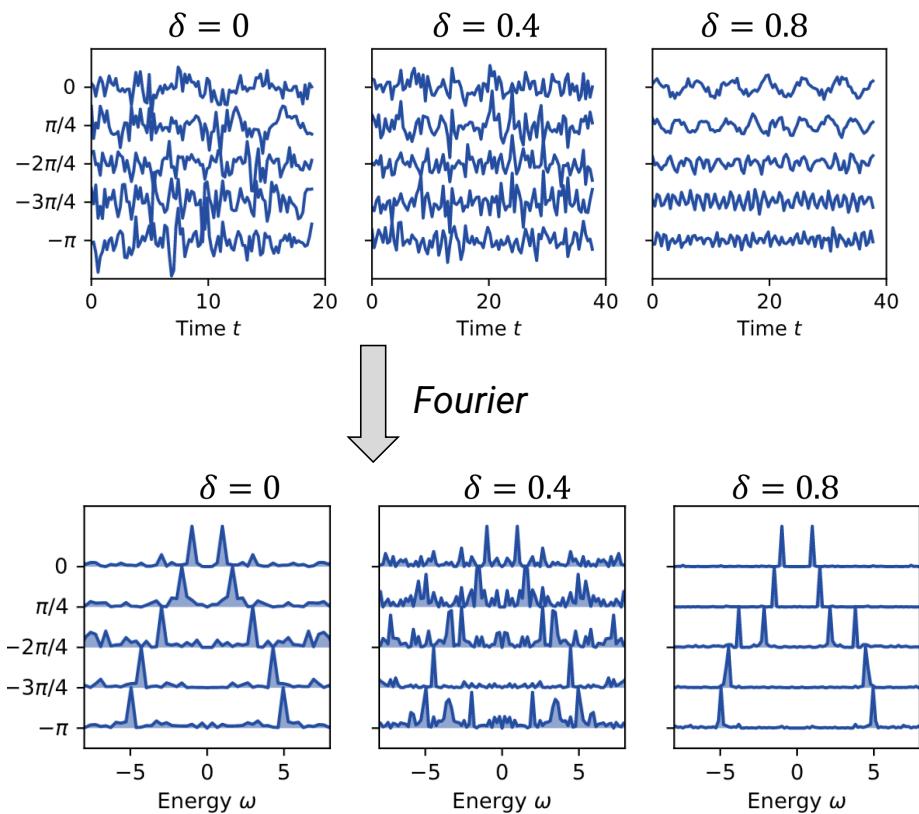
$$\mathcal{H}_0 = - \sum_{\langle i,j \rangle} \left[V_{nn} + (-1)^i \delta/2 \right] c_i^\dagger c_j - \mu \sum_i c_i^\dagger c_i$$

Compressed circuit run on *ibm_auckland*



Choose **B** to create a momentum eigenstate

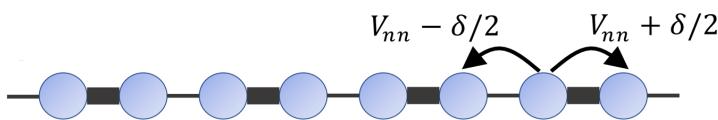
$$G_k^R(t) = -i\theta(t) \langle \psi_0 | \{c_k(t), c_k^\dagger(0)\} | \psi_0 \rangle$$



Linear Response -> Green's function

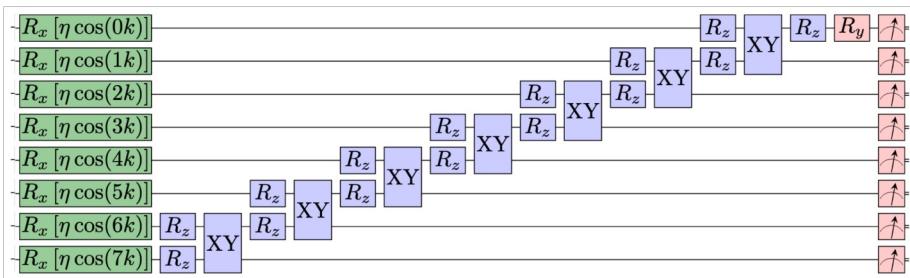
2302.10219

Su-Schrieffer-Heeger model for polyacetylene



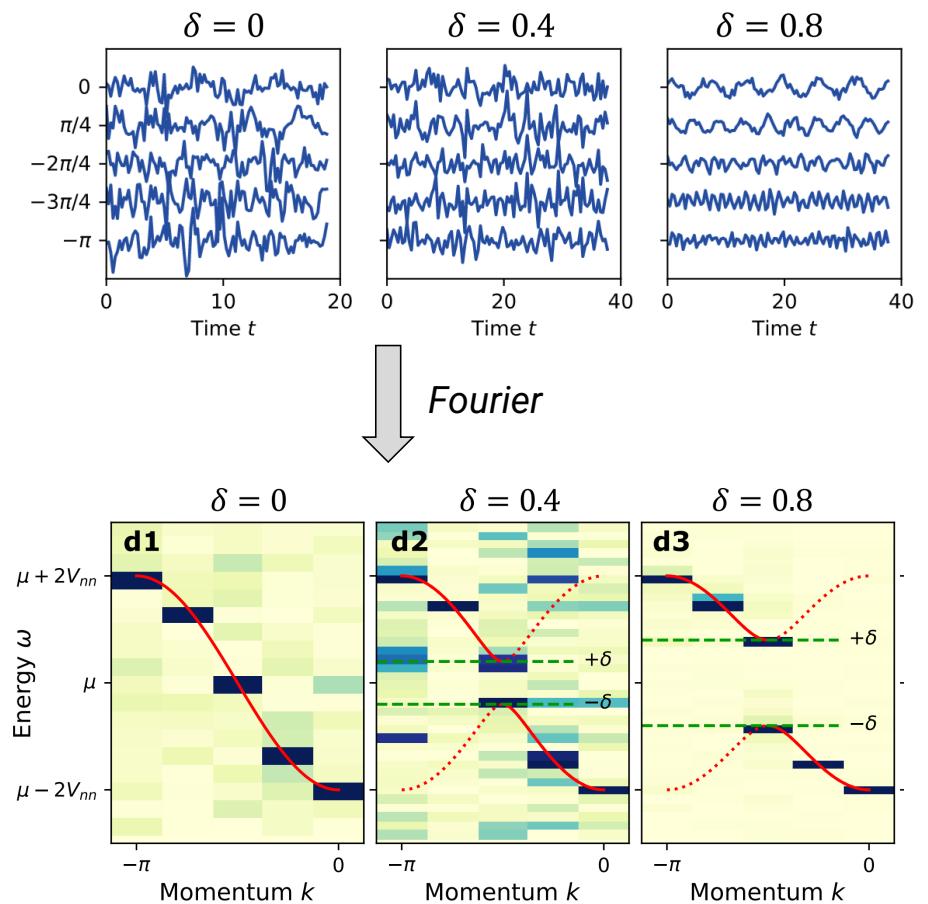
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Compressed circuit run on *ibm_auckland*



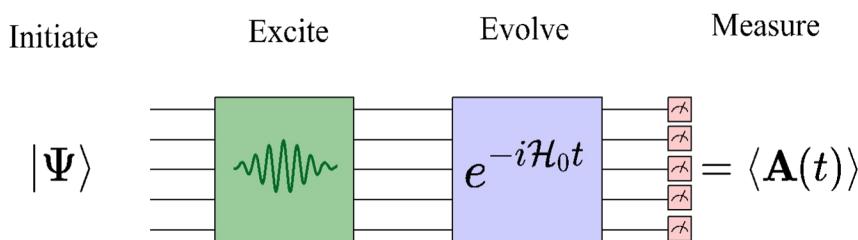
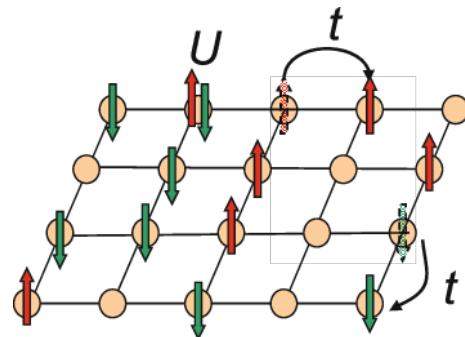
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$$G_k^R(t) = -i\theta(t) \langle \psi_0 | \{c_k(t), c_k^\dagger(0)\} | \psi_0 \rangle$$



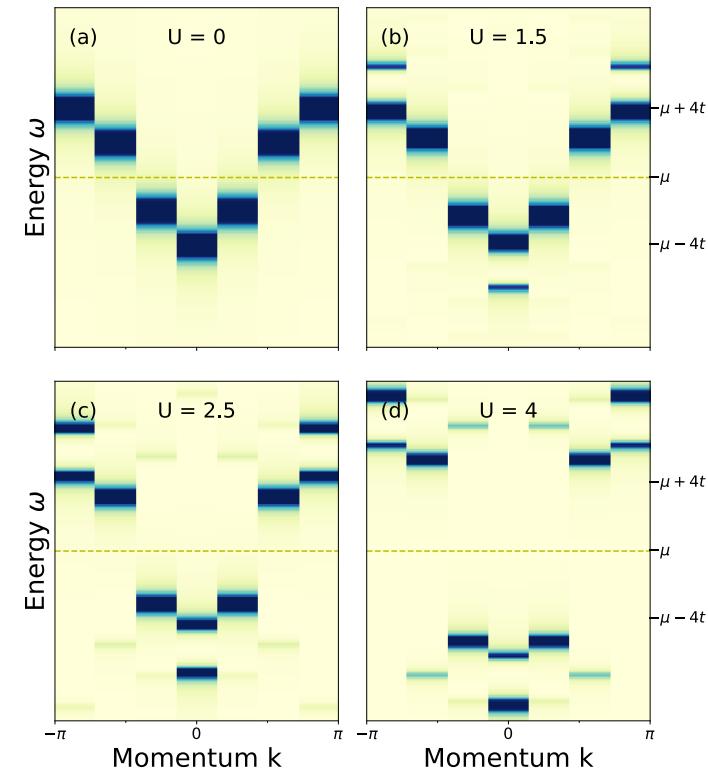
Linear Response -> Green's function

2302.10219



Choose \mathbf{B} to create a momentum eigenstate

$$G_k^R(t) = -i\theta(t)\langle\psi_0|\{c_k(t), c_k^\dagger(0)\}|\psi_0\rangle$$



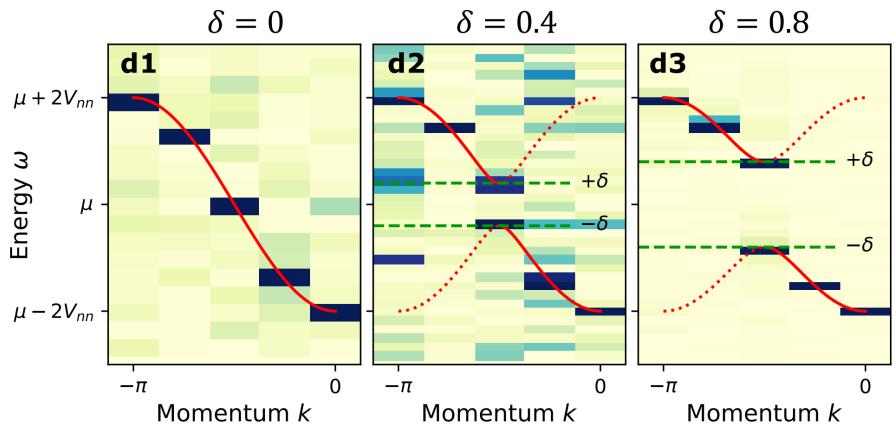
Simulating Physics with Computers

Richard P. Feynman

Department of Physics, California Institute of Technology, Pasadena, California 91107

Received May 7, 1981

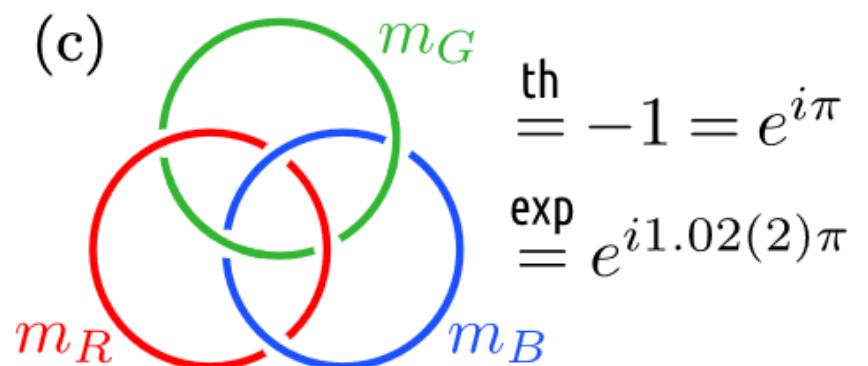
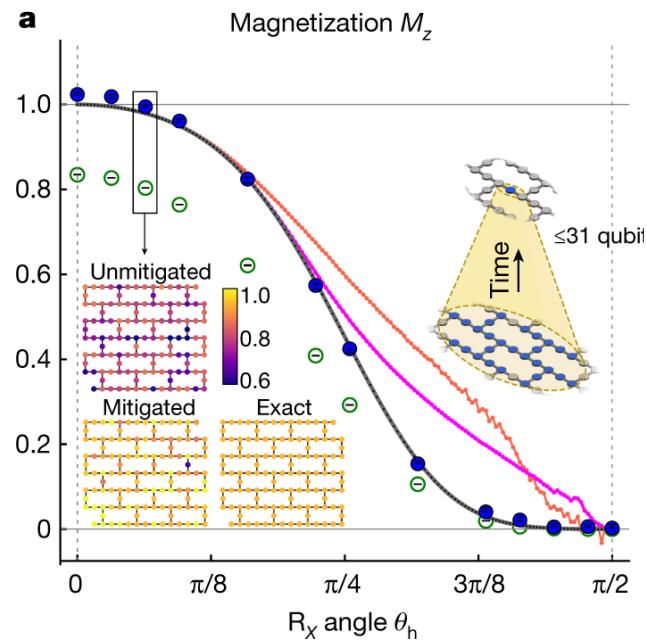
1. Can classical physics be simulated by a classical computer? ✓
2. Can quantum physics be simulated by a classical computer? ?
3. Can physics be simulated by a quantum computer? ✓



Bespoke quantum simulator



Digital algorithms



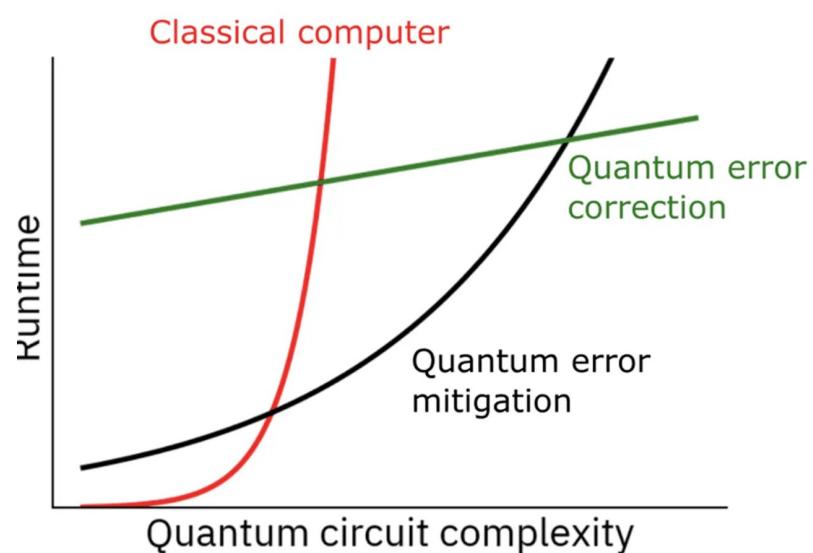
"Evidence for the utility of quantum computing before fault tolerance"
10.1038/s41586-023-06096-3

"Creation of Non-Abelian Topological Order and Anyons on a
Trapped-Ion Processor," arXiv:2305.03766.

Bespoke quantum simulator

Digital algorithms

- Schor's algorithm
- Integer factorization
- Linear solvers (HHL)
- Quantum Adiabatic Optimization
- .
- .
- .

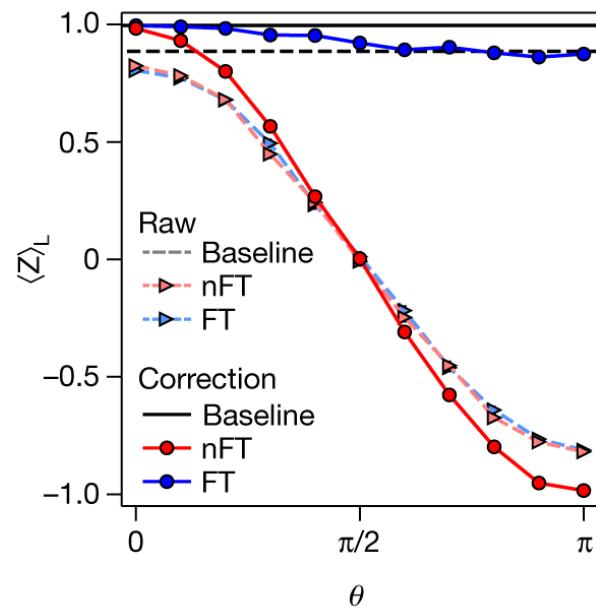


Bespoke quantum simulator



Digital algorithms

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- .



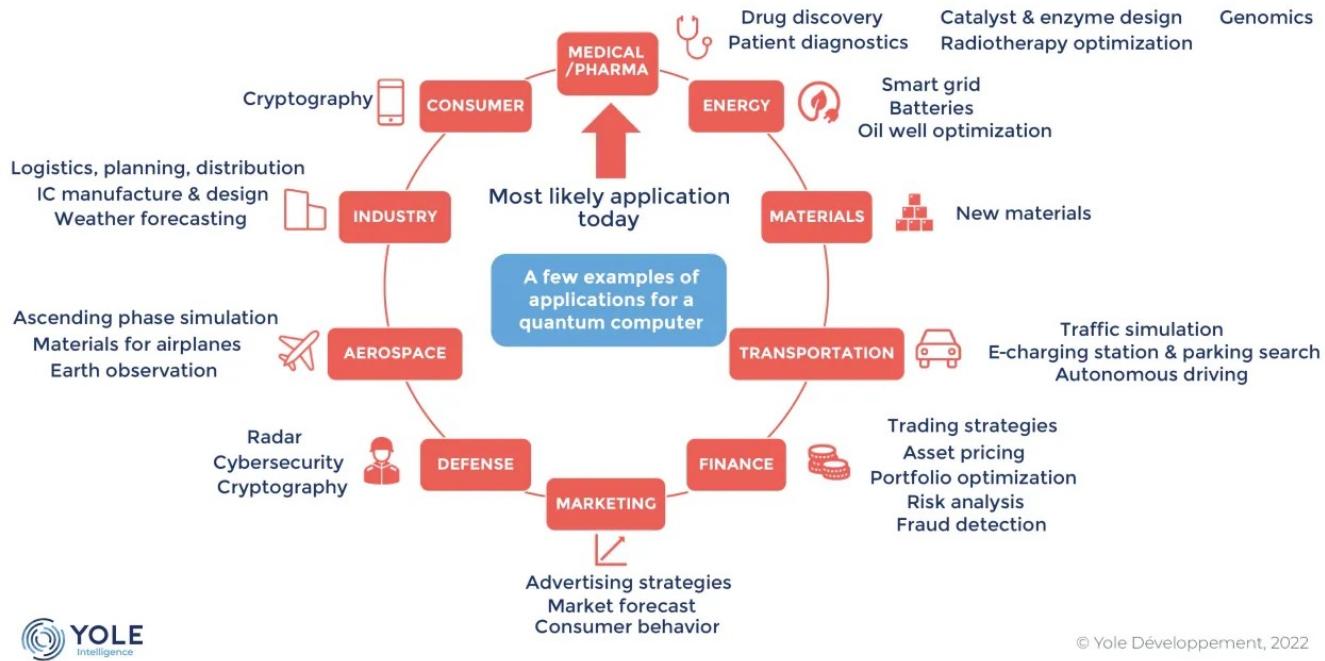
“Fault-tolerant control of an error-corrected qubit”

10.1038/s41586-021-03928-y

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QUANTUM COMPUTING – MULTIPLE COMPLEX PROBLEMS IN MULTIPLE MARKETS

Source: Quantum Technologies report, Yole Développement, 2021





Ising formulations of many NP problems

Andrew Lucas*

Lyman Laboratory of Physics, Department of Physics, Harvard University, Cambridge, MA, USA

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Ryan Babbush, *Harvard University, USA*

Bryan A. O’Gorman, *NASA, USA*

***Correspondence:**

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e-mail: lucas@fas.harvard.edu

We provide Ising formulations for many NP-complete and NP-hard problems, including all of Karp’s 21 NP-complete problems. This collects and extends mappings to the Ising model from partitioning, covering, and satisfiability. In each case, the required number of spins is at most cubic in the size of the problem. This work may be useful in designing adiabatic quantum optimization algorithms.

Keywords: spin glasses, complexity theory, adiabatic quantum computation, NP, algorithms

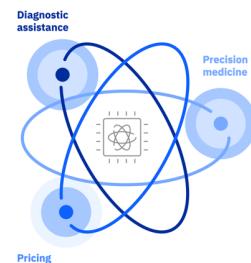
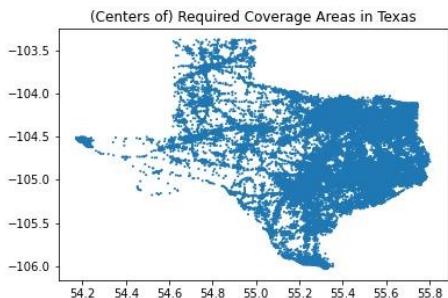
Problems with an unreasonably large solution space



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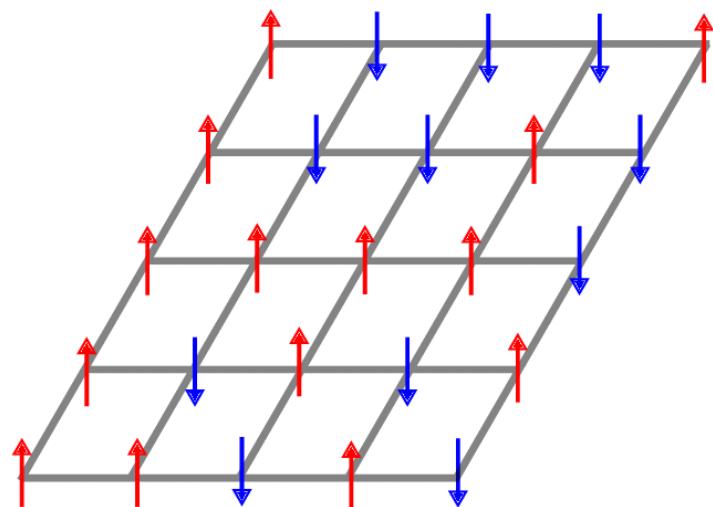
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Figure 1
Quantum computers may enable three key healthcare use cases that reinforce each other in a virtuous cycle. For instance, accurate diagnoses enable precise treatments, as well as a better reflection of patient risks in pricing models.



Ising Model

$$\mathcal{H} = -J \sum_i \vec{\sigma}_i \cdot \vec{\sigma}_{i+1} + h_x \sum_i \sigma_i^x$$



Problems with an unreasonably large solution space



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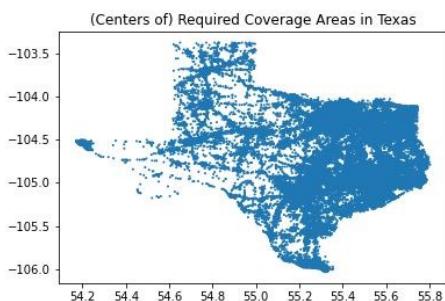


Figure 1
Quantum computers may enable three key healthcare use cases that reinforce each other in a virtuous cycle. For instance, accurate diagnoses enable precise treatments, as well as a better reflection of patient risks in pricing models.

Variational algorithms

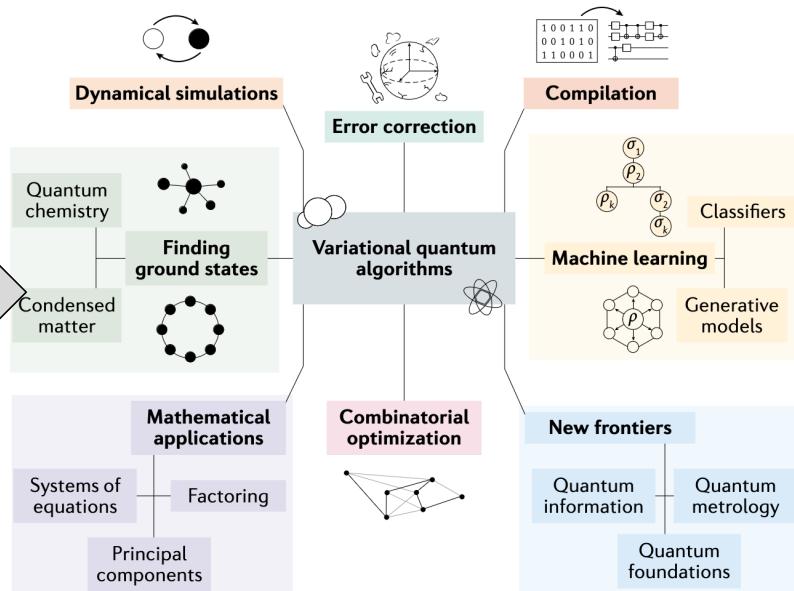


Fig. 1 | Applications of variational quantum algorithms. Many applications have been envisaged for variational quantum algorithms. Here we show some of the key applications that are discussed in this Review.

Problems with an unreasonably large solution space



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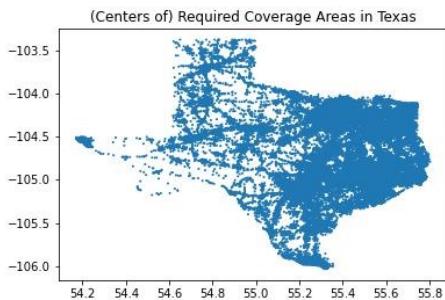
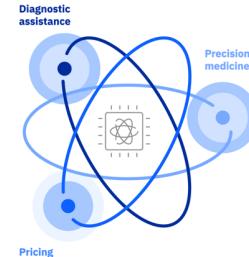


Figure 1
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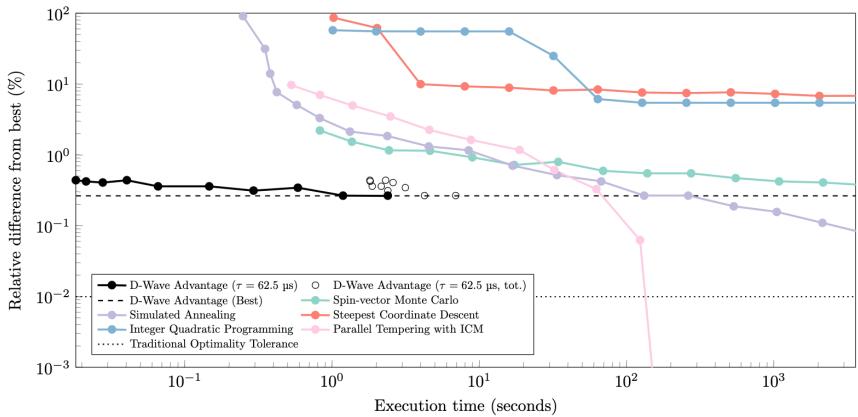


On the Emerging Potential of Quantum Annealing Hardware for Combinatorial Optimization

Byron Tasseff
Los Alamos National Laboratory, Los Alamos, NM 87545

Tameem Albash
University of New Mexico, Albuquerque, NM 87131

Zachary Morrell, Marc Vuffray, Andrey Y. Lokhov, Sidhant Misra, Carleton Coffrin*
Los Alamos National Laboratory, Los Alamos, NM 87545



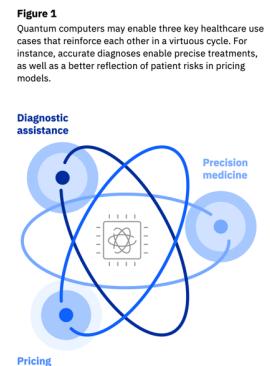
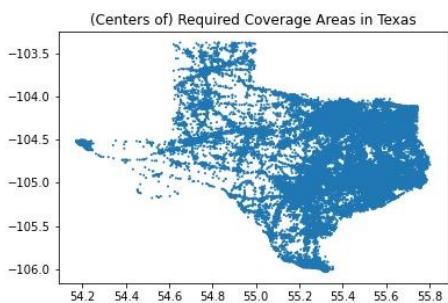
Why quantum computing?

Problems with an unreasonably large solution space

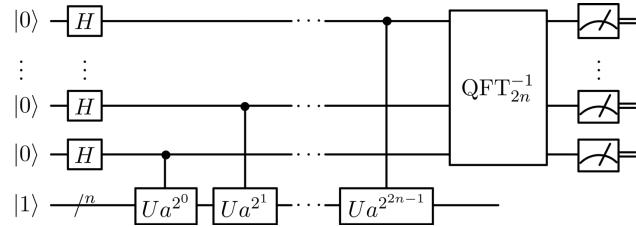
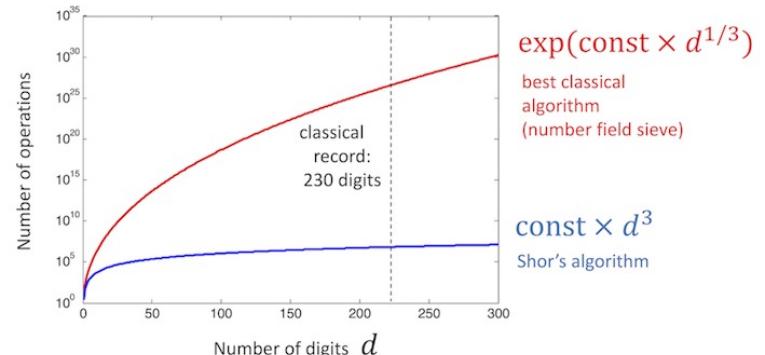


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Efficient algorithms



<https://quantum-computing.ibm.com/>

Why quantum computing?

Problems with an unreasonably large solution space



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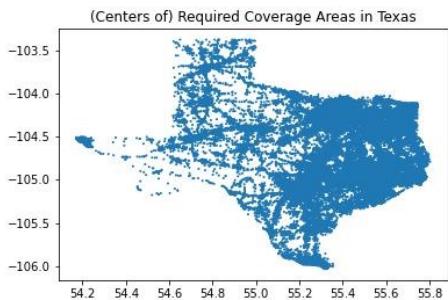
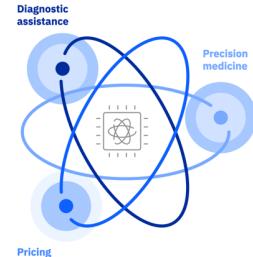


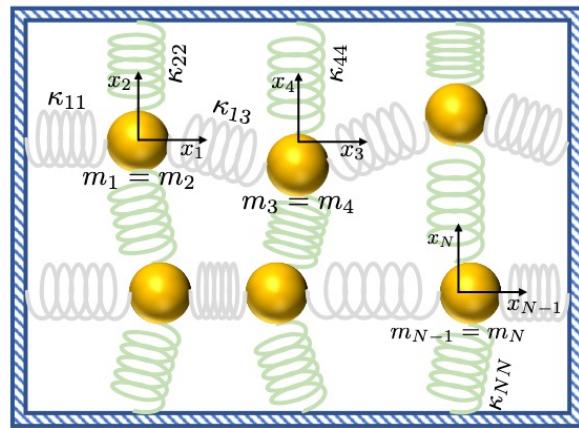
Figure 1
Quantum computers may enable three key healthcare use cases that reinforce each other in a virtuous cycle. For instance, accurate diagnoses enable precise treatments, as well as a better reflection of patient risks in pricing models.



Efficient algorithms

Exponential quantum speedup in simulating coupled classical oscillators

Ryan Babbush,¹ Dominic W. Berry,² Robin Kothari,¹ Rolando D. Somma,¹ and Nathan Wiebe^{3, 4, 5}



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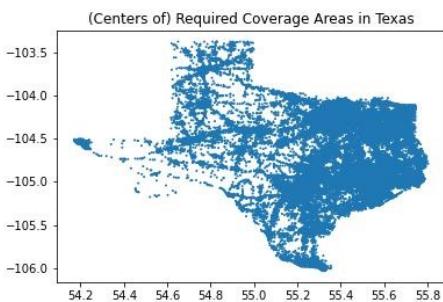
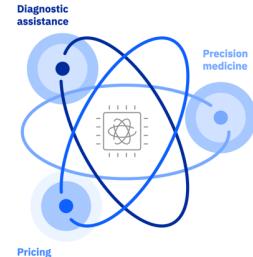


Figure 1
Quantum computers may enable three key healthcare use cases that reinforce each other in a virtuous cycle. For instance, accurate diagnoses enable precise treatments, as well as a better reflection of patient risks in pricing models.



Efficient algorithms

A quantum algorithm for the linear Vlasov equation with collisions

Abtin Ameri

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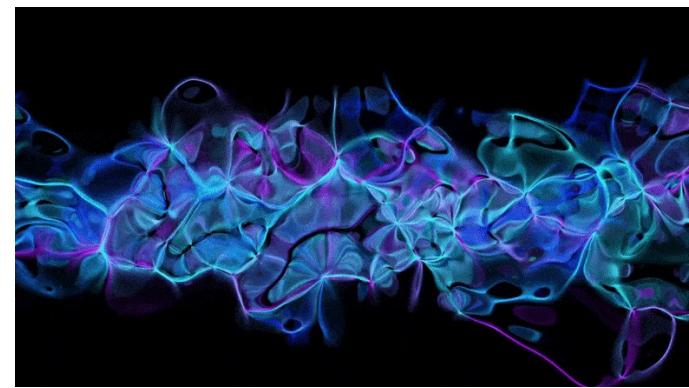
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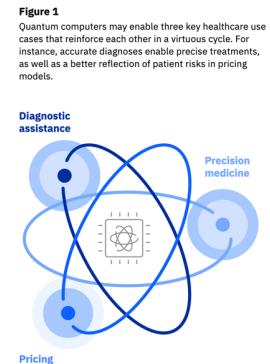
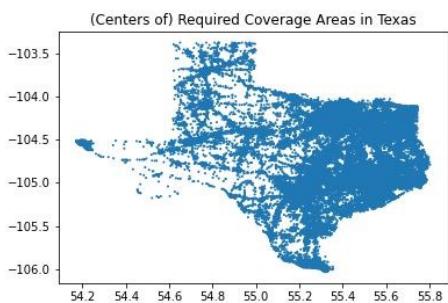
Erika Ye

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(Dated: March 8, 2023)



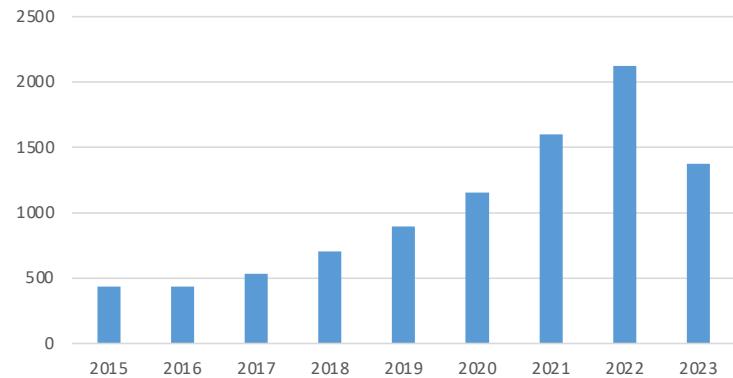
Why quantum computing?

Problems with an unreasonably large solution space



Efficient algorithms

arXiv hits for "Quantum Algorithm"



(data from June 2023)

Simulating Physics with Computers

Richard P. Feynman

Department of Physics, California Institute of Technology, Pasadena, California 91107

Received May 7, 1981

1. Can classical physics be simulated by a classical computer?
2. Can quantum physics be simulated by a classical computer?
3. Can physics be simulated by a quantum computer?
4. Can classical physics be simulated by a quantum computer?

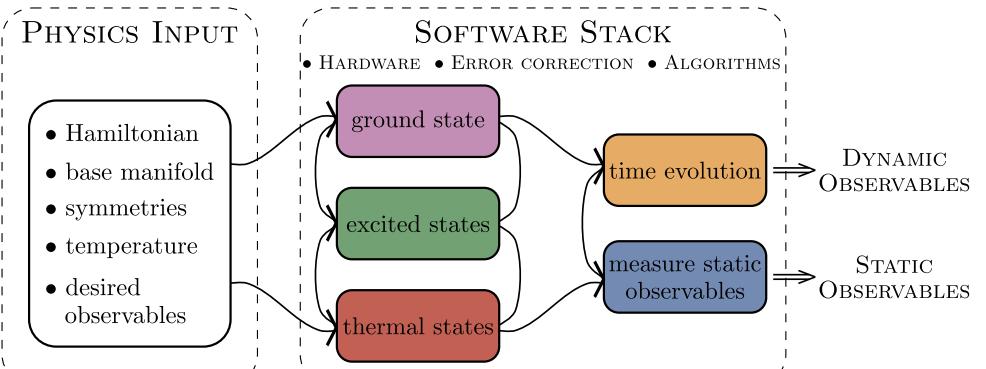
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