

CS 381, Spring 2020

Homework 3 (Semantics)

Please follow carefully *all* of the following steps:

1. Prepare a Haskell or literate Haskell file (ending in `.hs` or `.lhs`, respectively) that compiles without errors in GHCi. (Put all non-working parts and all non-code answers in comments in the file.)
2. Submit *one* solution per group (each group can have up to 5 members) through Canvas.

Late submissions will **not** be accepted. Do **not** send solutions by email.

Exercise 1. A Stack Language

Consider the stack language S defined by the following grammar.

$$\begin{aligned} S &::= C \mid C;S \\ C &::= LD\ Int \mid ADD \mid MULT \mid DUP \end{aligned}$$

An S -program essentially consists of a (non-empty) sequence of commands/operations C . The meaning of an S -program is to start with an empty stack and to perform its first operation on it, which results in a new stack to which the second operation in S (if it exists) is applied, and so on. The stack that results from the application of the last command is the result of the program.

The operation `LD` loads its integer parameter onto the stack. The operation `ADD` removes the two topmost integers from the stack and puts their sum onto the stack. If the stack contains fewer than two elements, `ADD` produces an error. Similarly, the operation `MULT` takes the two topmost integers from the stack and puts their product on top of the stack. It also produces an error if the stack contains fewer than two elements. Finally, the operation `DUP` places a second copy of the stack's topmost element on the stack. (You can find out the error condition for `DUP` yourself.) Here is a definition of the abstract syntax that you should use.

```
type Prog = [Cmd]

data Cmd = LD Int
         | ADD
         | MULT
         | DUP
```

Integer stacks should be represented by the type `[Int]`, that is, lists of integers, that is, your program should contain and use the following definition.

```
type Stack = [Int]
```

Define the semantics for the stack language as a Haskell function `sem` that yields the semantics of a program. Please note that the semantic domain has to be defined as a function domain (since the meaning of a stack program is a transformation of stacks) *and* as an error domain (since operations can fail). Therefore, `sem` has to have the following type where you have to find an appropriate type definition for `D`.

```
sem :: Prog -> D
```

To define `sem` you probably want to define an auxiliary function `semCmd` for the semantics of individual operations, which has the following type.

```
semCmd :: Cmd -> D
```

Hint. Test your functions with the programs `[LD 3,DUP,ADD,DUP,MULT]` and `[LD 3,ADD]` and the empty stack `[]` as inputs.

Exercise 2. Mini Logo

Consider the simplified version of Mini Logo (without macros), defined by the following abstract syntax.

```
data Cmd = Pen Mode
         | MoveTo Int Int
         | Seq Cmd Cmd
```

```
data Mode = Up | Down
```

The semantics of a Mini Logo program is ultimately a set of drawn lines. However, for the definition of the semantics a “drawing state” must be maintained that keeps track of the current position of the pen and the pen’s status (`Up` or `Down`). This state should be represented by values of the following type.

```
type State = (Mode,Int,Int)
```

The semantic domain representing a set of drawn lines is represented by the type `Lines`.

```
type Line  = (Int,Int,Int,Int)
type Lines = [Line]
```

Define the semantics of Mini Logo by giving two function definitions. First, define a function `semS` that has the following type.

```
semS :: Cmd -> State -> (State,Lines)
```

This function defines for each `Cmd` how it modifies the current drawing state and what lines it produces.

After that define the semantic function `sem'` of the following type. (The name `sem'` is used to avoid a conflict with the function `sem` from exercise 1 and allow all definitions to go into one file.)

```
sem' :: Cmd -> Lines
```

The function `sem'` should call `semS`. The initial state is defined to have the pen up and the current drawing position at `(0, 0)`.

Note. To test your semantics you can use the function `ppLines` defined in the Haskell file provided on the class web site. This function converts a list of lines into an svg file that can be rendered by most browsers into a picture.