

# Radiant exitance

In radiometry, **radiant exitance** or **radiant emittance** is the radiant flux emitted by a surface per unit area, whereas **spectral exitance** or **spectral emittance** is the radiant exitance of a surface per unit frequency or wavelength, depending on whether the spectrum is taken as a function of frequency or of wavelength. This is the emitted component of radiosity. The SI unit of radiant exitance is the watt per square metre (W/m<sup>2</sup>), while that of spectral exitance in frequency is the watt per square metre per hertz (W·m<sup>−2</sup>·Hz<sup>−1</sup>) and that of spectral exitance in wavelength is the watt per square metre per metre (W·m<sup>−3</sup>)—commonly the watt per square metre per nanometre (W·m<sup>−2</sup>·nm<sup>−1</sup>). The CGS unit erg per square centimeter per second (erg·cm<sup>−2</sup>·s<sup>−1</sup>) is often used in astronomy. Radiant exitance is often called "intensity" in branches of physics other than radiometry, but in radiometry this usage leads to confusion with radiant intensity.

## Contents

### Mathematical definitions

- Radiant exitance
- Spectral exitance

### SI radiometry units

### See also

### References

## Mathematical definitions

### Radiant exitance

**Radiant exitance** of a *surface*, denoted *M*<sub>e</sub> ("e" for "energetic", to avoid confusion with photometric quantities), is defined as<sup>[1]</sup>

$$M_{\mathrm{e}} = \frac{\partial \Phi_{\mathrm{e}}}{\partial A},$$

where

- ∂* is the partial derivative symbol;
- Φ*<sub>e</sub> is the radiant flux *emitted*;
- A* is the area.

If we want to talk about the radiant flux *received* by a surface, we speak of irradiance.

The radiant exitance of a black surface, according to the Stefan–Boltzmann law, is equal to:

$$M_{\mathrm{e}}^{\circ} = \sigma T^4,$$

where

- σ* is the Stefan–Boltzmann constant;

- $T$  is the temperature of that surface,

so for a real surface, the radiant exitance is equal to:

$$M_e = \varepsilon M_e^\circ = \varepsilon \sigma T^4,$$

where  $\varepsilon$  is the emissivity of that surface.

## Spectral exitance

**Spectral exitance in frequency** of a *surface*, denoted  $M_{e,\nu}$ , is defined as<sup>[1]</sup>

$$M_{e,\nu} = \frac{\partial M_e}{\partial \nu},$$

where  $\nu$  is the frequency.

**Spectral exitance in wavelength** of a *surface*, denoted  $M_{e,\lambda}$ , is defined as<sup>[1]</sup>

$$M_{e,\lambda} = \frac{\partial M_e}{\partial \lambda},$$

where  $\lambda$  is the wavelength.

The spectral exitance of a black surface around a given frequency or wavelength, according to the Lambert's cosine law and the Planck's law, is equal to:

$$M_{e,\nu}^\circ = \pi L_{e,\Omega,\nu}^\circ = \frac{2\pi h \nu^3}{c^2} \frac{1}{e^{\frac{h\nu}{kT}} - 1},$$

$$M_{e,\lambda}^\circ = \pi L_{e,\Omega,\lambda}^\circ = \frac{2\pi h c^2}{\lambda^5} \frac{1}{e^{\frac{hc}{\lambda kT}} - 1},$$

where

- $h$  is the Planck constant;
- $\nu$  is the frequency;
- $\lambda$  is the wavelength;
- $k$  is the Boltzmann constant;
- $c$  is the speed of light in the medium;
- $T$  is the temperature of that surface,

so for a real surface, the spectral exitance is equal to:

$$M_{e,\nu} = \varepsilon M_{e,\nu}^\circ = \frac{2\pi h \varepsilon \nu^3}{c^2} \frac{1}{e^{\frac{h\nu}{kT}} - 1},$$

$$M_{e,\lambda} = \varepsilon M_{e,\lambda}^\circ = \frac{2\pi h \varepsilon c^2}{\lambda^5} \frac{1}{e^{\frac{hc}{\lambda kT}} - 1}.$$

# SI radiometry units

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## SI radiometry units

Quantity		Unit		Dimension	Notes
Name	Symbol <sup>[nb 1]</sup>	Name	Symbol	Symbol	
<u>Radiant energy</u>	$Q_e$ <sup>[nb 2]</sup>	joule	J	$M \cdot L^2 \cdot T^{-2}$	Energy of electromagnetic radiation.
<u>Radiant energy density</u>	$w_e$	joule per cubic metre	J/m <sup>3</sup>	$M \cdot L^{-1} \cdot T^{-2}$	Radiant energy per unit volume.
<u>Radiant flux</u>	$\Phi_e$ <sup>[nb 2]</sup>	watt	$\underline{W} = J/s$	$M \cdot L^2 \cdot T^{-3}$	Radiant energy emitted, reflected, transmitted or received, per unit time. This is sometimes also called "radiant power".
<u>Spectral flux</u>	$\Phi_{e,\nu}$ <sup>[nb 3]</sup> or $\Phi_{e,\lambda}$ <sup>[nb 4]</sup>	watt per hertz or watt per metre	W/Hz or W/m	$M \cdot L^2 \cdot T^{-2}$ or $M \cdot L \cdot T^{-3}$	Radiant flux per unit frequency or wavelength. The latter is commonly measured in W·nm <sup>−1</sup> .
<u>Radiant intensity</u>	$I_{e,\Omega}$ <sup>[nb 5]</sup>	watt per steradian	W/sr	$M \cdot L^2 \cdot T^{-3}$	Radiant flux emitted, reflected, transmitted or received, per unit solid angle. This is a <i>directional</i> quantity.
<u>Spectral intensity</u>	$I_{e,\Omega,\nu}$ <sup>[nb 3]</sup> or $I_{e,\Omega,\lambda}$ <sup>[nb 4]</sup>	watt per steradian per hertz or watt per steradian per metre	W·sr <sup>−1</sup> ·Hz <sup>−1</sup> or W·sr <sup>−1</sup> ·m <sup>−1</sup>	$M \cdot L^2 \cdot T^{-2}$ or $M \cdot L \cdot T^{-3}$	Radiant intensity per unit frequency or wavelength. The latter is commonly measured in W·sr <sup>−1</sup> ·nm <sup>−1</sup> . This is a <i>directional</i> quantity.
<u>Radiance</u>	$L_{e,\Omega}$ <sup>[nb 5]</sup>	watt per steradian per square metre	W·sr <sup>−1</sup> ·m <sup>−2</sup>	$M \cdot T^{-3}$	Radiant flux emitted, reflected, transmitted or received by a <i>surface</i> , per unit solid angle per unit projected area. This is a <i>directional</i> quantity. This is sometimes also confusingly called "intensity".
<u>Spectral radiance</u>	$L_{e,\Omega,\nu}$ <sup>[nb 3]</sup> or $L_{e,\Omega,\lambda}$ <sup>[nb 4]</sup>	watt per steradian per square metre per hertz or watt per steradian	W·sr <sup>−1</sup> ·m <sup>−2</sup> ·Hz <sup>−1</sup> or W·sr <sup>−1</sup> ·m <sup>−3</sup>	$M \cdot T^{-2}$ or $M \cdot L^{-1} \cdot T^{-3}$	Radiance of a <i>surface</i> per unit frequency or wavelength. The latter is commonly measured in

		per square metre, per metre			$\text{W} \cdot \text{sr}^{-1} \cdot \text{m}^{-2} \cdot \text{nm}^{-1}$ . This is a <i>directional</i> quantity. This is sometimes also confusingly called "spectral intensity".
<u>Irradiance</u> <u>Flux density</u>	$E_e$ <sup>[nb 2]</sup>	watt per square metre	$\text{W}/\text{m}^2$	$\mathbf{M} \cdot \mathbf{T}^{-3}$	Radiant flux <i>received</i> by a <i>surface</i> per unit area. This is sometimes also confusingly called "intensity".
<u>Spectral irradiance</u> <u>Spectral flux density</u>	$E_{e,\nu}$ <sup>[nb 3]</sup> or $E_{e,\lambda}$ <sup>[nb 4]</sup>	watt per square metre per hertz or watt per square metre, per metre	$\text{W} \cdot \text{m}^{-2} \cdot \text{Hz}^{-1}$ or $\text{W}/\text{m}^3$	$\mathbf{M} \cdot \mathbf{T}^{-2}$ or $\mathbf{M} \cdot \mathbf{L}^{-1} \cdot \mathbf{T}^{-3}$	Irradiance of a <i>surface</i> per unit frequency or wavelength. This is sometimes also confusingly called "spectral intensity". Non-SI units of spectral flux density include <u>jansky</u> (1 Jy = $10^{-26} \text{ W} \cdot \text{m}^{-2} \cdot \text{Hz}^{-1}$ ) and <u>solar flux unit</u> (1 sfu = $10^{-22} \text{ W} \cdot \text{m}^{-2} \cdot \text{Hz}^{-1}$ = $10^4$ Jy).
<u>Radiosity</u>	$J_e$ <sup>[nb 2]</sup>	watt per square metre	$\text{W}/\text{m}^2$	$\mathbf{M} \cdot \mathbf{T}^{-3}$	Radiant flux <i>leaving</i> (emitted, reflected and transmitted by) a <i>surface</i> per unit area. This is sometimes also confusingly called "intensity".
<u>Spectral radiosity</u>	$J_{e,\nu}$ <sup>[nb 3]</sup> or $J_{e,\lambda}$ <sup>[nb 4]</sup>	watt per square metre per hertz or watt per square metre, per metre	$\text{W} \cdot \text{m}^{-2} \cdot \text{Hz}^{-1}$ or $\text{W}/\text{m}^3$	$\mathbf{M} \cdot \mathbf{T}^{-2}$ or $\mathbf{M} \cdot \mathbf{L}^{-1} \cdot \mathbf{T}^{-3}$	Radiosity of a <i>surface</i> per unit frequency or wavelength. The latter is commonly measured in $\text{W} \cdot \text{m}^{-2} \cdot \text{nm}^{-1}$ . This is sometimes also confusingly called "spectral intensity".
<u>Radiant exitance</u>	$M_e$ <sup>[nb 2]</sup>	watt per square metre	$\text{W}/\text{m}^2$	$\mathbf{M} \cdot \mathbf{T}^{-3}$	Radiant flux <i>emitted</i> by a <i>surface</i> per unit area. This is the emitted component of radiosity. "Radiant emittance" is an old term for this quantity. This is sometimes also confusingly called "intensity".
<u>Spectral exitance</u>		watt per square			Radiant exitance of

	$M_{e,v}$ <sup>[nb 3]</sup> or $M_{e,\lambda}$ <sup>[nb 4]</sup>	metre per hertz or watt per square metre, per metre	$W \cdot m^{-2} \cdot Hz^{-1}$ or $W/m^3$	$M \cdot T^{-2}$ or $M \cdot L^{-1} \cdot T^{-3}$	a <i>surface</i> per unit frequency or wavelength. The latter is commonly measured in $W \cdot m^{-2} \cdot nm^{-1}$ . "Spectral emittance" is an old term for this quantity. This is sometimes also confusingly called "spectral intensity".
<u>Radiant exposure</u>	$H_e$	joule per square metre	$J/m^2$	$M \cdot T^{-2}$	Radiant energy received by a <i>surface</i> per unit area, or equivalently irradiance of a <i>surface</i> integrated over time of irradiation. This is sometimes also called "radiant fluence".
<u>Spectral exposure</u>	$H_{e,v}$ <sup>[nb 3]</sup> or $H_{e,\lambda}$ <sup>[nb 4]</sup>	joule per square metre per hertz or joule per square metre, per metre	$J \cdot m^{-2} \cdot Hz^{-1}$ or $J/m^3$	$M \cdot T^{-1}$ or $M \cdot L^{-1} \cdot T^{-2}$	Radiant exposure of a <i>surface</i> per unit frequency or wavelength. The latter is commonly measured in $J \cdot m^{-2} \cdot nm^{-1}$ . This is sometimes also called "spectral fluence".
<u>Hemispherical emissivity</u>	$\varepsilon$			<b>1</b>	Radiant exitance of a <i>surface</i> , divided by that of a <i>black body</i> at the same temperature as that surface.
<u>Spectral hemispherical emissivity</u>	$\varepsilon_v$ or $\varepsilon_\lambda$			<b>1</b>	Spectral exitance of a <i>surface</i> , divided by that of a <i>black body</i> at the same temperature as that surface.
<u>Directional emissivity</u>	$\varepsilon_\Omega$			<b>1</b>	Radiance <i>emitted</i> by a <i>surface</i> , divided by that emitted by a <i>black body</i> at the same temperature as that surface.
<u>Spectral directional emissivity</u>	$\varepsilon_{\Omega,v}$ or $\varepsilon_{\Omega,\lambda}$			<b>1</b>	Spectral radiance <i>emitted</i> by a <i>surface</i> , divided by that of a <i>black body</i> at the same

					temperature as that surface.
<u>Hemispherical absorptance</u>	$A$			1	Radiant flux <i>absorbed</i> by a <i>surface</i> , divided by that received by that surface. This should not be confused with "absorbance".
<u>Spectral hemispherical absorptance</u>	$A_v$ or $A_\lambda$			1	Spectral flux <i>absorbed</i> by a <i>surface</i> , divided by that received by that surface. This should not be confused with "spectral absorbance".
<u>Directional absorptance</u>	$A_\Omega$			1	Radiance <i>absorbed</i> by a <i>surface</i> , divided by the radiance incident onto that surface. This should not be confused with "absorbance".
<u>Spectral directional absorptance</u>	$A_{\Omega,v}$ or $A_{\Omega,\lambda}$			1	Spectral radiance <i>absorbed</i> by a <i>surface</i> , divided by the spectral radiance incident onto that surface. This should not be confused with "spectral absorbance".
<u>Hemispherical reflectance</u>	$R$			1	Radiant flux <i>reflected</i> by a <i>surface</i> , divided by that received by that surface.
<u>Spectral hemispherical reflectance</u>	$R_v$ or $R_\lambda$			1	Spectral flux <i>reflected</i> by a <i>surface</i> , divided by that received by that surface.
<u>Directional reflectance</u>	$R_\Omega$			1	Radiance <i>reflected</i> by a <i>surface</i> , divided by that received by that surface.
<u>Spectral directional reflectance</u>	$R_{\Omega,v}$ or $R_{\Omega,\lambda}$			1	Spectral radiance <i>reflected</i> by a <i>surface</i> , divided by that received by that surface.
<u>Hemispherical</u>	$T$			1	Radiant flux

<u>transmittance</u>					<i>transmitted</i> by a <i>surface</i> , divided by that received by that surface.
<u>Spectral hemispherical transmittance</u>	$T_v$ or $T_\lambda$			<b>1</b>	Spectral flux <i>transmitted</i> by a <i>surface</i> , divided by that received by that surface.
<u>Directional transmittance</u>	$T_\Omega$			<b>1</b>	Radiance <i>transmitted</i> by a <i>surface</i> , divided by that received by that surface.
<u>Spectral directional transmittance</u>	$T_{\Omega,v}$ or $T_{\Omega,\lambda}$			<b>1</b>	Spectral radiance <i>transmitted</i> by a <i>surface</i> , divided by that received by that surface.
<u>Hemispherical attenuation coefficient</u>	$\mu$	reciprocal metre	$\text{m}^{-1}$	<b>L<sup>-1</sup></b>	Radiant flux <i>absorbed</i> and <i>scattered</i> by a <i>volume</i> per unit length, divided by that received by that volume.
<u>Spectral hemispherical attenuation coefficient</u>	$\mu_v$ or $\mu_\lambda$	reciprocal metre	$\text{m}^{-1}$	<b>L<sup>-1</sup></b>	Spectral radiant flux <i>absorbed</i> and <i>scattered</i> by a <i>volume</i> per unit length, divided by that received by that volume.
<u>Directional attenuation coefficient</u>	$\mu_\Omega$	reciprocal metre	$\text{m}^{-1}$	<b>L<sup>-1</sup></b>	Radiance <i>absorbed</i> and <i>scattered</i> by a <i>volume</i> per unit length, divided by that received by that volume.
<u>Spectral directional attenuation coefficient</u>	$\mu_{\Omega,v}$ or $\mu_{\Omega,\lambda}$	reciprocal metre	$\text{m}^{-1}$	<b>L<sup>-1</sup></b>	Spectral radiance <i>absorbed</i> and <i>scattered</i> by a <i>volume</i> per unit length, divided by that received by that volume.
See also: <a href="#">SI</a> · <a href="#">Radiometry</a> · <a href="#">Photometry</a>					

1. **Standards organizations** recommend that radiometric **quantities** should be denoted with suffix "e" (for "energetic") to avoid confusion with photometric or **photon** quantities.
2. Alternative symbols sometimes seen: *W* or *E* for radiant energy, *P* or *F* for radiant flux, *I* for irradiance, *W* for radiant exitance.
3. Spectral quantities given per unit **frequency** are denoted with suffix "**v**" (Greek)—not to be confused with suffix "v" (for "visual") indicating a photometric quantity.
4. Spectral quantities given per unit **wavelength** are denoted with suffix "**λ**" (Greek).
5. Directional quantities are denoted with suffix "**Ω**" (Greek).