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Abstract

We conduct a survey study on machine learning, its mathematical foundations, general techniques, and the latest progress in both the academia and the industry. However, most machine learners excel only at the task they are trained for - this is a huge limitation. Motivated by this, we study a new paradigm called the Never-Ending Language Learning (NELL)¹ and its potentials to overcome the singular nature of machine learners. Lastly, we design and implement a system based on NELL to predict the stock market performance. This is driven by the abundance of data, and the complex, interacting, non-singular nature of the task that a machine learner has yet to match a human on.

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1 Introduction

We have just entered the golden age of machine learning. The field has in fact been around for decades, born from artificial intelligence and pattern recognition. It wasn't until recently that we have the level of computational power and the abundance of data to apply it.

The machine learners have accomplished some truly astonishing feats. They are systems that are trained with a copious amount of data, which allows them to surpass the performance level of human experts. Today, they are actively being researched and deployed by the biggest tech companies such as Google, IBM, Microsoft, Facebook. In fact, their major products are powered by machine learning - Google AdSense, IBM Watson, and Facebook's M - doing tasks such as ads suggestion, image recognition, medical diagnosis, and natural language processing.

Typically, machine learning is best suited for the tasks that cannot be solved precisely or efficiently by algorithms. Many of these are what humans excel at - image recognition, language processing, pattern deduction. These capabilities are so trivial to us, yet they are so difficult to mimic by traditional algorithmic approaches. The prime example of "*a child can easily recognize a cat in a picture, but a super computer can't*" best illustrates the failure of the algorithmic methods. Machine learning comes in to save the day.

In a nutshell, one can think of it as a machine that "learns" from the data. On the implementation level, it is an automated regression software that can construct an impressively accurate model. The machine takes in a training set - input data where each entry is labeled with the intended output, then trains on it and learns to recognize the pattern. After that, when fed with new unlabeled input, it gives some predicted output based on its training. However, just like a typical regression model, its scope is strictly bounded to its training set. For example, a machine that recognizes cats cannot recognize a fish without extra training. Moreover, an image recognizer cannot diagnose diseases. In this sense a machine learner's scope is **singular**. We will address this issue later.

The mathematical foundations of machine learning is built atop regression theory and linear algebra. Next, we present the formalization of a problem in machine learning as well as the terminologies.

1.1 Formalization

The following formalization is standard in the literature, we reference Tom M. Mitchell's popular textbook *Machine Learning*².

Definition 1. A computer program is said to **learn** from experience E with respect to some class of tasks T and performance measure P , if its performance at tasks in T , as measured by P , improves with experience E .

We will use the terms *training* and *learning* interchangeably. Next, we define a **problem**.

Definition 2. A **problem** is a triple $\{T, P, E\}$. The goal of a machine learner solving the problem is to output a learned target function \hat{V} that approximates an ideal target function V . The target function maps from the vector of input features b to the set of output O .

The experience E represents the input data. It is the set of points specifying the configurations of the instances of the problem. To use it for training, the data must be *labeled* / *classified* - every input data must have its output. This is needed for the performance measure P . In the context, it is understood that the data is always labeled.

Often the data set is split into three parts - the training set, validation set, and test set, for obvious statistical reasons. The first is used to weight-tuning (see below) that may yield multiple candidates, the second for validating and choosing the best candidate, and the last for testing against new input data and detecting overfitters.

The feature vector b , output O , and the function representation for \hat{V} are defined by the programmer as deemed suitable. In a simple regression model, b is a list of chosen input features, O is the set of predicted values. Typically the target function \hat{V} will include a set of weights $W = \{w_i \mid i \in \{1, 2, \dots, n\}\}$ which are tuned during the learning. They serve as the “memory” of the machine to compute predicted output once it is trained.

Upon having an explicit representation, and given the training data, we can devise the learning mechanism. First, define an error term ϵ between the training data and the actual machine output. Then, use the error term to devise an algorithm that tunes the weights iteratively to minimize the error. The algorithm terminates on meeting a minimum threshold error, that is when the machine can perform sufficiently good.

Example 1. We provide an explicit example with the checkers game:

The checkers learning problem:

1. Task T : playing checkers
2. Performance measure P : percent of games won
3. Training experience E : games played against another computer

Next we need to determine the representations of the available knowledge. For the input feature vector b , we can choose a few board states, for instance,

$$b = \langle x_1, x_2, x_3, x_4 \rangle$$

where the x_i 's are respectively the numbers of black pieces, black kings, red pieces and red kings on the board. We can choose a simple linear combination as our target function,

$$\hat{V}(b) = w_0 + w_1x_1 + w_2x_2 + w_3x_3 + w_4x_4$$

where w_i 's are the weights to be tuned during the training. Our output set O is the list of moves at each game step given the features x_i 's at the time. We can define a bijection between the output range of $\hat{V}(b)$ and the O , but we will exclude it here.

Once we have a representation, devise a learning mechanism for training. Suppose now we have a set of positive (games won) training examples $\{< b, V_{train}(b) >\}$. Define the error term using simple sum of squares

$$E = \sum_{<b, V_{train}(b)> \in \text{training examples}} (V_{train}(b) - \hat{V}_{train}(b))^2$$

Then, using this, devise an algorithm A for training / weight-tuning. The error term above, when differentiated, yields gradient term of $\sim (V_{train}(b) - \hat{V}_{train}(b))$. One can imagine training as nodging a point closer to its true value, and the gradient gives the direction to nodge towards. This gives us a simple LMS algorithm for minimizing ϵ using that gradient term:

Algorithm LMS weight update (learning) algorithm

Initialize the weights w_i 's to random values. For each training example $< b, V_{train}(b) > :$

1. Use the current weights to compute $\hat{V}(b)$
2. For each weight w_i , update it by

$$w_i \leftarrow w_i + \eta (V_{train}(b) - \hat{V}_{train}(b)) x_i$$

where η is the parameter that moderates the stepsize. The algorithm terminates when w_i 's stop changing, i.e. when the error becomes sufficiently small (zero).

One can quickly see that the example machine learner above is just a simple regressor. Obviously this toy model will not be a good checker player. Nevertheless, given a huge training data, if we choose the right knowledge representation, feature vector b , target function \hat{V} , error term ϵ , and the learning algorithm, the resultant machine can perform very well.

To suit a different type of problem, we can employ a different **representation** - which we define to be the set $\{T, P, E, b, O\}$, as illustrated in Table 1.

Moreover, we can employ different **learning mechanisms** - which we define as the set of target function and learning algorithm, $\{\hat{V}, A\}$. This gives rise to the different techniques, or types, of machine learners such as the Neural Nets, Support Vector Machines, Deep Learning and etc. We will investigate the popular types in the next section.

A huge variety of machine learners today are being used for different purposes - most of the leading tech companies tweak and design their own. They may have very different

T	P	E	b	O
image recognition	correct labeling	labeled images	array of pixels	label of objects
driving a car	successful trip	test drives	traffic condition	wheel, pedals
text translation	correct translations	pretranslated texts	semantics	translated text
ads suggestion	ads click rate	ads metadata	user profile	ads displayed

Table 1: Different representations for various problems.

representations and **learning mechanisms**, but the overall idea is still the same - gather labeled data, define the representations and learning algorithms, and train. The entire process is very modular, and the resultant machines are **stagnant** - the machine no longer improve once training is done; and **singular** - they can only function very narrowly only on the tasks they are trained for. For our discussions, we call this the **stagnant & singular paradigm**. In fact, this paradigm can readily be observed across most of the popular machine learners today. This will serve as the primary motivation of our work.

1.2 Popular techniques

Before getting to the discussion on the paradigm, we take a quick look at the most common and powerful machine learners. These are derived from the same **stagnant & singular paradigm** by varying the **representations** and **learning mechanisms**.

1.2.1 Decision Tree

Decision tree is a popular method stemmed from artificial intelligence, used for hypothesis-searching and inductive reference. It uses a *tree representation*, where each node is a feature variable, and each edge is a value the feature takes on. The leaf nodes are the classification (output) values. Every path from the root to the leaf represents an instance of the feature b and its output o . Moreover, different paths can be combined with logical *OR* and *AND* to yield a more general hypothesis space.

For the *learning mechanism*, a common method is to use the entropy measure and entropy gain while branching on each node (making a decision) while descending the tree. Suppose the data has c classifications (e.g. $c = 2$ for binary classifiers), the entropy is defined as

$$Entropy(D) = \sum_{i=1}^c -p_i \log_2 p_i$$

where D is the data, p_i is the proportion of samples of class i in D . This allows us to judge the performance P and search for the target function \hat{V} by using the entropy gain for each

feature b ,

$$Gain(D, b) = Entropy(D) - \sum_{v \in Values(b)} \frac{|D_v|}{D} Entropy(D_v)$$

where D_v is the subset of D whose feature vector assumes the value equals to v .

Each path in the tree is a candidate hypothesis (collection of contributing features) to consider. Given the multitude of paths in the tree, the algorithm will end up with a set of valid and consistent hypotheses. To resolve them, we simply use the **Occam's razor** - choose the simplest hypothesis that fits the data. This will also prevent overfitting.

1.2.2 ANN with Perceptron

1.2.3 ANN with Gradient Descent

1.2.4 convnet

1.2.5 SVM

1.2.6 Deep Learning

1.3 Applications

Google translate, Google AdSense, Google DeepDream, DeepMind, Google Deep Learning (play game!), IBM Watson

1.4 Paradigm: Powers & Limitations

2 NELL as a New Paradigm

2.1 Inspiration & Features

2.2 Architecture

2.3 Applications

2.4 Powers & Limitations

3 NELL for Stock Market Prediction

3.1 Problem statement

3.2 Potential of NELL

3.3 Design

3.4 Implementation

3.5 Assessment

4 Future Work

4.1 Results, Performance, and Analysis

We immediately see several trends given by the fun function. A clear player order effect was found between nearly every AI. While some AIs were simply more powerful and able to win regardless of characteristics, in nearly every case we see that more wins are generated from the AI if they play first compared to when they play second. For some more closely related

AIs, the odds of winning changes in its favor given the player order effect. From this we can conclude that for certain comparable AIs, player order may greatly affect the outcome of the game.

Furthermore, in every case, the trend line from the total army plot simply shifted its intercept value but held consistent slope. This intercept can be credited to first round play. After the first round (when the first point is calculated) the army advantage can be a one player advantage. This first round however rarely changes the results of the game. Consider figure 1.

Figure 1.

Here the green and red dots represent AI0s and AI4s percent total armies respectively over time. Again, the dots only represent games in which a definitive winner was found. Here we see that AI0 has a clear advantage but when the player order is changed, AI4 wins more games. Notice, however, while the trend line shifts down, that the slope stays constant. This implies that while the game is certainly affected by player order, on average, the game develops the same regardless of player order.

For the same AI match, the fun function provides two survival charts. Now consider figure 2.

Figure 2.

In the first plot we see that player two holds several armies until near round 50. Suddenly over the next two rounds however, we see an incredible drop off. AI0 has mostly defensive characteristics. From this it appears that AI0 condenses its portion of the graph and builds armies. Somewhere near halfway through the game, it branches out and gains several territories in a very small period of time. When the order of the game is reversed we see a much more even trend. Both AIs seem to lose armies at a consistent rate. This effect could be accredited to player order effect or the characteristics of the players in regards to their section of the sub graph.

While these trends, in general, hold true, one AI in particular defied the general trends. We will call this AI, AI3. AI3, in general, tended to produce more wins when playing in the second player position. This trend was tested more rigorously against 15 new AIs. From this data, the fun function produced the win records for both AI3 and the other AIs for both player order. The difference between wins was then calculated. That is $\Delta win = AI3_wins - AIOpponent_wins$. This figure was calculated for both player orders. This data is represented in figure 3.

Figure 3.

As in figure 3, on average AI3 wins 3.625 games while playing second in comparison to playing first where the AI won only 0.5 games on average. This in turn would seem to offer a solution to the player order effect, mentioned above. By simply playing the AI3 characteristics (Survival, Defensive, Cautious, Carry), on average the advantage would go to the second player, thus making player order obsolete.

Another nuanced observation shows that this conclusion may not be entirely true. Under further observation, another AI which we will call AI4 (Survival, Aggressive, Tactical, Rusher) seemed to be superior to AI3 in both player orders. A more rigorous study of these two AIs revealed that the assumption was correct. The fun function showed that on average, AI4 wins more often than AI3. Consider figure 4 and figure 5.

Figure 4.

Figure 5.

Notice that these two figures show very low correlation when player order changes. When AI3 goes first, it grosses more wins than AI4. When AI3 goes second, however, AI4 wins the majority of the games. While by a narrow margin, when AI4 goes first, AI4 wins 56 more games than AI3 in a 500 game trial. Thus if AI3 plays second they will on average lose to AI4.

4.2 AI behaviors and Surprises

In this project several AIs were posed against each other in a game of Risk. Initially, it was predicted that a large player order effect would affect the game. This hypothesis held true for the majority of AIs that were tested in this experiment. AI3 however, proved that by using the correct strategy, a player would actually hold an advantage by going second in the game. From this however, AI4 proved that their still exist AIs that can beat AI3 while being the first player to move.

From this project, we advise future Risk players to abstain from declaring their player strategy until the player order is determined. From this, we advise that second players play a cautious, defensive game, while first players play with aggressive tendencies. A consistent analysis of strategy will reveal the best strategy for either player to take throughout the duration of the game.

5 Conclusion

We have reformatized the board game *Risk* as a graph optimization, and implemented an AI to solve the problem, i.e. to play the game. Several decision algorithms were devised based on graph properties, and they in turn form the personalities of the AI. Our study of 4 binary traits, or a total of 16 personality variations of the AI, is merely the beginning. We have discovered some interesting AI behaviours and performance at a level beyond any human players. One can potentially investigate even more variations of the traits.

For future studies, an analysis of subgraphs would provide deep insight into the value of individual territories. The AIs are built in such a way that the priority function is based off of current demographic of troops and shape of their graph. Evaluating the graph as a whole would provide insight to the value of different subgraphs that would proactively affect the priority function. This conditional thinking is much more like the ideas of a human player and thus could inform future strategies.

Furthermore, game shifts could be analyzed using the fun function and the aforementioned subgraph analysis. This would allow for defensive players an understanding of which territories that are worth defending and worth conceding. This shift parameter would allow for insight to game length, army distribution, and other key factors.

6 References

1. Carnegie Mellon University, *NELL: Never-Ending Language Learning*. <http://rtw.ml.cmu.edu/rtw/>
2. Tom M. Mitchell, *Machine Learning*. McGraw-Hill, 1997.