

XOR is Linear OR Not.

Truth Table

x_1	x_2	y	
0	0	0	$\sum_{i=0}^2 x_i w_i < 0$
1	0	1	$\sum_{i=0}^2 x_i w_i \geq 0$
0	1	1	$\sum_{i=0}^2 x_i w_i \geq 0$
1	1	0	$\sum_{i=0}^2 x_i w_i < 0$

Now

$$\text{Output} = w_1 x_1 + w_2 x_2 + w_0$$

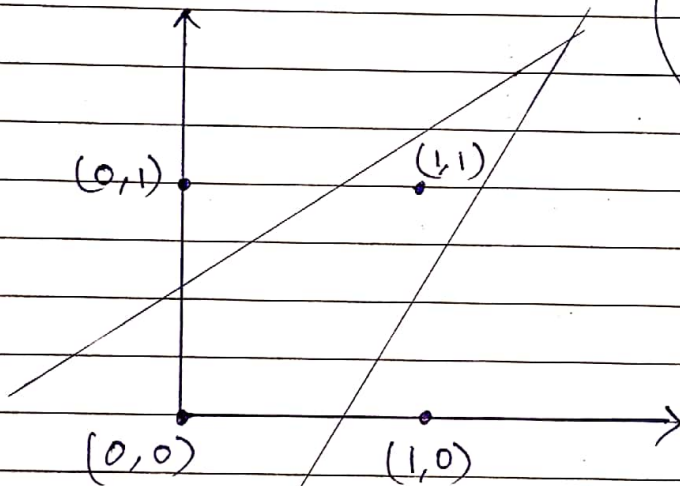
↑
Bias

$$\text{Threshold} = \theta = 1$$

$$\text{Bias} = w_0 = -\theta = -1$$

$$\text{Here } y = x_1 \oplus x_2$$

Now plotting the graph



$$w_0 + w_1 \cdot 0 + w_2 \cdot 0 < 0 \Rightarrow w_0 < 0$$

$$w_0 + w_1 + w_2 \geq 0 \Rightarrow w_1 \geq -w_0$$

$$w_0 + w_1 \cdot 0 + w_2 \geq 0 \Rightarrow w_2 \geq -w_0$$

$$w_0 + w_1 \cdot 0 + w_2 \cdot 0 < 0 \Rightarrow w_0 < 0$$

Linearly separable is if there exist ^{one} a line or plane such that all inputs which produce a 1 lie on one side of the line or plane and all input which produce a 0 lie on other side of the line or plane.

But in case of XOR we need a two line to separate a plane in such way that it divide a 1 on one side and 0's on other side. Hence XOR is not linear.