



UNIVERSITY OF NAIROBI

Loss Distributions For Motor Insurance Claim Severity

Case Study: Kenya

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Data Analysis

Introduction

The motor insurance claim severity data used was obtained from the annual reports of Insurance Regulatory Authority. The data was from 2016 – 2020 and contained 37 insurance companies, all licensed and regulated by IRA. Incurred claims for both motor commercial and motor private classes were analyzed side by side to obtain suitable models for each category. All the analysis was done using the R Programming Language.

Descriptive Statistics

Getting a summarised overview of the data was critical in discovering patterns, especially on skewness.

Table 1: Descriptive statistics for incurred claims (2016-2020)

Stat	Motor Commercial	Motor Private
No. Of Observations	185	185
Mean	296940.7	408137.7
Standard Error	23745.16	30003.67
Median	173695	271419
Standard Deviation	322969.1	408094.0
Kurtosis	5.937997	5.777819
Skewness	1.741602	1.683955
Minimum	0	-24861
Maximum	1470770	1992246
Sum	54934035	75505472

It is clearly evident that incurred claims data for both classes of motor insurance are positively skewed, with motor private having a higher mean than motor commercial.

The next step was to get a visual representation of the distribution of the data.

From the histograms we can affirm that the data from both classes is not only skewed to the right, but also long-tailed. This gives a good hint of the kind of distributions most appropriate to model the data.

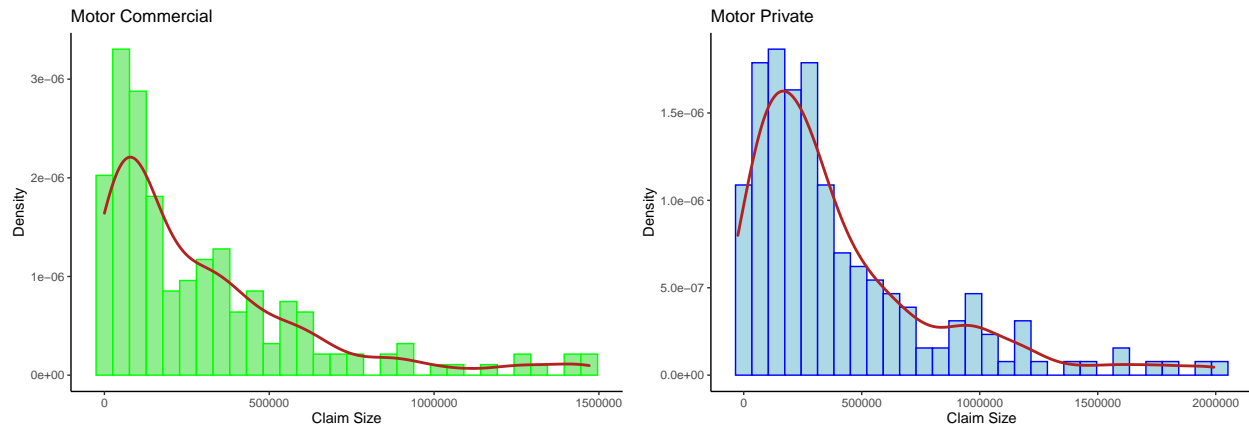


Figure 1: Histograms of original datasets

The Normal QQ-plots in Figure 2 show that the datasets don't match the normal standard distribution.

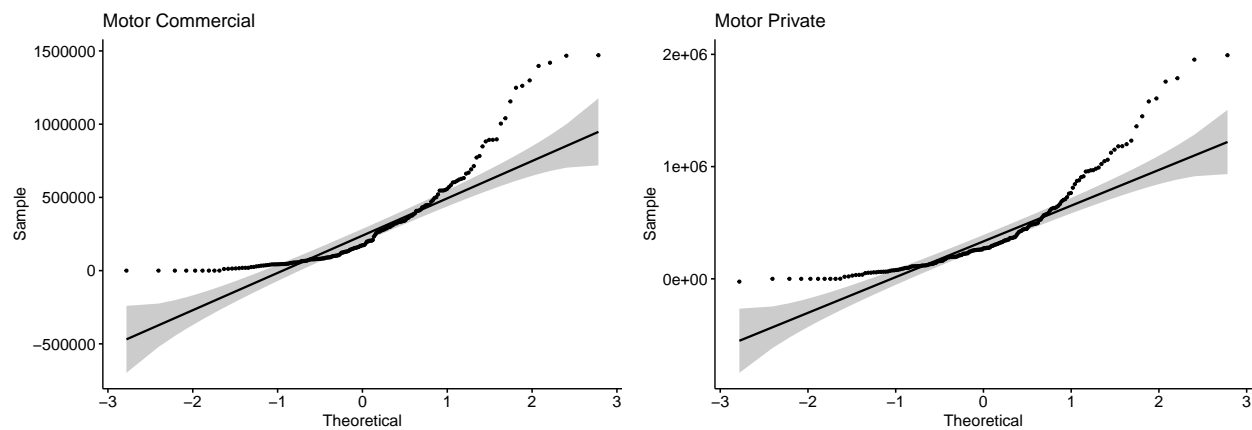


Figure 2: Normal QQ-plots of original data

This is a good indication that after fitting the distributions, non-parametric tests would be applied as opposed to parametric tests.

To make it simpler to work with, we transformed the data using the cube root function. QQ-Plots of the transformed data are shown in Figure 3.

The cube root transformed data seemed to be more suitable for fitting the distributions compared to the original data.

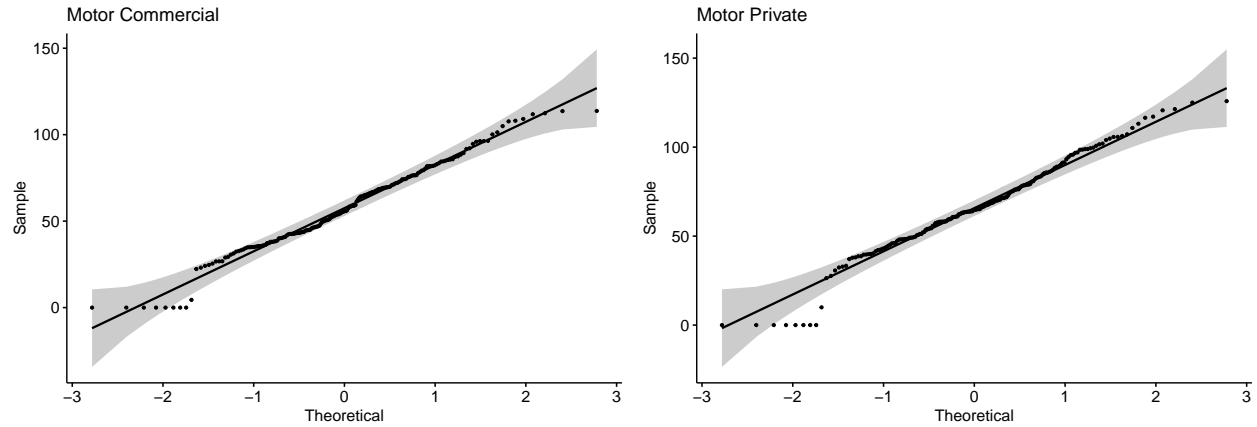


Figure 3: QQ-Plots of transformed data

Parameter Estimation

We used the Maximum Likelihood Estimation (MLE) method to obtain the various fitted distributions. Consequently, the most appropriate distribution is the one with the highest log-likelihood function (LLF).

Table 2: Estimated Parameters For Fitted Distributions

Distribution	Parameter	Motor Commercial	Motor Private
Exponential	Rate	0.02	0.01
	Std. Error	0.00	0.00
	LLF	-901.93	-920.29
Gamma	Shape	6.54	8.90
	Shape Std. Error	0.68	0.93
	Rate	0.11	0.13
	Rate Std. Error	0.01	0.01
	LLF	-800.47	-794.92
Log Normal	Mean Log	4.02	4.17
	Mean Log Std. Error	0.03	0.03
	SD Log	0.42	0.35
	SD Log Std. Error	0.02	0.02
	LLF	-810.28	-801.37
Weibull	Mean Log	2.91	3.33
	Mean Log Std. Error	0.17	0.19
	SD Log	67.40	76.47
	SD Log Std. Error	1.84	1.83
	LLF	-798.55	-795.27

Under the motor commercial class, Weibull distribution has the highest log-likelihood function (-798.55), followed by the Gamma distribution (-800.47), then Log-Normal (-810.28) and finally Exponential distribution (-901.93).

For motor private, Gamma distribution has the highest LLF (-794.92) followed closely by Weibull (-795.27), then Log-Normal (-801.37) and finally the Exponential distribution (-920.29).

From the LLF values, the Weibull distribution is the most appropriate for the motor commercial class and the Gamma distribution for motor private.

Goodness-Of-Fit Test

Typically, measures of goodness-of-fit summarize the discrepancy between observed values and the values expected under the model in question.

Two non-parametric tests were performed:

- Kolmogorov-Smirnov (K-S) test
- Anderson-Darling (A-D) test

Those two were used to determine the appropriateness of the fitted distributions to the incurred claims data.