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CPTS440
HW11

1 Decision trees)

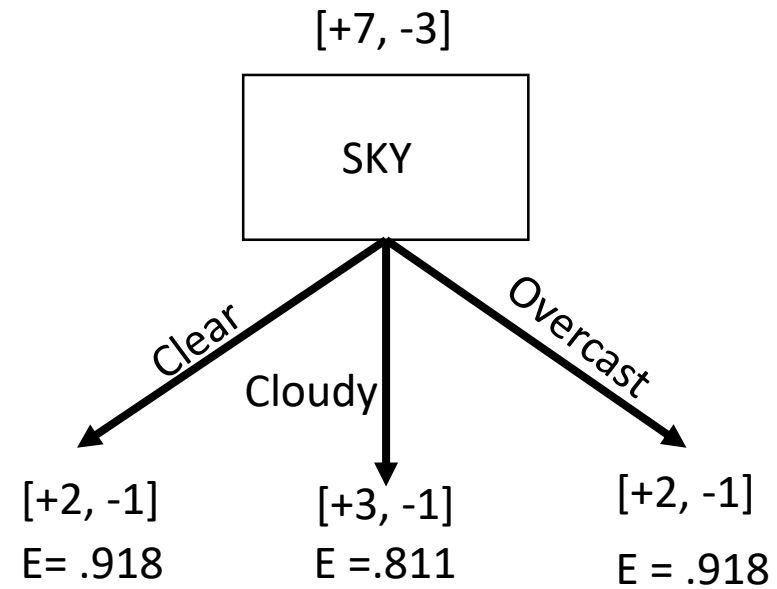
1A)

YES = 7

No = 0

$$\text{Entropy}(s) = -\frac{7}{10} \log_2 \frac{7}{10} - \frac{3}{10} \log_2 \frac{3}{10} = .882$$

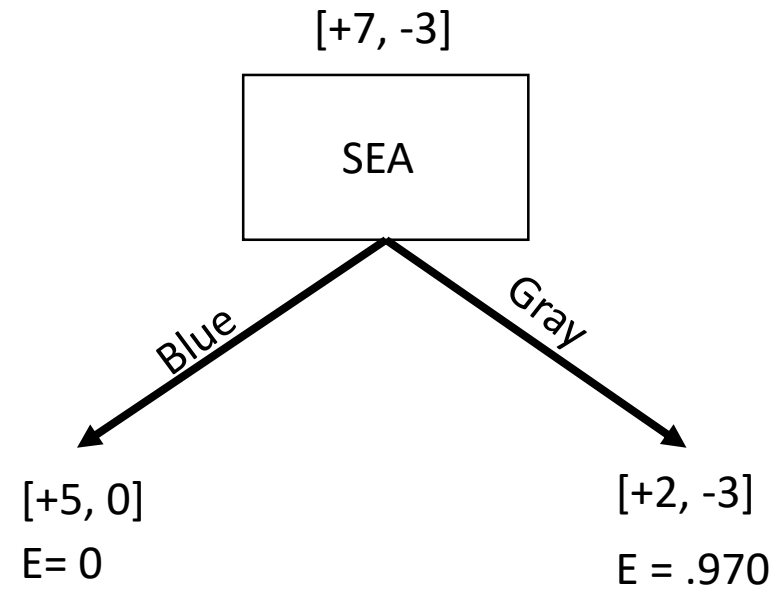
1B)



$$\begin{aligned}\text{Entropy}(S, \text{Sky}) &= .882 - \left[\frac{3}{10} (.918) + \frac{4}{10} (.811) + \frac{3}{10} (.918) \right] \\ &= .882 - .8752 \\ &= .0068\end{aligned}$$

Information gain = .0068

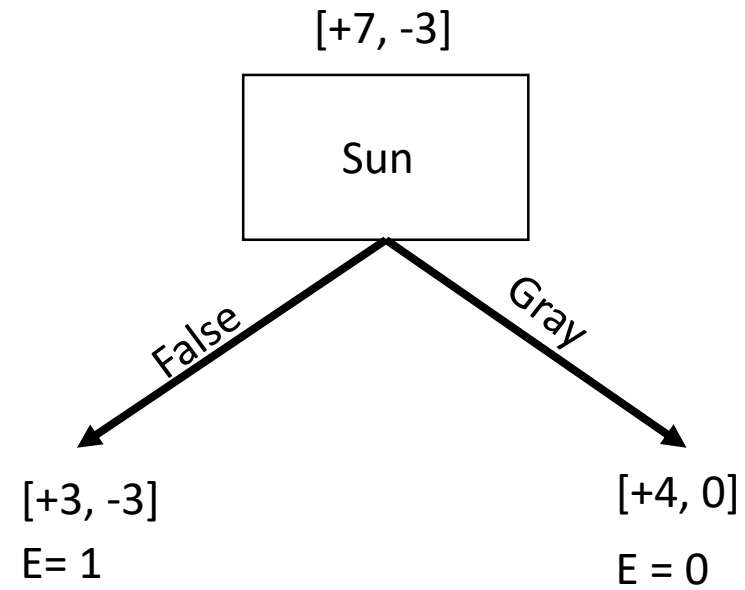
1C)



$$\begin{aligned}\text{Entropy}(S, \text{Sea}) &= .882 - \left[\frac{5}{10} 0 + \frac{5}{10} (.970) \right] \\ &= .882 - .450 \\ &= .3965\end{aligned}$$

Information gain = .3965

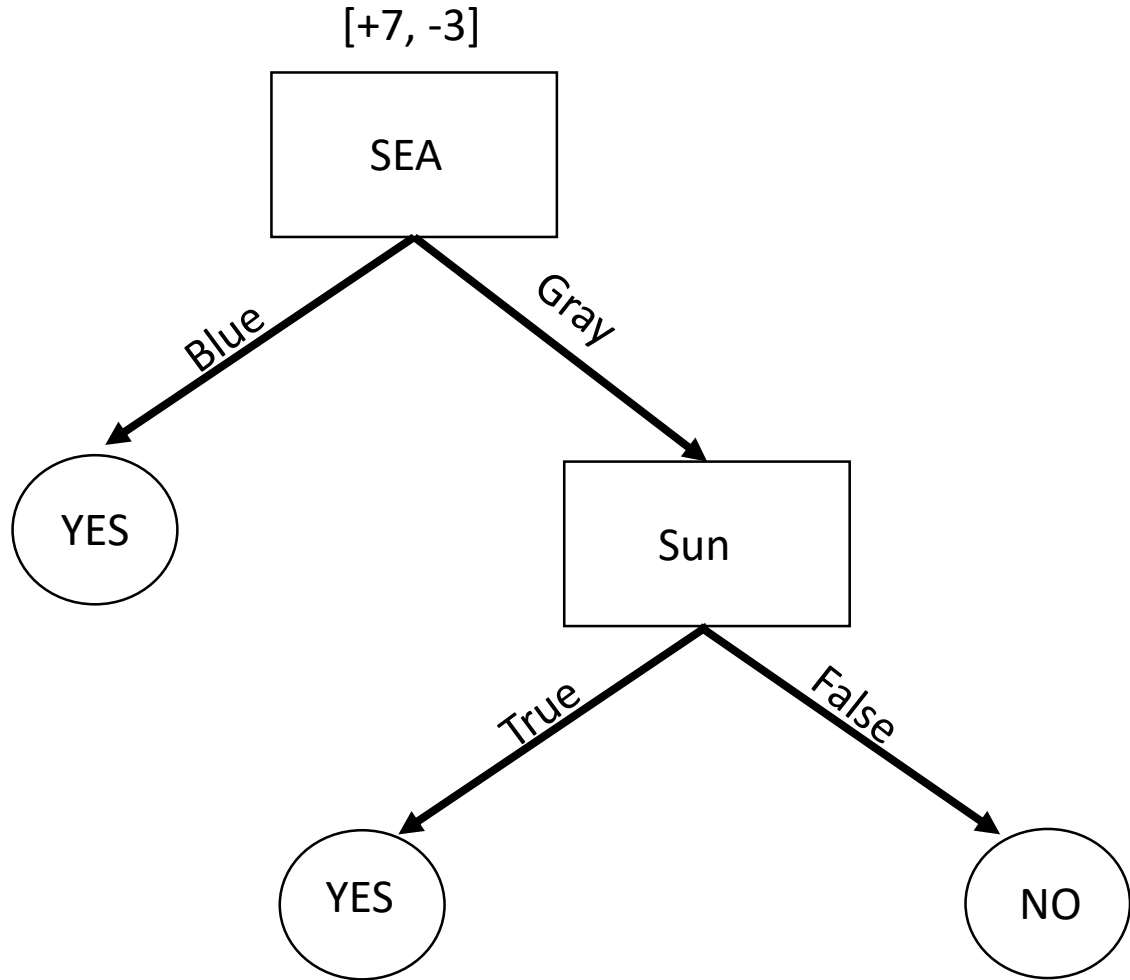
1D)



$$\begin{aligned}\text{Entropy}(S, \text{Sea}) &= .882 - \left[\frac{6}{10} 1 + \frac{4}{10} (0) \right] \\ &= .882 - .6 \\ &= .282\end{aligned}$$

Information gain = .282

1E)



WORK:

$$\text{Entropy}(\text{gray, sun}) = .970 - \left[\frac{2}{5} \text{entropy}(\text{true, sun}) + \frac{3}{5} \text{entropy}(\text{false, sun}) \right]$$

$$= .970 - [0 + 0]$$
$$\text{IG} = .970$$

$$\text{Entropy}(\text{gray, sun}) = .970 - \left[\frac{2}{5} \text{entropy}(\text{clear, sky}) + \frac{2}{5} \text{entropy}(\text{cloudy, sun}) + \frac{2}{5} \text{entropy}(\text{overcast, sky}) \right]$$

$$= .970 - \left[\frac{2}{5} (1) + \frac{2}{5} (1) + \frac{2}{5} (0) \right]$$
$$= .970 - .8 = .17$$
$$\text{IG} = .17$$

1F)

How would the learned Decision Tree classify the new instance <Sky=overcast,Sea=gray,Sun=true>

It would classify it as **Sail= yes**

2 perceptron)

2A)

Sky	Sea	Sun	Sail
1	1	1	1
1	2	2	1
1	2	1	0
2	1	2	1
2	1	1	1
2	2	2	1
2	2	1	0
3	1	2	1
3	1	1	1
3	2	1	0

2 B)

Rule: if $W * X$ is greater than 0 then 1(yes) else 0(no)

I decided to code this instead of having the TA's try to decipher my hand writing. (the data in results of each pass is on the next page)

Code ->

```
import numpy as np
import itertools
def perceptron():
    output = open("output.txt", "w")
    sail_data = list()
    sail_data_labels = list()
    for data, label in zip(open("data.txt", "r"), open("datalabels.txt", "r")):
        temp = list(map(float, data.split(",")))
        temp2 = np.array(temp)
        sail_data.append(temp2)
        sail_data_labels.append(int(label.strip('\n')))
    weight = np.zeros(4, np.float) #weight
    for i in range(len(weight)):
        weight[i] = 1.0
    for k in range(3):
        tempstr = "[pass " + str(k + 1) + "]\n"
        output.write(tempstr)
        for j in range(len(sail_data)):
            x = sail_data[j]
            yHat_t = np.dot(x, weight)
            correct_label = sail_data_labels[j]

            if yHat_t > 0:
                yHat_t = 1
            else:
                yHat_t = 0

            if yHat_t != correct_label:
                weight = weight + (.5 *(correct_label-yHat_t)*x )
                tempstr = str(weight.tolist()) + "\n"
                output.write(tempstr)
            else:
                output.write("Guess Correct\n")
        tempstr = "Trained weight: " + str(weight.tolist()) + "\n"
        output.write(tempstr)
        output.close()
if __name__ == "__main__":
    perceptron()
```


2 B continued)

Pass 1	Pass 2	Pass 3
Guess Correct	[0.5, 0.0, -1.0, 1.0]	Guess Correct
Guess Correct	Guess Correct	Guess Correct
[0.5, 0.5, 0.0, 0.5]	Guess Correct	Guess Correct
Guess Correct	Guess Correct	Guess Correct
Guess Correct	Guess Correct	Guess Correct
Guess Correct	Guess Correct	Guess Correct
[0.0, -0.5, -1.0, 0.0]	Guess Correct	Guess Correct
[0.5, 1.0, -0.5, 1.0]	Guess Correct	Guess Correct
Guess Correct	Guess Correct	Guess Correct
[0.0, -0.5, -1.5, 0.5]	Guess Correct	Guess Correct

Trained weight: [0.5, 0.0, -1.0, 1.0]

2 c How would the learned perceptron classify the new instance <Sky=overcast,Sea=gray,Sun=true>? Show your work.) [3, 2,1]

$$X = [1, 3, 2, 1]$$

$$\text{Weight} = [0.5, 0.0, -1.0, 1.0]$$

$$Y_{\text{hat}} = \text{Weight} * X$$

$$Y_{\text{hat}} = -0.5 < 0 \text{ so } Y_{\text{hat}} = \text{no}$$

Guess: NO