

Penentuan Faktor Pertumbuhan Anak

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```
#Library
library(readxl)

data <- read_excel("Tugas FA - WiscsemData.xlsx")
head(data)

## # A tibble: 6 x 13
##   client agemate info comp arith simil vocab digit pictcomp parang block
##   <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl>
## 1      3      3      8      7      13      9      12      9      6      11      12
## 2      4      3      9      6      8      7      11      12      6      8      7
## 3      5      3      13     18     11     16     15      6     18      8     11
## 4      6      3      8      11      6     12      9      7     13      4      7
## 5      7      2     10      3      8      9     12      9      7      7     11
## 6      8      3     11      7     15     12     10     12      6     12     10
## # ... with 2 more variables: object <dbl>, coding <dbl>

str(data)

## tibble [175 x 13] (S3: tbl_df/tbl/data.frame)
## $ client : num [1:175] 3 4 5 6 7 8 9 10 12 13 ...
## $ agemate : num [1:175] 3 3 3 3 2 3 3 2 3 3 ...
## $ info : num [1:175] 8 9 13 8 10 11 6 7 10 9 ...
## $ comp : num [1:175] 7 6 18 11 3 7 13 10 8 10 ...
## $ arith : num [1:175] 13 8 11 6 8 15 7 10 8 8 ...
## $ simil : num [1:175] 9 7 16 12 9 12 8 15 14 11 ...
## $ vocab : num [1:175] 12 11 15 9 12 10 11 10 9 9 ...
## $ digit : num [1:175] 9 12 6 7 9 12 6 7 9 11 ...
## $ pictcomp: num [1:175] 6 6 18 13 7 6 14 8 10 10 ...
## $ parang : num [1:175] 11 8 8 4 7 12 9 14 11 12 ...
## $ block : num [1:175] 12 7 11 7 11 10 14 11 10 9 ...
## $ object : num [1:175] 7 12 12 12 4 5 14 10 9 13 ...
## $ coding : num [1:175] 9 14 9 11 10 10 10 12 6 13 ...
```

Matrix eigen vector

```
data_matriks <- as.matrix(data)
data_matriks_korelasi <- cor(data_matriks)
data_matriks_eigen <- eigen(data_matriks_korelasi)
data_matriks_vektor <- data_matriks_eigen$vectors
data_matriks_vektor_transpose <- t(data_matriks_vektor)
data_matriks_vektor %%% data_matriks_vektor_transpose

##           [,1]      [,2]      [,3]      [,4]      [,5]
## [1,] 1.0000000e+00 1.040834e-16 -1.457168e-16 1.370432e-16 2.151057e-16
## [2,] 1.040834e-16 1.000000e+00 9.020562e-17 3.625572e-16 -3.989864e-17
## [3,] -1.457168e-16 9.020562e-17 1.000000e+00 -1.110223e-16 0.000000e+00
## [4,] 1.370432e-16 3.625572e-16 -1.110223e-16 1.000000e+00 -4.371503e-16
## [5,] 2.151057e-16 -3.989864e-17 0.000000e+00 -4.371503e-16 1.000000e+00
## [6,] -4.579670e-16 -3.755676e-16 -1.110223e-16 -2.706169e-16 3.053113e-16
## [7,] -7.632783e-17 5.863365e-16 -2.220446e-16 2.220446e-16 1.110223e-16
## [8,] 6.418477e-16 -2.059984e-16 2.671474e-16 -3.556183e-17 1.127570e-15
## [9,] 3.248279e-16 8.131516e-17 1.908196e-17 2.649790e-16 -5.898060e-17
## [10,] -3.625572e-16 -1.011344e-15 -3.191891e-16 -5.221518e-16 1.873501e-16
## [11,] 1.092876e-16 -1.561251e-17 2.914335e-16 -1.422473e-16 -6.591949e-16
## [12,] -1.682682e-16 2.081668e-17 2.220446e-16 -2.602085e-16 7.910339e-16
## [13,] 2.428613e-16 4.510281e-16 1.387779e-17 1.700029e-16 -1.838807e-16
##           [,6]      [,7]      [,8]      [,9]     [,10]
## [1,] -4.579670e-16 -7.632783e-17 6.418477e-16 3.248270e-16 -3.625572e-16
## [2,] -3.755676e-16 5.863365e-16 -2.059984e-16 8.131516e-17 -1.011344e-15
## [3,] -1.110223e-16 -2.220446e-16 2.671474e-16 1.908196e-17 -3.191891e-16
## [4,] -2.706169e-16 2.220446e-16 -3.556183e-17 2.649790e-16 -5.221518e-16
## [5,] 3.053113e-16 1.110223e-16 1.127570e-15 -5.898060e-17 1.873501e-16
## [6,] 1.000000e+00 6.938894e-17 -1.873501e-16 5.854692e-17 3.972517e-16
## [7,] 6.938894e-17 1.000000e+00 1.283695e-16 -6.938894e-17 -4.163336e-16
## [8,] -1.873501e-16 1.283695e-16 1.000000e+00 -6.470519e-16 1.062518e-16
## [9,] 5.854692e-17 -6.938894e-17 -6.470519e-16 1.000000e+00 1.229485e-16
## [10,] 3.972517e-16 -4.163336e-16 1.062518e-16 1.229485e-16 1.000000e+00
## [11,] 3.122502e-16 -1.249001e-16 3.018419e-16 -1.474515e-16 -3.313322e-16
## [12,] -6.487866e-16 -3.608225e-16 -4.128642e-16 -4.163336e-16 -2.168404e-16
## [13,] 1.422473e-16 1.387779e-17 -1.769418e-16 4.800847e-16 -7.042977e-16
##           [,11]      [,12]      [,13]
## [1,] 1.092876e-16 -1.682682e-16 2.428613e-16
## [2,] -1.561251e-17 2.081668e-17 4.510281e-16
## [3,] 2.914335e-16 -2.220446e-16 1.387779e-17
## [4,] -1.422473e-16 -2.602085e-16 1.700029e-16
## [5,] -6.591949e-16 7.910339e-16 -1.838807e-16
## [6,] 3.122502e-16 -6.487866e-16 1.422473e-16
## [7,] -1.249001e-16 -3.608225e-16 1.387779e-17
## [8,] 3.018419e-16 -4.128642e-16 -1.769418e-16
## [9,] -1.474515e-16 -4.163336e-16 4.800847e-16
## [10,] -3.313322e-16 -2.168404e-16 -7.042977e-16
## [11,] 1.000000e+00 7.979728e-16 1.006140e-16
## [12,] 7.979728e-16 1.000000e+00 -4.475587e-16
## [13,] 1.006140e-16 -4.475587e-16 1.000000e+00
```

3 Sampel eigen vektor

```
eigen_vektor <- data_matriks_vektor[,1:3]
eigen_vektor

##           [,1]      [,2]      [,3]
## [1,] -0.02501413  0.42834312  0.22273772
## [2,] -0.06419603 -0.01594669 -0.40698838
## [3,] -0.37470045 -0.27238702 -0.07085062
## [4,] -0.38390549 -0.01532265 -0.03827933
## [5,] -0.30796348 -0.23274052  0.09954685
## [6,] -0.37938209 -0.09266052 -0.20195768
## [7,] -0.37749189 -0.26472530 -0.04482546
## [8,] -0.21465614 -0.29172059  0.30885079
## [9,] -0.28611507  0.35313262 -0.17251921
## [10,] -0.23161635  0.30633302  0.11598853
## [11,] -0.29432550  0.34052084  0.10707086
## [12,] -0.23575765  0.42460452  0.05205189
## [13,] -0.04901539 -0.09548765  0.75682155
```

Diagonal matrix

```
matriks_diagonal <- data_matriks_eigen$values[1:3]
matriks_diagonal_value <- diag(matriks_diagonal, 3,3)
```

Loading factor

```
load_factor <- eigen_vektor %%% sqrt(matriks_diagonal_value)
load_factor

##           [,1]      [,2]      [,3]
## [1,] -0.04903158  0.53452363  0.24115297
## [2,] -0.12583420 -0.01989966 -0.44063689
## [3,] -0.73447114 -0.33990810 -0.07670832
## [4,] -0.75251444 -0.01912093  0.04144414
## [5,] -0.60365631 -0.29043376  0.10777707
## [6,] -0.74364789 -0.11562982 -0.21865490
## [7,] -0.73994280 -0.33034715 -0.04853149
## [8,] -0.42075942 -0.36403421  0.33438560
## [9,] -0.56083002  0.44066945 -0.18678255
## [10,] -0.45400407  0.38226885  0.12557809
## [11,] -0.57692374  0.42493138  0.11592314
## [12,] -0.46212105  0.52985827  0.05635538
## [13,] -0.09607778 -0.11915776  0.81939316
```

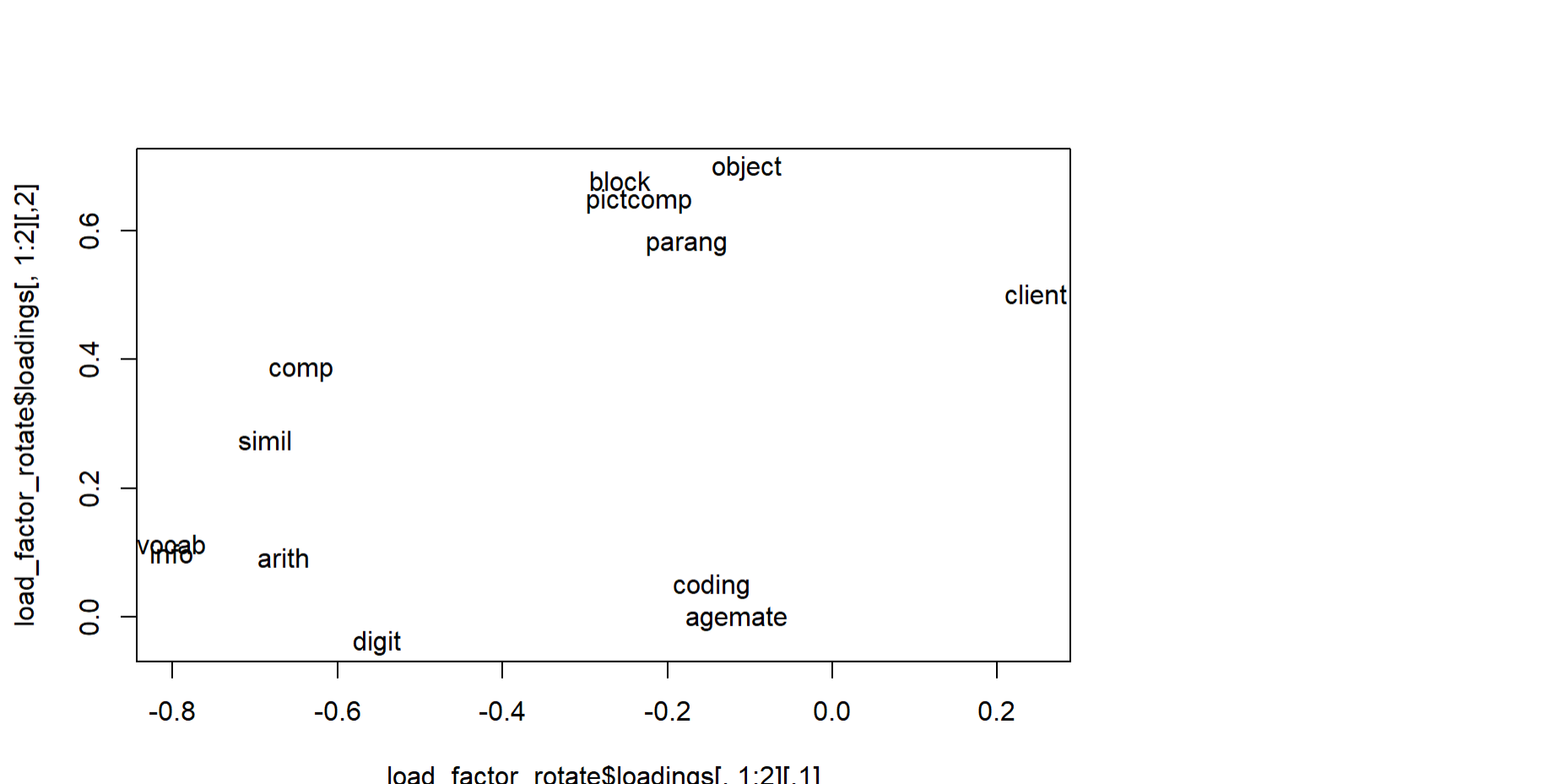
Matriks Invers

```
data_matriks_korelasi_invers <- solve(data_matriks_korelasi)
data_matriks_korelasi_invers

##           client      agemate      info      comp      arith
## client      1.11061815  0.033654880 -0.04799109 -0.05051364 -0.012529317
## agemate      0.03365488  1.036379515 -0.05782591  0.01538460  0.011816983
## info         0.04799109 -0.057825914  2.06256825 -0.13888007 -0.500627749
## comp         -0.05051364  0.015384597 -0.13888007  1.81581017 -0.256468796
## arith        0.01252932  0.011816983 -0.50062775 -0.25646880  1.506064158
## simil        0.15909067 -0.063735367 -0.27956549 -0.34849833 -0.141032555
## vocab         0.22568064  0.038691491 -0.83140230 -0.41154421 -0.005449071
## digit        -0.04879022 -0.042478757 -0.24954960 -0.06732920 -0.097296509
## pictcomp     -0.18023639  0.001520763  0.06500115 -0.29077069  0.068105065
## parang       -0.17879538 -0.064812381 -0.05429335  0.11742479 -0.133489923
## block        -0.03720763 -0.100065981  0.09221296 -0.18470174 -0.228235914
## object       -0.05830429  0.080941802 -0.12746812 -0.21853625  0.259111792
## coding       0.00823179  0.103951906  0.15193022 -0.04044767 -0.083482090
##           simil      vocab      digit      pictcomp      parang
## client      0.15909067  0.225680643 -0.04879022 -0.180236389 -0.17879538
## agemate     -0.06373537  0.038691491 -0.04247876  0.001520763 -0.06481238
## info        -0.27956549 -0.831402302 -0.24954960  0.065001152 -0.05429335
## comp        -0.34849833 -0.411544210 -0.06732920 -0.290770690  0.11742479
## arith       -0.14103256 -0.005449071 -0.09729651  0.068105065 -0.13348992
## simil       1.84790615 -0.439275722 -0.10014671 -0.248798089 -0.29431818
## vocab       -0.43927572  2.108659658 -0.09843701 -0.109561047  0.15640940
## digit       -0.10014671 -0.098437013  1.22332358  0.028981826 -0.09186433
## pictcomp    -0.24879809 -0.109561047  0.02898183  1.455805030 -0.07418153
## parang      -0.29431818  0.156409400  0.09186433 -0.074181533  1.29774233
## block       0.11672229 -0.218588037  0.10174713 -0.268406504 -0.30705327
## object      -0.15088013  0.088675668  0.06250029 -0.225588135 -0.12708186
## coding      0.15622600 -0.170348609 -0.20409833  0.153818469 -0.02847740
##           block      object      coding
## client      -0.03720763 -0.05830429  0.00823179
## agemate     -0.10006598  0.08094180  0.10395191
## info        0.09221296 -0.12746812  0.15193022
## comp        -0.18470174 -0.21853625 -0.04044767
## arith       -0.22823591  0.25911179 -0.08348209
## simil       0.11672229 -0.15088013  0.15622600
## vocab       -0.21858804  0.08867567 -0.17034861
## digit       0.10174713  0.06250029 -0.20409833
## pictcomp    -0.26840650 -0.22558813  0.15381847
## parang      -0.30705327 -0.12708186 -0.02847740
## block       1.51702930 -0.36357129 -0.11991989
## object      -0.36357129  1.37606961 -0.07337641
## coding      -0.11991989 -0.07337641  1.10607065
```

Plot

```
load_factor_rotate <- varimax(load_factor)
plot(load_factor_rotate$loadings[,1:2], type = "n")
text(load_factor_rotate$loadings[,1:2], labels=names(data), cex = 1)
```



Menghitung koefisien faktor

```
koefisien_faktor <- data_matriks_korelasi_invers %%% load_factor_rotate$loadings
koefisien_faktor

##           [,1]      [,2]      [,3]
## client      0.17405686  0.31821078  0.169579367
## agemate     -0.03371412 -0.037617197 -0.374149622
## info        -0.27859005 -0.08788024 -0.055984184
## comp        -0.17145049  0.09044172 -0.046742748
## arith       -0.23309804 -0.06090762  0.099391727
## simil       -0.20264466  0.01947867 -0.190591945
## vocab       -0.27652441 -0.07913652 -0.032814804
## digit       -0.21891141 -0.10302199  0.299136269
## pictcomp    0.03012044  0.29591461 -0.135714928
## parang      0.03275780  0.28123103  0.074408317
## block       0.02962205  0.32029692  0.061426372
## object      0.08223779  0.35461399  0.006281224
## coding      -0.06374535  0.03221438  0.700013996
```