

IT 143
DISCRETE MATHEMATICS
FINAL EXAMINATION

MARBA IQUEN I

BSIT 1A

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1. Set Theory:

Set theory is a fundamental branch of mathematics that deals with the study of sets, which are collections of objects. In computer science, set theory provides a foundation for many areas, such as data structures, databases, and algorithms. Sets are used to represent and manipulate collections of items, and various operations like union, intersection, and complement are performed on sets.

Example: In data structures, set theory is used in implementing sets, which are often called hash sets or hash tables. These data structures allow efficient insertion, deletion, and retrieval of elements. For example, a set can be used to store a collection of unique email addresses in an email management system, enabling fast searching and eliminating duplicate entries.

2. Probability:

Probability is a mathematical concept that quantifies the likelihood of an event occurring. In computer science, probability theory is crucial for various applications, including machine learning, cryptography, network protocols, and algorithm analysis. It helps in making decisions under uncertain or probabilistic conditions.

Example: In machine learning, probability theory is used in the field of Bayesian inference. Bayesian models leverage probability distributions to update beliefs about unknown quantities as new data becomes available. For instance, in spam filtering, a probabilistic model can be used to estimate the probability of an email being spam based on certain features, allowing the system to classify incoming emails as spam or non-spam.

3. Propositional Logic:

Propositional logic, also known as Boolean logic, is a branch of formal logic that deals with the study of logical relationships between propositions. It provides a framework for representing and manipulating logical statements using logical operators like AND, OR, and NOT. In computer science, propositional logic forms the basis for designing circuits, programming languages, and automated reasoning systems.

Example: In circuit design, propositional logic is essential for creating logical circuits that perform specific computations. The logic gates, such as AND, OR, and NOT gates, are used to implement the Boolean functions. For example, a half-adder circuit can be designed using propositional logic to perform addition of two binary digits.

4. Relations and Functions:

Relations and functions are mathematical concepts that describe the relationships between elements in sets. In computer science, they are used to model various real-world scenarios and provide a foundation for database management systems, formal languages, and computational complexity theory.

Example: In database management systems, relations (tables) are used to represent and store data. The relationships between tables can be defined using keys, primary and foreign, which establish connections between different tables. For instance, in a customer order system, a "Customers" table and an "Orders" table can be related through a customer ID field, allowing efficient retrieval and management of customer order information.

5. Graph Theory:

Graph theory is a branch of mathematics that studies graphs, which are structures composed of vertices (nodes) and edges (connections). In computer science, graph theory is used to model and solve problems related to network analysis, optimization, routing algorithms, social networks, and data visualization.

Example: In network analysis, graph theory plays a crucial role. Network graphs can represent connections between entities, such as nodes representing computers and edges representing network connections. Graph algorithms, like Dijkstra's algorithm, can then be employed to find the shortest path between two nodes in a network, aiding in efficient routing and optimization of network traffic.