Mesh TensorFlow

Running models of sufficiently large size pose practical difficulties

- taking advantage of the inherent parallelism afforded by multiple computational units (processors, cores)
- insufficient memory per processor to contain a model's parameters

Fortunately, there are programming abstractions that mitigate these difficulties.

Mesh-TensorFlow (https://arxiv.org/pdf/1811.02084.pdf) is an extension of TensorFlow that provides a clean API for dealing with various forms of parallelism.

We provide a very brief introduction

 motivated by its use in implementing the MoE in the FFN of the Switch Transformer

Note that this is an extension of "low-level" TensorFlow, **not** higher level Keras.

Forms of parallelism

We assume

- a collection of computational units (referred to as processors)
- that are able to communicate with one another
 - by a arbitary communication fabric

We want our models to be able to take advantage of the multiple processors.

The two common forms of parallelism are

- data parallelism
 - each example in a mini-batch is independent
 - split the batch across processors
- model parallelism
 - when a model's parameters are too large to fit into memory of a single processor
 - split the parameters (and computation) across multiple processors

To illustrate: Consider

- ullet A batch ${f X}$ of m examples, each a one-dimensional vector of length n: ${f X} \in \mathbb{R}^{m imes n}$
- A vector \mathbf{w} of length n: $\mathbf{w} \in \mathbb{R}^n$
 - lacktriangledown e.g., one row of a weight matrix f W implementing the Dense operation of f X*f W
- ullet We want to compute the dot product of every example with old w

$$\mathbf{X^{(i)}\cdot w}$$

for every example i

Data parallelism

This is the simplest form of parallelism

• split the examples into groups

$$\mathbf{X} = egin{pmatrix} \mathbf{X}^{(0:g-1)} \ \mathbf{X}^{(g:2*g-1)} \ dots \ X^{(m-g:m-1)} \end{pmatrix}$$

Dispatch

- a single group (e.g., $\mathbf{X}^{(s:e)}$) to a single processor
- ullet the weights old w to each processor

Each processor (e.g., the one assigned examples $\mathbf{X}^{(s:e)}$) computes $\mathbf{X}^{(s:e)}*\mathbf{w}$

n.b., multiplication of matrix and vector results in vector output

• that is dot product of each row of matrix and the right vector

Model parallelism

Suppose dimension n is so large that a single processor's memory cannot accommodate either vector

- ullet corresponding to a single example $\mathbf{X^{(i)}}$
- \bullet corresponding to ${f w}$

Dispatch a group

• $\mathbf{X}_{s:e}^{(\mathbf{i})}$ and $\mathbf{w}_{s:e}$ to a single processor p which computes the dot product $h^{(p)} = \mathbf{X}_{s:e}^{(\mathbf{i})} \cdot \mathbf{w}_{s:e}$

Note that $h^{(p)}$ is a scalar.

Gather (using the communication network) the $h_{(p)}$ from all processors p $\mathbf{h}=[h^{(0)},h^{(1)},\dots,h^{(rac{n}{g})}]$

$${f h} = [h^{(0)}, h^{(1)}, \ldots, h^{(rac{n}{g})}]$$

Reduce the vector ${f h}$ to a scalar

• by summing over its elements

Backward pass

We have illustrated the fundamental ideas of parallelism

• using a computation from the forward pass of a Neural Network

The backward pass (gradient flow) can also be implemented

• but requires Gather and Reduce operations

Defining parallelism in Mesh-TensorFlow

As per our illustration, implementing the two forms of parallelism involves

- splitting Tensors
- and possibly gathering/reducing sub-results

Mesh-TensorFlow provides a simple notation for describing how to split a Tensor

• everything else (dispatching, gathering, reducing) is automatic

A Tensor has multiple dimensions.

In Mesh-TensorFlow, we can give each dimension a *name* and a size.

For example, the first dimension of most Tensors in a Neural Network is the "batch" dimension.

• We can specify a dimension named "batch", of size 100:

batch_dim = mtf.Dimension("batch", 100)

Mesh-TensorFlow also allows the user to specify

- The logical (not physical connectivity) organization of processors.
 - Treating 4 processors as a one-dimensional vector

```
mesh_shape = [("all_processors", 4)]
```

- Layout rules: how a named dimension is split into groups
 - To specify data parallelism (split batch across processors)

```
layout_rules = [("batch", "all_processors")]
```

Mesh-TensorFlow thus provides a simple but powerful API

- for distributing data and computation
- across multiple processors

We illustrate with an example taken from the <u>Mesh TensorFlow github</u> (https://github.com/tensorflow/mesh#example-network-mnist)

<u>Mesh-TensorFlow program for MNIST classification task</u> (<u>https://github.com/tensorflow/mesh#example-network-mnist</u>)

Name the dimensions

```
# tf_images is a tf.Tensor with shape [100, 28, 28] and dtype tf.float32
# tf_labels is a tf.Tensor with shape [100] and dtype tf.int32
graph = mtf.Graph()

mesh = mtf.Mesh(graph, "my_mesh")
batch_dim = mtf.Dimension("batch", 100)

rows_dim = mtf.Dimension("rows", 28)
cols_dim = mtf.Dimension("cols", 28)
hidden_dim = mtf.Dimension("hidden", 1024)
classes_dim = mtf.Dimension("classes", 10)
```

Compute logits loss, and update weights via Gradient Descent

```
images = mtf.import_tf_tensor(
    mesh, tf_images, shape=[batch_dim, rows_dim, cols_dim])
labels = mtf.import_tf_tensor(mesh, tf_labels, [batch_dim])

w1 = mtf.get_variable(mesh, "w1", [rows_dim, cols_dim, hidden_dim])
w2 = mtf.get_variable(mesh, "w2", [hidden_dim, classes_dim])

# einsum is a generalization of matrix multiplication (see numpy.einsum)
hidden = mtf.relu(mtf.einsum(images, w1, output_shape=[batch_dim, hidden_dim]))
logits = mtf.einsum(hidden, w2, output_shape=[batch_dim, classes_dim])

loss = mtf.reduce_mean(mtf.layers.softmax_cross_entropy_with_logits(
    logits, mtf.one_hot(labels, classes_dim), classes_dim))

w1_grad, w2_grad = mtf.gradients([loss], [w1, w2])
update_w1_op = mtf.assign(w1, w1 - w1_grad * 0.001)
update_w2_op = mtf.assign(w2, w2 - w2_grad * 0.001)
```

Specify mesh of processors and layout of computation

Layout for data parallelism

The following layout implements data parallelism

- Any Tensor with a dimension named "batch" dimension
 - images, h, logits and their gradients
- is split across all devices ("all_processors")
 devices = ["gpu:0", "gpu:1", "gpu:2", "gpu:3"]
 mesh_shape = [("all_processors", 4)]
 layout_rules = [("batch", "all_processors")]
 mesh_impl = mtf.placement_mesh_impl.PlacementMeshImpl(
 mesh_shape, layout_rules, devices)

Layout for model parallelism

Alternatively, we can use a layout to implement model parallelism

- Any Tensor with a dimension named "hidden" is split
 - hidden w1, w2
- is split across all devices ("all_processors")

```
layout_rules=[("hidden", "all_processors")]
```

Layout for data and model parallelism

We create a 2D mesh of processors

• rows are named processor_rows, columns are named processor_cols mesh_shape = [("processor_rows", 2), ("processor_cols", 2)]

And use the layout

```
layout_rules = [("batch", "processor_rows"), ("hidden", "processor_cols")]
```

Layout splits

- Tensors with a "batch" dimension across the processor rows (data parallelism)
 - replicating them for every processor column
- Tensors with a "hidden" dimension across processor columns (model parallelism)
 - replicating them for every processor row layout_rules = [("batch", "processor_rows"), ("hidden", "processor_cols")]

So the processors

- in first row has half the examples
- in the second row has half the examples
- in the first column has half the weights
- in the second column has half the weights

So each quadrant (one processor)

- computes the dot product of half the examples on half the weights
- for the hidden tensor
 - has **both** "batch" and "hidden" dimensions
 - so is distributed across all 4 quadrants of the mesh

These are combined into a single result batch via a reduction

- all reduce operation
- communication across processors
 - or partially reduced dot products (i.e., scalars)

"Lower" the logical layout unto the physical devices lowering = mtf.Lowering(graph, {mesh:mesh_impl})

Illustrations of layouts

Appendix A (https://arxiv.org/pdf/1811.02084.pdf#page=11) provides nice illustrations

- of layouts
- for an example similar to the MNIST program

Notation

- Tensors are split by vertical and horizontal lines
- Blue integers indicate which processor a piece of a Tensor has been dispatched to
 - some pieces are dispatched to multiple processors

Data parallelism

Data parallelism

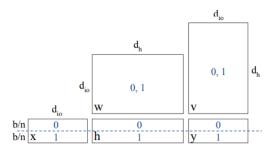


Figure 2: The data-parallel layout for the Two Fully-Connected Layers example, with n=2 processors $\in \{0,1\}$. Blue numbers on matrices indicate the ranks of the processors the matrix slices reside on. The batch dimension is split among all processors. w and v are fully replicated.

Attribution: https://arxiv.org/pdf/1811.02084.pdf#page=12

- \mathbf{X} (and result $\mathbf{h} = \mathbf{X} * \mathbf{W}$) are split along the batch dimension
 - groups assigned to processors 0, 1
- \mathbf{W} is not split
 - full ${f W}$ is replicated across processors 0,1

Thus, processors 0, 1 are able to compute their subset of \mathbf{X} , times \mathbf{W}

ullet resulting ${f h}$ is split (along batch dimension) across processors 0,1

Model parallelism

Model parallelism

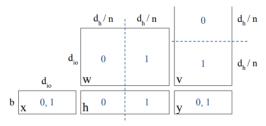


Figure 3: The model-parallel layout for the Two Fully-Connected Layers example, with n=2 processors $\in \{0,1\}$. Blue numbers on matrices indicate the ranks of the processors the matrix slices reside on. The hidden dimension is split among all processors. x and y are fully replicated.

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- X is not split
 - replicated to processors 0, 1
- **W** is split (across columns)
 - groups assigned to processors 0, 1

Thus

- processor 0 can compute the full $\mathbf X$ times the first group of $\mathbf W$
- processor 0 can compute the full ${\bf X}$ times the second group of ${\bf W}$
- resulting in \mathbf{h} split across processors 0, 1

Data and Model parallelism

Here, 4 processors are arranged into a 2×2 mesh.

Data and Model parallelism

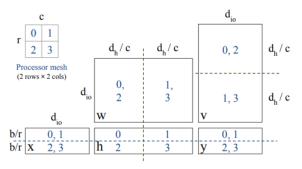


Figure 4: The mixed data-and-model-parallel layout for the Two Fully-Connected Layers example. There are 4 processors, arranged into a 2-by-2 mesh. Each processor is assigned a serialized rank which is used to label matrix slices that it owns.

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 ${f X}$ (and result ${f h}={f X}*{f W}$) are split along the batch dimension

- one group is replicated
 - assigned to processors 0, 1
- second group is replicated
 - \blacksquare assigned to processors 2, 3
- W is split (across columns)
- one group is replicated
 - lacktriangle assigned to processors 0, 2
- second group is replicated
 - assigned to processors (1, 3)

Thus

- processor 0 can compute first group of $\mathbf X$ times first group of $\mathbf W$
- ullet processor 1 can compute first group of ${f X}$ times second group of ${f W}$
- processor 2 can compute second group of ${\bf X}$ times first group of ${\bf W}$
- ullet processor 3 can compute second group of ${f X}$ times second group of ${f W}$

Note that result \mathbf{h} is split across *both

- batch dimension (due to the data parallel split of X)
- ullet model dimension (due to model parallel split of ${f W}$)

```
In [2]: print("Done")
```

Done