

```
In [1]: %run Latex_macros.ipynb  
        %run beautify_plots.py
```

In [2]: *# My standard magic ! You will see this in almost all my notebooks.*

```
from IPython.core.interactiveshell import InteractiveShell  
InteractiveShell.ast_node_interactivity = "all"
```

```
# Reload all modules imported with %aimport
```

```
%load_ext autoreload
```

```
%autoreload 1
```

```
%matplotlib inline
```

# Feature Importance

Given the  $n$  features in  $\mathbf{x}$ , which are the "most important" ?

The multiple trees in a Random Forest offer several ways to answer this question.

## Importance: Decrease in Impurity

Recall that the question that splits the examples corresponding to a node is chosen so as to maximize Information Gain.

One method of measuring the importance of  $\mathbf{x}_j$  is the amount of impurity decrease it creates.

- For each feature  $x_j$ 
  - find each node  $n$  in *any* tree in the forest with question  $(j, v)$  for *any*  $v$ 
    - compute the information gain of the split on  $(j, v)$
  - average the information gain across all such nodes

That is, how much does impurity decrease when  $\mathbf{x}_j$  is used in a question.

- This is a biased method
  - Recall the universe of possible values of  $\mathbf{x}_j$  is  $V_j$
  - Larger  $|V_j|$  means  $\mathbf{x}_j$  is more likely to appear in a questions
    - e.g., when  $\mathbf{x}_j$  is a continuous variable that has been made discrete
  - So  $\mathbf{x}_j$  will appear in more questions

## Importance: Permutation importance

Let's consider building one tree from bootstrapped sample  $S$ .

Create another sample  $S'$ , derived from  $S$  by *permuting* the values of  $\mathbf{x}_j$ .

- maintains the unconditional distribution of  $\mathbf{x}_j$
- breaks the correlation of  $\mathbf{x}_j$  with the target and other features

We can now measure the importance of  $\mathbf{x}_j$  as

- the change in out of bag accuracy of the tree built from  $S$  and  $S'$ .

That is, if  $\mathbf{x}_j$  is unimportant, then permuting its values should have little effect on accuracy.

Permutation Importance, feature  $j$

$\mathbf{X}$ 

$\mathbf{x}_1$	$\mathbf{x}_2$	...	$\mathbf{x}_j$	...	$\mathbf{x}_n$
$\mathbf{x}_1^{(1)}$	$\mathbf{x}_2^{(1)}$	...	$\mathbf{x}_j^{(1)}$	...	$\mathbf{x}_n^{(1)}$
$\mathbf{x}_1^{(2)}$	$\mathbf{x}_2^{(2)}$	...	$\mathbf{x}_j^{(2)}$	...	$\mathbf{x}_n^{(2)}$
$\vdots$	$\vdots$		$\vdots$		$\vdots$
$\mathbf{x}_1^{(i)}$	$\mathbf{x}_2^{(i)}$	...	$\mathbf{x}_j^{(i)}$	...	$\mathbf{x}_n^{(i)}$
$\vdots$	$\vdots$		$\vdots$		$\vdots$
$\mathbf{x}_1^{(n)}$	$\mathbf{x}_2^{(n)}$	...	$\mathbf{x}_j^{(n)}$	...	$\mathbf{x}_n^{(n)}$



Score

 $\mathbf{X}_{\text{Perm}}$ 

$\mathbf{x}_1$	$\mathbf{x}_2$	...	$\mathbf{x}_j$	...	$\mathbf{x}_n$
$\mathbf{x}_1^{(1)}$	$\mathbf{x}_2^{(1)}$	...	$\mathbf{x}_j^{(i_1)}$	...	$\mathbf{x}_n^{(1)}$
$\mathbf{x}_1^{(2)}$	$\mathbf{x}_2^{(2)}$	...	$\mathbf{x}_j^{(i_2)}$	...	$\mathbf{x}_n^{(2)}$
$\vdots$	$\vdots$		$\vdots$		$\vdots$
$\mathbf{x}_1^{(i)}$	$\mathbf{x}_2^{(i)}$	...	$\mathbf{x}_j^{(i_i)}$	...	$\mathbf{x}_n^{(i)}$
$\vdots$	$\vdots$		$\vdots$		$\vdots$
$\mathbf{x}_1^{(n)}$	$\mathbf{x}_2^{(n)}$	...	$\mathbf{x}_j^{(i_n)}$	...	$\mathbf{x}_n^{(n)}$

Score<sub>Perm</sub>Score - Score<sub>Perm</sub>



Permutation importance also has issues

- may be biased if  $\mathbf{x}_j$  is strongly correlated with another feature  $\mathbf{x}_{j'}$

In that case  $\mathbf{x}_{j'}$  may compensate for the permuted  $\mathbf{x}_j$ , making  $\mathbf{x}_j$  seem unimportant.

```
In [4]: print("Done")
```

Done