

# Support Vector Classifier (SVC)

We introduce another model for the Classification task: the Support Vector Classifier (SVC).

We motivate this classifier by some examples.

Consider the following linearly separable dataset and two separating lines:

Linear separating boundary

Is one separating line "better" than the other ?

Intuitively, the first line feels more fragile

- The distance between the line and the closest example is smaller in the first plot than the second
- If the red point located exactly on the line moved a small amount, we would misclassify it
- Not as likely to generalize out of sample as well

Something else to consider:

- How sensitive is our classifier to additional examples *that are far from the original boundary*

Consider the two rows in the plot below

- The second plot in each row adds a cluster of examples on the right side, mid-way

## Sensitivity to far-from-boundary examples

As you can see

- Logistic Regression is sensitive
- SVC is not

Why should points far away from the original separating boundary affect the fit ?

The answer, of course, is the Loss function.

We will see that the SVC uses a much different loss that has several advantages.

The SVC introduces two additional separating lines that are parallel to the separating boundary

- At a distance  $m$  on either side of the boundary
  - measured by length of a line orthogonal to the boundary
- $m$  is called the *margin*
- These two lines define a "buffer" of width twice the margin

We draw two plots with different size margins

Margin



The concept of margin helps to address the two issues raised above.

- Given a choice of two separating boundaries (each with perfect separation)
  - The one with the larger margin is "better"
- An example that is correctly classified and lies *outside* the buffer
- Should not affect the Loss Function

From the above examples

- It may not be possible to have both
  - A large margin and
  - A boundary that separates classes perfectly
  - The left plot, for example

Requiring perfect separation and no examples in the buffer is called *Hard Margin* classification.

- Allowing either condition to be false is called *Soft Margin* classification

A *Soft Margin* classifier allows violations but imposes a *penalty* (by increasing the Loss).

An SVC classifier is a Soft Margin classifier.

The main difference between an SVC and Logistic Regression classifier

- Different Loss functions

The SVC Loss functions differs from Cross Entropy (used in Logistic Regression) in that

- There are examples with **zero** loss
- Those that are correctly classified and outside the buffer

We will dig into the loss function for the SVC shortly.

# Support Vector Machines (SVM)

We have seen that many datasets, in raw form, are not linearly separable.

Transformations of the raw data must be applied to induce Linear Separability.

*A Support Vector Machine* combines

- Transformations specialized for the mathematics of an SVC
- An SVC

There is a special subclass of transformation functions called **kernel functions** that

- Uses a clever mathematical trick
- To achieve the effect of applying an expensive transformation
- Without actually creating transformed data !

The SVM helps to automate the transformations.

# Key concepts

Just like Logistic Regression, the SVC will:

- Use the features  $\mathbf{x}^{(i)}$  to compute a "score"  $\hat{g}^{(i)}$
- Compare the predicted score to a threshold
- Predict Positive if the score exceeds the threshold; Negative otherwise

The score is linear in the features

$$s(\mathbf{x}) = \Theta^T \mathbf{x} \quad \text{score}$$

$$s(\mathbf{x}) = 0 \quad \text{equation of separating boundary}$$

$$\hat{\mathbf{y}}^{(i)} = \begin{cases} \text{Negative} & \text{if } \hat{s}^{(i)} < 0 \\ \text{Positive} & \text{if } \hat{s}^{(i)} \geq 0 \end{cases}$$



The SVC and SVM incorporate several "tricks"

- A clever Loss Function (Hinge Loss)
- Large Margin Classification
- Kernel Transformations

The combined effect can be overwhelming and makes the SVC/SVM seem complex

- and it *does* involve a bit of math

We will try to reduce the complexity by tackling each trick separately.

In [5]: `print("Done")`

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