

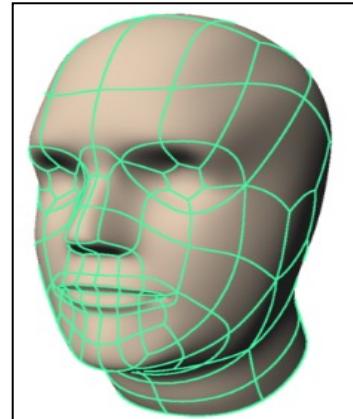
Introduction to Computer Graphics

April 8, 2021
Kenshi Takayama

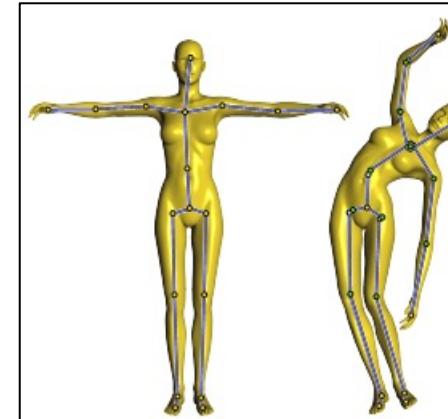
Course overview

- Lecture basic stuff on 4 topics
- 2~3 lectures per topic, 12 lectures in total

Modeling



Animation



Rendering



Image processing

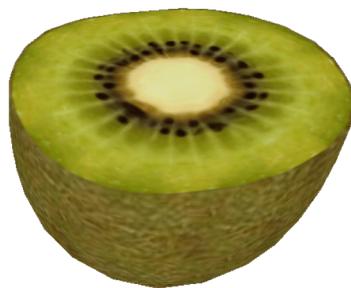


Lecturer

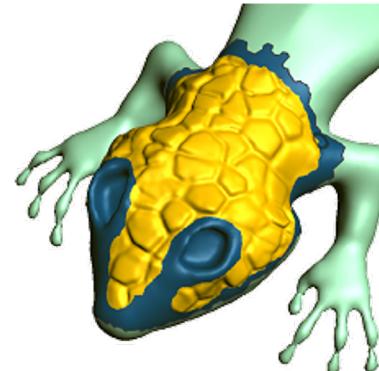
- Kenshi Takayama (Assist. Prof. @NII)
 - <http://research.nii.ac.jp/~takayama/>
 - takayama@nii.ac.jp



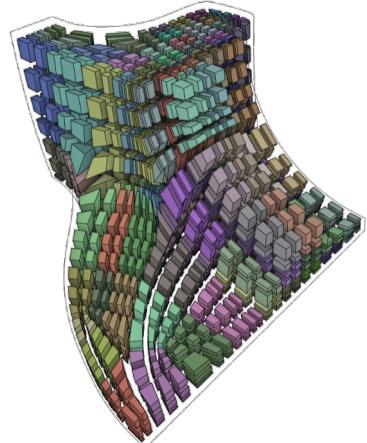
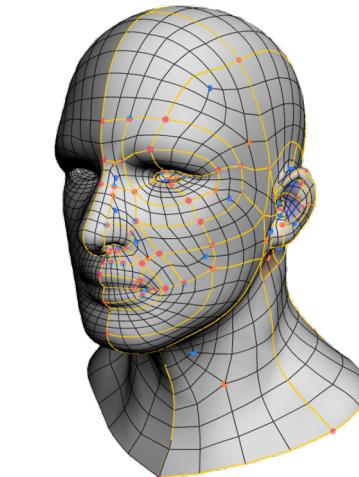
TA : Koki Endo @Igarashi Lab MSc
endo-k-88st0@g.ecc.u-tokyo.ac.jp



Modeling objects with internal structures



UI for 3D modeling



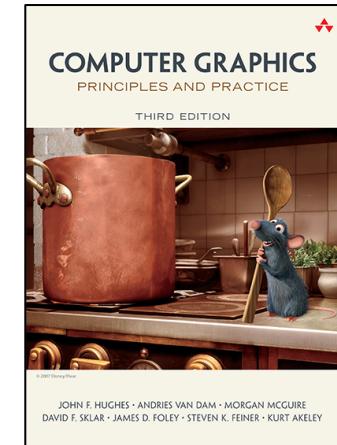
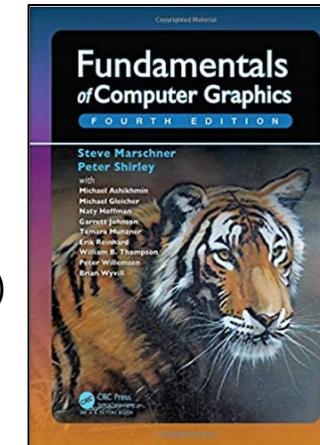
Generation of quad/hexahedral meshes

Grading

- Programming assignments only
 - No exam, no attendance check
- Two types of assignments: Basic & Advanced
 - Basic: 1 assignment per topic (4 in total), very easy
 - Advanced: For motivated students
- Deadline:
 - Basic: 2 weeks after announcement
 - Advanced: end of July
- Evaluation criteria
 - 1 assignment submitted → **C** (bare minimum for the degree)
 - 4 assignments submitted → **B** or higher
 - Distribution of **S** & **A** will be decided based on the quality/creativity of submissions and the overall balance in the class
- More details explained later

Course information

- Website
 - <http://research.nii.ac.jp/~takayama/teaching/utokyo-iscg-2021/>
- Famous textbooks (not used in the class)
 - Fundamentals of Computer Graphics (978-1568814698)
 - Computer Graphics: Principles and Practice (978-0321399526)



Coordinate transformations

Linear transformation

$$\text{In 2D: } \begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} a & b \\ c & d \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

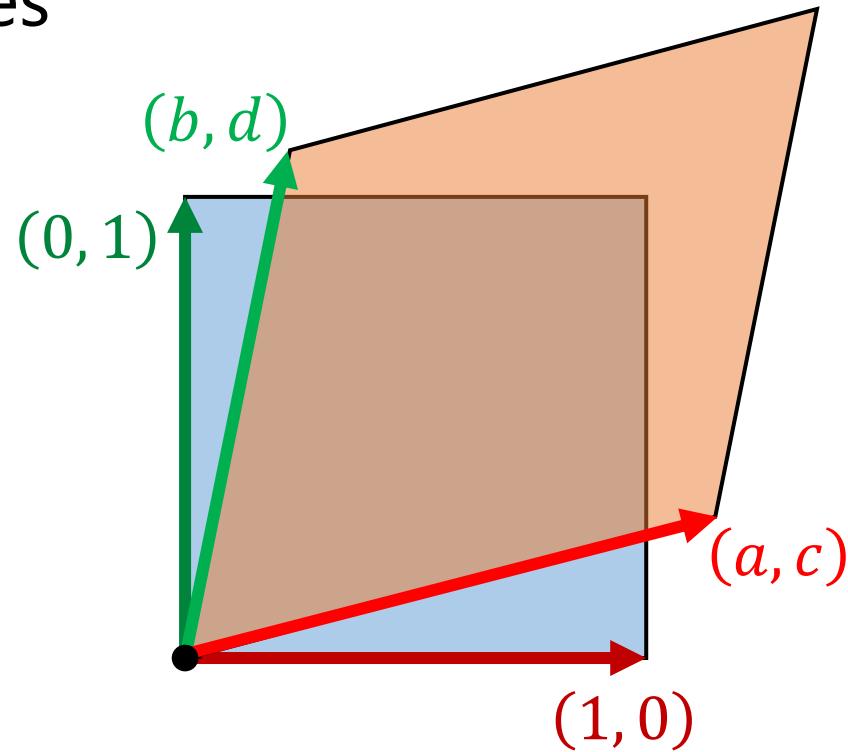
$$\text{In 3D: } \begin{bmatrix} x' \\ y' \\ z' \end{bmatrix} = \begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix}$$

- Intuition: Mapping of coordinate axes

$$\begin{bmatrix} a \\ c \end{bmatrix} = \begin{bmatrix} a & b \\ c & d \end{bmatrix} \begin{bmatrix} 1 \\ 0 \end{bmatrix}$$

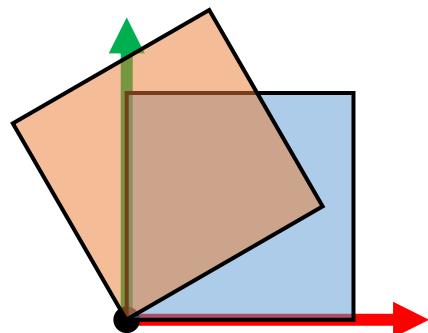
$$\begin{bmatrix} b \\ d \end{bmatrix} = \begin{bmatrix} a & b \\ c & d \end{bmatrix} \begin{bmatrix} 0 \\ 1 \end{bmatrix}$$

- Origin stays put

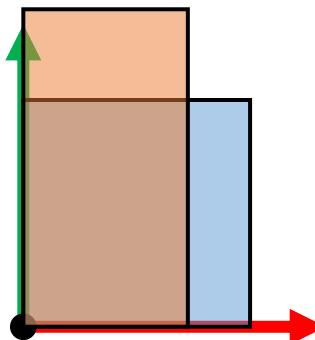


Special linear transformations

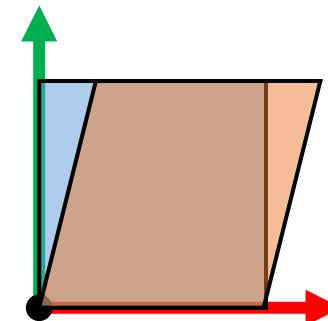
Rotation



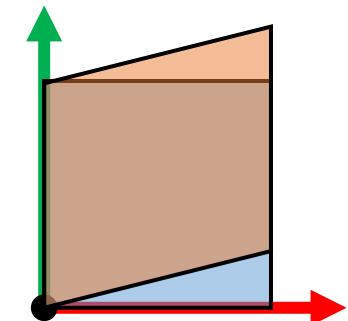
Scaling



Shearing (X dir.)



Shearing (Y dir.)



$$\begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix}$$

$$\begin{bmatrix} s_x & 0 \\ 0 & s_y \end{bmatrix}$$

$$\begin{bmatrix} 1 & k \\ 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 \\ k & 1 \end{bmatrix}$$

Linear transformation + translation = Affine transformation

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} a & b \\ c & d \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} + \begin{bmatrix} t_x \\ t_y \end{bmatrix} \iff \begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} a & b & t_x \\ c & d & t_y \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

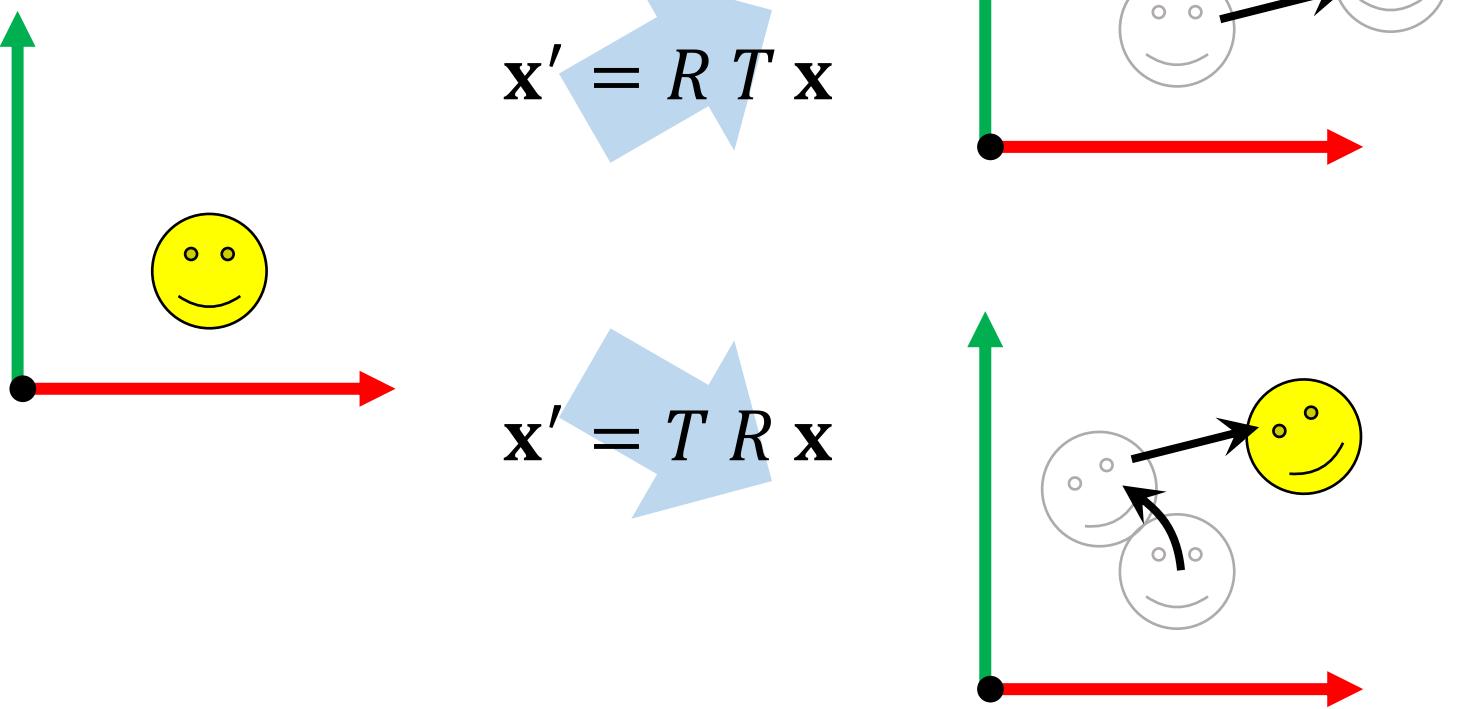
- **Homogeneous coordinates:** Use a 3D (4D) vector to represent a 2D (3D) point
- Can concisely represent linear transformation & translation as matrix multiplication
 - Easier implementation

Combining affine transformations

- Just multiply matrices
- Careful with the ordering!

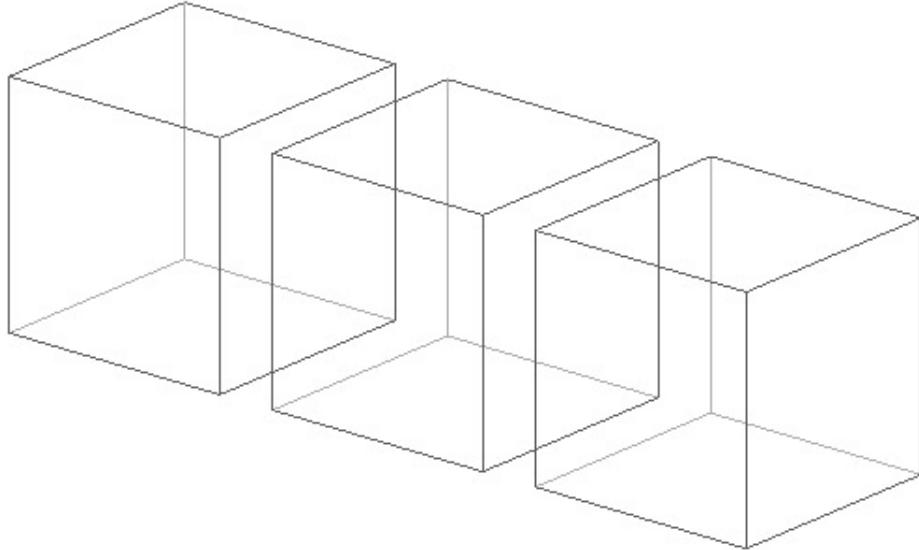
$$R = \begin{bmatrix} \cos \theta & -\sin \theta & 0 \\ \sin \theta & \cos \theta & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$T = \begin{bmatrix} 1 & 0 & t_x \\ 0 & 1 & t_y \\ 0 & 0 & 1 \end{bmatrix}$$

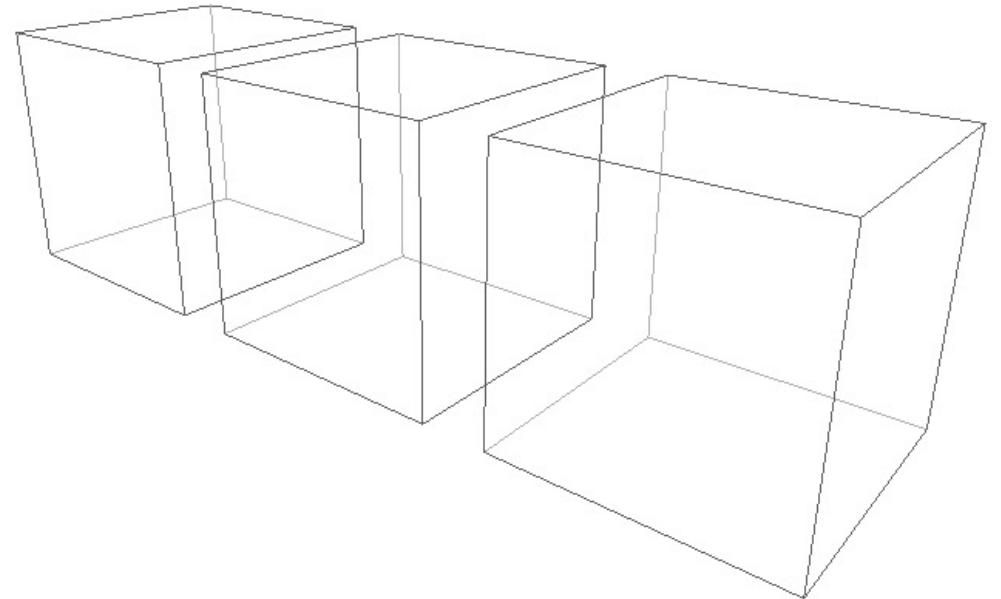


Another role of homogeneous coordinates: Perspective projection

- Objects' apparent sizes on the screen are inversely proportional to the object-camera distance



Orthographic projection



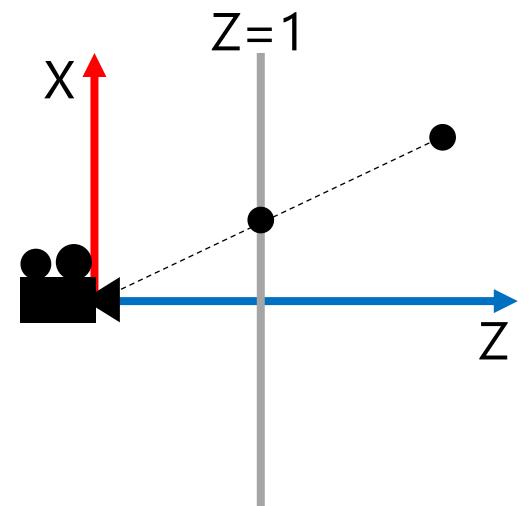
Perspective projection

Another role of homogeneous coordinates: Perspective projection

- When $w \neq 0$, 4D homogeneous coordinate (x, y, z, w) represents a 3D position $\left(\frac{x}{w}, \frac{y}{w}, \frac{z}{w}\right)$
- Camera at the origin, screen on the plane $Z=1$
→ (p_x, p_y, p_z) is projected to $(w_x, w_y) = \left(\frac{p_x}{p_z}, \frac{p_y}{p_z}\right)$

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} p_x \\ p_y \\ p_z \\ 1 \end{bmatrix} = \begin{bmatrix} p_x \\ p_y \\ p_z + 1 \\ p_z \end{bmatrix} = \begin{bmatrix} p_x/p_z \\ p_y/p_z \\ 1 + 1/p_z \\ 1 \end{bmatrix} \begin{array}{l} \xrightarrow{\hspace{1cm}} w_x \\ \xrightarrow{\hspace{1cm}} w_y \\ \xrightarrow{\hspace{1cm}} w_z \end{array}$$

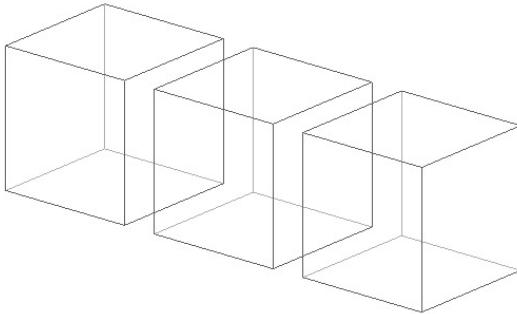
Projection matrix



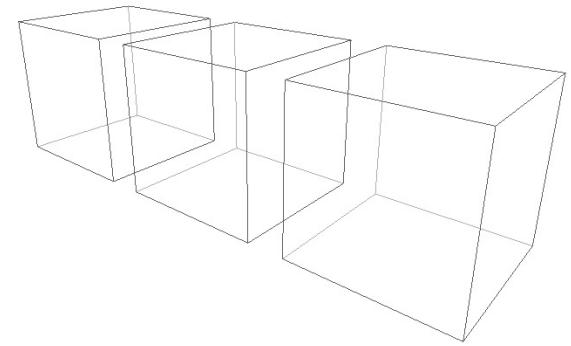
- w_z (depth value) is used for occlusion test → Z-buffering

Orthographic projection

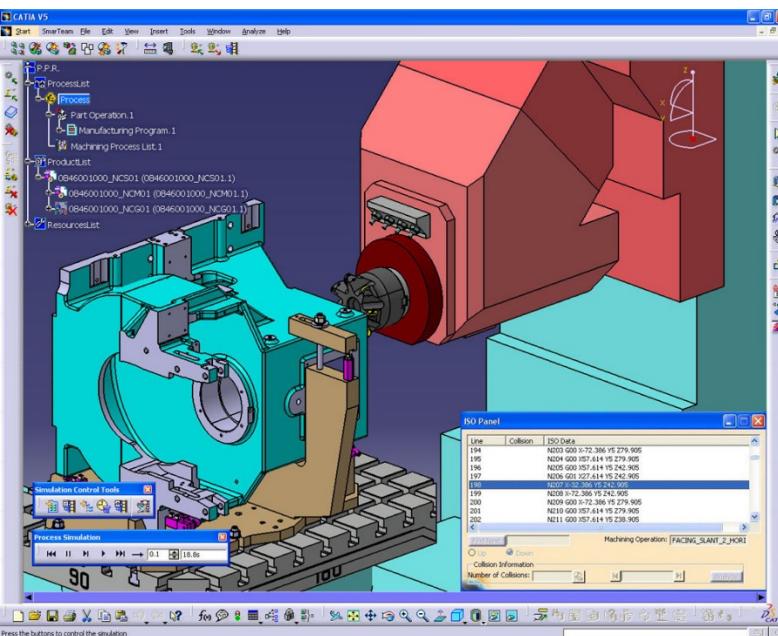
- Objects' apparent sizes don't depend on the camera position
- Simply ignore Z coordinates
- Frequently used in CAD



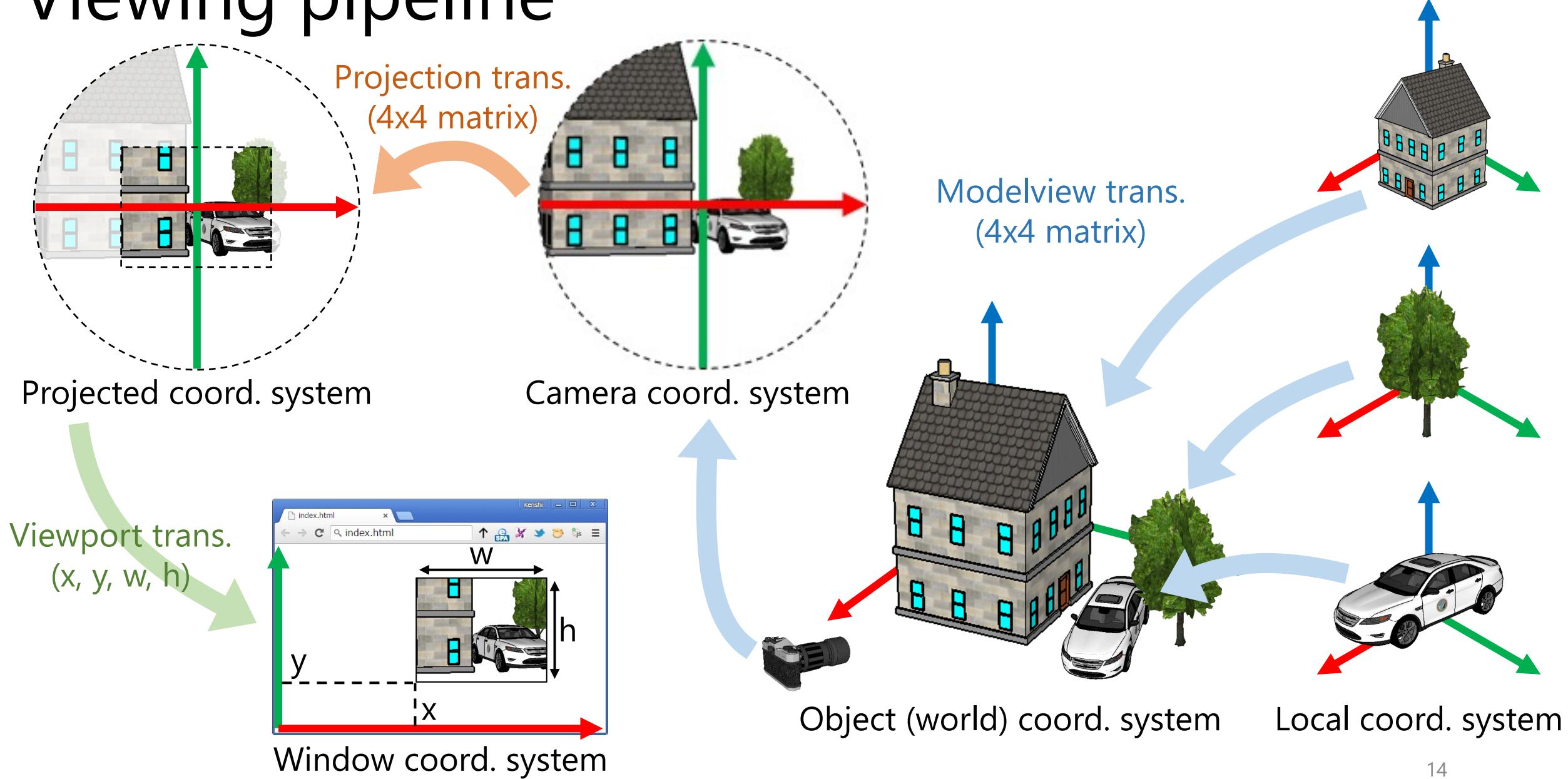
Orthographic



Perspective



Viewing pipeline



Classical OpenGL code

```
glViewport(0, 0, 640, 480);
glMatrixMode(GL_PROJECTION);
glLoadIdentity();
gluPerspective(
    45.0,           // field of view
    640 / 480,     // aspect ratio
    0.1, 100.0);  // depth range

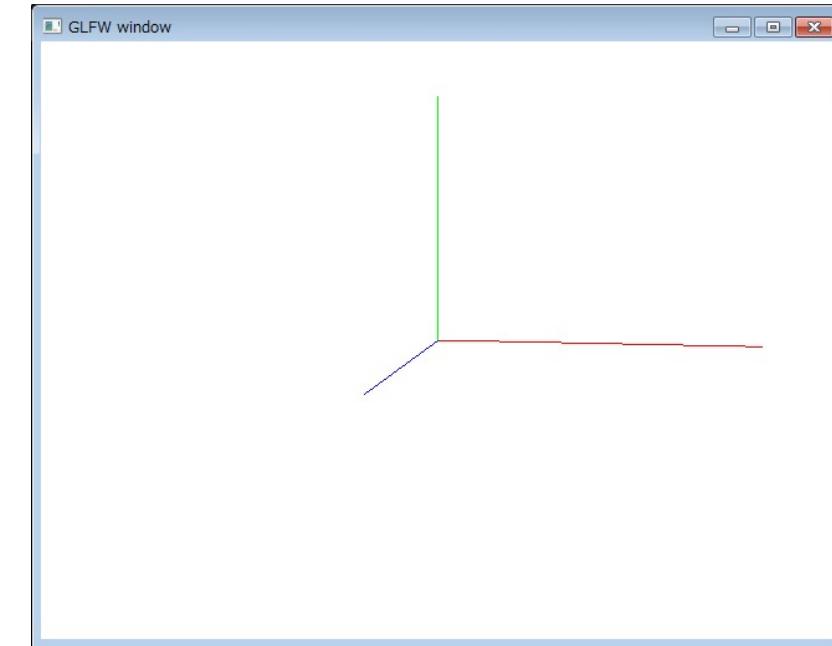
glMatrixMode(GL_MODELVIEW);
glLoadIdentity();
gluLookAt(
    0.5, 0.5, 3.0, // view point
    0.0, 0.0, 0.0, // focus point
    0.0, 1.0, 0.0); // up vector

glBegin(GL_LINES);
glColor3d(1, 0, 0); glVertex3d(0, 0, 0); glVertex3d(1, 0, 0);
glColor3d(0, 1, 0); glVertex3d(0, 0, 0); glVertex3d(0, 1, 0);
glColor3d(0, 0, 1); glVertex3d(0, 0, 0); glVertex3d(0, 0, 1);
glEnd();
```

} Viewport transform

} Projection transform

} Modelview transform

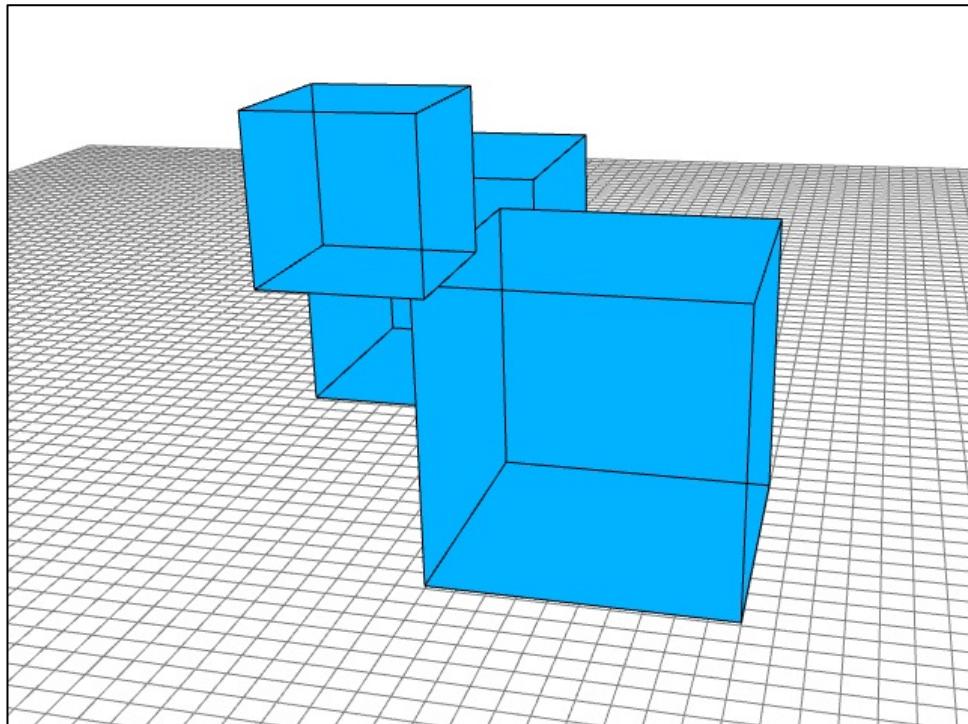


Output

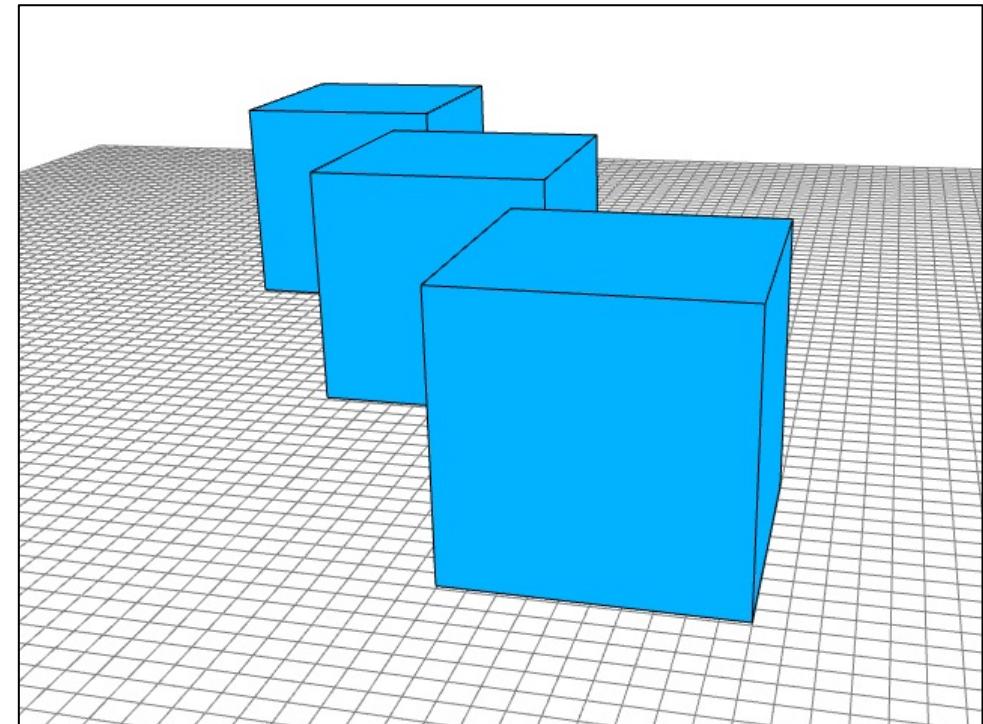
} Scene content

Z-buffering

Hidden surface removal



Without hidden surface removal

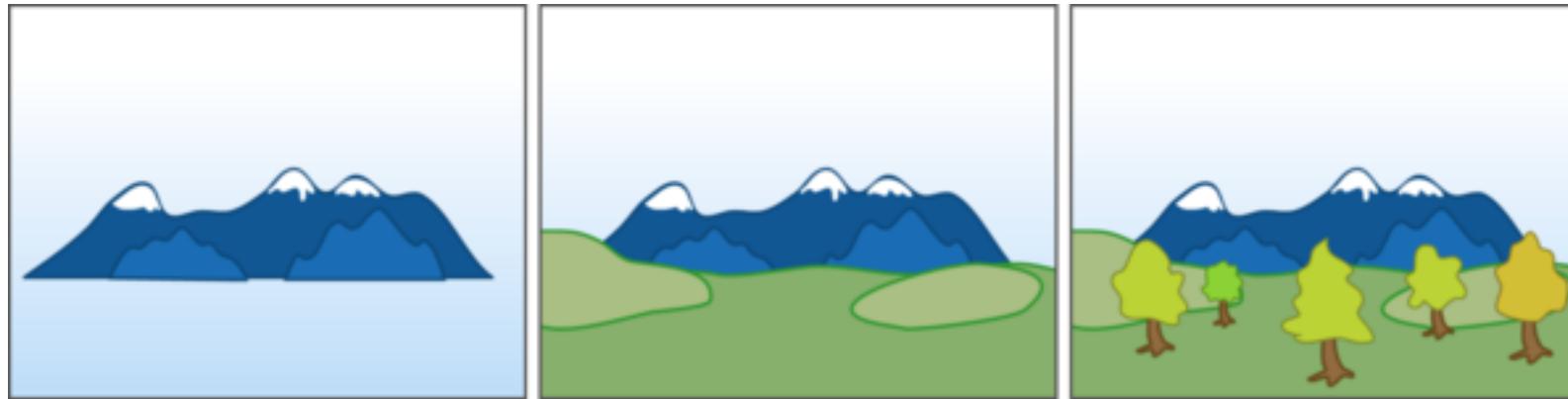


With hidden surface removal

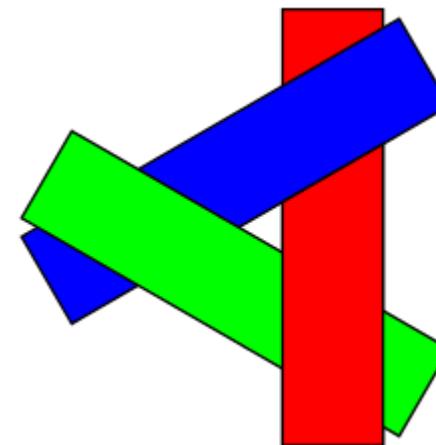
- Classic problem in CG

Painter's algorithm

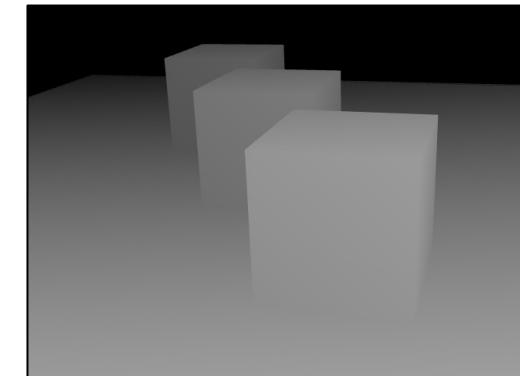
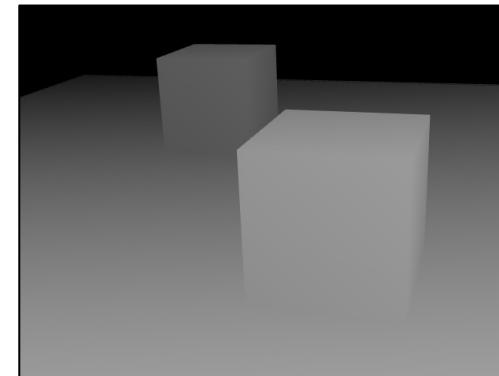
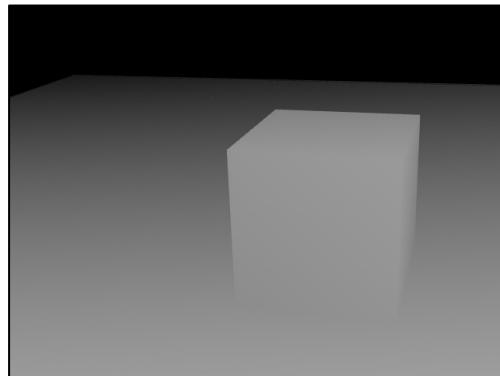
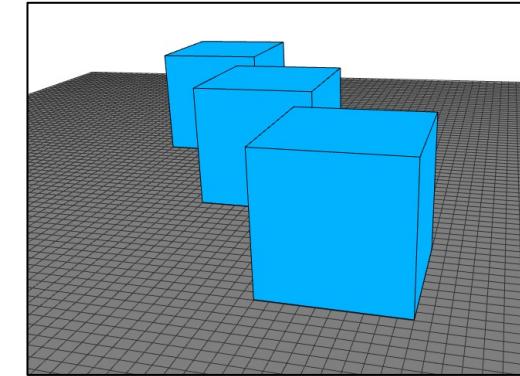
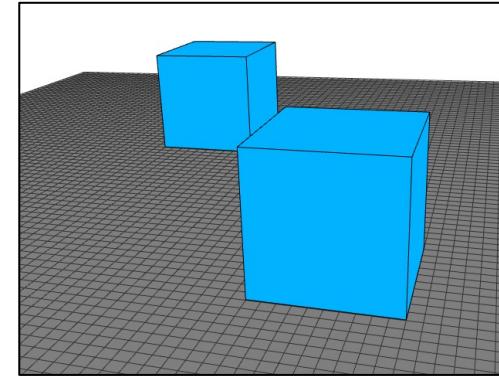
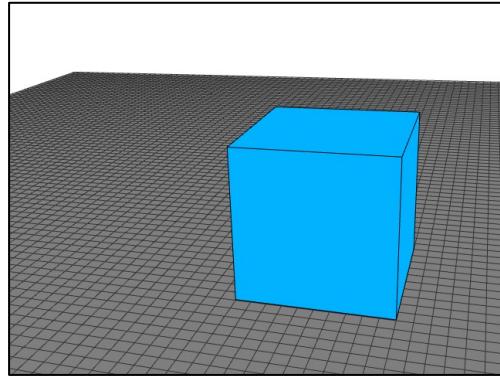
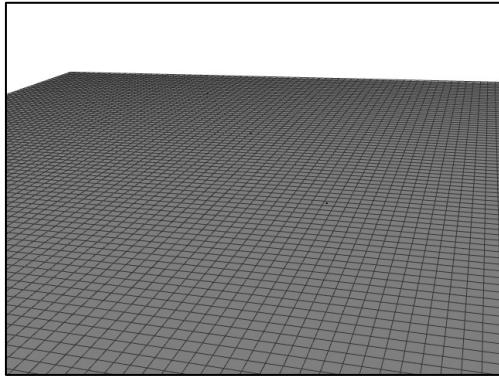
- Sort objects according to distances to camera, then draw them in the back-to-front order



- Fundamentally ill-suited for many cases
 - Sorting is also not always straightforward



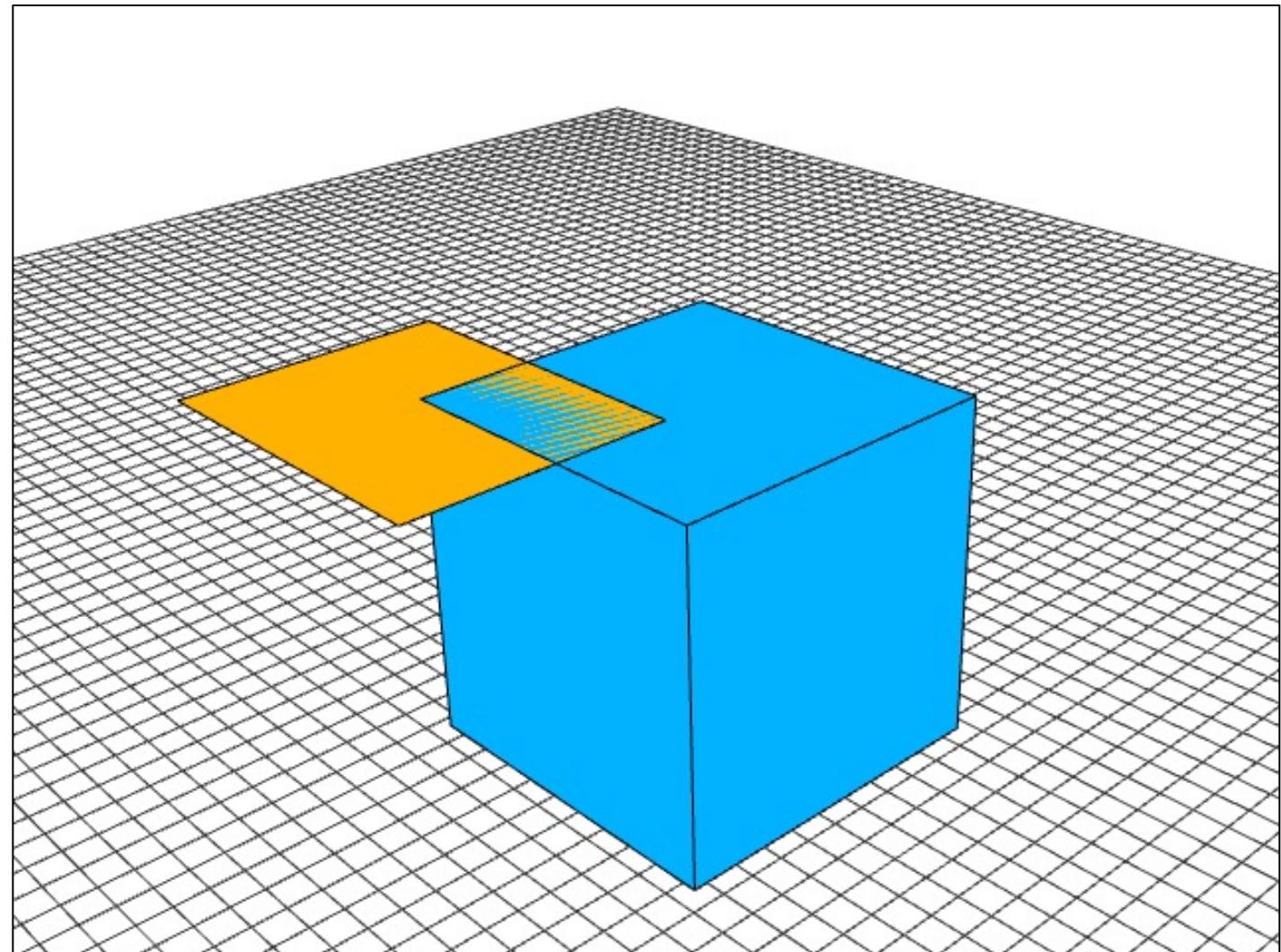
Z-buffering



- For each pixel, store distance to the camera (depth)
- More memory-consuming, but today's standard

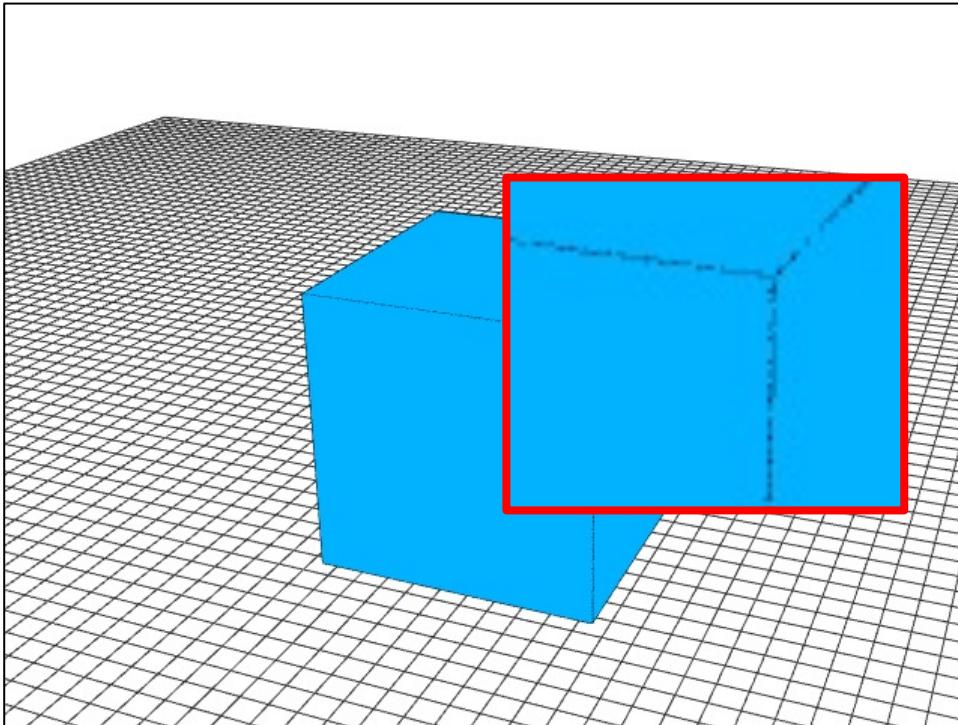
Typical issues with Z-buffering: Z-fighting

- Multiple polygons at exact same position
- Impossible to determine which is front/back
- Strange patterns due to rounding errors

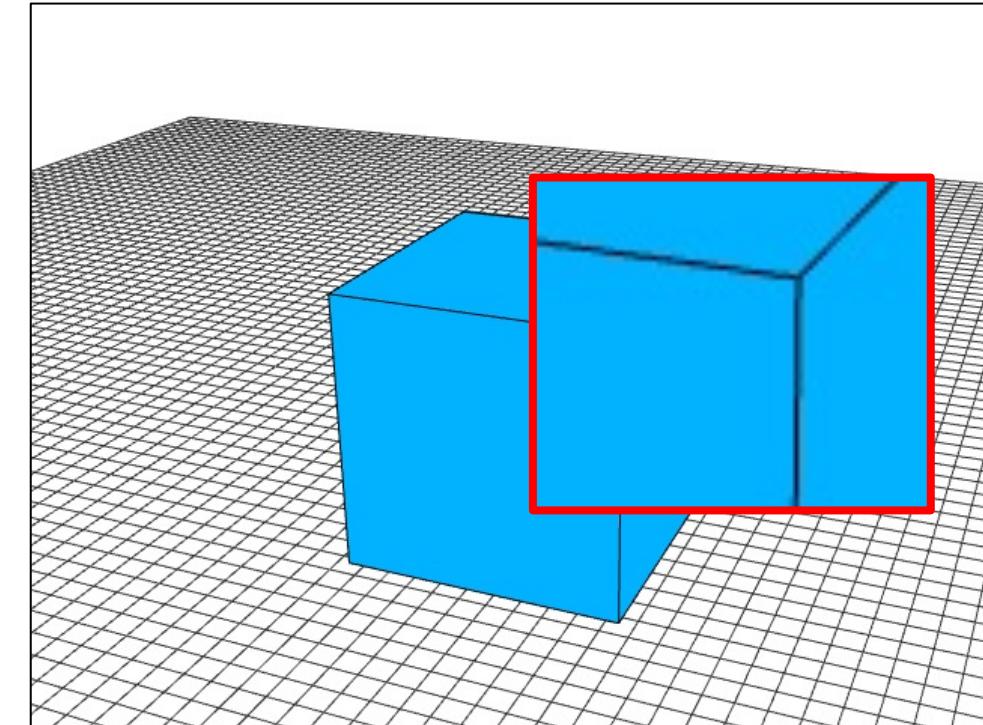


Typical issues with Z-buffering: Simultaneous drawing of faces and lines

- Dedicated OpenGL trick: `glPolygonOffset`



Without polygon offset

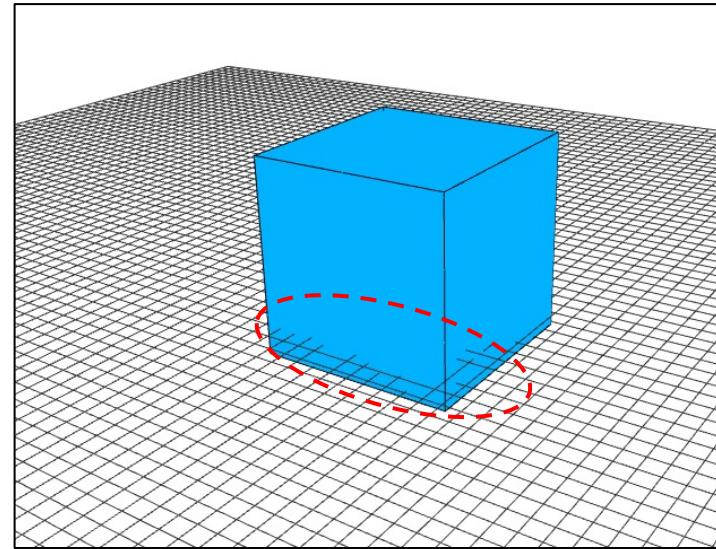


With polygon offset

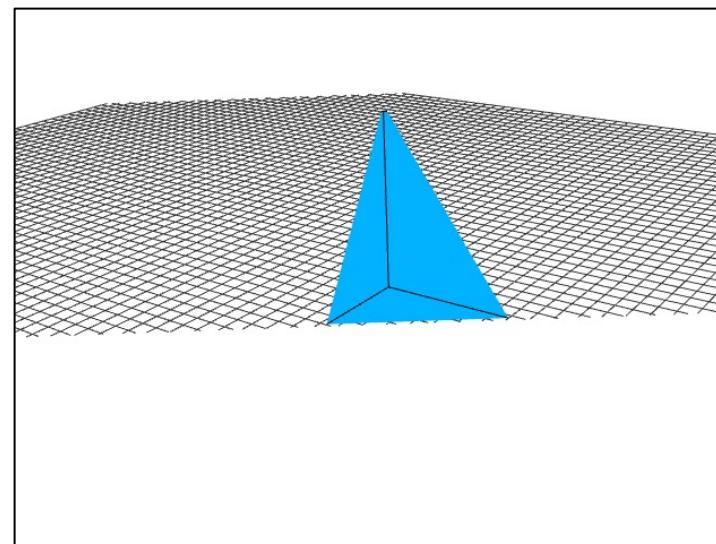
Typical issues with Z-buffering: Depth range

```
gluPerspective(  
    45.0,           // field of view  
    640 / 480,      // aspect ratio  
    0.1, 1000.0); // zNear, zFar
```

- Fixed bits for Z-buffer
 - Typically, 16~24bits
- Larger depth range
 - Larger drawing space, less accuracy
- Smaller depth range
 - More accuracy, smaller drawing space (clipped)



zNear=0.0001
zFar = 1000



zNear=50
zFar = 100

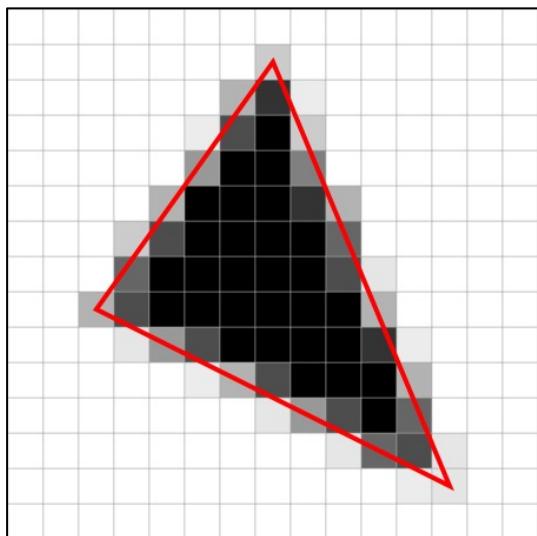
Rasterization vs Ray-tracing

Purpose

Real-time CG (games)

Idea

Per-polygon processing



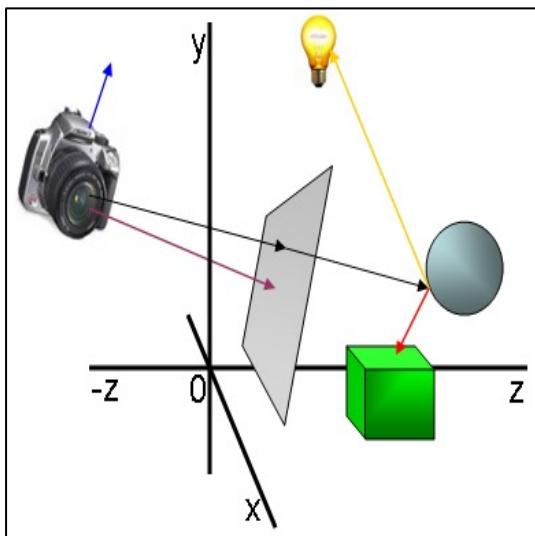
One polygon
updates multiple
pixels

Hidden surface
removal

Z-buffering
(OpenGL / DirectX)

High-quality CG (movies)

Per-pixel (ray) processing



One ray interacts
with multiple
polygons

By nature

More details by Prof. Hachisuka

Quaternions

Rotation about arbitrary axis

- Needed in various situations (e.g. camera manipulation)

$$R_x(\theta) = \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos\theta & -\sin\theta \\ 0 & \sin\theta & \cos\theta \end{bmatrix} \quad \text{about X-axis}$$
$$R_y(\theta) = \begin{bmatrix} \cos\theta & 0 & \sin\theta \\ 0 & 1 & 0 \\ -\sin\theta & 0 & \cos\theta \end{bmatrix} \quad \text{about Y-axis}$$
$$R_z(\theta) = \begin{bmatrix} \cos\theta & -\sin\theta & 0 \\ \sin\theta & \cos\theta & 0 \\ 0 & 0 & 1 \end{bmatrix} \quad \text{about Z-axis}$$

$$R = \begin{bmatrix} \cos\theta + u_x^2(1 - \cos\theta) & u_xu_y(1 - \cos\theta) - u_z\sin\theta & u_xu_z(1 - \cos\theta) + u_y\sin\theta \\ u_yu_x(1 - \cos\theta) + u_z\sin\theta & \cos\theta + u_y^2(1 - \cos\theta) & u_yu_z(1 - \cos\theta) - u_x\sin\theta \\ u_zu_x(1 - \cos\theta) - u_y\sin\theta & u_zu_y(1 - \cos\theta) + u_x\sin\theta & \cos\theta + u_z^2(1 - \cos\theta) \end{bmatrix}.$$

about arbitrary axis

(u_x, u_y, u_z) : axis vector

- Problems with matrix representation

- Overly complex!

Degree of Freedom

- Should be represented by 2 DoF (axis direction) + 1 DoF (angle) = 3 DoF
- Can't handle interpolation (blending) well

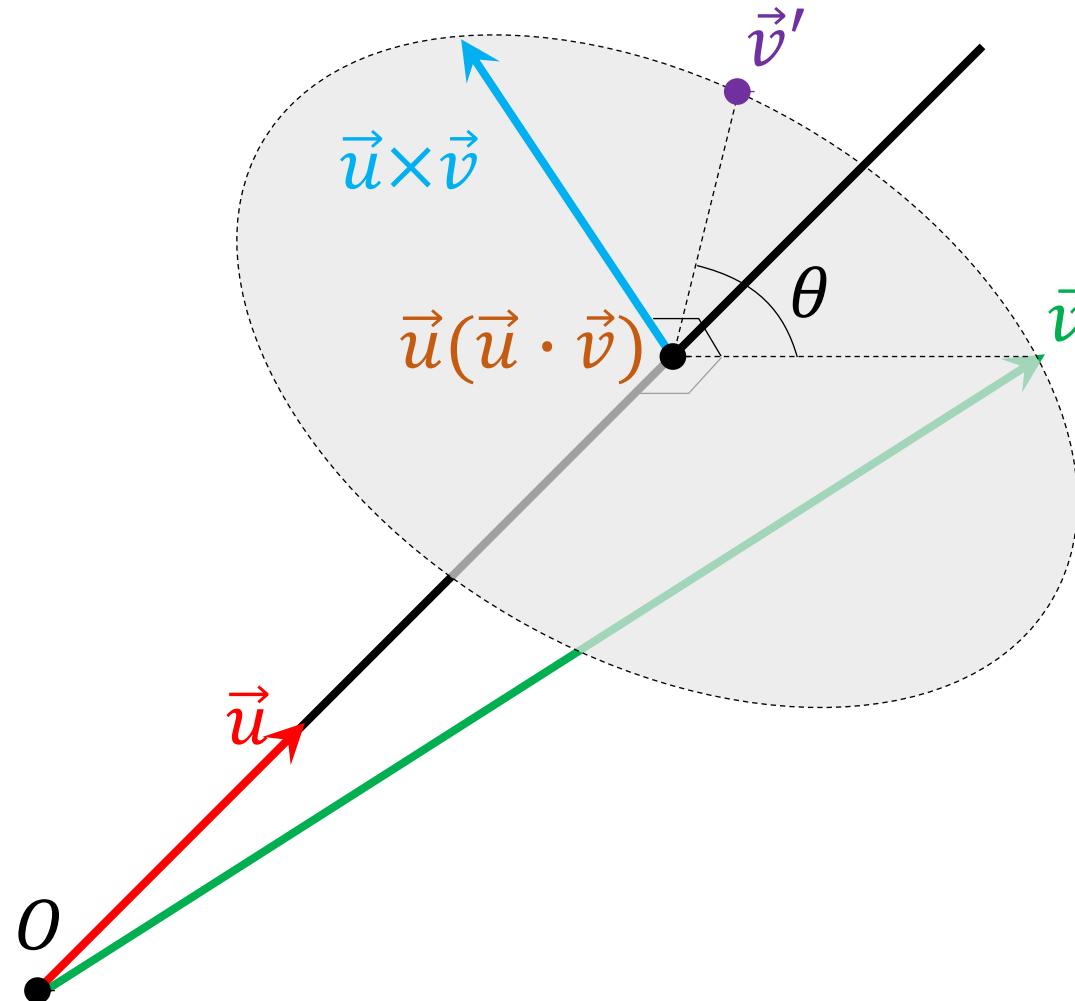
Geometry of axis-angle rotation

\vec{u} : axis (unit vector)

θ : angle

\vec{v} : input position

\vec{v}' : output position



$$\vec{v}' = (\vec{v} - \vec{u}(\vec{u} \cdot \vec{v})) \cos \theta + (\vec{u} \times \vec{v}) \sin \theta + \vec{u}(\vec{u} \cdot \vec{v})$$

Complex number & quaternion

- Complex number
 - $\mathbf{i}^2 = -1$
 - $\mathbf{c} = (a, b) := a + b \mathbf{i}$
 - $\mathbf{c}_1 \mathbf{c}_2 = (a_1, b_1)(a_2, b_2) = a_1 a_2 - b_1 b_2 + (a_1 b_2 + b_1 a_2) \mathbf{i}$
- Quaternion
 - $\mathbf{i}^2 = \mathbf{j}^2 = \mathbf{k}^2 = \mathbf{ijk} = -1$
 - $\mathbf{ij} = -\mathbf{ji} = \mathbf{k}, \quad \mathbf{jk} = -\mathbf{kj} = \mathbf{i}, \quad \mathbf{ki} = -\mathbf{ik} = \mathbf{j}$ Not commutative!
 - $\mathbf{q} = (a, b, c, d) := a + b \mathbf{i} + c \mathbf{j} + d \mathbf{k}$
 - $\mathbf{q}_1 \mathbf{q}_2 = (a_1, b_1, c_1, d_1)(a_2, b_2, c_2, d_2)$
$$= (a_1 a_2 - b_1 b_2 - c_1 c_2 - d_1 d_2) + (a_1 b_2 + b_1 a_2 + c_1 d_2 - d_1 c_2) \mathbf{i}$$
$$+ (a_1 c_2 + c_1 a_2 + d_1 b_2 - b_1 d_2) \mathbf{j} + (a_1 d_2 + d_1 a_2 + b_1 c_2 - c_1 b_2) \mathbf{k}$$

Notation by scalar + 3D vector

- $\mathbf{q}_1 = a_1 + b_1 \mathbf{i} + c_1 \mathbf{j} + d_1 \mathbf{k} \coloneqq a_1 + (b_1, c_1, d_1) = a_1 + \vec{v}_1$
- $\mathbf{q}_2 = a_2 + b_2 \mathbf{i} + c_2 \mathbf{j} + d_2 \mathbf{k} \coloneqq a_2 + (b_2, c_2, d_2) = a_2 + \vec{v}_2$
- $\mathbf{q}_1 \mathbf{q}_2 = (a_1 a_2 - b_1 b_2 - c_1 c_2 - d_1 d_2) +$
 $(a_1 b_2 + a_2 b_1 + c_1 d_2 - d_1 c_2) \mathbf{i} +$
 $(a_1 c_2 + a_2 c_1 + d_1 b_2 - b_1 d_2) \mathbf{j} +$
 $(a_1 d_2 + a_2 d_1 + b_1 c_2 - c_1 b_2) \mathbf{k}$
 $= (a_1 + \vec{v}_1)(a_2 + \vec{v}_2) = (a_1 a_2 - \vec{v}_1 \cdot \vec{v}_2) + a_1 \vec{v}_2 + a_2 \vec{v}_1 + \vec{v}_1 \times \vec{v}_2$

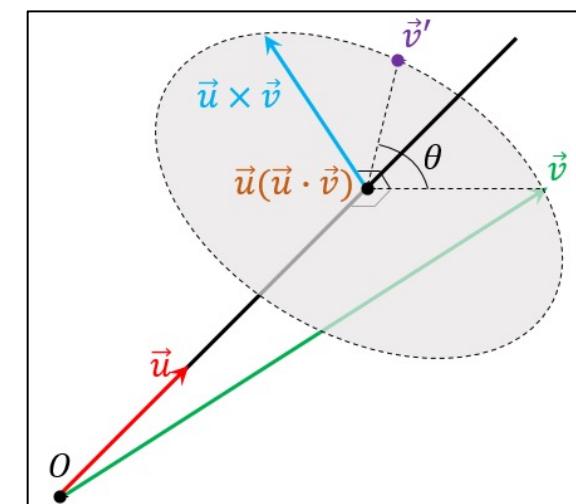
Rotation using quaternions

$$q = \cos \frac{\alpha}{2} + \vec{u} \sin \frac{\alpha}{2}$$

Note: \vec{u} is a unit vector

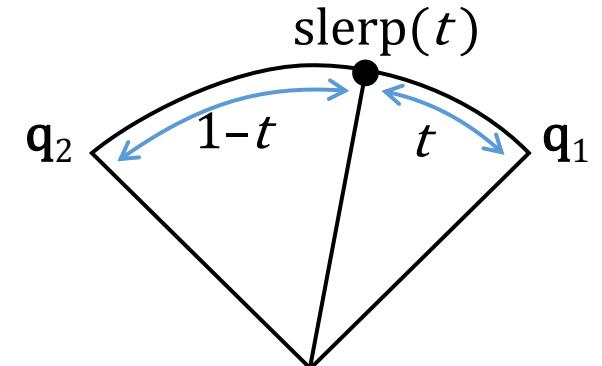
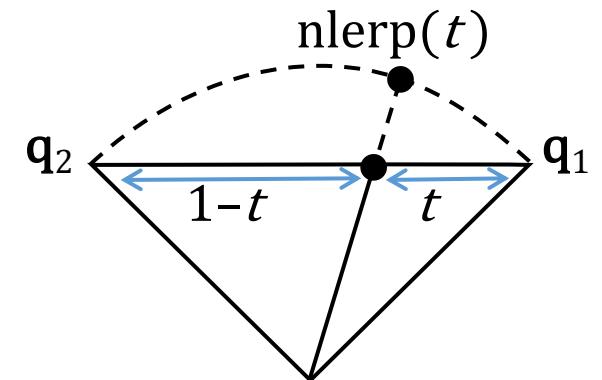
$$\begin{aligned}\vec{v}' &= q\vec{v}q^{-1} = \left(\cos \frac{\alpha}{2} + \vec{u} \sin \frac{\alpha}{2}\right) \vec{v} \left(\cos \frac{\alpha}{2} - \vec{u} \sin \frac{\alpha}{2}\right) \\ &= \vec{v} \cos^2 \frac{\alpha}{2} + (\vec{u}\vec{v} - \vec{v}\vec{u}) \sin \frac{\alpha}{2} \cos \frac{\alpha}{2} - \vec{u}\vec{v}\vec{u} \sin^2 \frac{\alpha}{2} \\ &= \vec{v} \cos^2 \frac{\alpha}{2} + 2(\vec{u} \times \vec{v}) \sin \frac{\alpha}{2} \cos \frac{\alpha}{2} - (\vec{v}(\vec{u} \cdot \vec{u}) - 2\vec{u}(\vec{u} \cdot \vec{v})) \sin^2 \frac{\alpha}{2} \\ &= \vec{v}(\cos^2 \frac{\alpha}{2} - \sin^2 \frac{\alpha}{2}) + (\vec{u} \times \vec{v})(2 \sin \frac{\alpha}{2} \cos \frac{\alpha}{2}) + \vec{u}(\vec{u} \cdot \vec{v})(2 \sin^2 \frac{\alpha}{2}) \\ &= \vec{v} \cos \alpha + (\vec{u} \times \vec{v}) \sin \alpha + \vec{u}(\vec{u} \cdot \vec{v})(1 - \cos \alpha) \\ &= (\vec{v} - \vec{u}(\vec{u} \cdot \vec{v})) \cos \alpha + (\vec{u} \times \vec{v}) \sin \alpha + \vec{u}(\vec{u} \cdot \vec{v})\end{aligned}$$

- Interesting theory behind
 - Clifford algebra
 - Geometric algebra
- Also important for physics & robotics



Rotation interpolation using quaternions

- Linear interp + normalization (nlerp)
 - $\text{nlerp}(\mathbf{q}_1, \mathbf{q}_2, t) := \text{normalize}((1 - t)\mathbf{q}_1 + t \mathbf{q}_2)$
 - ☺less computation, ☹non-uniform angular speed
- Spherical linear interpolation (slerp)
 - $\Omega = \cos^{-1}(\mathbf{q}_1 \cdot \mathbf{q}_2)$
 - $\text{slerp}(\mathbf{q}_1, \mathbf{q}_2, t) := \frac{\sin(1-t)\Omega}{\sin \Omega} \mathbf{q}_1 + \frac{\sin t\Omega}{\sin \Omega} \mathbf{q}_2$
 - ☹more computation, ☺constant angular speed



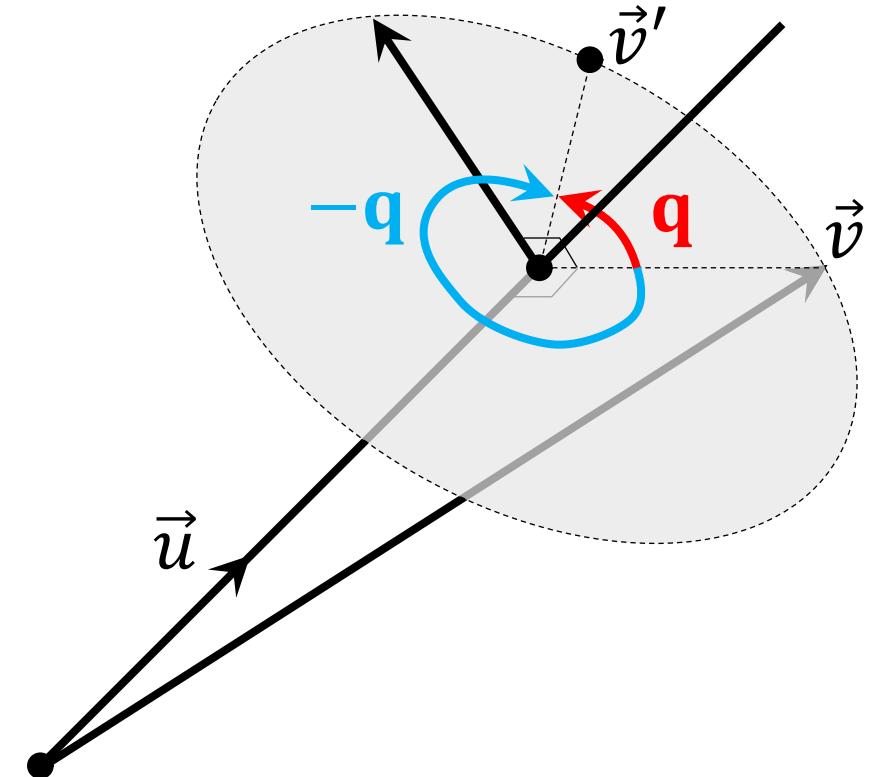
Signs of quaternions

- Quaternion with angle θ :

- $\mathbf{q} = \cos \frac{\theta}{2} + \vec{u} \sin \frac{\theta}{2}$

- Quaternion with angle $\theta - 2\pi$:

- $\cos \frac{\theta-2\pi}{2} + \vec{u} \sin \frac{\theta-2\pi}{2} = -\mathbf{q}$



- When interpolating from \mathbf{q}_1 to \mathbf{q}_2 , negate \mathbf{q}_2 if $\mathbf{q}_1 \cdot \mathbf{q}_2$ is negative
 - Otherwise, the interpolation path becomes longer

How to work on assignments

Choices for implementing real-time CG

- Two kinds of APIs for using GPU
 - Different API designs (slightly?)
 - Both supported by most popular programming languages
- Many choices for system- & language-dependent parts
 - GUI management, handling images, ...
 - Many libraries:
 - GUI: GLUT (C), GLFW (C), SDL (C), Qt (C++), MFC (C++), wxWidgets (C++), Swing (Java), ...
 - Images: libpng, OpenCV, ImageMagick
- Often quite some work to get started



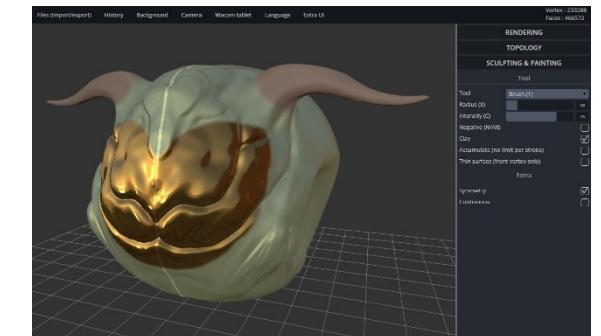
OpenGL®



Microsoft
DirectX

WebGL = JavaScript + OpenGL

- Runs on many (mobile) browsers
- HTML-based → can easily handle multimedia & GUI
- No compiling!
 - Quick trial & error
- Some performance concerns
- Increasingly popular today



Hurdle in WebGL development: OpenGL ES

- No support for legacy OpenGL API
- Reasons:
 - Less efficient
 - Burden on hardware vendors

- Allowed API:

Prepare arrays, send them to GPU, draw them using custom shaders

Immediate mode
Polygonal primitives
Light & material
Transform. matrices
Display list
Default shaders

Shaders
Shader variables
Arrays
Drawing

glBegin, glVertex, glColor, glTexCoord
GL_QUADS, GL_POLYGON
glLight, glMaterial
GL_MODELVIEW, GL_PROJECTION
glNewList

glCreateShader, glShaderSource,
glCompileShader, glCreateProgram,
glAttachShader, glLinkProgram,
glUseProgram
glGetAttribLocation,
glEnableVertexAttribArray,
glGetUniformLocation, glUniform
glCreateBuffer, glBindBuffer,
glBufferData, glVertexAttribPointer
glDrawArrays

```
#include <GL/glut.h>
void disp( void ) {
    float f;
    glClear(GL_COLOR_BUFFER_BIT);
    glPushMatrix();
    for(f = 0 ; f < 1 ; f += 0.1) {
        glColor3f(f , 0 , 0);
        glCallList(1);
    }
    glPopMatrix();
    glFlush();
}
void setDispList( void ) {
    glNewList(1, GL_COMPILE);
    glBegin(GL_POLYGON);
    glVertex2f(-1.2 , -0.9);
    glVertex2f(0.6 , -0.9);
    glVertex2f(-0.3 , 0.9);
    glEnd();
    glTranslatef(0.1 , 0 , 0);
    glEndList();
}
int main(int argc , char ** argv) {
    glutInit(&argc , argv);
    glutInitWindowSize(400 , 300);
    glutInitDisplayMode(GLUT_RGBA);
    glutCreateWindow("Kitty on your lap");
    glutDisplayFunc(disp);
    setDispList();
    glutMainLoop();
}
```

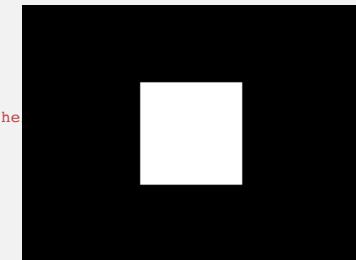


C / OpenGL 1.x

```
<html>
    <head>
        <title>WebGL Demo</title>
        <script src="gl-matrix-min.js"></script>
        <script>
main();
function main() {
    const canvas = document.querySelector('#glcanvas');
    const gl = canvas.getContext('webgl');
    if (!gl) {
        alert('Unable to initialize WebGL!');
        return;
    }
    const vsSource =
        `attribute vec4 aVertexPosition;
        uniform mat4 uModelViewMatrix;
        uniform mat4 uProjectionMatrix;
        void main()
            gl_Position = uModelViewMatrix * aVertexPosition;
        `;
    const fsSource =
        `void main()
            gl_FragColor = vec4(1.0, 0.0, 0.0, 1.0);
        `;
    const shaderProgram = gl.createProgram();
    program: shaderProgram;
    attribLocations: {};
    vertexPosition: 0;
    uniformLocations: {};
    projectionMatrix: 1;
    modelViewMatrix: 2;
    };
    const buffers = {};
    drawScene(gl);
}
function initProgram(gl, vsSource, fsSource) {
    const positionAttributeLocation = gl.getAttribLocation(shaderProgram, "aVertexPosition");
    const positionUniformLocation = gl.getUniformLocation(shaderProgram, "uModelViewMatrix");
    const projectionUniformLocation = gl.getUniformLocation(shaderProgram, "uProjectionMatrix");
    gl.bindBuffer(gl.ARRAY_BUFFER, buffers.position);
    gl.vertexAttribPointer(positionAttributeLocation, 3, gl.FLOAT, false, 0, 0);
    gl.enableVertexAttribArray(positionAttributeLocation);
    gl.uniformMatrix4fv(projectionUniformLocation, 1, false, mat4.create());
    gl.uniformMatrix4fv(modelViewMatrix, 1, false, mat4.create());
}
function drawScene(gl) {
    gl.viewport(0, 0, gl.canvas.clientWidth, gl.canvas.clientHeight);
    gl.clearColor(0.0, 0.0, 0.0, 1.0);
    gl.clearDepth(1.0);
    gl.enable(gl.DEPTH_TEST);
    gl.depthFunc(gl.LEQUAL);
    gl.clear(gl.COLOR_BUFFER_BIT | gl.DEPTH_BUFFER_BIT);
    const fieldOfView = 45 * Math.PI / 180;
    const aspect = gl.canvas.clientWidth / gl.canvas.clientHeight;
    const zNear = 0.1;
    const zFar = 100.0;
    const projectionMatrix = mat4.create();
    mat4.perspective(projectionMatrix, fieldOfView, aspect, zNear, zFar);
    const modelViewMatrix = mat4.create();
    mat4.translate(modelViewMatrix, modelViewMatrix, [-0.5, 0.0, -6.0]);
    mat4.multiply(modelViewMatrix, projectionMatrix, modelViewMatrix);
    gl.drawArrays(gl.TRIANGLE_STRIP, 0, 4);
}
</script>
</head>
<body>
<div id="glcanvas" style="width: 100%; height: 100%; position: absolute; left: 0; top: 0; background-color: black; overflow: hidden; margin: auto; border: 1px solid black; border-radius: 10px; z-index: 1000; "></div>
</body>
</html>
```

WebGL

```
{
    const numComponents = 2;
    const type = gl.FLOAT;
    const normalize = false;
    const stride = 0;
    const offset = 0;
    gl.bindBuffer(gl.ARRAY_BUFFER, buffers.position);
    gl.vertexAttribPointer(
        programInfo.attribLocations.vertexPosition,
        numComponents,
        type,
        normalize,
        stride,
        offset);
    gl.enableVertexAttribArray(programInfo.attribLocations.vertexPosition);
}
function initProgram(gl, vsSource, fsSource) {
    const shaderProgram = loadShader(gl, gl.VERTEX_SHADER, vsSource);
    const fragmentShader = loadShader(gl, gl.FRAGMENT_SHADER, fsSource);
    const program = gl.createProgram();
    gl.attachShader(program, vertexShader);
    gl.attachShader(program, fragmentShader);
    gl.linkProgram(program);
    if (!gl.getProgramParameter(program, gl.LINK_STATUS)) {
        console.error(`There was an error linking the shader program: ${gl.getProgramInfoLog(program)}`);
    }
    const positionAttributeLocation = gl.getAttribLocation(shaderProgram, "aVertexPosition");
    const positionUniformLocation = gl.getUniformLocation(shaderProgram, "uModelViewMatrix");
    const projectionUniformLocation = gl.getUniformLocation(shaderProgram, "uProjectionMatrix");
    gl.bindBuffer(gl.ARRAY_BUFFER, buffers.position);
    gl.vertexAttribPointer(positionAttributeLocation, numComponents, type, normalize, stride, offset);
    gl.enableVertexAttribArray(positionAttributeLocation);
    gl.uniformMatrix4fv(positionUniformLocation, 1, false, mat4.create());
    gl.uniformMatrix4fv(projectionUniformLocation, 1, false, mat4.create());
}
function drawScene(gl) {
    const positionAttributeLocation = gl.getAttribLocation(shaderProgram, "aVertexPosition");
    const positionUniformLocation = gl.getUniformLocation(shaderProgram, "uModelViewMatrix");
    const projectionUniformLocation = gl.getUniformLocation(shaderProgram, "uProjectionMatrix");
    gl.bindBuffer(gl.ARRAY_BUFFER, buffers.position);
    gl.vertexAttribPointer(positionAttributeLocation, numComponents, type, normalize, stride, offset);
    gl.enableVertexAttribArray(positionAttributeLocation);
    gl.uniformMatrix4fv(positionUniformLocation, 1, false, mat4.create());
    gl.uniformMatrix4fv(projectionUniformLocation, 1, false, mat4.create());
    gl.drawArrays(gl.TRIANGLE_STRIP, offset, vertexCount);
}
function loadShader(gl, type, source) {
    const shader = gl.createShader(type);
    gl.shaderSource(shader, source);
    gl.compileShader(shader);
    if (!gl.getShaderParameter(shader, gl.COMPILE_STATUS)) {
        console.error(`There was an error compiling the shader: ${gl.getShaderInfoLog(shader)}`);
    }
    return shader;
}
function initProgram(gl, vsSource, fsSource) {
    const shaderProgram = loadShader(gl, gl.VERTEX_SHADER, vsSource);
    const fragmentShader = loadShader(gl, gl.FRAGMENT_SHADER, fsSource);
    const program = gl.createProgram();
    gl.attachShader(program, vertexShader);
    gl.attachShader(program, fragmentShader);
    gl.linkProgram(program);
    if (!gl.getProgramParameter(program, gl.LINK_STATUS)) {
        console.error(`There was an error linking the shader program: ${gl.getProgramInfoLog(program)}`);
    }
}
```



Libraries for easing WebGL development

- Many popular ones:
 - three.js, O3D, OSG.JS, ...
- All APIs are high-level, quite different from legacy OpenGL API ☹
- Good for casual users, but maybe not for CS students (?)

```
<script src="js/three.min.js"></script>
<script>
var camera, scene, renderer, geometry, material, mesh;
function init() {
    scene = new THREE.Scene();
    camera = new THREE.PerspectiveCamera( 75, 640 / 480, 1, 1000 );
    camera.position.z = 1000;
    geometry = new THREE.BoxGeometry( 200, 200, 200 );
    material = new THREE.MeshBasicMaterial({color:0xff0000, wireframe:true});
    mesh = new THREE.Mesh( geometry, material );
    scene.add( mesh );
    renderer = new THREE.WebGLRenderer();
    renderer.setSize(640, 480);
    document.body.appendChild( renderer.domElement );
}
function animate() {
    requestAnimationFrame( animate );
    render();
}
function render() {
    mesh.rotation.x += 0.01;
    mesh.rotation.y += 0.02;
    renderer.render( scene, camera );
}
init();
animate();
</script>
```

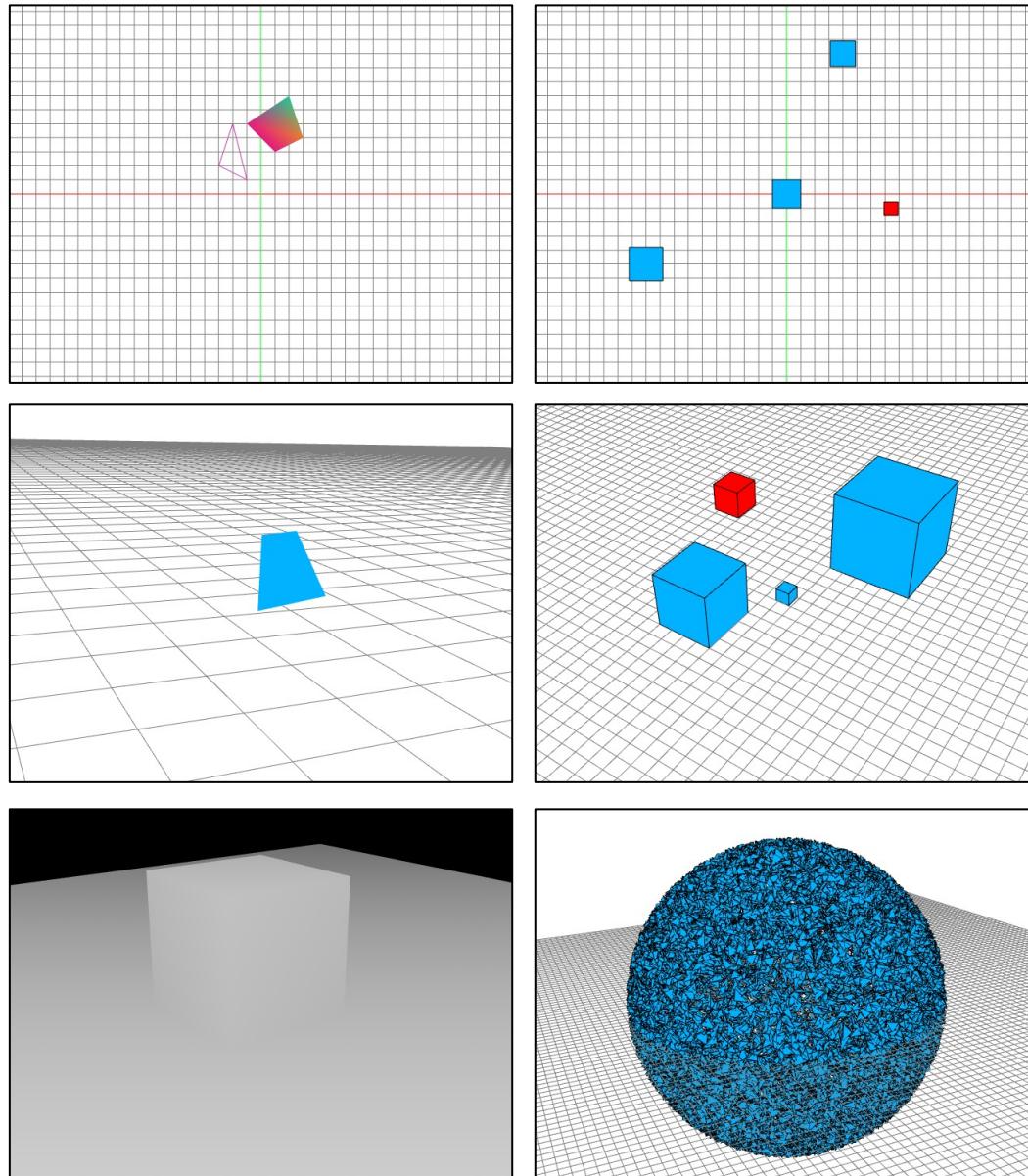
three.js

High-level API



legacygl.js

- Developed by me for this course
 - <https://bitbucket.org/kenshi84/legacygl.js>
 - Demos & tutorial
- Assignemnts' sample codes will be mostly using this
 - Try playing with it and see how it works



WebGL development using Glitch

- A free web space for putting js/html/css
- Online editing and quick previewing

<https://glitch.com/>

The screenshot shows the Glitch web interface. At the top, there's a browser-like header with a back/forward button, refresh, and address bar containing the URL <https://glitch.com/edit/#!/legacygl-js?path=demo/hello2d.html:1:0>. Below the header is the project navigation bar with 'legacygl-js' and a 'Show' dropdown. The main area has tabs for 'demo/hello2d.html' and a search icon.

The left sidebar shows the project structure:

- New File
- assets
- demo/
 - displist.html
 - hello2d.html
 - hello3d.html
 - meshviewer.html
 - pick2d.html
 - pick3d.html
 - quaternion... c.html
 - z-buffer.html
- boundingbox.js
- camera.js
- colormap.js
- drawutil.js
- gl-matrix-util.js
- gl-matrix.js
- glu.js
- halfedge.js

The 'hello2d.html' file is currently selected, indicated by a purple highlight.

The central code editor displays the following code:

```
1<html>
2
3<head>
4<title>legacygl.js Demo: Hello World 2D</title>
5<script src="../gl-matrix.js"></script>
6<script src="../gl-matrix-util.js"></script>
7<script src="../legacygl.js"></script>
8<script src="../drawutil.js"></script>
9<script src="../camera.js"></script>
10<script src="../util.js"></script>
11<script type="text/javascript">
12var gl;
13var canvas;
14var legacygl;
15var drawutil;
16var camera;
17
18function draw() {
19    gl.clear(gl.COLOR_BUFFER_BIT);
20    // projection and camera position
21    var eyez = camera.eye[2];
22    mat4.perspective(legacygl.uniforms.projection.value, Math
23    camera.lookAt(legacygl.uniforms.modelview.value);
24    // xy-grid
25    legacygl.color(0.5, 0.5, 0.5);
```

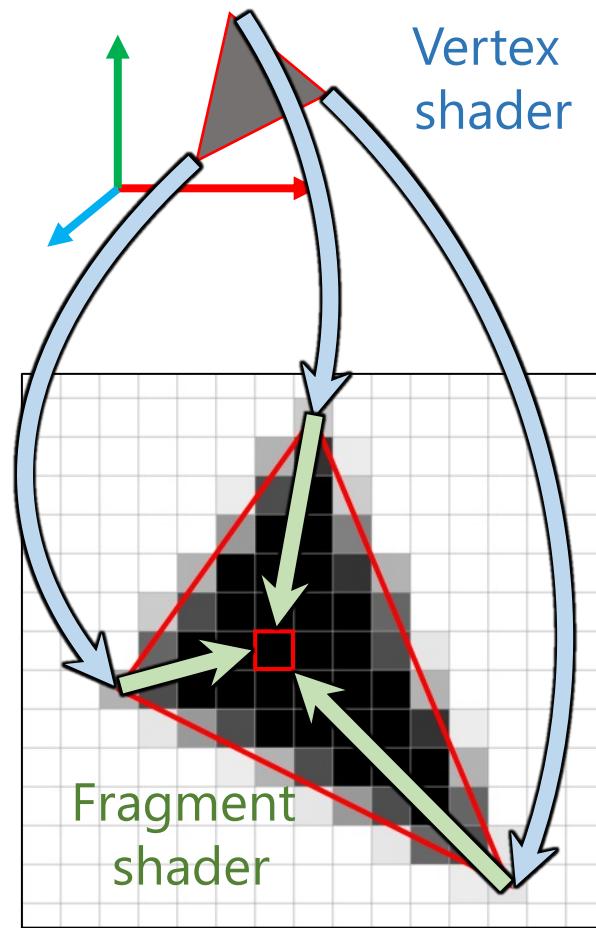
The right side shows the preview of the 'legacygl.js Demo: Hello World 2D' application. It features a 2D coordinate system with a grid. A 3D cube is rendered at the origin (0,0,0), colored with a gradient from blue to red. A vertical green line and a horizontal red line intersect at the center of the cube, representing the camera's view frustum.

How to work on assignments

- Implement your solution using WebGL, upload it to the web, submit the URL via LMS
 - Glitch is recommended, but other means (e.g. GitHub Pages, your own server) is also OK
 - Include some descriptions/discussions/etc in the HTML page
 - OK to use other WebGL libraries (e.g. three.js)
- Other programming languages (e.g. C++) are also allowed
 - Should compile and run on typical computing systems
 - Include source+binary+doc in a single ZIP file, upload it somewhere (e.g. Google Drive), submit its URL
- If you have any questions, don't hesitate to contact TA or me!

Shaders

- Vertex shader: per-vertex processing
 - Per-vertex data passed by `glBufferData`
 - Vertex position, color, texture coordinate, ...
 - Mandatory operation: Specify vertex location on the screen after coordinate transformation (`gl_Position`)
- Fragment shader: per-pixel processing
 - Do something with rasterized (=linearly interpolated) data
 - Mandatory operation: Specify pixel color to be drawn (`gl_FragColor`)
- GLSL (OpenGL Shading Language) codes passed to GPU as strings
→ compiled at runtime



Shader variables

- uniform variables

- Readable from vertex/fragment shaders
- Passed to GPU separately from vertex arrays (glUniform)
- Examples: modelview/projection matrices, flags

- attribute variables

- Readable only from vertex shaders
- Vertex array data passed to GPU via glBufferData
- Examples: XYZ position, RGB color, UV texcoord

- varying variables

- Written by vertex shader, read by fragment shader
- Per-vertex data linearly interpolated at this pixel

(Grammar differs slightly across versions)

```
uniform mat4 u_modelview;
uniform mat4 u_projection;
attribute vec3 a_vertex;
attribute vec3 a_color;
varying vec3 v_color;
void main(void) {
    gl_Position = u_projection
                  * u_modelview
                  * vec4(a_vertex, 1.0);
    v_color = a_color;
}
```

Vertex shader

```
precision mediump float;
varying vec3 v_color;
void main(void) {
    gl_FragColor.rgb = v_color;
    gl_FragColor.a   = 1.0;
}
```

Fragment shader

Tips for JavaScript beginners (=me)

- 7 types: String / Bool / Number / Function / Object / null / undefined
 - Unlike C++
- Number: always double precision
 - No distinction between integer & floating point
- Object: associative map with string keys
 - `x.abc` is equivalent to `x["abc"]` (as if a "member")
 - `{ abc : y }` is equivalent to `{ "abc" : y }`
 - Non-string keys are implicitly converted to strings
- Arrays are special objects with keys being consecutive integers
 - With additional capabilities: `.length` , `.push()` , `.pop()` , `.forEach()`
- Always pass-by-value when assigning & passing arguments
 - No language support for "deep copy"
- When in doubt, use `console.log(x)`

References

- OpenGL
 - Official spec
<https://www.opengl.org/sdk/docs/man/html/indexflat.php>
- WebGL/JavaScript/HTML5
 - Learning WebGL
<http://learningwebgl.com/blog/?p=11>
 - Official spec
<https://www.khronos.org/registry/webgl/specs/1.0/>
 - Mozilla Developer Network
 - https://developer.mozilla.org/en-US/docs/Web/API/WebGL_API
 - An Introduction to JavaScript for Sophisticated Programmers
<http://casual-effects.blogspot.jp/2014/01/>
 - Effective JavaScript
<http://effectivejs.com/>

References

- http://en.wikipedia.org/wiki/Affine_transformation
- http://en.wikipedia.org/wiki/Homogeneous_coordinates
- [http://en.wikipedia.org/wiki/Perspective_\(graphical\)](http://en.wikipedia.org/wiki/Perspective_(graphical))
- <http://en.wikipedia.org/wiki/Z-buffering>
- <http://en.wikipedia.org/wiki/Quaternion>