Introduction to Computer Graphics

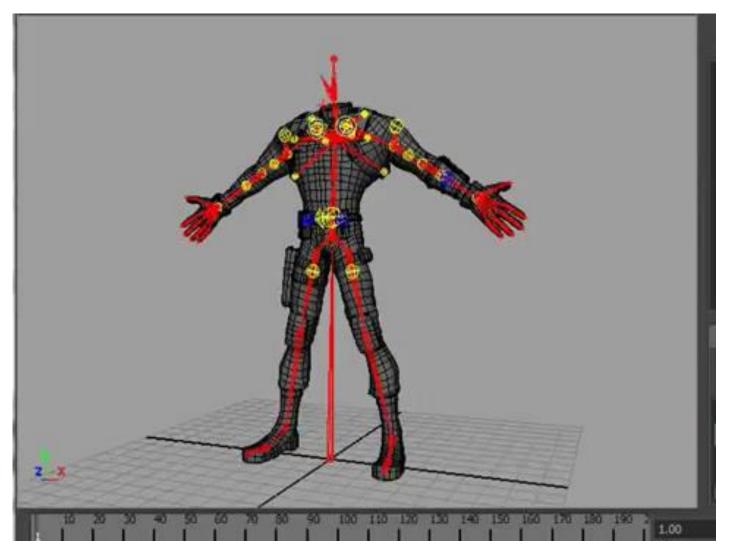
Animation (1) –

May 18, 2017 Kenshi Takayama

Skeleton-based animation

- Simple
- Intuitive

• Low comp. cost



https://www.youtube.com/watch?v=DsoNab58QVA

Representing a pose using skeleton

Tree structure consisting of bones & joints

• Each bone holds relative rotation angle w.r.t. parent joint

 Whole body pose determined by the set of joint angles (Forward Kinematics)

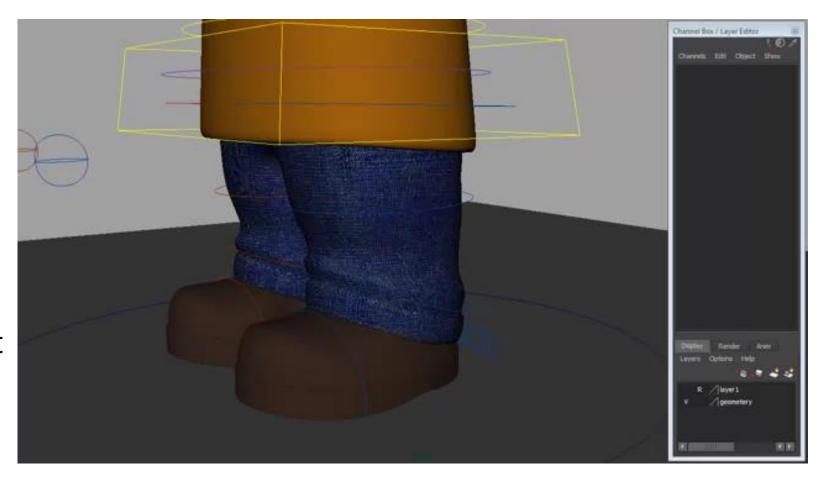
Deeply related to robotics



Inverse Kinematics

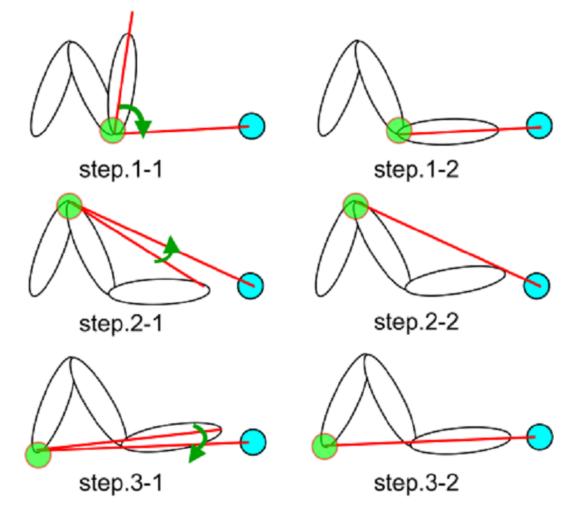
 Find joint angles s.t. an end effector comes at a given goal position

- Typical workflow:
 - Quickly create pose using IK, fine adjustment using FK



Simple method to solve IK: Cyclic Coordinate Descent

- Change joint angles one by one
 - S.t. the end effector comes as close as possible to the goal position
 - Ordering is important! Leaf → root
- Easy to implement → Basic assignment
- More advanced
 - Jacobi method (directional constraint)
 - Minimizing elastic energy [Jacobson 12]



IK minimizing elastic energy

Fast Automatic Skinning Transformations

Alec Jacobson¹
Ilya Baran²
Ladislav Kavan¹
Jovan Popović³
Olga Sorkine¹

¹ETH Zurich

²Disney Research, Zurich

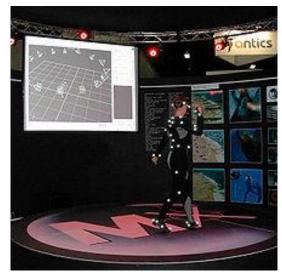
³Adobe Systems, Inc.

This video contains narration.

Ways to obtain/measure motion data

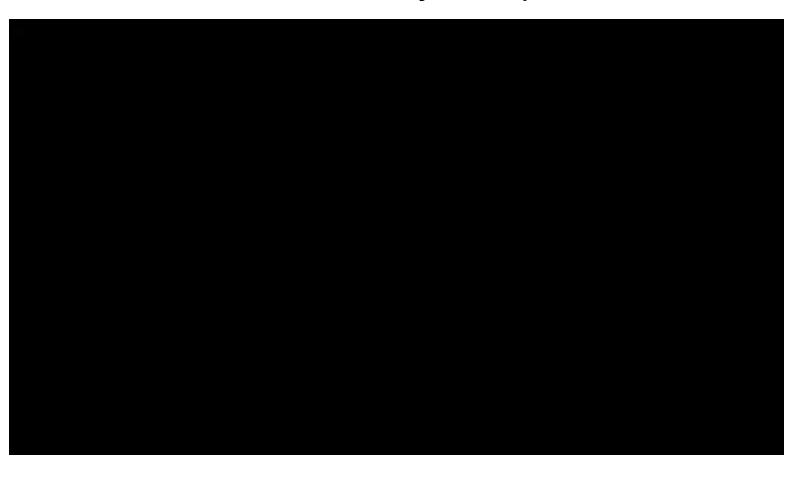
Optical motion capture

Put markers on the actor, record video from many viewpoints (~48)

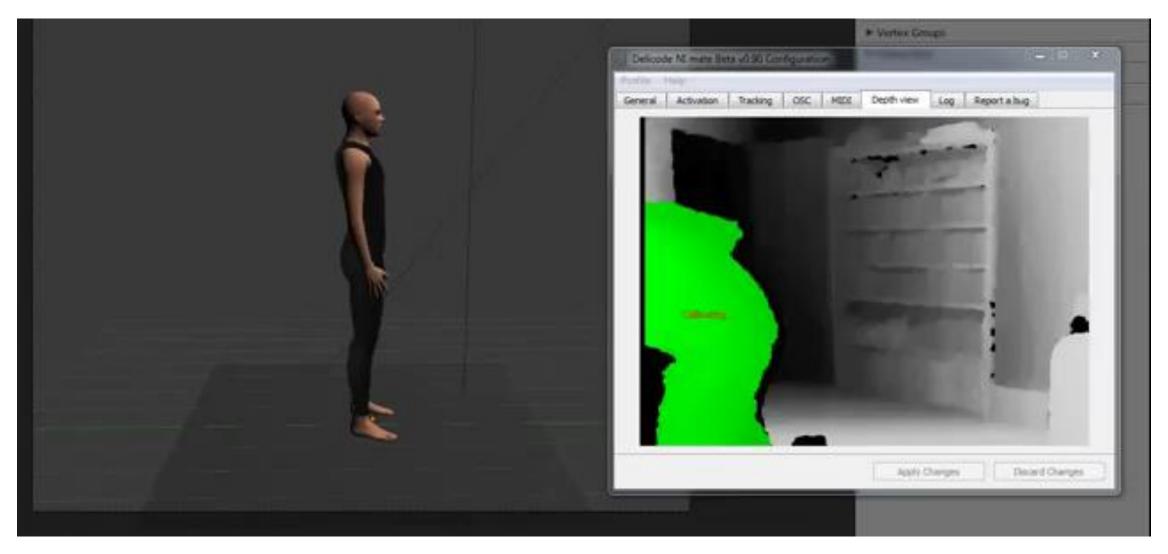




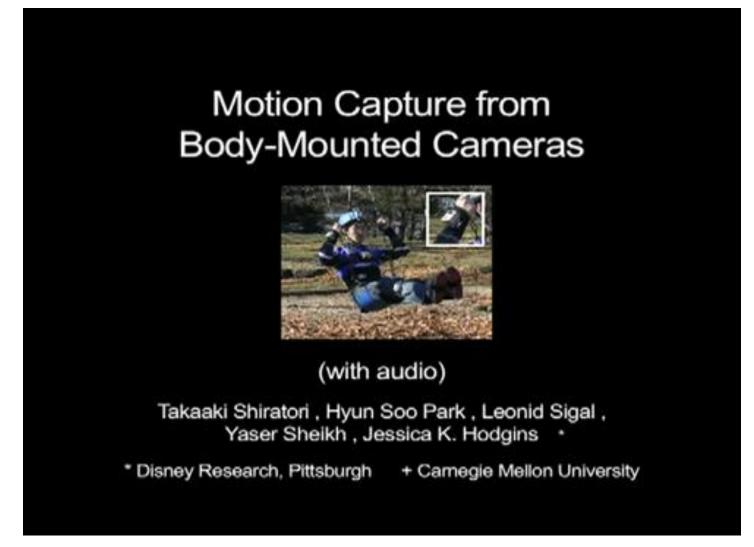
from Wikipedia



Mocap using inexpensive depth camera



Mocap designed for outdoor scene



https://www.youtube.com/watch?v=xbl-NWMfGPs

Motion database

- http://mocap.cs.cmu.edu/
- 6 categories, 2605 in total
- Free for research purposes
 - Interpolation, recombination, analysis, search, etc.















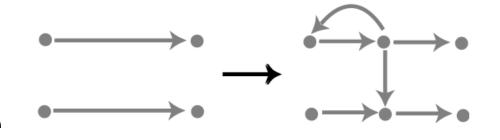


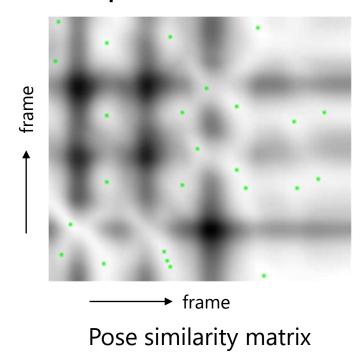


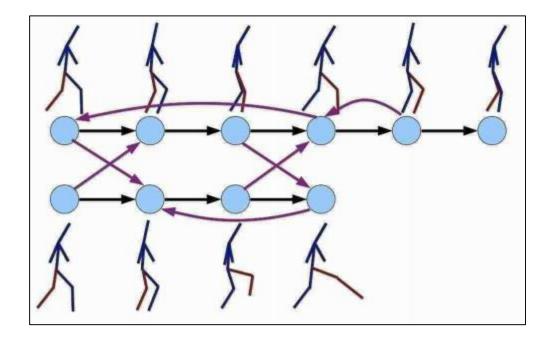


Recombining motions

 Allow transition from one motion to another if poses are similar in certain frame







Generating motion through simulation

- For creatures unsuitable for mocap
 - Too dangerous, nonexistent, ...
- Natural motion respecting body shape
- Can interact with dynamic environment

Generalizing Locomotion Style to New Animals with Inverse Optimal Regression

Kevin Wampler

Zoran Popović

Jovan Popović

(with audio)

https://www.youtube.com/watch?v=KF_a1c7zytw

Creating poses using special devices

Tangible and Modular Input Device for Character Articulation

Alec Jacobson¹

Daniele Panozzo¹

Oliver Glauser¹

Cédric Pradalier²

Otmar Hilliges¹

Olga Sorkine-Hornung¹

¹ETH Zurich ²GeorgiaTech Lorraine



This video contains narration

Many topics about character motion

Character Motion
Synthesis by
Topology Coordinates

Edmond S.L. HO and Taku Komura

School of Informatics University of Edinburgh Interaction between multiple persons

https://www.youtube.com/watch?v=1S 6wSKI nU

Synthesis of Detailed Hand Manipulations Using Contact Sampling

> Yuting Ye C. Karen Liu Georgia Institute of Technology

Grasping motion

https://www.youtube.com/
watch?v=x8c27XYTLTo

Aggregate Dynamics for Dense Crowd Simulation

Submission 0042

Crowd simulation

https://www.youtube.com/watch?v=pqBSNAOsMDc

Space-Time Planning with Parameterized Locomotion Controllers

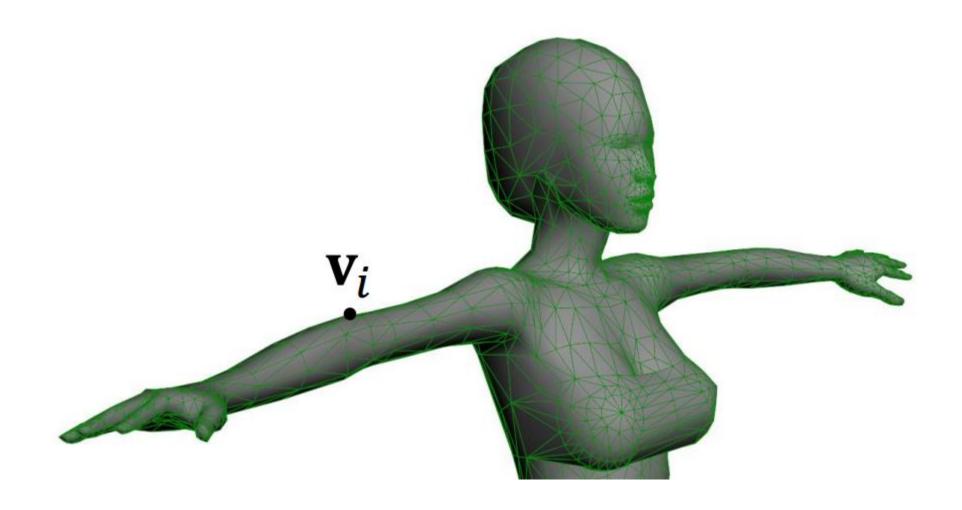
Sergey Levine Vongjoon Lee Vladlen Koltun Zoran Popović
Stanford University University of Washington

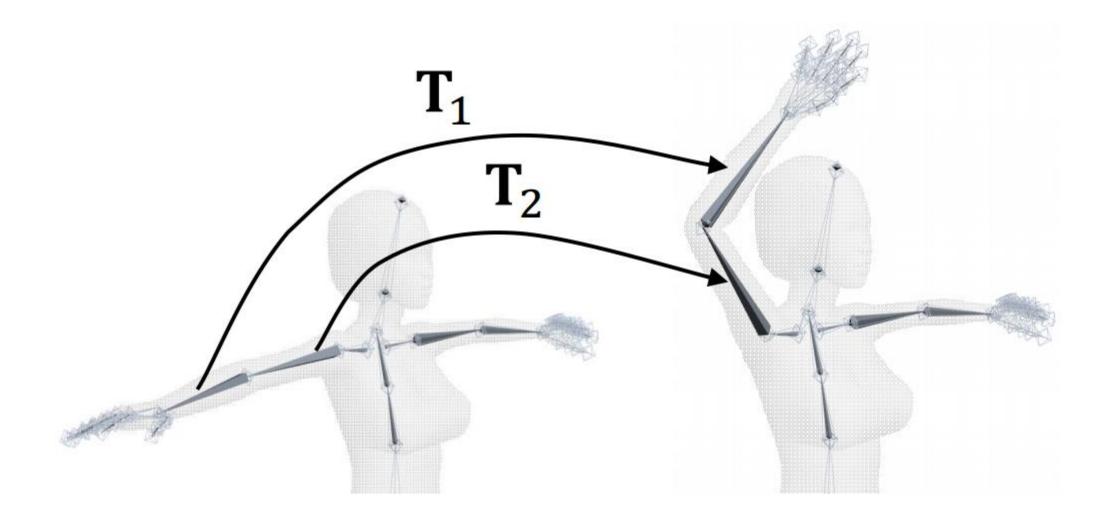
Path planning

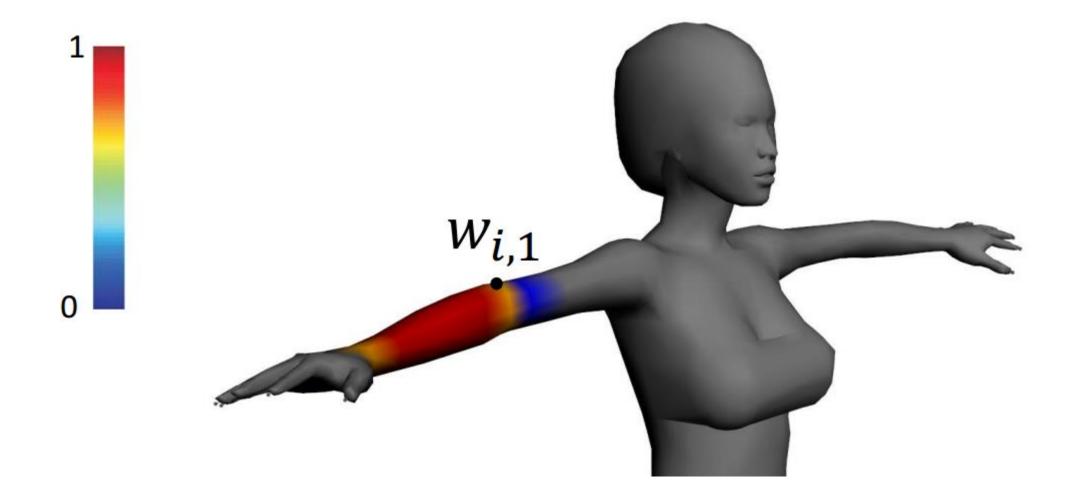
https://vimeo.com/33409868

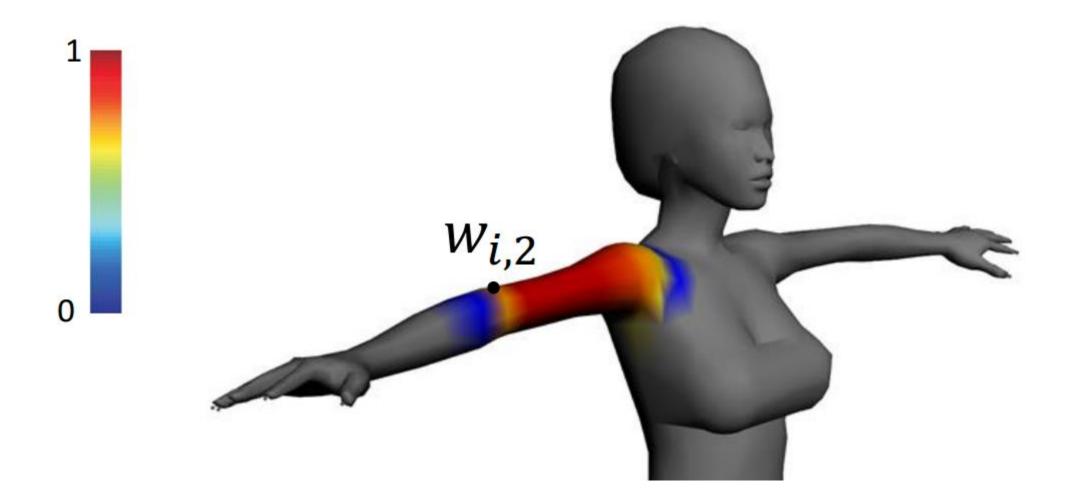
Character motion synthesis by topology coordinates [Ho EG09]
Aggregate Dynamics for Dense Crowd Simulation [Narain SIGGRAPHAsia09]
Synthesis of Detailed Hand Manipulations Using Contact Sampling [Ye SIGGRAPH12]
Space-Time Planning with Parameterized Locomotion Controllers.[Levine TOG11]

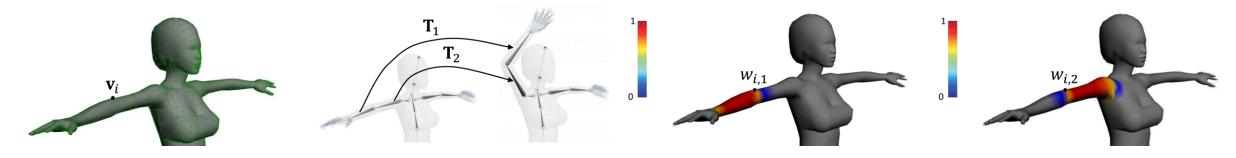
Skinning











$$\mathbf{v}_i' = \mathrm{blend}(\langle w_{i,1}, \mathbf{T}_1 \rangle, \langle w_{i,2}, \mathbf{T}_2 \rangle, \dots)(\mathbf{v}_i)$$

- Input
 - Vertex positions
 - Transformation per bone
 - Weight from each bone to each vertex

$$\{\mathbf{v}_i\} \ i = 1, ..., n$$

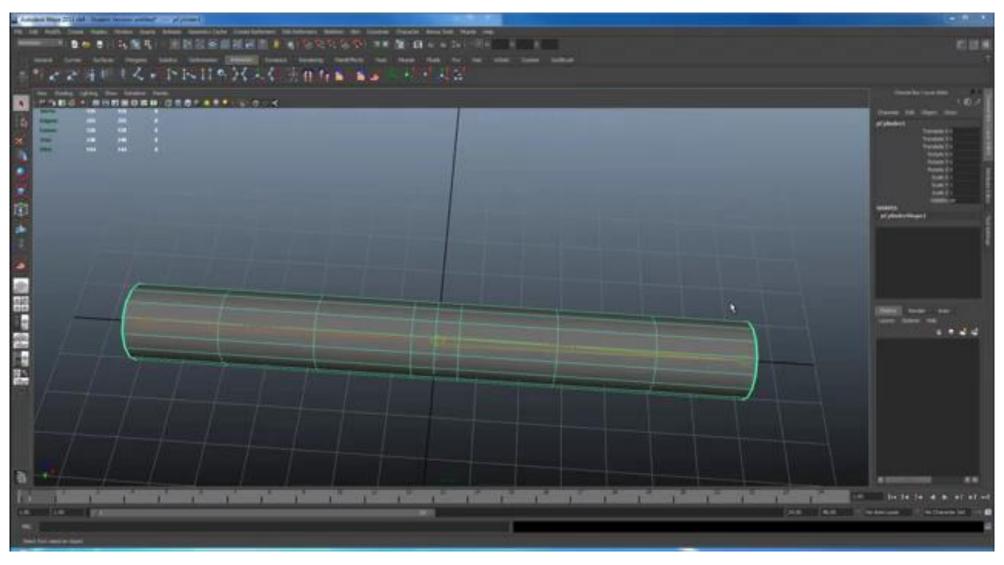
 $\{\mathbf{T}_j\} \ j = 1, ..., m$
 $\{w_{i,j}\} \ i = 1, ..., n \ j = 1, ..., m$

- Output
 - Vertex positions after deformation

$$\{\mathbf{v}_i'\}\ i=1,...,n$$

- Main focus
 - How to define weights $\{w_{i,j}\}$
 - How to blend transformations

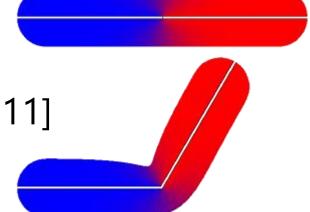
Simple way to define weights: painting



Automatic weight computation

• Define weight w_j as a smooth scalar field that takes 1 on the j-th bone and 0 on the other bones

- Minimize 1st-order derivative $\int_{\Omega} \|\nabla w_j\|^2 dA$ [Baran 07]
 - Approximate solution only on surface → easy & fast
- Minimize 2nd-order derivative $\int_{\Omega} (\Delta w_j)^2 dA$ [Jacobson 11]
 - Introduce inequality constraints $0 \le w_j \le 1$
 - Quadratic Programming over the volume → high-quality



Simple way to blend transformations: Linear **B**lend **S**kinning

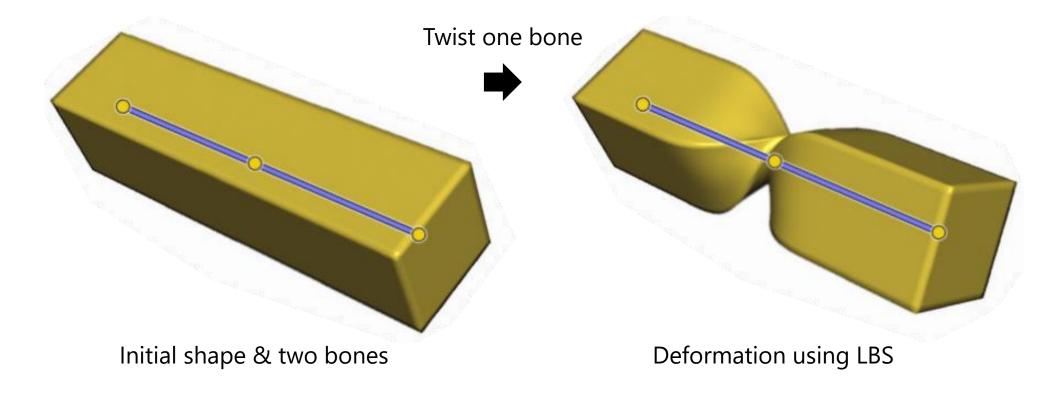
• Represent rigid transformation \mathbf{T}_j as a 3×4 matrix consisting of rotation matrix $\mathbf{R}_j \in \mathbb{R}^{3\times3}$ and translation vector $\mathbf{t}_j \in \mathbb{R}^3$

$$\mathbf{v}_i' = \left(\sum_j w_{i,j}(\mathbf{R}_j \ \mathbf{t}_j)\right) \begin{pmatrix} \mathbf{v}_i \\ 1 \end{pmatrix}$$

- Simple and fast
 - Implemented using vertex shader: send $\{\mathbf{v}_i\}$ & $\{w_{i,j}\}$ to GPU at initialization, send $\{\mathbf{T}_i\}$ to GPU at each frame

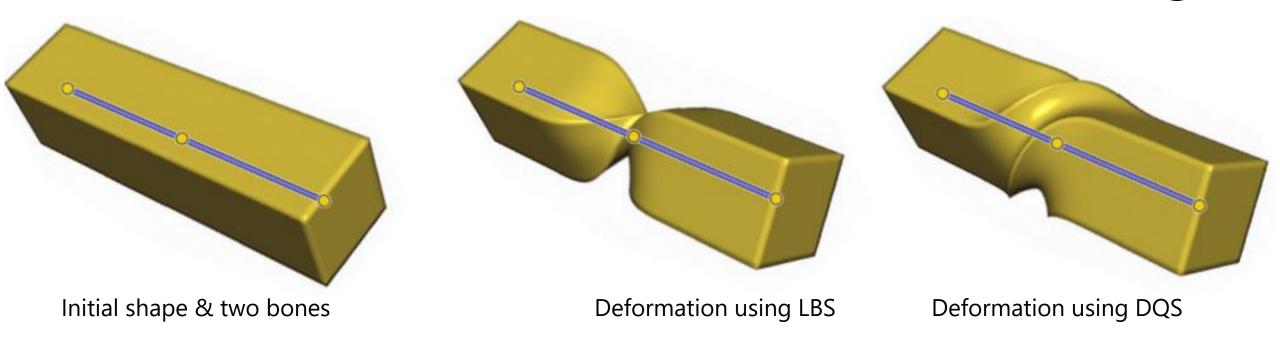
Standard method

Artifact of LBS: "candy wrapper" effect



- Linear combination of rigid transformation is not a rigid transformation!
 - Points around joint concentrate when twisted

Alternative to LBS: Dual Quaternion Skinning



- Idea
 - Quaternion (four numbers) → 3D rotation
 - Dual quaternion (two quaternions) → 3D rigid motion (rotation + translation)

Dual number & dual quaternion

- Dual number
 - Introduce dual unit ε & its arithmetic rule $\varepsilon^2 = 0$ (cf. imaginary unit i)
 - Dual number is sum of primal & dual components:

$$\hat{a} \coloneqq a_0 + \varepsilon a_{\varepsilon}$$

• Dual conjugate:

$$\bar{\hat{a}} = \overline{a_0 + \varepsilon a_{\varepsilon}} = a_0 - \varepsilon a_{\varepsilon}$$

$$a_0, a_{\varepsilon} \in \mathbb{R}$$

- Dual quaternion
 - Quaternion whose elements are dual numbers
 - Can be written using two quaternions

$$\widehat{\mathbf{q}} \coloneqq \mathbf{q}_0 + \varepsilon \mathbf{q}_{\varepsilon}$$

• Dual conjugate:
$$\overline{\widehat{\mathbf{q}}} = \overline{\mathbf{q}_0 + \varepsilon \mathbf{q}_\varepsilon} = \mathbf{q}_0 - \varepsilon \mathbf{q}_\varepsilon$$

• Quaternion conjugate:
$$\hat{\mathbf{q}}^* = (\mathbf{q}_0 + \varepsilon \mathbf{q}_{\varepsilon})^* = \mathbf{q}_0^* + \varepsilon \mathbf{q}_{\varepsilon}^*$$

Arithmetic rules for dual number/quaternion

- For dual number $\hat{a} = a_0 + \varepsilon a_{\varepsilon}$:
 - Reciprocal

$$\frac{1}{\hat{a}} = \frac{1}{a_0} - \varepsilon \frac{a_\varepsilon}{a_0^2}$$

Square root

$$\sqrt{\hat{a}} = \sqrt{a_0} + \varepsilon \frac{a_{\varepsilon}}{2\sqrt{a_0}}$$

• Trigonometric

$$\sin \hat{a} = \sin a_0 + \varepsilon a_{\varepsilon} \cos a_0$$

$$\cos \hat{a} = \cos a_0 - \varepsilon a_{\varepsilon} \sin a_0$$

Easily derived by combining usual arithmetic rules with new rule $\varepsilon^2=0$

From Taylor expansion

• For dual quaternion $\hat{\mathbf{q}} = \mathbf{q}_0 + \varepsilon \mathbf{q}_{\varepsilon}$:

$$\|\widehat{\mathbf{q}}\| = \sqrt{\widehat{\mathbf{q}}^* \widehat{\mathbf{q}}} = \|\mathbf{q}_0\| + \varepsilon \frac{\langle \mathbf{q}_0, \mathbf{q}_{\varepsilon} \rangle}{\|\mathbf{q}_0\|}$$

Inverse

$$\widehat{\mathbf{q}}^{-1} = \frac{\widehat{\mathbf{q}}^*}{\|\widehat{\mathbf{q}}\|^2}$$

• Unit dual quaternion satisfies $\|\widehat{\mathbf{q}}\| = 1$

•
$$\Leftrightarrow$$
 $\|\mathbf{q}_0\| = 1 \& \langle \mathbf{q}_0, \mathbf{q}_{\varepsilon} \rangle = 0$

Dot product as 4D vectors

Rigid transformation using dual quaternion

• Unit dual quaternion representing rigid motion of translation $\vec{\mathbf{t}} = (t_x, t_y, t_z)$ and rotation \mathbf{q}_0 (unit quaternion):

$$\widehat{\mathbf{q}} = \mathbf{q}_0 + \frac{\varepsilon}{2} \vec{\mathbf{t}} \mathbf{q}_0$$

Note: 3D vector is considered as quaternion with zero real part

• Rigid transformation of 3D position $\vec{\mathbf{v}} = (v_x, v_y, v_z)$ using unit dual quaternion $\hat{\mathbf{q}}$:

$$\widehat{\mathbf{q}}(1+\varepsilon\overrightarrow{\mathbf{v}})\overline{\widehat{\mathbf{q}}^*}=1+\varepsilon\overrightarrow{\mathbf{v}'}$$

• $\overrightarrow{\mathbf{v}'}$: 3D position after transformation

Rigid transformation using dual quaternion

•
$$\widehat{\mathbf{q}} = \mathbf{q}_0 + \frac{\varepsilon}{2} \overrightarrow{\mathbf{t}} \mathbf{q}_0$$

•
$$\hat{\mathbf{q}}(1 + \varepsilon \vec{\mathbf{v}})\overline{\hat{\mathbf{q}}^*} = \left(\mathbf{q}_0 + \frac{\varepsilon}{2}\vec{\mathbf{t}}\mathbf{q}_0\right)(1 + \varepsilon \vec{\mathbf{v}})\left(\mathbf{q}_0^* + \frac{\varepsilon}{2}\mathbf{q}_0^*\vec{\mathbf{t}}\right)$$

$$= \left(\mathbf{q}_0 + \frac{\varepsilon}{2}\vec{\mathbf{t}}\mathbf{q}_0\right)\left(\mathbf{q}_0^* + \varepsilon \vec{\mathbf{v}}\mathbf{q}_0^* + \frac{\varepsilon}{2}\mathbf{q}_0^*\vec{\mathbf{t}}\right)$$

$$= \mathbf{q}_0\mathbf{q}_0^* + \frac{\varepsilon}{2}\vec{\mathbf{t}}\mathbf{q}_0\mathbf{q}_0^* + \varepsilon \mathbf{q}_0\vec{\mathbf{v}}\mathbf{q}_0^* + \frac{\varepsilon}{2}\mathbf{q}_0\mathbf{q}_0^*\vec{\mathbf{t}}$$

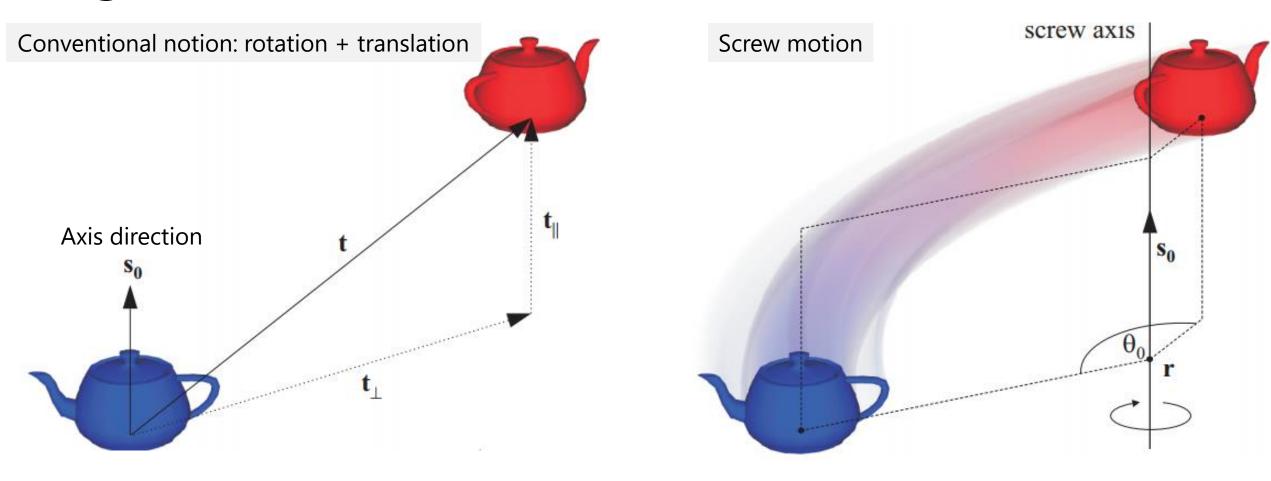
$$= 1 + \varepsilon(\vec{\mathbf{t}} + \mathbf{q}_0\vec{\mathbf{v}}\mathbf{q}_0^*)$$

3D position $\vec{\mathbf{v}}$ rotated by quaternion \mathbf{q}_0

$$((0+\vec{\mathbf{t}})\mathbf{q}_0)^* = \mathbf{q}_0^*(0+\vec{\mathbf{t}})^*$$
$$= -\mathbf{q}_0^*\vec{\mathbf{t}}$$

$$\|\mathbf{q}_0\|^2 = 1$$

Rigid transformation as "screw motion"



- Any rigid motion is uniquely described as screw motion
 - (Up to antipodality)

Screw motion & dual quaternion

• Unit dual quaternion $\hat{\mathbf{q}}$ can be written as:

$$\widehat{\mathbf{q}} = \cos\frac{\widehat{\theta}}{2} + \widehat{\mathbf{s}}\sin\frac{\widehat{\theta}}{2}$$

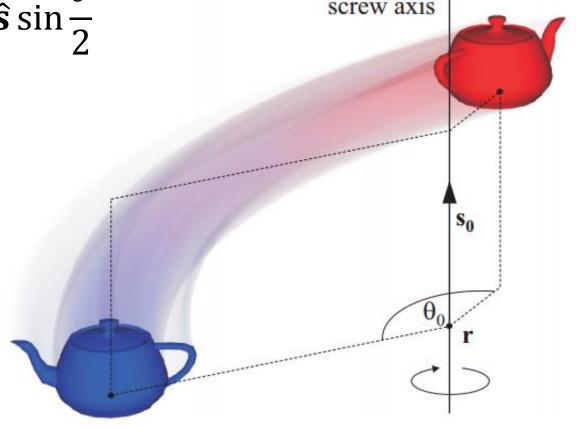
•
$$\hat{\theta} = \theta_0 + \varepsilon \theta_{\varepsilon}$$

•
$$\hat{\mathbf{s}} = \overrightarrow{\mathbf{s}_0} + \varepsilon \overrightarrow{\mathbf{s}_\varepsilon}$$

$$\theta_0, \theta_{\varepsilon}$$
 : real number

$$\overrightarrow{\mathbf{s}_0}$$
, $\overrightarrow{\mathbf{s}_{\varepsilon}}$: unit 3D vector

- Geometric meaning
 - $\overrightarrow{s_0}$: direction of rotation axis
 - θ_0 : amount of rotation
 - θ_{ε} : amount of translation parallel to $\overrightarrow{\mathbf{s}_0}$
 - $\overrightarrow{\mathbf{s}_{\varepsilon}}$: when rotation axis passes through $\overrightarrow{\mathbf{r}}$, it satisfies $\overrightarrow{\mathbf{s}_{\varepsilon}} = \overrightarrow{\mathbf{r}} \times \overrightarrow{\mathbf{s}_{0}}$



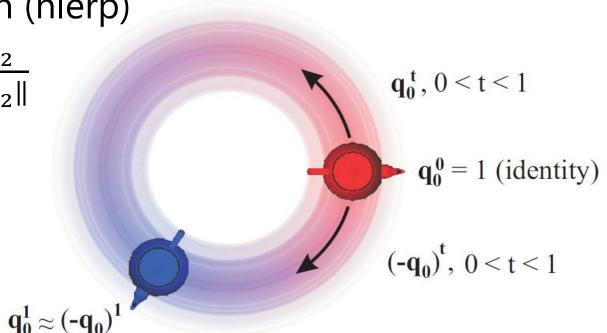
Interpolating two rigid transformations

Linear interpolation + normalization (nlerp)

nlerp(
$$\widehat{\mathbf{q}}_1$$
, $\widehat{\mathbf{q}}_2$, t) :=
$$\frac{(1-t)\widehat{\mathbf{q}}_1 + t\widehat{\mathbf{q}}_2}{\|(1-t)\widehat{\mathbf{q}}_1 + t\widehat{\mathbf{q}}_2\|}$$

• Note: $\hat{\mathbf{q}} & -\hat{\mathbf{q}}$ represent same transformation with opposite path

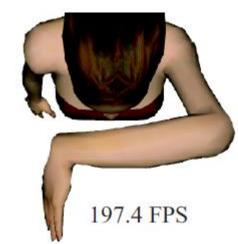
• If 4D dot product of non-dual components of $\hat{\mathbf{q}}_1$ & $\hat{\mathbf{q}}_2$ is negative, use $-\hat{\mathbf{q}}_2$ in the interpolation



Blending rigid motions using dual quaternion

blend(
$$\langle w_1, \widehat{\mathbf{q}}_1 \rangle$$
, $\langle w_2, \widehat{\mathbf{q}}_2 \rangle$, ...) :=
$$\frac{w_1 \widehat{\mathbf{q}}_1 + w_2 \widehat{\mathbf{q}}_2 + \cdots}{\|w_1 \widehat{\mathbf{q}}_1 + w_2 \widehat{\mathbf{q}}_2 + \cdots\|}$$

- Akin to blending rotations using quaternion
- Same input format as LBS & low computational cost
- Standard feature in many commercial CG packages

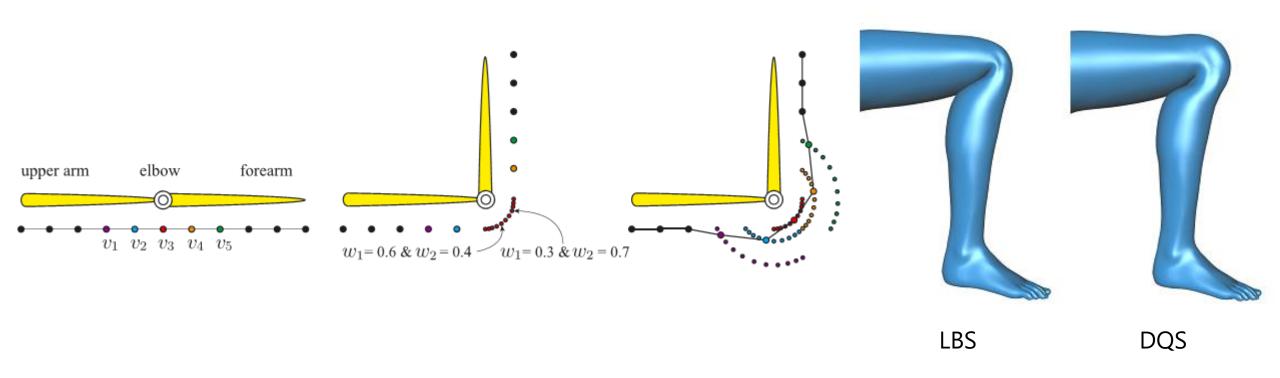




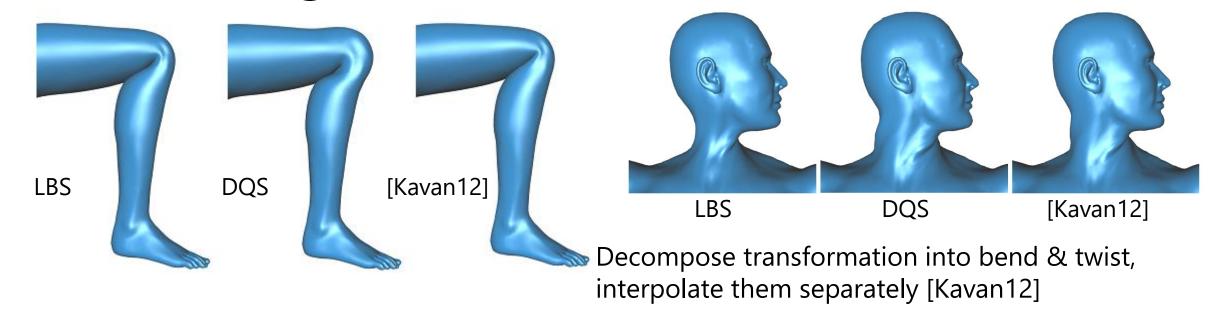
122 FPS

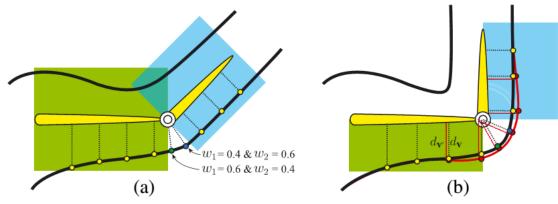
Artifact of DQS: "bulging" effect

Produces ball-like shape around the joint when bended



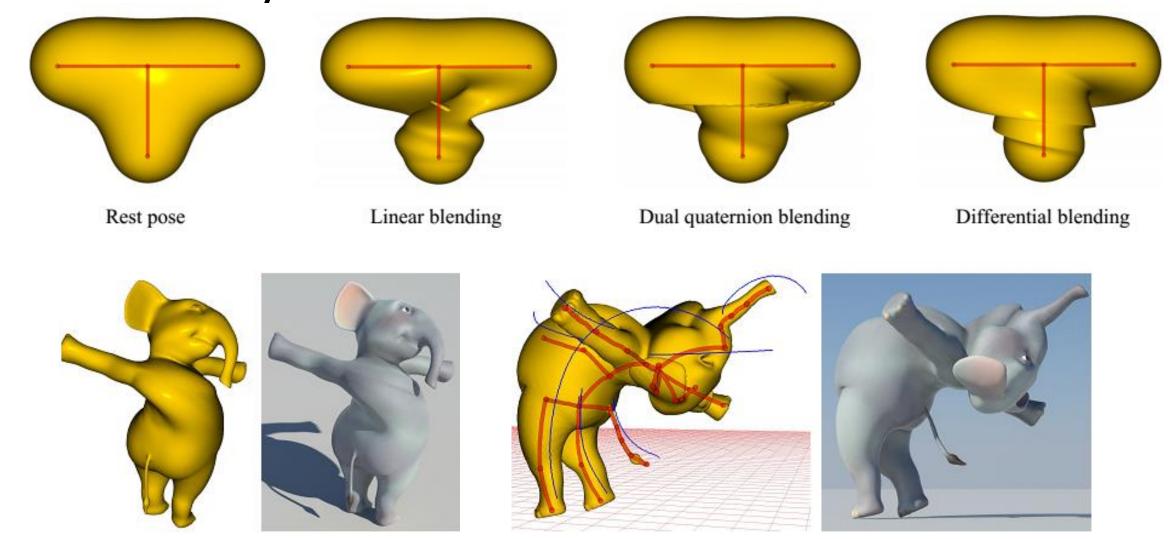
Overcoming DQS's drawback





After deforming using DQS, offset vertices along normals [Kim14]

Limitation of DQS: Cannot represent rotation by more than 360°



Skinning for avoiding self-intersections

Make use of implicit functions

Implicit Skinning:

Real-Time Deformation with Contact Modeling

Siggraph 2013

Rodolphe Vaillant (1,2), Loïc Barthe (1), Gaël Guennebaud (3), Marie-Paule Cani (4), Damien Rohmer (5), Brian Wyvill (6), Olivier Gourmel (1), Mathias Paulin (1)

(1) IRIT - Université de Toulouse, (2) University of Victoria, (3) Inria Bordeaux, (4) LJK - Grenoble Universités - Inria, (5) CPE Lyon - Inria, (6) University of Bath

This video contains narration

Other deformation mechanisms than skinning

Unified point/cage/skeleton handles [Jacobson 11]

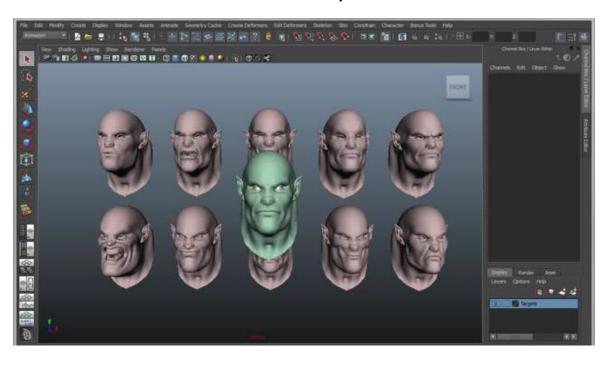
Bounded Biharmonic Weights for Real-Time Deformation

Alec Jacobson¹ Ilya Baran² Jovan Popović³ Olga Sorkine^{1,4}

¹New York University ²Disney Research, Zurich ³Adobe Systems, Inc. ⁴ETH Zurich

This video contains narration

BlendShape



https://www.youtube.com/watch?v=P9fqm8vgdB8

https://www.youtube.com/watch?v=BFPAIU8hwQ4

References

- http://en.wikipedia.org/wiki/Motion_capture
- http://skinning.org/
- http://mukai-lab.org/category/library/legacy