

Replicate Heathcote and Perri (2002)

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This exercise replicates the work of Heathcote and Perri (2002). All data, python, dynare and L^AT_EX files are pushed to <https://github.com/ryanlhxu/TestEcon/tree/master/dsge>

1 Model

1.1 Environment

- Two countries with identical and infinitely lived household. The preference of Household is

$$U(c_i(s^t), 1 - n_i(s^t)) = \frac{1}{\gamma} [c_i^\mu(s^t)(1 - n_i(s^t))^{1-\mu}]^\gamma \quad (1)$$

- The probability of any state $s^t \in S$ is $\pi(s^t)$, and

$$z(s^t) = Az(s^{t-1}) + \varepsilon(s^t) \quad (2)$$

where A is a 2×2 matrix.

- The I -firms (intermediate-goods-producing) in country 1 produce one good called a , while those in country 2 produce a different good called b . The technology is

$$F(z_i(s^t), k_i(s^t), n_i(s^t)) = e^{z_i(s^t)} k_i^\theta(s^t) n_i^{1-\theta}(s^t) \quad (3)$$

- The F -firms (final-goods-producing) buy intermediate goods to produce final goods. The technology is

$$G(a_i(s^t), b_i(s^t)) = \begin{cases} [\omega_1 a_i(s^t)^{(\sigma-1)/\sigma} + (1 - \omega_1) b_i(s^t)^{(\sigma-1)/\sigma}]^{\sigma/(\sigma-1)}, & i = 1 \\ [(1 - \omega_1) a_i(s^t)^{(\sigma-1)/\sigma} + \omega_1 b_i(s^t)^{(\sigma-1)/\sigma}]^{\sigma/(\sigma-1)}, & i = 2 \end{cases} \quad (4)$$

with $\omega > 0.5$ determines the home bias.

- Firms are competitive and market are complete.

1.2 Household's problem

The household in country i maximize the expected discounted sum of future period utilities at data 0.

$$\begin{aligned} \max_{c_i(s^t), x_i(s^t), n_i(s^t)} \quad & \sum_{-\infty}^{\infty} \sum_{s^t} \pi(s^t) \beta^t U(c_i(s^t), 1 - n_i(s^t)), \\ \text{subject to} \quad & c_i(s^t) + x_i(s^t) + q_i^a(s^t) \sum_{s_{t+1}} Q(s^t, s_{t+1}) B_i(s^t, s_{t+1}) \\ & = q_i^a(s^t) (w_i(s^t) n_i(s^t) - r_i(s^t) k_i(s^t)) + q_i^a(s^t) B_i(s^{t-1}, s_t) \end{aligned}$$

1.3 I -firms' problem

$$\begin{aligned} \max_{k_i(s^t), n_i(s^t)} \quad & \{F(z_i(s^t), k_i(s^t), n_i(s^t)) - w_i(s^t) n_i(s^t) - r_i(s^t) k_i(s^t)\} \\ \text{subject to} \quad & k_i(s^t), n_i(s^t) \geq 0 \end{aligned}$$

Investment augments the capital stock in the standard way:

$$k_i(s^{t+1}) = (1 - \delta) k_i(s^t) + x_i(s^t) \quad (5)$$

1.4 F -firms' problem

$$\begin{aligned} \max_{a_i(s^t), b_i(s^t)} \quad & \{G_i(a_i(s^t), b_i(s^t)) - q_i^a(s^t) a_i(s^t) - q_i^b(s^t) b_i(s^t)\} \\ \text{subject to} \quad & a_i(s^t), b_i(s^t) \geq 0, \end{aligned}$$

where $q_i^a(s^t), q_i^b(s^t)$ are prices of goods a and b in country i in units of final good produced in country i .

1.5 Equilibrium

An equilibrium is a set of prices for all s^t and for all $t \geq 0$ such that when household solve their problems taking these prices as given and all market clear.

Market clearing conditions:

- Goods a and b market

$$a_1(s^t) + a_2(s^t) = F(z_1(s^t), k_1(s^t), n_1(s^t)) \quad (6)$$

$$b_1(s^t) + b_2(s^t) = F(z_2(s^t), k_2(s^t), n_2(s^t)) \quad (7)$$

- Final goods market

$$c_i(s^t) + x_i(s^t) = G_i(a_i(s^t), b_i(s^t)), \quad i = 1, 2 \quad (8)$$

- Bond market

$$B_1(s^t, s_{t+1}) + B_2(s^t, s_{t+1}) = 0, \quad \forall s_{t+1} \in S \quad (9)$$

1.6 Additional Variables

Gross domestic product in country i ,

$$y_i(s^t) = q_i^a(s^t)F(z_i(s^t), k_i(s^t), n_i(s^t)) \quad (10)$$

Netexports for country 1 as a fraction of GDP for country 1,

$$nx(s^t) = \frac{q_1^a a_2(s^t) - q_1^b(s^t) b_1(s^t)}{y_i(s^t)} \quad (11)$$

Ratio of imports to non-traded domestic intermediate good production measured at base year prices,

$$ir(s^t) = \frac{\bar{q}b_1(s^t)}{\bar{q}a_1(s^t)} = \frac{b_1(s^t)}{a_1(s^t)} \quad (12)$$

Terms of trade,

$$p_i(s^t) = \frac{q_i^b(s^t)}{q_i^a(s^t)} = \frac{\omega_2}{\omega_1} ir(s^t)^{-1/\sigma}, \quad i = 1, 2 \quad (13)$$

The real exchange rate,

$$rx(s^t) = \frac{q_1^a(s^t)}{q_2^a(s^t)} = \frac{q_1^b(s^t)}{q_2^b(s^t)} \quad (14)$$

2 Computation: Complete Market

We can easily show that in the **decentralized economy**, the prices are,

$$r_1(s^t) = F_{1k}(s^t) \quad (15)$$

$$r_2(s^t) = F_{2k}(s^t) \quad (16)$$

$$w_1(s^t) = F_{1n}(s^t) \quad (17)$$

$$w_2(s^t) = F_{2n}(s^t) \quad (18)$$

$$q_1^a(s^t) = G_{1a}(s^t) \quad (19)$$

$$q_1^b(s^t) = G_{1b}(s^t) \quad (20)$$

$$q_2^a(s^t) = G_{2a}(s^t) \quad (21)$$

$$q_2^b(s^t) = G_{2b}(s^t) \quad (22)$$

```

1 // wage
2 w_1 = (1-theta)*f_1/n_1;
3 w_2 = (1-theta)*f_2/n_2;
4
5 // interest rate
6 r_1 = theta*f_1/k_1(-1);
7 r_2 = theta*f_2/k_2(-1);
8
9 // intermediate good pricing
10 qa_1 = omega*a_1^(rho-1)*((omega*a_1^rho+(1-omega)*b_1^rho)^(1/rho-1));
11 qb_1 = (1-omega)*b_1^(rho-1)*((omega*a_1^rho+(1-omega)*b_1^rho)^(1/rho-1));
12 qa_2 = (1-omega)*a_2^(rho-1)*(((1-omega)*a_2^rho+omega*b_2^rho)^(1/rho-1));
13 qb_2 = omega*b_2^(rho-1)*(((1-omega)*a_2^rho+omega*b_2^rho)^(1/rho-1));

```

Since **complete market** of the decentralized economy is equivalent to social planner's problem, we solve the **centralized problem** such that we could get rid of the financial market to avoid complexity.

Since the two countries are symmetric, we set the P.O weight to 1/2.

$$\max_{c_i, k_i, n_i, a_i, b_i} \sum_{i \in 1,2} \frac{1}{2} \sum_{-\infty}^{\infty} \sum_{s^t} \pi(s^t) \beta^t U(c_i(s^t), 1 - n_i(s^t)), \quad (23)$$

$$\text{subject to} \quad a_1(s^t) + a_2(s^t) = F(z_1(s^t), k_1(s^t), n_1(s^t)) \quad (24)$$

$$b_1(s^t) + b_2(s^t) = F(z_2(s^t), k_2(s^t), n_2(s^t)) \quad (25)$$

$$c_1(s^t) + x_1(s^t) = G_1(a_1(s^t), b_1(s^t)) \quad (26)$$

$$c_2(s^t) + x_2(s^t) = G_2(a_2(s^t), b_2(s^t)) \quad (27)$$

$$(1 - \delta)k_1(s^t) + x_1(s^t) = k_1(s^{t+1}) \quad (28)$$

$$(1 - \delta)k_2(s^t) + x_2(s^t) = k_2(s^{t+1}) \quad (29)$$

```

1 //output
2 f_1=exp(z_1)*k_1(-1)^theta*n_1^(1-theta);
3 f_2=exp(z_2)*k_2(-1)^theta*n_2^(1-theta);
4
5 //feasibale constraint
6 x_1+c_1= (omega*a_1^rho+(1-omega)*b_1^rho)^(1/rho);
7 x_2+c_2= ((1-omega)*a_2^rho+omega*b_2^rho)^(1/rho);
8
9 // capital formation
10 k_1 = x_1+(1-delta)*k_1(-1);
11 k_2 = x_2+(1-delta)*k_2(-1);
12

```

```

13 // intermediate good
14 a_1+ a_2 = f_1;
15 b_1+ b_2 = f_2;

```

Put the Lagrangian coefficients on the constraints,

$$\mathcal{L} = \sum_i 1/2 \sum_t \sum_{s^t} \pi(s^t) \beta^t \left(U_i(s^t) + \lambda_i(s^t) [G_i(s^t) - c_i(s^t) - x_i(s^t)] \right) \quad (30)$$

$$+ 1/2 \sum_t \sum_{s^t} \pi(s^t) \beta^t \left(\phi_1 [F_1(s^t) - a_1(s^t) - a_2(s^t)] + \phi_2 [F_2(s^t) - b_1(s^t) - b_2(s^t)] \right) \quad (31)$$

F.O.Cs

$a_i(s^t)$:

$$\lambda_1(s^t) G_{1a}(s^t) = \phi_1(s^t) \quad (32)$$

$$\lambda_2(s^t) G_{2a}(s^t) = \phi_1(s^t) \quad (33)$$

```

1 //F.O.C to a_i
2 lambda_1* qa_1 =lambda_2* qa_2;

```

$b_i(s^t)$:

$$\lambda_1(s^t) G_{1b}(s^t) = \phi_2(s^t) \quad (34)$$

$$\lambda_2(s^t) G_{2b}(s^t) = \phi_2(s^t) \quad (35)$$

```

1 //F.O.C to b_i
2 lambda_1* qb_1 =lambda_2* qb_2;

```

$c_i(s^t)$:

$$U_{1c}(s^t) = \lambda_1(s^t) \quad (36)$$

$$U_{2c}(s^t) = \lambda_2(s^t) \quad (37)$$

```

1 // F.O.C. to consumption: Lagrangian
2 lambda_1 = mu*((c_1^mu*(1-n_1)^(1-mu))^gamma)/c_1;
3 lambda_2 = mu*((c_2^mu*(1-n_2)^(1-mu))^gamma)/c_2;

```

$n_i(s^t)$:

$$U_{1n}(s^t) = \phi_1(s^t) F_{1n}(s^t) \quad (38)$$

$$U_{2n}(s^t) = \phi_2(s^t) F_{2n}(s^t) \quad (39)$$

```

1 // F.O.C to labor
2 (1-mu)*((c_1^mu*(1-n_1)^(1-mu))^gamma)/(1-n_1) = (lambda_1*qa_1)*w_1;
3 (1-mu)*((c_2^mu*(1-n_2)^(1-mu))^gamma)/(1-n_2) = (lambda_2*qb_2)*w_2;

```

$k_i(s^{t+1})$:

$$\lambda_1(s^t) = \beta \sum \pi(s^{t+1}|s^t) \left[\phi_1(s^{t+1}) F_{1k}(s^{t+1}) + (1 - \delta) \right] \quad (40)$$

$$\lambda_2(s^t) = \beta \sum \pi(s^{t+1}|s^t) \left[\phi_2(s^{t+1}) F_{2k}(s^{t+1}) + (1 - \delta) \right] \quad (41)$$

```

1 //F.O.C to capital
2 beta*lambda_1(1)*(qa_1(1) * r_1(1)+1-delta)=lambda_1;
3 beta*lambda_2(1)*(qb_2(1) * r_2(1)+1-delta)=lambda_2;

```

3 Result

3.1 Filter

First, we use the U.S. data to do the HP filter. The database is downloaded from Perri's website.¹ As an example, the filter result of $\log GDP$ is shown in figure (3.3). We report all the result in table (1).

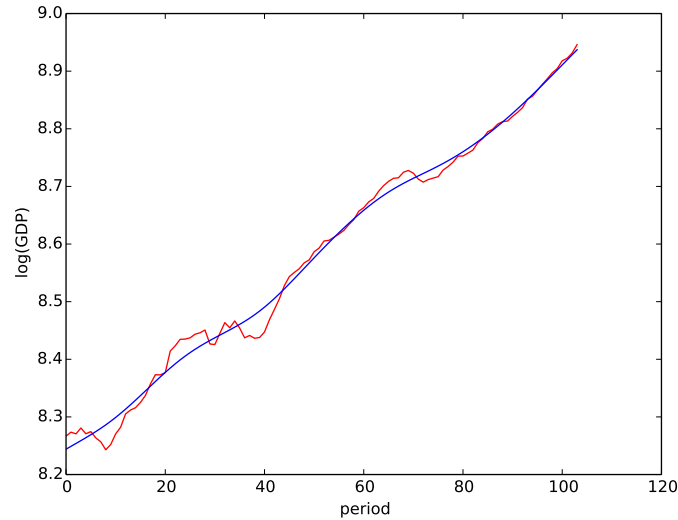


Figure 1: $\log GDP$

¹http://fperri.net/research_data.htm

Table 1: Result

Volatilities	% std. dev.	% std. dev % std. dev of y				% std. dev.			
Economy	y	c	x	n	ex	im	nx	ir	
US data	1.67	0.81	2.84	0.66	3.90	5.40	0.45	/	
Complete markets	1.11	0.55	2.95	0.33	0.75	0.91	0.19	0.72	
Correlation									
Economy	c, y	x, y	n, y	ex, y	im, y	nx, y	p, y	rx, y	
US data	0.87	0.95	0.87	0.32	0.82	-0.49	-0.24	0.13	
Complete markets	0.97	0.97	0.97	0.71	0.95	-0.77	0.77	0.77	
Cross country correlation									
	correlation between				% std. dev.				
Economy	y_1, y_2	c_1, c_2	x_1, x_2	n_1, n_2	p	rx			
US data	0.58	0.36	0.30	0.43	3.00	3.72			
Complete markets	0.43	0.73	-0.33	-0.04	0.68	0.45			

3.2 Solve the Model

The results of our simulations under the benchmark parameterization are summarized in table (1).

The model predicts correlations in consumption exceeding those in production whereas the reverse is true in data. Moreover the model fails to predict a strong cross-country output correlation. In the data, investment and employment both tend to be positively correlated across countries. However, in the model, both these correlations are negative.

The model generates too little volatility in trade quantities and international relative prices. Besides, in the data, net exports are counter-cyclical because imports are more strongly procyclical than exports. The complete markets model reproduces these features.

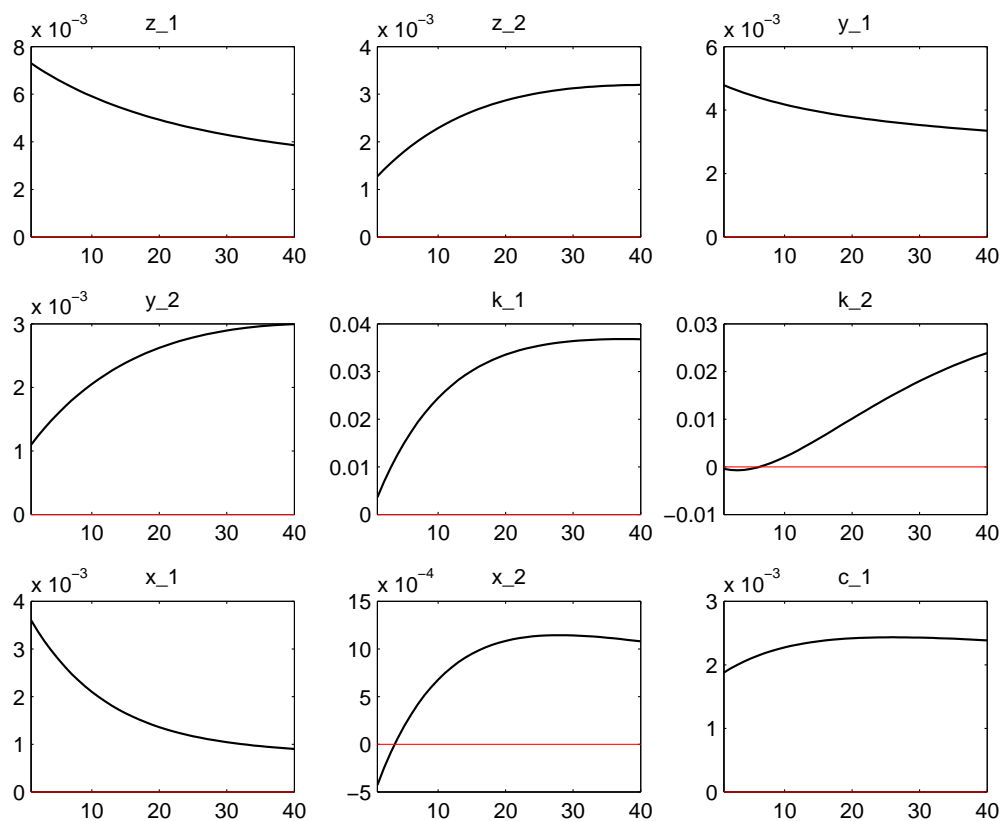
3.3 Impulse Function

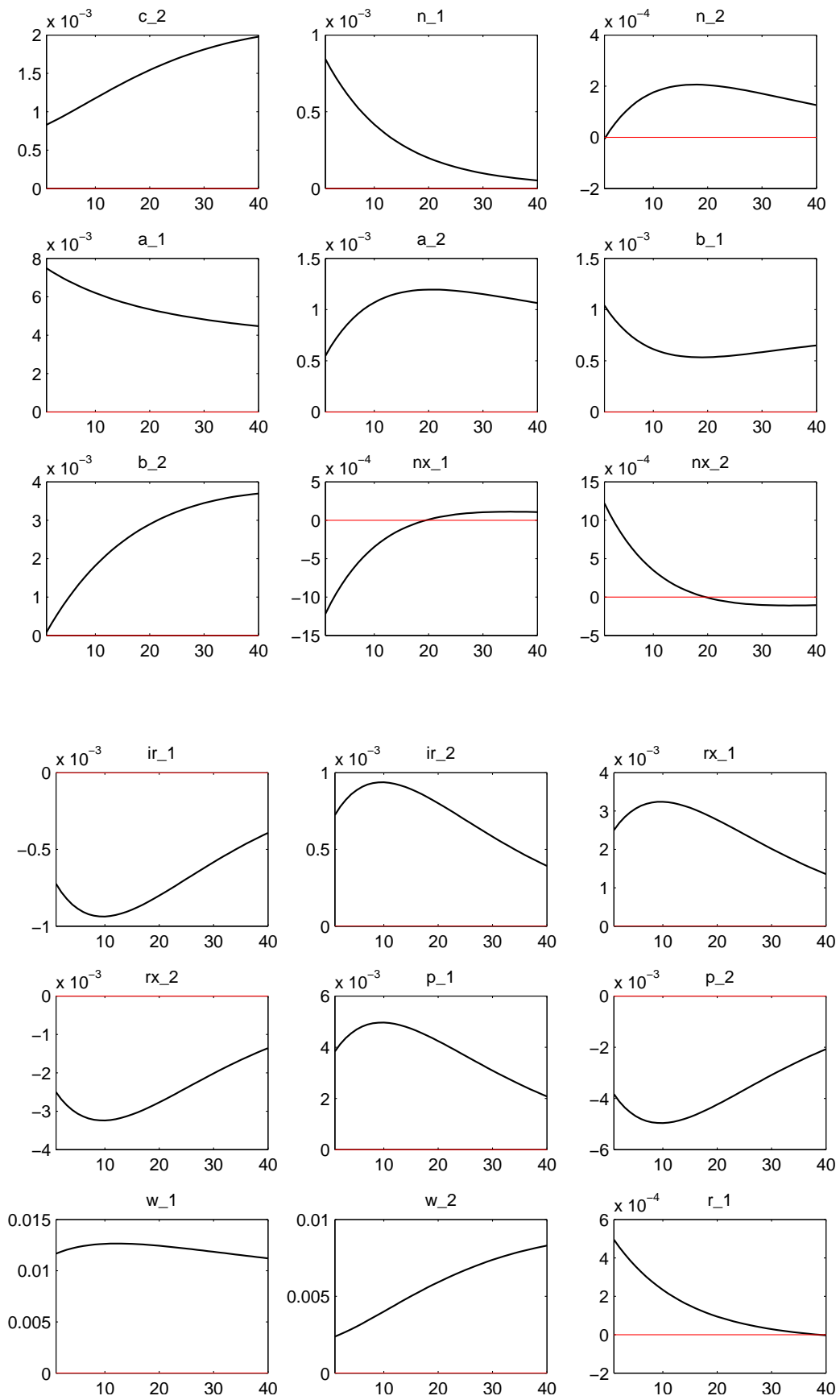
When markets are complete, a positive productivity shock in country 1 leads to an increase in domestic investment and output, and a fall in foreign investment and output. Since country-specific risks are perfectly insured, consumption rises in both countries. However, the increase in domestic investment is larger than the increase in foreign consumption, and country 1's trade

deficit widens. Backus, Kehoe and Kydland describe these responses as a tendency to “make hay where the sun shines” (BKK, 1995, p.340), meaning that a trade deficit is the result of shifting resources to invest in the temporarily more productive location.

The increase in the real wage in country 1 following the productivity increase induces households there to increase labor supply, while in country 2 the positive wealth effect of the shock leads to a reduction in labor supply. Lower labor supply implies lower output, and the increase in consumption in country 2 therefore requires a reduction in investment. The fact that investment and employment move in opposite directions following a shock explains why in a simulation the cross-country correlations in employment and investment are negative, and why the correlation in output is less than the correlation in productivity.

As the productivity shock decays, the productivity gap between the two countries narrows given spill-overs in the law of motion for z : After some date country 2 runs a deficit to permit replacement of its depleted capital stock.





3.4 Robustness Check: Home Bias

	$\omega = 0.5$	$\omega = 0.75$	$\omega = 0.9$	Benchmark
$corr(y_1, y_2) - corr(c_1, c_2)$				
Data	0.22			
Complete market	-0.01	-0.16	-0.36	-0.30
$corr(x_1, x_2)$				
Data	0.30			
Complete market	0.16	-0.35	-0.30	-0.33
% std. dev. terms of trade (p)				
Data	3.00			
Complete market	1.00	0.81	0.62	0.68

Appendix

A HP Filter: Python Code

```

1 import os
2 import numpy as np
3 import matplotlib.pyplot as plt
4 import math
5
6 # HP filter of the data
7 # database is downloaded from perri's website
8
9 # set the working directory
10 os.chdir("/home/xuliheng/github/TestEcon/dsge")
11 os.getcwd()
12
13 # read csv data and convert it to ndarray
14 data_type="|S6, "<f8, "<f8"
15 data =np.genfromtxt('data.csv', dtype=data_type, delimiter=',', names=True)
16 print data.dtype.names
17 # GDP data
18 gdp = [math.log(i) for i in data["GDP"]]
19

```

```

20 # HP filter of GDP
21 import statsmodels.api as sm
22 gdp_cycle, gdp_trend = sm.tsa.filters.hpfilter(gdp,1600)
23 '''
24 plt.plot(gdp,'-r')
25 plt.plot(gdp_trend,'-b')
26 plt.xlabel('period')
27 plt.ylabel('log(GDP)')
28 plt.show()
29 '''
30 # std of GDP
31 gdp_std = np.std(gdp_cycle)
32 print gdp_std
33 # filter of other variables
34 var_std = {}
35 var_std["GDP"] = gdp_std
36 var_corr = {}
37 # filter of other variables
38 for i in range(2,12):
39     var_name = data.dtype.names[i]
40     if var_name != "Net_Exports":
41         var = [math.log(j) for j in data[var_name]]
42     else:
43         var = data[var_name]
44     #debug
45     #if i==2:
46     #    print var_name
47     var_cycle, var_trend = sm.tsa.filters.hpfilter(var,1600)
48     var_corr[var_name] = np.corrcoef(gdp_cycle, var_cycle)[0][1]
49     if var_name in ["Total_C", "GFCF", "Civilian_Emp"]:
50         var_std[var_name] = np.std(var_cycle)/gdp_std
51         #if i==2:
52         #    print var_std
53     else:
54         var_std[var_name] = np.std(var_cycle)
55 print var_std
56 print var_corr
57
58 across_corr = {}
59 data2_type = " | S6, "+"<f8, "*3+"<f8"
60 data2 = np.genfromtxt('data2.csv', dtype=data2_type, delimiter=',', names=True)
61 for i in range(1,5):

```

```

62     var_name = data2.dtype.names[i]
63     var_2 = [math.log(k) for k in data2[var_name]]
64     var_1 = [math.log(k) for k in data[var_name]]
65     var_1_cycle, var_1_trend = sm.tsa.filters.hpfilter(var_1,1600)
66     var_2_cycle, var_2_trend = sm.tsa.filters.hpfilter(var_2,1600)
67     across_corr[var_name]=np.corrcoef(var_1_cycle, var_2_cycle)[0][1]
68 print across_corr

```

B The Full Dynare Code

```

1  var z_1,z_2,y_1,y_2,k_1, k_2, x_1, x_2, c_1, c_2, n_1,n_2, a_1, a_2, b_1, b_2,
    nx_1,nx_2,ir_1,ir_2,rx_1,rx_2,p_1,p_2, w_1,w_2,r_1,r_2,qa_1,qa_2,qb_1,qb_2,
    lambda_1,lambda_2,f_1,f_2,yy_1,kk_1,xx_1,cc_1,aa_1,bb_1,nn_1,rr_1,yy_2,kk_2,
    xx_2,cc_2,aa_2,bb_2,nn_2,rr_2;
2  varexo eps_1, eps_2;
3
4  parameters beta, mu, gamma, theta, delta, rho, omega, A_1_1, A_1_2, A_2_1, A_2_2;
5
6  beta = 0.99;
7  mu    = 0.34;
8  gamma = -1;
9  theta =0.36;
10 delta = 0.025;
11 rho = -1/9;
12 omega = 0.85;
13 A_1_1=0.97;
14 A_1_2=0.025;
15 A_2_1=0.025;
16 A_2_2=0.97;
17
18 model;
19 //shock
20 z_1 = A_1_1 * z_1(-1) + A_1_2*z_2(-1)+eps_1;
21 z_2 = A_2_1 * z_1(-1) + A_2_2*z_2(-1)+eps_2;
22
23 //output
24 f_1=exp(z_1)*k_1(-1)^theta*n_1^(1-theta);
25 f_2=exp(z_2)*k_2(-1)^theta*n_2^(1-theta);
26
27 //feasibile constraint
28 x_1+c_1= (omega*a_1^rho+(1-omega)*b_1^rho)^(1/rho);

```

```

29 x_2+c_2= ((1-omega)*a_2^rho+omega*b_2^rho)^(1/rho);
30
31 // capital formation
32 k_1 = x_1+(1-delta)*k_1(-1);
33 k_2 = x_2+(1-delta)*k_2(-1);
34
35 // intermediate good
36 a_1+ a_2 = f_1;
37 b_1+ b_2 = f_2;
38
39 // wage in price of intermediate good
40 w_1 = (1-theta)*f_1/n_1;
41 w_2 = (1-theta)*f_2/n_2;
42
43 // Lagragian
44 lambda_1 = mu*((c_1^mu*(1-n_1)^(1-mu))^gamma)/c_1;
45 lambda_2 = mu*((c_2^mu*(1-n_2)^(1-mu))^gamma)/c_2;
46
47 // interest rate in price of intermediate good
48 r_1 = theta*f_1/k_1(-1);
49 r_2 = theta*f_2/k_2(-1);
50
51 // intermediate good pricing
52 qa_1 = omega*a_1^(rho-1)*((omega*a_1^rho+(1-omega)*b_1^rho)^(1/rho-1));
53 qb_1 = (1-omega)*b_1^(rho-1)* ((omega*a_1^rho+(1-omega)*b_1^rho)^(1/rho-1));
54 qa_2 = (1-omega)*a_2^(rho-1)*(((1-omega)*a_2^rho+omega*b_2^rho)^(1/rho-1));
55 qb_2 = omega*b_2^(rho-1)*(((1-omega)*a_2^rho+omega*b_2^rho)^(1/rho-1));
56
57 // foc to labor
58 (1-mu)*((c_1^mu*(1-n_1)^(1-mu))^gamma)/(1-n_1) = (lambda_1*qa_1)*w_1;
59 (1-mu)*((c_2^mu*(1-n_2)^(1-mu))^gamma)/(1-n_2) = (lambda_2*qb_2)*w_2;
60
61 //foc to capital
62 beta*lambda_1(1)*(qa_1(1) * r_1(1)+1-delta)=lambda_1;
63 beta*lambda_2(1)*(qb_2(1) * r_2(1)+1-delta)=lambda_2;
64
65 //foc to a_1
66 lambda_1* qa_1 =lambda_2* qa_2;
67
68 //foc to b_1
69 lambda_1* qb_1= lambda_2* qb_2;
70

```

```

71 // gdp
72 y_1=qa_1*f_1;
73 y_2=qb_2*f_2;
74
75 //net export ratio
76 nx_1=(qa_1*a_2-qb_1*b_1)/y_1;
77 nx_2=(qb_2*b_1-qa_2*a_2)/y_2;
78
79 //import ratio
80 a_1*ir_1=b_1;
81 b_2*ir_2=a_2;
82
83 //terms of trade
84 qa_1*p_1=qb_1;
85 qb_2*p_2=qa_2;
86
87 //real exchange rate
88 rx_1*qa_2=qa_1;
89 rx_2*qa_1=qa_2;
90 kk_1=log(k_1);
91 nn_1 = log(n_1);
92 xx_1 =log(x_1);
93 cc_1=log(c_1);
94 aa_1=log(a_1);
95 bb_1=log(b_1);
96 rr_1 =log(r_1);
97 yy_1=log(y_1);
98 kk_2=log(k_2);
99 nn_2 = log(n_2);
100 xx_2 =log(x_2);
101 cc_2=log(c_2);
102 aa_2=log(a_2);
103 bb_2=log(b_2);
104 rr_2 =log(r_2);
105 yy_2=log(y_2);
106 end;
107
108 initval;
109 k_1=5.84336;
110 k_2=5.84336;
111 x_1=0.146084;
112 x_2=0.146084;

```

```

113 c_1=0.42366;
114 c_2=0.42366;
115 n_1=0.307182;
116 n_2=0.307182;
117 f_1=0.887017;
118 f_2=0.887017;
119 y_1=0.569744;
120 y_2=0.569744;
121 rx_1=1;
122 rx_2=1;
123 ir_1=0.209896;
124 ir_2=0.209896;
125 p_1=1;
126 p_2=1;
127 nx_1=1.39e-09;
128 nx_2=-3.30e-10;
129 eps_1=0;
130 eps_2=0;
131 z_1=0;
132 z_2=0;
133 a_1=0.733135;
134 a_2=0.153882;
135 b_1=0.153882;
136 b_2=0.733135;
137 w_1 =1.84806;
138 w_2 = 1.84806;
139 r_1 = 0.0546477;
140 r_2 = 0.0546477;
141 qa_1 = 0.642314;
142 qb_1 = 0.642314;
143 qa_2 = 0.642314;
144 qb_2 = 0.642314;
145 lambda_1 = 1.3692;
146 lambda_2 = 1.3692;
147 kk_1=log(k_1);
148 nn_1 = log(n_1);
149 xx_1 =log(x_1);
150 cc_1=log(c_1);
151 aa_1=log(a_1);
152 bb_1=log(b_1);
153 rr_1 =log(r_1);
154 yy_1=log(y_1);

```

```

155 kk_2=log(k_2);
156 nn_2 = log(n_2);
157 xx_2 =log(x_2);
158 cc_2=log(c_2);
159 aa_2=log(a_2);
160 bb_2=log(b_2);
161 rr_2 =log(r_2);
162 yy_2=log(y_2);
163 end;
164
165
166 steady;
167 check;
168
169 shocks;
170 var eps_1=0.0073^2;
171 var eps_2=0.0044^2;
172 var eps_1 , eps_2= 0.29*0.0073*0.0044;
173 end;
174
175 stoch_simul(periods=2000,order=1,ar=10,hp_filter=1600,replic=1000,graph_format =
    eps);

```