

Direct measurement of the  $\bar{K}N \rightarrow \pi\Sigma$  scattering amplitude below the  $\bar{K}N$  threshold employing the  $d(K^-, N)\pi\Sigma^-$  reaction

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# Chapter 1

## Introduction

### 1.1 Discovery of the $\Lambda(1405)$

The  $\Lambda(1405)$  is a hyperon resonance state with strangeness  $S = -1$ , isospin  $I = 0$  spin-parity  $J^P = \frac{1}{2}^-$ . This resonance state was first predicted by Dalitz and Tuan [1] in 1959. They analyzed the  $\bar{K}N$  scattering data and found that the  $I = 0$   $\bar{K}N$  scattering amplitude has a resonance pole below the  $\bar{K}N$  mass threshold. They suggested that this resonance pole is a bound state of  $\bar{K}N$  [3]. Later,  $\Lambda(1405)$  was first reported in a hydrogen bubble chamber experiment at the Lawrence Radiation Laboratory: the  $K^- p \rightarrow \Sigma\pi\pi\pi$  reaction with a  $K^-$  beam of  $1.15\text{GeV}/c$ .

A high-statistics generation experiment of  $\Lambda(1405)$  was performed at CERN [4]. In this experiment,  $K^- p \rightarrow \Sigma^+(1660)\pi^- \rightarrow \Lambda(1405)\pi^+\pi^-$  reaction was measured using a  $4.2\text{GeV}/c$   $K^-$  beam. Dalitz and Deloff deduced mass  $M = 1406.5 \pm 4.0 \text{ MeV}/c^2$  and width  $\Gamma = 50 \pm 2.0 \text{ MeV}/c^2$  of  $\Lambda(1405)$  from fitting of this data. In the latest Particle Data Group, the mass of *Lambda*(1405) was determined to be  $M = 1405.1^{+1.3}_{-1.0}\text{MeV}/c^2$  and *Gamma* =  $50\text{GeV}/c^2$  from these analyses. This method of analysis is called the phenomenological method.

### 1.2 Recent situation of $\Lambda(1405)$

Wise et al. confirmed that the  $\Lambda(1405)$  resonance pole is located below the  $\bar{K}N$  threshold using a chiral Lagrangian with a strangeness  $S = -1$  sector [6]. In the 2000's, the chiral unitary model proposed that  $\Lambda(1405)$  is a dynamical generated molecular state consisting of two poles [7]. The higher pole is coupled to the  $\bar{K}N$  channel, while the lower pole is coupled to the  $\pi\sigma$  channel. Therefore, they claim that the pole coupled to  $\bar{K}N$  shifts to a higher position than the previously mentioned  $1405 \text{ MeV}/c$ . This approach is called the chiral unitary approach.

Photoproduction of  $\Lambda(1405)$  was performed at LEPS in Spring-8 [8]. In

that experiment, the  $\gamma p \rightarrow K^+ \Lambda(1405)$  reaction at  $E_\gamma = 1.5 - 2.4\text{GeV}$  was used to measure the  $K^+$  scattered at  $0.8 < \cos \theta_{K^+} < 1.0$ . They reported  $\pi^+ \Sigma^-$  and  $\pi^- \Sigma^+$  and observed a difference between the two spectra. This fact implies the existence of an interference term between  $I = 0$  and  $I = 1$ , suggesting that  $\Lambda(1405)$  is a dynamically generated state.

The CLAS Collaboration reported highly-statistical photoproduction of  $\Lambda(1405)$ . The spectra of  $\pi^- \Sigma^+$ ,  $\pi^0 \Sigma^0$ , and  $\pi^- \Sigma^+$  are measured for total energies  $2.55 < W < 2.85\text{GeV}$  and  $K^+$  scattering angles of  $0.6 < \cos \theta_{K^+} < 0.9$  in the center-of-mass frame [9,10]. T. Nakamura et al. reproduced those spectra finely well using the chiral unitary model, although the reaction mechanism is not simple [11]. L. Roca et al. constructed a model with two poles using photonuclear reactions with a potential with free parameters based on the chiral unitary model [12]. They deduced a high pole is located above  $1405 \text{ MeV}/c^2$ , albeit with many parameters.

HADES Collaboration reported the spectra of  $\Lambda(1405) \rightarrow \pi^\mp \Sigma^\pm$  using the  $pp \rightarrow K^+ \Lambda(1405)$  reaction with a  $1405\text{GeV}/c$   $p$  beam [13]. The peak position of the spectra was located below  $1400\text{GeV}/c$ . M. Hassanvand et al. obtained the mass and width of  $\Lambda(1405)$  with  $M = 1405.1_{-9}^{+11} \text{ MeV}/c^2$  and  $\Gamma = 62 \pm 10 \text{ MeV}/c^2$  by adapting phenomenological analysis [14]. On the other hand, J. Siebenzonen et al. argue that the data can be reproduced in a two pole structure such as the chiral unitary model [15].

### 1.3 $\bar{K}N$ interaction and $\Lambda(1405)$

As mentioned before,  $\Lambda(1405)$  is closely related to the  $KN$  interaction. One way to measure the  $\bar{K}N$  interaction on the  $\bar{K}N$  threshold is to measure X-rays from Kaonic hydrogen. In this method, the  $\bar{K}N$  interaction is determined by measuring the shift of the X-ray emitted from the Kaonic hydrogen from the electromagnetic interaction. The results of this measurement were previously thought to be repulsive, but the E228 experiment performed at KEK-PS by Iwasaki et al. concluded that the interaction is attractive [16].

Then, the SIDDHARTA collaboration performed experiments with higher precision [17]. The results of this experiment were used as a constraint for analyzing  $\bar{K}N$  scattering, and the pole position of  $\Lambda(1405)$  was deduced by several theorists [18].

### 1.4 J-PARC E31 experiment and $d(K^-, n)$ reaction

In this situation, direct measurement of  $\bar{K}N \rightarrow \pi \Sigma$  scattering is desired. But the reaction can not happen in free space due to energy conservation. This reaction using a  $K^-$  beam of  $644\text{-}844\text{MeV}/c$  has been measured at CERN using a bubble chamber and a  $K^- d \rightarrow n \pi^+ \Sigma^-$  spectrum has been reported [19]. This spectrum was calculated using the chiral unitary model

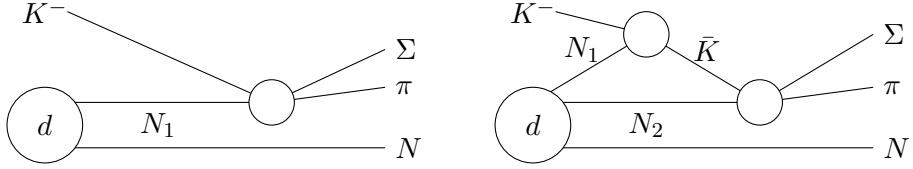


Figure 1.1: Feynman diagrams about  $d(K^-, N)\pi\Sigma$  reaction. The left and right figures indicate about 1-step and 2-step reactions, respectively.

and reproduced reasonably well [20, 21]. However, since only the  $\pi^+\Sigma^-$  spectrum is reported in this experiment, interference cannot be discussed.

For the reason, we performed the J-PARC E31 experiment [28]. The experimental setup is described in detail in the next chapter.???. In this experiment, a  $1.0\text{GeV}/c$   $K^-$  beam is irradiated to the deuterium target and the forward scattered nucleons are measured. The final state is then identified as the  $\pi\Sigma$  state to confirm that a reaction has occurred in which the backward-scattered  $\bar{K}$  mesons have scattered with the remaining nucleons to become  $\pi\Sigma$ . In this reaction, The momentum transfer near the  $\pi\Sigma$  invariant mass near the  $\bar{K}N$  threshold is as low as  $0.25\text{GeV}/c$ , so the angular momentum transfer becomes small and S-wave scattering is expected to be dominant in the 2-step  $\bar{K}N \rightarrow \pi\Sigma$  scattering.

In the final state of  $\pi\Sigma n$ , the 1-step reaction is also considered in which  $\pi\Sigma$  is produced by direct scattering with a nucleon. In this case, the emitted nucleon has a Fermi momentum in deuterium  $< 0.2\text{GeV}/c$ , and all the momentum of the  $K^-$  beam is given to  $\pi\Sigma$ , and its invariant mass appears in the high  $1.9\text{GeV}/c^2$  region. Therefore, the contribution from the 1-step reaction in the region of interest near the  $\bar{K}N$  threshold is negligible.

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