

Direct measurement of the $\bar{K}N \rightarrow \pi\Sigma$ scattering
amplitude below the $\bar{K}N$ threshold employing the
 $d(K^-, N)''\pi\Sigma''$ reaction

Kentaro Inoue

November 2, 2022

Contents

1	Introduction	3
1.1	Discovery of the $\Lambda(1405)$	3
1.2	Recent situation of $\Lambda(1405)$	3
1.3	$\bar{K}N$ interaction and $\Lambda(1405)$	4
1.4	J-PARC E31 experiment and $d(K^-, n)$ reaction	4

Chapter 1

Introduction

1.1 Discovery of the $\Lambda(1405)$

The $\Lambda(1405)$ is a hyperon resonance state with strangeness $S = -1$, isospin $I = 0$ spin-parity $J^P = \frac{1}{2}^-$. This resonance state was first predicted by Dalitz and Tuan [1] in 1959. They analyzed the $\bar{K}N$ scattering data and found that the $I = 0$ $\bar{K}N$ scattering amplitude has a resonance pole below the $\bar{K}N$ mass threshold. They suggested that this resonance pole is a bound state of $\bar{K}N$ [3]. Later, $\Lambda(1405)$ was first reported in a hydrogen bubble chamber experiment at the Lawrence Radiation Laboratory: the $K^-p \rightarrow \Sigma\pi\pi\pi$ reaction with a K^- beam of 1.15GeV/c.

A high-statistics generation experiment of $\Lambda(1405)$ was performed at CERN [4]. In this experiment, $K^-p \rightarrow \Sigma^+(1660)\pi^- \rightarrow \Lambda(1405)\pi^+\pi^-$ reaction was measured using a 4.2GeV/c K^- beam. Dalitz and Deloff deduced mass $M = 1406.5 \pm 4.0$ MeV/ c^2 and width $\Gamma = 50 \pm 2.0$ MeV/ c^2 of $\Lambda(1405)$ from fitting of this data. In the latest Particle Data Group, the mass of $\Lambda(1405)$ was determined to be $M = 1405.1^{+1.3}_{-1.0}$ MeV/ c^2 and $\Gamma = 50$ MeV/ c^2 from these analyses. This method of analysis is called the phenomenological method.

1.2 Recent situation of $\Lambda(1405)$

Wise et al. confirmed that the $\Lambda(1405)$ resonance pole is located below the $\bar{K}N$ threshold using a chiral Lagrangian with a strangeness $S = -1$ sector [6]. In the 2000's, the chiral unitary model proposed that $\Lambda(1405)$ is a dynamical generated molecular state consisting of two poles [7]. The higher pole is coupled to the $\bar{K}N$ channel, while the lower pole is coupled to the $\pi\sigma$ channel. Therefore, they claim that the pole coupled to $\bar{K}N$ shifts to a higher position than the previously mentioned 1405 MeV/c. This approach is called the chiral unitary approach.

Photoproduction of $\Lambda(1405)$ was performed at LEPS in Spring-8 [8]. In

that experiment, the $\gamma p \rightarrow K^+ \Lambda(1405)$ reaction at $E_\gamma = 1.5 - 2.4 \text{ GeV}$ was used to measure the K^+ scattered at $0.8 < \cos \theta_{K^+} < 1.0$. They reported $\pi^+ \Sigma^-$ and $\pi^- \Sigma^+$ and observed a difference between the two spectra. This fact implies the existence of an interference term between $I = 0$ and $I = 1$, suggesting that $\Lambda(1405)$ is a dynamically generated state.

The CLAS Collaboration reported highly-statistical photoproduction of $\Lambda(1405)$. The spectra of $\pi^- \Sigma^+$, $\pi^0 \Sigma^0$, and $\pi^- \Sigma^+$ are measured for total energies $2.55 < W < 2.85 \text{ GeV}$ and K^+ scattering angles of $0.6 < \cos \theta_{K^+} < 0.9$ in the center-of-mass frame [9, 10]. T. Nakamura et al. reproduced those spectra finely well using the chiral unitary model, although the reaction mechanism is not simple [11]. L. Roca et al. constructed a model with two poles using photonuclear reactions with a potential with free parameters based on the chiral unitary model [12]. They deduced a high pole is located above $1405 \text{ MeV}/c^2$, albeit with many parameters.

HADES Collaboration reported the spectra of $\Lambda(1405) \rightarrow \pi^\mp \Sigma^\pm$ using the $pp \rightarrow K^+ \Lambda(1405)$ reaction with a $1405 \text{ GeV}/c$ p beam [13]. The peak position of the spectra was located below $1400 \text{ GeV}/c$. M. Hassanvand et al. obtained the mass and width of $\Lambda(1405)$ with $M = 1405.1_{-9}^{+11} \text{ MeV}/c^2$ and $\Gamma = 62 \pm 10 \text{ MeV}/c^2$ by adapting phenomenological analysis [14]. On the other hand, J. Siebenson et al. argue that the data can be reproduced in a two pole structure such as the chiral unitary model [15].

1.3 $\bar{K}N$ interaction and $\Lambda(1405)$

As mentioned before, $\Lambda(1405)$ is closely related to the $\bar{K}N$ interaction. One way to measure the $\bar{K}N$ interaction on the $\bar{K}N$ threshold is to measure X-rays from Kaonic hydrogen. In this method, the $\bar{K}N$ interaction is determined by measuring the shift of the X-ray emitted from the Kaonic hydrogen from the electromagnetic interaction. The results of this measurement were previously thought to be repulsive, but the E228 experiment performed at KEK-PS by Iwasaki et al. concluded that the interaction is attractive [16].

Then, the SIDDHARTA collaboration performed experiments with higher precision [17]. The results of this experiment were used as a constraint for analyzing $\bar{K}N$ scattering, and the pole position of $\Lambda(1405)$ was deduced by several theorists [18].

1.4 J-PARC E31 experiment and $d(K^-, n)$ reaction

In this situation, direct measurement of $\bar{K}N \rightarrow \pi \Sigma$ scattering is desired. But the reaction can not happen in free space due to energy conservation. This reaction using a K^- beam of $644\text{--}844 \text{ MeV}/c$ has been measured at CERN using a bubble chamber and a $K^- d \rightarrow n \pi^+ \Sigma^-$ spectrum has been reported [19]. This spectrum was calculated using the chiral unitary model

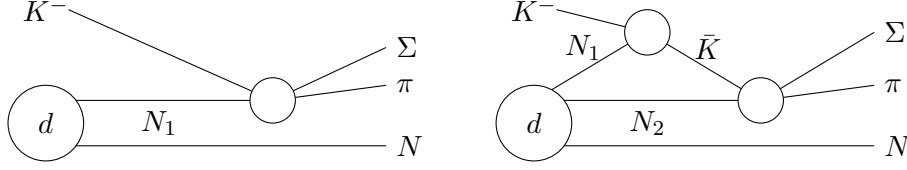


Figure 1.1: Fynman diagrams about $d(K^-, N)\pi\Sigma$ reaction. The left and right figures indicate about 1-step and 2-step reactions, respectively.

and reproduced reasonably well [20, 21]. However, since only the $\pi^+\Sigma^-$ spectrum is reported in this experiment, interference cannot be discussed.

For the reason, we performed the J-PARC E31 experiment [28]. The experimental setup is described in detail in the next chapter.?? In this experiment, a $1.0\text{GeV}/c$ K^- beam is irradiated to the deuterium target and the forward scattered nucleons are measured. The final state is then identified as the $\pi\Sigma$ state to confirm that a reaction has occurred in which the backward-scattered \bar{K} mesons have scattered with the remaining nucleons to become $\pi\Sigma$. In this reaction, The momentum transfer near the $\pi\Sigma$ invariant mass near the $\bar{K}N$ threshold is as low as $0.25\text{GeV}/c$, so the angular momentum transfer becomes small and S-wave scattering is expected to be dominant in the 2-step $\bar{K}N \rightarrow \pi\Sigma$ scattering.

In the final state of $\pi\Sigma n$, the 1-step reaction is also considered in which $\pi\Sigma$ is produced by direct scattering with a nucleon. In this case, the emitted nucleon has a Fermi momentum in deuterium $< 0.2\text{GeV}/c$, and all the momentum of the K^- beam is given to $\pi\Sigma$, and its invariant mass appears in the high $1.9\text{GeV}/c^2$ region. Therefore, the contribution from the 1-step reaction in the region of interest near the $\bar{K}N$ threshold is negligible.

Bibliography

- [1] R. H. Dalitz and S. F. Tuan, Phys. Rev. Lett. **2** (1959).
"Possible Resonant State in Pion-Hyperon Scattering"
- [2] M. H. Alston, L. W. Alvarez, P. Eberhard and M. L. Good,
Phys. Rev. Lett. **6**, 698 (1961).
"Study of Resonances of the $\Sigma - \pi$ System"
- [3] R. H. Dalitz, T. C. Wong and G. Rajasekaran,
Phys Rev. **153**, 1617 (1967)
"Model Calculation for the $Y^*(1405)$ Resonance State"
- [4] R. J. Hemingway, Nucl Phys B **253**, 742 (1985).
"Production of $\Lambda(1405)$ in K^-p Reactions at 4.2GeV/ c "
- [5] R. H. Dalitz and A. Deloff, J. Phys. G17, 281 (1991).
"The Shape and Parameters of the $\Lambda(1405)$ Resonance"
- [6] N.KaiserP.B.Siegel and W.Weise, Nucl Phys A **594**, 325 (1995).
"Chiral Dynamics and the Low-Energy Kaon-Nucleon Interaction"
- [7] D. Jido et al., Nucl. Phys. A **725**, 181 (2003).
"Chiral Dynamics of the Two $\Lambda(1405)$ States"
- [8] M. Niiyama et al., Phys. Rev. C **78**, 035202 (2008).
"Photoproduction of $\Lambda(1405)$ and $\Sigma(1385)$ on the proton at $E_\gamma = 1.5$ -
2.4GeV/ c "
- [9] K. Morita for the CLAS Collaboration,
Phys. Rev. C **87**, 035206 (2013).
"Measurement of the $\pi\Sigma$ photoproduction line shapes near the $\Lambda(1405)$ "
- [10] K. Morita for the CLAS Collaboration,
Phys. Rev. Lett. **112**, 082004 (2014).
"Spin and parity measurement of the $\Lambda(1405)$ baryon"
- [11] S. X. Nakamura and D. Jido, Phys. Theor. Exp. Phys., **2014**, 023D01
(2014).
"Lambda (1405) photoproduction based on the chiral unitary model"

- [12] L. Roca and E. Oset, Phys. Rev. C **87**, 055201 (2013).
"Λ(1405) poles obtained from $\pi^0\Sigma^0$ photoproduction data"
- [13] G. Agakishiev for the HADES Collaboration,
Phys. Rev C **87**, 025201 (2013).
"Baryonic Resonances to the $\bar{K}N$ threshold: The case of Λ(1405) in pp collisions"
- [14] M. Hassanvand et al., Phys. Rev. C **87**, 055202 (2013)
"Theoretical analysis of $\Lambda(1405) \rightarrow (\pi\Sigma)^0$ mass spectra produced in $p + p \rightarrow p + \Lambda(1405) + p$ reactions"
- [15] J. Siebenson and L. Fabbietti, Phys. Rev. C **88**, 055201 (2013)
"Investigation of the Λ(1405) line shape observed in pp collisions"
- [16] M. Iwasaki et al., Phys. Rev. Lett. **78**, 3067 (1997).
"Observation of Kaonic Hydrogen K_α X Rays"
- [17] M. Bazzi et al., Phys. Lett. B **704**, 113 (2011).
"A New Measurement of Kaonic Hydrogen X-Rays"
- [18] T. Hyodo and U.-G. Meißner, PDG Review, Tables and Plots, Section.83
"Pole Structure of the Λ(1405) Region"
- [19] O. Braun et al., Nucl. Phys. B **129**, 1 (1977).
"New Information About the Kaon-Nucleon-Hyperon Coupling Constants $g(KN\Sigma(1197))$, $g(KN\Sigma(1385))$ and $g(KN\Lambda(1405))$ "
- [20] D. Jido, E. Oset and T. Sekihara, Eur. Phys. J. A **42**, 257 (2009).
"Kaonic Production of Λ(1405) off deuteron target in chiral dynamics"
- [21] J. Yamagata-Sekihara, T. Sekihara, and D. Jido, Prog. Theor. Exp. Phys.**2013**, 043D02 (2013).
"Production of hyperon resonances induced by kaons on a deuteron target"
- [22] A. D. Martin, Nucl. Phys. B **179**, 33 (1981).
"Kaon-Nucleon Parameters"
- [23] J. D. Davies et al., Phys. Lett. B **83**, 55 (1979).
"Observation of Kaonic Hydrogen Atom X-rays"
- [24] M. Izycki et al., Z. Phys. A **297**, 11 (1980).
"Results of the Search for K-series X-rays from Kaonic Hydrogen"
- [25] H. Zhang et al., Phys. Rev. C **88**, 035204 (2013).
"Partial-wave analysis of $\bar{K}N$ scattering reactions"

- [26] H. Zhang et al., Phys. Rev. C **88**, 035205 (2013).
"Multichannel parametrization of $\bar{K}N$ scattering amplitudes and extraction of resonance parameters"
- [27] P. M. Bird et al., Nucl. Phys. A **404**, 482 (1983).
"Kaonic Hydrogen Atom X-rays"
- [28] H. Noumi et al., Proposals for the 15th PAC meeting
"Spectroscopic study of hyperon resonances below $\bar{K}N$ threshold via the (K^-, n) reaction on Deuteron"
- [29] Y. Ikeda, T. Hyodo, and W. Weise, Nucl. Phys. A **881**, 98 (2012)
"Chiral SU(3) theory of antikaon–nucleon interactions with improved threshold constraints"
- [30] T. Hashimoto et al., Phys. Rev. Lett. **128**, 112503 (2022).
"Measurements of Strong-Interaction Effects in Kaonic-Helium Isotopes at Sub-eV Precision with X-Ray Microcalorimeters"
- [31] J. Zmeskal et al., J-PARC P57 Proposal
"Measurement of the Strong Interaction Induced Shift and Width of the 1s State of Kaonic Deuterium at J-PARC"
- [32] G. P. Gopal et al., Nucl. Phys. B **119**, 362 (1977).
"Partial-wave analyses of KN two-body reactions between 1480 and 2170 MeV"
- [33] Jonathan M. M. Hall et al., Phys. Rev. Lett. **114**, 132002 (2016).
"Lattice QCD Evidence that the $\Lambda(1405)$ Resonance is an Antikaon-Nucleon Molecule"
- [34] H. Kamano et al., Phys. Rev. C **90**, 065202 (2014).
"Dynamical Coupled-Channels Model of K^-p Reactions: Determination of Partial Wave Amplitudes"
Phys. Rev. C **92**, 025205 (2015).
"Dynamical Coupled-Channels Model of K^-p Reactions. Extraction of Λ^* and Σ^* Hyperon Resonances"
Phys. Rev. C **95**, 044903(E) (2015).
- [35] J. Esmaili, Y. Akaishi, and T. Yamazaki, Phys. Lett. B **686**, 23 (2010)
"Experimental confirmation of the $\Lambda(1405)$ ansatz from resonant formation of a K^-p quasi-bound state in K^- absorption by ^3He and ^4He "
- [36] M. Niiyama et al., Phys. Rev. C **78**, 035202 (2008).
"Photoproduction of $\Lambda(1405)$ and $\Sigma(1385)$ on the proton at $E_\gamma = 1.5$ - $2.4\text{GeV}/c$ "

- J. K. Ahn, Nucl. Phys. A **721**, 715c (2002).
 "Λ(1405) photoproduction at Spring-8/LEPS"
- [37] J.C.Nacher et al., Phys. Lett. B **455**, 55 (1999).
 "Photoproduction of the Λ(1405) on the proton and nuclei"
- [38] A. Cieplý and J. Smejkal, Nucl. Phys. A **881**, 115 (2012).
 "Chirally motivated $\bar{K}N$ amplitudes for in-medium applications"
- [39] L.Fabbietti et al., Nucl. Phys. A **914**, 60 (2013).
- [40] K. Miyagawa, J. Haidenbauer, and H. Kamada Phys. Rev. C **97**, 055209 (2018)
 "Faddev approach to the reaction $K - d \rightarrow \pi \Sigma n$ at $p_K = 1.0 \text{ GeV}/c$ "
- [41] S. Kawasaki et al., JPS Conf. Proc. **13**, 020018 (2017).
 "Spectroscopic Experiment of Λ(1405) via the In-flight $d(K^-, n)n$ Reaction at J-PARC K1BR.8"
- [42] E. Oset, A. Ramos, and C. Bennhold, Phys. Lett. B **527**, 99 (2002); **530**, 260(E) (2002).
 "Low lying $S = -1$ excited baryons and chiral symmetry"
- [43] H. Zhang, et al., Phys. Rev. C **88**, 035204 (2013). "Partial-wave analysis of $\bar{K}N$ scattering reactions"
- [44] S. Ohnishi et al, Phys. Rev. C **93**, 025207 (2016).
 "Structure of the Λ(1405) and the $K^-d \rightarrow \pi \Sigma n$ reaction"
- [45] H. Kamano et al., Phys. Rev. C **94**, 065205 (2016).
 "Toward Establishing Low-Lying Λ and Σ Hyperon Resonances with the $\bar{K} + d \rightarrow \pi + Y + N$ Reaction"
- [46] T. Hyodo and D. Jido, Prog. Part. Nucl. Phys. **67**, 55 (2012).
 "The Nature of the Λ(1405) Resonance in Chiral Dynamics"
- [47] K. Agari et al, Prog. Theor. Exp. Phys., 02B009 (2012)
- [48] K. Agari et al, Prog. Theor. Exp. Phys., 02B011 (2012)
- [49] TRANSPORT <http://linac96.web.cern.ch/Linac96/Proceedings/Thursday/THP72/Paper.pdf>
- [50] T. K. Ohska et al., Nuclear Science, IEEE Transactions on **33**, 98 (1986).
- [51] M. Shiozawa and et al., A new TKO system manager board for a dead-time-free data acquisition system, in 1994 IEEE Nuclear Science Symposium-NSS'94, pages 632–635, (1994)
- [52] M. Iio et al., Nucl. Instrum. Methods Phys. Res., Sect. A **687**, 1 (2012).

- [53] S. Agostinelli et al., Nucl. Instrum. Methods Phys. Res., Sect. **A** 506, 250 (2003)
J. Allison et al., IEEE Transactions on Phys. Sci. 53, 207 (2006)
J.Allison et al., Nucl. Instrum. Methods Phys. Res., Sect. **A** 835, 186 (2016)
- [54] K. Fuji, https://www-jlc.kek.jp/subg/offl/lib/docs/helix_manip/node3.html (1968).
- [55] Opera Electromagnetic FEA Solution Software
- [56] V. Flaminio et al., CERN-HARA-87-01, 121 (1983).
- [57] M.Jones et el, Nucl. Phys. B **90**, 349 (1975)
- [58] R. Barlow and C. Beeston, Comp. Phys. Comm. **77**, 219 (1993).
- [59] A. Nappi, Comp. Phys. Comm. **180**, 269 (2009).
- [60] M. jones, R. Levi, Setti, D. Merrill and R. D. Tripp, Phys. Rev. B**90**, 349 (1975).
- [61] M. Bernheim and et. el., Nucl. Phys. A**365**, 349, (1981).
- [62] R. Machleidt, Phys. Rev. C**63**, 024001 (2001).
- [63] S. Agostinelli et al., Nuclear Instruments and Methods in Physics Research Section A: Accelerators, Spectrometers, Detectors and Associated Equipment **506**, 250 (2003).
J.Allison et el., Nuclear Instruments and Methods in Physics Research Section A: Accelerators, Spectrometers, Detectors and Associated Equipment **835**, 186 (2016).