Lecture 3: Confidence Intervals via Bootstrapping

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Today's Learning Goals

By the end of this lecture, you should be able to:

- 1. Define what a confidence interval is and why we want to generate one.
- 2. Explain how the bootstrap sampling distribution can be used to create confidence intervals
- Write a computer script to calculate confidence intervals for a population parameter using bootstrapping.
- 4. Effectively visualize point estimates and confidence intervals.
- 5. Interpret and explain results from confidence intervals.

Loading R Packages

Let us load the libraries for data wrangling, analysis, and plotting.

```
library(cowplot)
library(infer)
library(scales)
library(tidyverse)
options(repr.matrix.max.rows = 6)
```

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1. Fundamentals of Confidence Intervals

A confidence interval is a plausible range of values for the population parameter **under a certain percentage of confidence**.

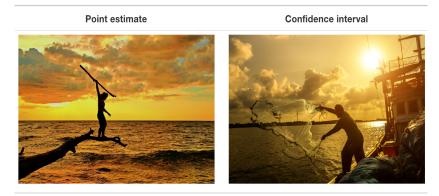


Fig. 3 Image from Ismay and Kim (2021): Figure 8.15.

1.1. Why confidence intervals?

- If we report a point estimate, we probably will not hit the exact value of the population parameter.
- If we report a range of plausible values, we have a good shot at capturing the parameter.

1.2. Bootstrap confidence intervals with the percentile method

One way to calculate a range of plausible values for the population parameter (**to be estimated!**) is using the middle 95% of the distribution of bootstrap sample estimates to determine our endpoints:

- Our endpoints are at the 2.5th and 97.5th percentiles.
- For the bootstrap distribution below, the values of 21 and 29.3.

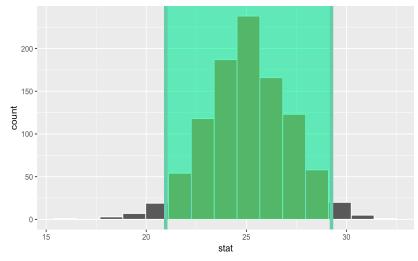


Fig. 4 Example of a bootstrap confidence interval.

1.3. What does a 95% confidence interval mean?

It means that if we were to repeat the process of sampling and calculating a 95% confidence interval multiple times, 95% of the time, we would expect our population parameter's value to lie within the confidence interval. We will check what this means in practice during this lecture.

1.4. Why 95%?

95% is the standard level of confidence in Statistics. Other typical levels are 90 and 99%. If we hold everything else constant (e.g., sample size n), a higher confidence level corresponds to a wider confidence interval and a lower confidence level to a narrower confidence interval. The chosen level depends on the downstream analysis and what chances we are willing to take of being wrong.

2. Calculating Confidence Intervals in R

The infer package has a function called get_confidence_interval() that we can use to compute confidence intervals.

2.1. The Airbnb Dataset

Let us use the listings data. Suppose we are interested in the **population** proportion corresponding to those listings involving the *entire home/apartment*, π_E .

2.1.1. Loading the Population Data Set

The **population** data <u>listings</u> contains an <u>id</u> number, neighbourhood, type of room, the number of people the rental accommodates, number of bathrooms, bedrooms, beds, and the <u>price</u> per night.

```
listings <- read_csv("data/listings.csv")

Rows: 4938 Columns: 74

— Column specification

Delimiter: ","
chr (24): listing_url, name, description, neighborhood_overview, picture_ur...
dbl (37): id, scrape_id, host_id, host_listings_count, host_total_listings_...
lgl (8): host_is_superhost, host_has_profile_pic, host_identity_verified, ...
date (5): last_scraped, host_since, calendar_last_scraped, first_review, la
```

```
i Use `spec()` to retrieve the full column specification for this data.
i Specify the column types or set `show_col_types = FALSE` to quiet this message.
```

We will select the columns corresponding id, room_type, and price per night. The variable price will also be used at the end of this lecture.

```
listings <- listings %>%
  select(id, room_type, price) %>%
  mutate(room_type = as.factor(room_type), price =
as.numeric(gsub('[$,]','', price)))
listings # N = 4,938 (Population Size)
```

id	room_type	price
<dbl></dbl>	<fct></fct>	<dbl></dbl>
10080	Entire home/apt	150
13357	Entire home/apt	132
13358	Entire home/apt	85
÷	:	÷
45398550	Private room	53.29
45400161	Entire home/apt	145.00
45401776	Entire home/apt	135.00

A tibble: 4938 × 3

2.1.2. Calculating the true π_E

For the sake of our example, we already know that $\pi_E=0.756$.

```
listings %>%
  group_by(room_type) %>%
  summarise(n = n()) %>%
  mutate(freq = round(n / sum(n), 3))
```

room_type	n	freq
<fct></fct>	<int></int>	<dbl></dbl>
Entire home/apt	3731	0.756
Hotel room	4	0.001
Private room	1179	0.239
Shared room	24	0.005

A tibble: 4 × 3

Since we are interested in room_type Entire home/apt, let us rename the other levels as Other. Function recode_factor() from dplyr can be used for this purpose.

room_type	n	freq	
<fct></fct>	<int></int>	<dbl></dbl>	
Entire home/apt	3731	0.756	
Other	1207	0.244	

A tibble: 2 × 3

2.1.3. First things first!

To start with our inferential inquiry, we will draw a random sample of size n=40.

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```
set.seed(552) # For reproducibility.
sample <- rep_sample_n(listings, size = 40)
sample</pre>
```

replicate	id	room_type	price
<int></int>	<dbl></dbl>	<fct></fct>	<dbl></dbl>
1	28390229	Entire home/apt	94
1	26356375	Entire home/apt	200
1	43480074	Entire home/apt	171
÷	÷	:	÷
1	19894347	Entire home/apt	95.00
1	31864754	Entire home/apt	87.86
1	26308916	Entire home/apt	150.00

A grouped_df: 40 × 4

We can see that the base sample estimate is $\hat{\pi}_E=0.8$.

```
sample %>%
  group_by(room_type) %>%
  summarise(n = n()) %>%
  mutate(freq = round(n / sum(n), 3))
```

room_type	n	freq
<fct></fct>	<int></int>	<dbl></dbl>
Entire home/apt	32	0.8
Other	8	0.2

A tibble: 2 × 3

2.2. Bootstraping with infer

Using sample, we will draw b=1,000 bootstrap samples of size n=40. Then, we will obtain the corresponding b=1,000 bootstrap_estimates $\hat{\pi}_E^{(B)}$.

 $X_i^{(B)} = \begin{cases} 1 & \text{if the listing is an entire home or apartment in the bootstrap sampl} \\ 0 & \text{otherwise.} \end{cases}$

$$\hat{\pi}_E^{(B)} = rac{\sum_{i=1}^n X_i^{(B)}}{n}.$$

```
set.seed(552) # For reproducibility.
bootstrap_estimates <- sample %>%
    specify(response = room_type, success = "Entire home/apt") %>%
    generate(reps = 1000, type = "bootstrap") %>%
    calculate(stat = "prop")
bootstrap_estimates
```

replicate	stat
<int></int>	<dbl></dbl>
1	0.800
2	0.775
3	0.800
:	÷
998	0.800
999	0.675
1000	0.750

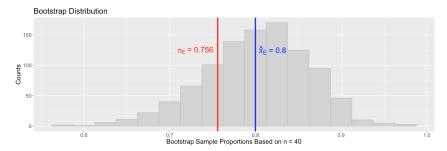
A infer: 1000 × 2

2.3. Plotting the bootstrap distribution

We can make a histogram with the bootstrap_estimates (the red line indicates the real π_E , where the blue line shows the estimated $\hat{\pi}_E$). Note the bootstrap sampling distribution is left-skewed with respect to π_E , but centred around $\hat{\pi}_E$.

```
options(repr.plot.width = 15, repr.plot.height = 5)
bootstrap_dist_plot <- bootstrap_estimates %>%
    ggplot(aes(x = stat)) +
    geom_histogram(binwidth = 0.025, color = "gray", fill = "lightgray") +
    labs(x = "Bootstrap Sample Proportions Based on n = 40", y = "Counts") +
    ggtitle("Bootstrap Distribution") +
    theme(text = element_text(size = 16.5)) +
    geom_vline(xintercept = 0.756, color = "red", size = 1.5) +
    geom_vline(xintercept = 0.8, color = "blue", size = 1.5) +
    annotate("text", x = 0.73, y = 125, label = expression(pi["E"] ~ "=
0.756"), size = 7, color = "red") +
    annotate("text", x = 0.82, y = 125, label = expression(hat(pi)["E"] ~ "=
0.8"), size = 7, color = "blue")
```





2.4. Calculating bootstrap confidence intervals with

infer

Let us use get_confidence_interval() to calculate the 95% confidence intervals using the percentile method:

```
ci_95 <- bootstrap_estimates %>%
  get_confidence_interval(level = 0.95, type = "percentile")
ci_95
```

upper_ci	lower_ci	
<dbl></dbl>	<dbl></dbl>	
0.9	0.675	

A tibble: 1 × 2

What if we wanted 99% confidence intervals?

```
ci_99 <- bootstrap_estimates %>%
  get_confidence_interval(level = 0.99, type = "percentile")
ci_99
```


0.005	0.05
0.625	0.95

A tibble: 1 × 2

What about 90%?

```
ci_90 <- bootstrap_estimates %>%
  get_confidence_interval(level = 0.90, type = "percentile")
ci_90
```

lower_ci upper_ci

<dbl></dbl>		<dbl></dbl>	
	0.7	0.9	

A tibble: 1 × 2

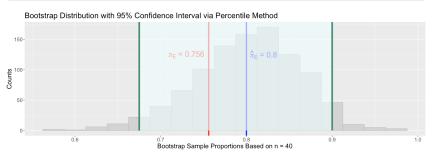
Attention

Lower confidence levels correspond to narrower confidence intervals while holding everything else constant.

2.5. Visualizing the 95% confidence intervals on the boostrap distribution

The infer package has a handy function called shade_confidence_interval(), which needs
the corresponding endpoints (i.e., the lower and upper bounds).

```
bootstrap_dist_plot_ci_95 <- bootstrap_dist_plot +
    shade_confidence_interval(endpoints = ci_95, color = "aquamarine4", fill
= "azure") +
    ggtitle("Bootstrap Distribution with 95% Confidence Interval via
Percentile Method")
suppressWarnings(print(bootstrap_dist_plot_ci_95))</pre>
```



2.6. Visualizing different levels of confidence

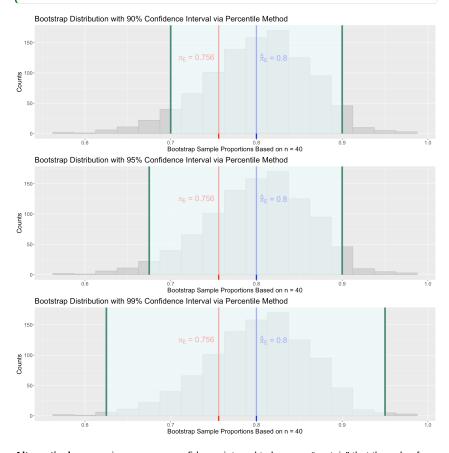
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Let us see how the width of the confidence interval changes based on our confidence level. As we previously noted, the interval width increases as we increase the level of confidence while holding everything else constant such as the base sample size n. Suppose you want a narrower interval (i.e., more precise!) without increasing your base sample size n. Then, you will need to sacrifice a certain level of confidence.

```
bootstrap_dist_plot_ci_90 <- bootstrap_dist_plot +
    shade_confidence_interval(endpoints = ci_90, "aquamarine4", fill =
"azure") +
    ggtitle("Bootstrap Distribution with 90% Confidence Interval via
Percentile Method")

bootstrap_dist_plot_ci_99 <- bootstrap_dist_plot +
    shade_confidence_interval(endpoints = ci_99, "aquamarine4", fill =
"azure") +
    ggtitle("Bootstrap Distribution with 99% Confidence Interval via
Percentile Method")</pre>
```

```
options(repr.plot.width = 15, repr.plot.height = 15)
suppressWarnings(print(plot_grid(bootstrap_dist_plot_ci_90,
bootstrap_dist_plot_ci_95, bootstrap_dist_plot_ci_99, ncol = 1)))
```



Alternatively: as we increase our confidence interval to be more "*certain*" that the value for our population parameter of interest that we are trying to estimate falls in that plausible range, we widen it.

2.7. Interpreting our confidence interval

Recall our 95% confidence interval:

```
ci_95
```

lower_ci	upper_ci
<dbl></dbl>	<dbl></dbl>
0.675	0.9

A tibble: 1 × 2

We used boostrapping to come up with this range of plausible values for the **population** proportion corresponding to those <u>listings</u> involving the *entire home/apartment* class

$$\pi_E = 0.756.$$

If we had a different sample of size n=40 and constructed a 95% confidence interval, would it contain the population parameter value as well?

Let us run another simulation!

2.8. Confidence Interval Simulation

Let us calculate m=100 different confidence intervals derived from m=100 different random samples drawn from <code>listings</code> and see how many times the confidence intervals contain the true population parameter π_E .

```
Step 1: Get m=100 listings_samples of n=40
```

We use the $rep_sample_n()$ function and nest() the samples in the tibble listing_samples.

```
set.seed(552) # For reproducibility.
listing_samples <- listings %>%
  rep_sample_n(size = 40, reps = 100, replace = FALSE) %>%
  nest()
print(listing_samples)
```

```
# A tibble: 100 \times 2
# Groups: replicate [100]
  replicate data
      <int> <list>
         1 <tibble [40 × 3]>
2
         2 <tibble [40 × 3]>
3
          3 <tibble [40 × 3]>
         4 <tibble [40 × 3]>
5
          5 <tibble [40 × 3]>
         6 <tibble [40 × 3]>
6
         7 <tibble [40 × 3]>
7
8
         8 <tibble [40 × 3]>
9
         9 <tibble [40 × 3]>
10
         10 <tibble [40 × 3]>
# ... with 90 more rows
```

Step 2: Create a function for boostrap confidence intervals for each base_sample

For a **binary-type** variable, the function $\mathtt{ci_pipeline}$ takes a **single** base_sample fo size n and draws 1000 bootstrap samples. It computes the **estimated proportion** of interest and then its 95% bootstrap confidence interval.

```
ci_pipeline <- function(base_sample) {
    set.seed(552)

base_sample %>%
    specify(response = room_type, success = "Entire home/apt") %>%
    generate(reps = 1000, type = "bootstrap") %>%
    calculate(stat = "prop") %>%
    get_confidence_interval(level = 0.95, type = "percentile")
}
```

Let us check whether $\[\] \]$ works properly by using it with our very first sample in

this lecture:

```
ci_pipeline(sample)
```

lower_ci upper_ci

<dbl></dbl>	<dbl></dbl>	
0.675	0.9	

A tibble: 1 × 2

Step 3: Create a function to compute the observed point estimate $\hat{\pi}_E$ for each <code>base_sample</code>

Recall our assumed Bernoulli trial in this inferential inquiry:

 $X_i = \begin{cases} 1 & \text{if the listing is an entire home or apartment in the base sample,} \\ 0 & \text{otherwise.} \end{cases}$

Hence, our **estimator** of π_E is defined as

$$\hat{\pi}_E = rac{\sum_{i=1}^n X_i}{n}.$$

Function point_est_pipeline() computes the **estimate** $\hat{\pi}_E$ per base sample.

```
point_est_pipeline <- function(base_sample) {
  base_sample %>%
    specify(response = room_type, success = "Entire home/apt") %>%
    calculate(stat = "prop")
}
```

Let us check whether point_est_pipeline() works properly by using it with our very first sample in this lecture:

```
point_est_pipeline(sample)
```

stat

<dbl>

0.8

A infer:

1 × 1

Step 4: Calculate $\hat{\pi}_E$ and confidence intervals for each of the m=100 samples

Once we have our functions ci_pipeline() and point_est_pipeline(), we will use them to compute the point estimate and 95% bootstrap confidence intervals for each of the m=100 samples stored in listing_samples.

```
set.seed(552) # For reproducibility.
listing_samples <- listing_samples %>%
  mutate(
    percentile_ci = map(data, ci_pipeline),
    point_estimate = map(data, point_est_pipeline)
)
print(listing_samples)
```

```
# A tibble: 100 × 4
# Groups: replicate [100]
   replicate data
                                     percentile_ci
                                                          point_estimate
        <int> <list>
                                     st>
                                                          st>
             1 <tibble [40 \times 3] <tibble [1 \times 2] <infer [1 \times 1] >
             2 <tibble [40 \times 3]> <tibble [1 \times 2]> <infer [1 \times 1]>
3
             3 <tibble [40 \times 3] <tibble [1 \times 2] <infer [1 \times 1] >
             4 < tibble [40 \times 3] > < tibble [1 \times 2] > < infer [1 \times 1] >
            5 <tibble [40 \times 3]> <tibble [1 \times 2]> <infer [1 \times 1]>
 5
 6
             6 <tibble [40 \times 3]> <tibble [1 \times 2]> <infer [1 \times 1]>
             7 <tibble [40 \times 3] <tibble [1 \times 2] <infer [1 \times 1] >
8
             8 <tibble [40 \times 3]> <tibble [1 \times 2]> <infer [1 \times 1]>
             9 <tibble [40 \times 3] <tibble [1 \times 2] <infer [1 \times 1] >
9
            10 <tibble [40 \times 3]> <tibble [1 \times 2]> <infer [1 \times 1]>
10
# ... with 90 more rows
```

Step 5: Label which confidence intervals capture the population parameter

Now that we have all the m=100 95% confidence intervals and their corresponding point estimates (i.e., $\hat{\pi}_E$), we can check which ones caught the true population parameter $\pi_E=0.756$.

```
listing_samples <- listing_samples %>%
  unnest(percentile_ci) %>%
  unnest(point_estimate) %>%
  mutate(Captured = lower_ci <= 0.756 & 0.756 <= upper_ci)
print(listing_samples)</pre>
```

```
# A tibble: 100 × 6
# Groups: replicate [100]
  replicate data
                              lower_ci upper_ci stat Captured
      <int> <list>
                                 <dbl> <dbl> <dbl> <lgl>
          1 <tibble [40 × 3]>
1
                                 0.675
                                          0.9
                                               0.8
                                                      TRUE
          2 <tibble [40 × 3]>
                                          0.875 0.75
                                 0.625
                                                      TRUE
          3 <tibble [40 \times 3]>
3
                                 0.624
                                          0.875 0.75
                                                      TRUE
4
          4 <tibble [40 × 3]>
                                 0.55
                                          0.825 0.7
                                                      TRUE
          5 <tibble [40 × 3]>
                                 0.775
                                          0.975 0.875 FALSE
          6 <tibble [40 × 3]>
6
                                 0.5
                                          0.8 0.65 TRUE
                                          0.85 0.725 TRUE
7
          7 <tibble [40 × 3]>
                                 0.575
                                 0.6
8
          8 <tibble [40 × 3]>
                                          0.875 0.75 TRUE
                                          0.925 0.825 TRUE
9
          9 <tibble [40 × 3]>
                                 0.7
10
         10 <tibble [40 × 3]>
                                 0.65
                                          0.925 0.8
# ... with 90 more rows
```

How many intervals, out of the 100, captured $\pi_E=0.756$?

95% of the total 100!

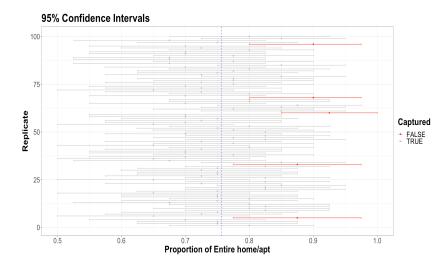
```
listing_samples %>%
  group_by(Captured) %>%
  summarise(n = n()) %>%
  mutate(freq = round(n / sum(n), 3))
```

Captured	n	treq
<lgl></lgl>	<int></int>	<dbl></dbl>
FALSE	5	0.05
TRUE	95	0.95

A tibble: 2 × 3

Step 6: Visualize confidence intervals

The plot below shows the m=100 95% bootstrap confidence intervals as horizontal lines with the true population parameter π_E as a vertical dashed blue line. Dots indicate each point estimate $\hat{\pi}_E$. We highlight those intervals not containing π_E in red (5 out of 100). Code is not provided since this will be a lab2 exercise.



2.9. Interpreting our confidence interval

Going back to our original calculation of a 95% confidence interval for our one sample:

lower_ci	upper_ci
<dbl></dbl>	<dbl></dbl>
0.675	0.9

A tibble: 1 × 2

Thus, for this specific example, we would write:

We are 95% "confident" that the true **population** proportion corresponding to those listings involving the *entire home/apartment*, π_E , is somewhere between 0.675 and 0.9.

We use quotation marks around **confident** to emphasize that, while 95% relates to the reliability of our confidence interval construction procedure, a constructed confidence interval is our best guess of an interval that contains the population parameter.

3. Visualizing Continuous Confidence intervals

The histograms and lines we have been using so far are helpful to learn about confidence intervals. However, this is not the most practical way to communicate confidence intervals to a general audience.

Instead, we should show as much data as possible (without overplotting) while highlighting the estimate and its confidence interval.

Let us explore this with a continuous variable, such as price per night. Moreover, we will visualize two samples from the listings data: a small sample and a large sample (where we will encounter overplotting issues).



For the sake of this visualization example, we will only focus on the inference for the **overall population** price μ_{price} . We will not consider the categorical variable room_type, even though it is also possible to perform this disaggregated analysis. We will explore this matter in lab2.

3.1. What is the real μ_{price} ?

Let us compute the population parameter μ_{price} via the population data listings.

```
pop_mean_price <- listings %>%
   summarize(pop_mean_price = round(mean(price), 2))
pop_mean_price
```

pop_mean_price

<dbl>
163.01

A tibble: 1 × 1

3.2. A small sample of n=50

We start with a small sample of size n=50 drawn from listings.

```
set.seed(1234) # For reproducibility.
sample_n50 <- rep_sample_n(listings, size = 50) %>%
  select(replicate, id, price)
sample_n50
```

replicate	id	price
<int></int>	<dbl></dbl>	<dbl></dbl>
1	15037603	115
1	8556170	99
1	32477935	350
:	:	:
1	17683724	205
1	14580511	99
1	27226611	85

A grouped_df: 50 × 3

The sample mean $\hat{\mu}_{price}$ is:

```
sample_n50 %>%
summarise(mean_price = round(mean(price), 2))
```

replicate mean_price

<int></int>	<dbl></dbl>
1	156.22

A tibble: 1 × 2

Then, using sample_n50, we obtain our 95% bootstrap confidence interval with b=1,000 bootstrap_estimates:

```
set.seed(1234) # For reproducibility.
bootstrap_ci_n50 <- sample_n50 %>%
   specify(response = price) %>%
   generate(reps = 1000, type = "bootstrap") %>%
   calculate(stat = "mean") %>%
   get_confidence_interval(level = 0.95, type = "percentile")
bootstrap_ci_n50
```

lower_ci upper_ci

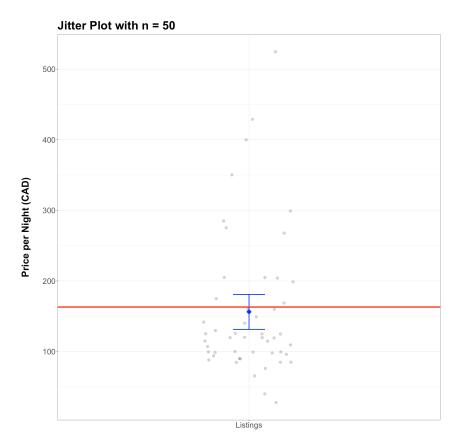
<dbl> <dbl>

131.359 180.7545

A tibble: 1 × 2

Next, we obtain a jitter plot with sample_n50 via geom_jitter(). This class of plot overlaps all sampled price points whose values are depicted on the y-axis. We also included $\mu_{\rm price}$ as horizontal red line with geom_hline(). The 95% confidence interval bootstrap_ci_n50 is added via geom_errorbar() in blue.

```
sample_n50_jitter_plot <- ggplot(sample_n50, aes(x = "Listings", y =</pre>
price)) +
  stat_summary(fun = mean, geom = "point", shape = 18, size = 6, color =
"blue") +
  geom_errorbar(data = bootstrap_ci_n50, aes(
    x = "Listings",
    y = mean(sample_n50$price),
  ymin = lower_ci, ymax = upper_ci
), size = 1, color = "blue", width = 0.1) +
labs(x = "", y = "Price per Night (CAD)\n") +
  geom_hline(yintercept = 163.01, color = "red", size = 1.5) +
  ggtitle("Jitter Plot with n = 50") +
  theme_bw() +
  geom\_jitter(alpha = 0.2, width = 0.15, size = 3) +
  theme(
    text = element_text(size = 25),
    plot.title = element_text(face = "bold"),
    axis.title = element_text(face = "bold"),
    legend.title = element_text(face = "bold"),
sample_n50_jitter_plot
```



We can see in the plot above that μ_{price} is captured by <code>bootstrap_ci_n50</code>.

3.3. A large sample of n=300:

```
set.seed(1234) # For reproducibility.
sample_n300 <- rep_sample_n(listings, size = 300) %>%
select(replicate, id, price)
sample_n300
```

replicate	id	price
<int></int>	<dbl></dbl>	<dbl></dbl>
1	15037603	115
1	8556170	99
1	32477935	350
:	÷	÷
1	40598848	779
1	28331525	150
1	11550687	40

A grouped_df: 300×3

The sample mean $\hat{\mu}_{\mathrm{price}}$ is:

```
sample_n300 %>%
summarise(mean_price = round(mean(price), 2))
```

replicate mean_price

<int></int>	<dbl></dbl>
1	161.34

A tibble: 1 × 2

Then, using sample_n300, we obtain our 95% bootstrap confidence interval with b=1,000 bootstrap_estimates:

```
set.seed(2021) # For reproducibility.
bootstrap_ci_n300 <- sample_n300 %>%
   specify(response = price) %>%
   generate(reps = 1000, type = "bootstrap") %>%
   calculate(stat = "mean") %>%
   get_confidence_interval(level = 0.95, type = "percentile")
bootstrap_ci_n300
```

lower_ci upper_ci

<dbl> <dbl> 146.167 179.4488

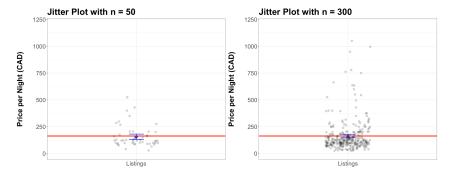
A tibble: 1 × 2

Finally, the respective jitter plot.

```
sample_n300_jitter_plot <- ggplot(sample_n300, aes(x = "Listings", y =</pre>
 stat_summary(fun = mean, geom = "point", shape = 18, size = 6, color =
"blue") +
  geom_errorbar(data = bootstrap_ci_n300, aes(
    x = "Listings"
    y = mean(sample_n300$price),
 ymin = lower_ci, ymax = upper_ci
), size = 1, color = "blue", width = 0.1) +
labs(x = "", y = "Price per Night (CAD)\n") +
  geom_hline(yintercept = 163.01, color = "red", size = 1.5) +
  ggtitle("Jitter Plot with n = 300") +
  theme_bw() +
  geom_jitter(alpha = 0.2, width = 0.15, size = 3) +
  theme(
    text = element_text(size = 25),
    plot.title = element_text(face = "bold"),
    axis.title = element_text(face = "bold"),
    legend.title = element_text(face = "bold"),
```

Now, we compare the jitter plots of both sample sizes.

```
options(repr.plot.width = 20, repr.plot.height = 8)
plot_grid(sample_n50_jitter_plot + coord_cartesian(ylim = c(0, 1200)),
sample_n300_jitter_plot + coord_cartesian(ylim = c(0, 1200)), ncol = 2)
```



Both 95% confidence intervals are **accurate**, since they capture the true $\mu_{\rm price}$. Nonetheless, the interval for n=300 is narrower. Hence, we can see that increasing our

simple size makes our interval more precise while still keeping the same confidence level.

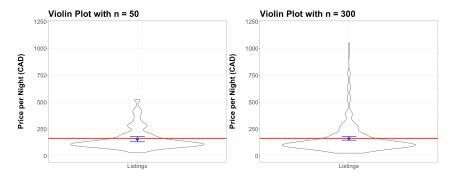
Note an important thing for the jitter plot with n=300: overplotting is quite evident. We can overcome this issue with another class of plots: violins plots.

3.4. Violin Plots

By G. Alexi Rodríguez-Arelis
Violin plots are basically empirical density plots. They show frequency patterns of our data in
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terms of the variable of interest.

```
sample_n50_violin_plot <- ggplot(sample_n50, aes(x = "Listings", y =</pre>
price)) +
  geom_violin() +
  stat_summary(fun = mean, geom = "point", shape = 18, size = 6, color =
  geom_errorbar(data = bootstrap_ci_n50, aes(
    x = "Listings",
    y = mean(sample_n50$price),
    ymin = lower_ci, ymax = upper_ci
  ), size = 1, color = "blue", width = 0.1) + labs(x = "", y = "Price per Night (CAD)\n") +
  geom_hline(yintercept = 163.01, color = "red", size = 1.5) + ggtitle("Violin Plot with n = 50") +
  theme_bw() +
  theme(
    text = element_text(size = 25),
    plot.title = element_text(face = "bold"),
    axis.title = element_text(face = "bold"),
    legend.title = element_text(face = "bold"),
sample_n300_violin_plot <- ggplot(sample_n300, aes(x = "Listings", y =</pre>
price)) +
  geom_violin() +
  stat_summary(fun = mean, geom = "point", shape = 18, size = 6, color =
  geom_errorbar(data = bootstrap_ci_n300, aes(
    x = "Listings"
    y = mean(sample_n300$price),
    ymin = lower_ci, ymax = upper_ci
  ), size = 1, color = "blue", width = 0.1) + labs(x = "", y = "Price per Night (CAD)\n") +
  geom_hline(yintercept = 163.01, color = "red", size = 1.5) +
  ggtitle("Violin Plot with n = 300") +
  theme_bw() +
  theme(
    text = element_text(size = 25),
    plot.title = element_text(face = "bold"),
    axis.title = element_text(face = "bold"),
    legend.title = element_text(face = "bold"),
```

```
plot_grid(sample_n50_violin_plot + coord_cartesian(ylim = c(0, 1200)), sample_n300_violin_plot + coord_cartesian(ylim = c(0, 1200)), ncol = 2)
```



4. Estimation Recap

 A sample statistic is not equal to a population parameter. However, a sample that is representative enough can provide an accurate and precise estimate.

- We would report this sample estimate with a confidence bound around it.
- Since we cannot sample from a population multiple times, we instead bootstrap from the one sample we have to estimate the sampling variability.

5. Acknowledgements

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