$\omega(k)$

$\omega(k) = 0$

$k$

$\omega(k) = \dfrac{-\beta k}{k^2 + \frac{1}{L_d^2}}$

$\omega(k) = -L_d^2 \beta k$