

# CSE 3302 Programming Language

Homework2 - Fall 2026

Due Date: Feb.2, 2026, 11:59 PM

## Problem1 - 30%

Prove by induction: If  $\text{add } n_1 \ n_2 \ n_3$ , then  $\text{add } n_2 \ n_1 \ n_3$  (the commutative law of addition), where  $\text{add } n_1 \ n_2 \ n_3$  is the judgment form for addition defined in the lecture (slide page 23).

(Hint: You may begin by proving the following lemma: If  $n \ \text{nat}$ , then  $\text{add } n \ Z \ n$ .)

## Problem2 - 30%

Prove **Lemma 2** using *induction on the derivation of*  $\text{len } l \ n$ , instead of append. (slide page 35).

## Problem3 - 40%

- (a) Give an inductive definition of the judgment form  $\text{leq } n_1 \ n_2$ , which indicates that  $n_1$  is less than or equal to  $n_2$ , and  $n_1$  and  $n_2$  are defined by judgement form  $n \ \text{nat}$  in the lecture.
- (b) Prove by induction: If  $n_1 \ \text{nat}$ ,  $n_2 \ \text{nat}$ ,  $\text{leq } n_1 \ n_2$  and  $\text{leq } n_2 \ n_1$ , then  $n_1 = n_2$ .

**Submission Format:** Submit only the .pdf version of your homework (typed submissions are preferred; Scanned images must be readable). File must be named `lastname_studentID_hw2.pdf`.