## An Introduction to OCaml



adapted from course by Stephen Edwards @ Columbia

The Basics

**Functions** 

Tuples, Lists, and Pattern Matching

**User-Defined Types** 

Modules and Compilation

A Complete Interpreter in Three Slides

Exceptions; Directed Graphs

**Standard Library Modules** 

#### An Endorsement?

A PLT student accurately summed up using OCaml:

Never have I spent so much time writing so little that does so much.

I think he was complaining, but I'm not sure.

Other students have said things like

It's hard to get it to compile, but once it compiles, it works.

# Why OCaml?

- It's Great for Compilers
  I've written compilers in C++, Python, Java, and OCaml,
  and it's much easier in OCaml.
- i It's Succinct Would you prefer to write 10000 lines of code or 5000?
- Its Type System Catches Many Bugs
  It catches missing cases, data structure misuse, certain off-by-one errors, etc. Automatic garbage collection and lack of null pointers makes it safer than Java.
- Lots of Libraries
   All sorts of data structures, I/O, OS interfaces, graphics, support for compilers, etc.
- Lots of Support
   Many websites, free online books and tutorials, code samples, etc.

#### OCaml in One Slide

Apply a function to each list element; save results in a list

```
"Is recursive"
                                  Passing a function
Case
                                                           Pattern
splitting
                  # let rec map f = function
                                                           Matching
                       [] -> []
                                                      Polymorphic
Local name
                       head :: tail ->
declaration
                          let r = f head in
                                                         Types inferred
                                map f tail;;
List support
                  val map : ('a -> 'b) -> 'a list -> 'b list
 Recursion
                    map (function x -> x + 3) [1;5;9];;
Anonymous
                      int list = [4; 8; 12]
functions
```

# The Basics

# Hello World in OCaml: Interpret or Compile

#### Create a "hello.ml" file:

```
print_endline "Hello World!"
```

#### Run it with the interpreter:

```
$ ocaml hello.ml
Hello World!
```

#### Compile a native executable and run:

```
$ ocamlopt -o hello hello.ml
$ ./hello
Hello World!
```

#### Use ocamlbuild (recommended):

```
$ ocambuild hello.native
```

\$ ./hello.native

Hello World!

#### Hello World in OCaml: REPL

The interactive Read-Eval-Print Loop

Double semicolons ;; mean "I'm done with this expression"

#quit terminates the REPL

Other directives enable tracing, modify printing, and display types and values

Use <u>ledit ocaml</u> or <u>utop</u> instead for better line editing (history, etc.)

#### Comments

#### **OCaml**

```
(* This is a multiline comment in OCaml *)

(* Comments
    (* like these *)
    do nest
*)

(* OCaml has no *)
(* single-line comments *)
```

## C/C++/Java

```
/* This is a multiline
comment in C */

/* C comments
/* do not
nest
*/

// C++/Java also has
// single-line comments
```

# **Basic Types and Expressions**

```
# 42 + 17;;
-: int = 59
# 42.0 +. 18.3;;
- : float = 60.3
# 42 + 60.3;;
Error: This expression has type
float but an expression was
expected of type int
# 42 + int of float 60.3;;
-: int = 102
# true || (3 > 4) && not false;;
- : bool = true
# "Hello " ^ "World!";;
- : string = "Hello World!"
# String.contains "Hello" 'o';;
- : bool = true
# ();;
-: unit = ()
# print_endline "Hello World!";;
Hello World!
- : unit = ()
```

Integers

Floating-point numbers

Floating-point operators must be explicit (e.g., +.)

Only explicit conversions, promotions (e.g., int\_of\_float)

**Booleans** 

Strings

The unit type is like "void" in C and Java

# **Standard Operators and Functions**

+ *. /. ** Floating-point arithmetic  ceil floor sqrt exp log log10 cos sin tan acos asin atan  not &&    Boolean operators  = <> Structual comparison (polymorphic)  == != Comparisons (polymorphic)  < > <= >= Comparisons (polymorphic)	+ - * / mod	Integer arithmetic
log log10 cos sin tan acos asin atan  not &&    Boolean operators  = ⇔ Structual comparison (polymorphic)  == != Physical comparison (polymorphic)	+ *. /. **	Floating-point arithmetic
= <> Structual comparison (polymorphic) == != Physical comparison (polymorphic)	log log10 cos sin	Floating-point functions
== != Physical comparison (polymorphic)	not &&	Boolean operators
< > <= >= Comparisons (polymorphic)	-	Structual comparison (polymorphic) Physical comparison (polymorphic)
	< > <= >=	Comparisons (polymorphic)

# Structural vs. Physical Equality

# ==, != Physical equality compares pointers

```
# 1 == 3;;
- : bool = false
# 1 == 1;;
- : bool = true
# 1.5 == 1.5;;
- : bool = false (* Huh? *)
# let f = 1.5 in f == f;;
- : bool = true
# "a" == "a";;
- : bool = false (* Huh? *)
# let a = "hello" in a == a;;
- : bool = true
```

# =, <> Structural equality compares values

```
# 1 = 3;;
-: bool = false

# 1 = 1;;
-: bool = true

# 1.5 = 1.5;;
-: bool = true

# let f = 1.5 in f = f;;
-: bool = true

# "a" = "a";;
-: bool = true
```

Use structural equality to avoid headaches

#### If-then-else

#### if expr then expr else expr

3

If-then-else in OCaml is an expression. The else part is compulsory, expr<sub>1</sub> must be Boolean, and the types of expr<sub>2</sub> and expr<sub>3</sub> must match.

```
# if 3 = 4 then 42 else 17;;
- : int = 17
# if "a" = "a" then 42 else 17;;
- : int = 42
# if true then 42 else "17";;
This expression has type string but is here used with type int
```

# Naming Expressions with let

**let**  $name = expr_1$  **in**  $expr_2$  Bind name to  $expr_1$  in  $expr_2$  only

**let** name = expr

Bind name to expr forever after

```
# let x = 38 in x + 4;
 -: int = 42
# let x = (let y = 2 in y + y) * 10 in x;;
-: int = 40
# x + 4;;
Unbound value x
# let x = 38::
val x : int = 38
# x + 4;;
-: int = 42
# let x = (let y = 2) * 10 in x;;
Error: Syntax error: operator expected.
# let x = 10 in let y = x;
Error: Syntax error
```

# Let is Not Assignment

Let can be used to bind a succession of values to a name. This is not assignment: the value disappears in the end.

```
# let a = 4 in
  let a = a + 2 in
  let a = a * 2 in
  a;;
- : int = 12

# a;;
Unbound value a
```

This looks like sequencing, but it is really data dependence.

# Let is Really Not Assignment

OCaml picks up the values in effect where the function (or expression) is defined.

Global declarations are not like C's global variables.

```
# let a = 5;
val a : int = 5
# let adda x = x + a;
val adda : int -> int = <fun>
# let a = 10;; (* a here is a diff var (copy) *)
val a : int = 10
# adda 0;;
-: int = 5
           (* adda sees a = 5 *)
# let adda x = x + a;;
val adda : int -> int = <fun>
# adda 0;;
-: int = 10
                      (* adda sees a = 10 *)
```

# **Functions**

#### **Functions**

A function is just another type whose value can be defined with an expression.

```
# fun x -> x * x;;
- : int -> int = <fun>
# (fun x -> x * x) 5;; ( function application
-: int = 25
# fun x -> (fun y -> x * y);;
-: int \rightarrow int \rightarrow int = \langle fun \rangle
# fun x y -> x y*; sh*orthand* )
-: int \rightarrow int \rightarrow int = \langle fun \rangle
# (fun x -> (fun y -> (x+1) * y)) 3 5;;
-: int = 20
# let square = fun x \rightarrow x * x;
val square : int -> int = <fun>
# square 5::
-: int = 25
# let square x = x  *x;; ( shorthand *)
val square : int -> int = <fun>
# square 6;;
-: int = 36
```

# Let is Like Function Application

```
let name = expr_1 in expr_2
(fun name -> expr_2) expr_1
```

Both mean "expr , with name replaced by expr "  $_{1}$ 

```
# let a = 3 in a + 2;;

-: int = 5

# (fun a -> a + 2) 3;;

-: int = 5
```

Semantically equivalent; let is easier to read

#### **Recursive Functions**

#### **OCaml**

```
let rec gcd a b =
  if a = b then
    a
  else if a > b then
    gcd (a - b) b
  else
    gcd a (b - a)
```

```
C/C++/Java
int gcd(int a, int b)
{
  while (a != b) {
    if (a > b)
        a -= b;
    else
        b -= a;
  }
  return a;
}
```

let rec allows for recursion

Use recursion instead of loops

Tail recursion runs efficiently in OCaml

#### **Recursive Functions**

By default, a name is not visible in its defining expression.

```
# let fac n = if n < 2 then 1 else n * \underline{\text{fac}} (n-1);;
Unbound value fac
```

The rec keyword makes the name visible.

```
# let rec fac n = if n < 2 then 1 else n * fac (n-1);;
val fac : int -> int = <fun>
# fac 5;;
- : int = 120
```

The and keyword allows for mutual recursion.

# First-Class and Higher Order Functions

First-class functions: name them, pass them as arguments

```
# let appadd = fun f -> (f 42) + 17;;
val appadd : (int -> int) -> int = <fun>

# let plus5 x = x + 5;;
val plus5 : int -> int = <fun>

# appadd plus5;;
- : int = 64
```

#### Higher-order functions: functions that return functions

```
# let makeInc i = fun x -> x + i;;
val makeInc : int -> int -> int = <fun>
# let i5 = makeInc 5;;
val i5 : int -> int = <fun>
# i5 10;;
- : int = 15
```

# Tuples, Lists, and Pattern Matching

#### **Tuples**

Pairs or tuples of different types separated by commas.

Very useful lightweight data type, e.g., for function arguments.

```
# (42, "Arthur");;
- : int * string = (42, "Arthur")
# (42, "Arthur", "Dent");;
-: int string string = (42, "Arthur", "Dent")
# let p = (42, "Arthur");;
val p: int * string = (42, "Arthur")
# fst p;;
-: int = 42
# snd p::
- : string = "Arthur"
# let trip = ("Douglas", 42, "Adams");;
val trip : string * int * string = ("Douglas", 42, "Adams")
# let (fname, , Iname) = trip in (Iname, fname);;
- : string string = ("Adams", "Douglas")
```

## Lists

```
(* Literals *)
                (* The empty list *)
[];;
[1];;
               (* A singleton list *)
                 (* A list of two integers *)
[42; 16];;
(* cons: Put something at the beginning *)
7 :: [5; 3];; (* Gives [7; 5; 3] *)
[1; 2] :: [3; 4];; (* BAD: type error *)
(* concat: Append a list to the end of another *)
[1; 2] @ [3; 4];; (* Gives [1; 2; 3; 4] *)
(* Extract first entry and remainder of a list *)
List.hd [42; 17; 28];; (* = 42 *)
List.tl [42; 17; 28];; (* = [17; 28] *)
```

The elements of a list must all be the same type.

:: is very fast; @ is slower—O(n)

Pattern: create a list with cons, then use *List.rev*.

#### Some Useful List Functions

#### Three great replacements for loops:

- List.map f [a1; ...;an] = [f a1; ...;f an]

  Apply a function to each element of a list to produce another list.
- ¡ List.fold\_left f a [b1; ...;bn] =
   f (...(f (f a b1) b2)...) bn

Apply a function to a partial result and an element of the list to produce the next partial result.

- List.iter f [a1; ...;an] =
  begin f a1; ...; f an; () end
  Apply a function to each element of a list; produce a
  unit result.
- ¡ List.rev [a1; ...; an] = [an; ... ;a1]

  Reverse the order of the elements of a list.

# List Functions Illustrated

```
# List.map (fun a -> a + 10) [42; 17; 128];;
-: int list = [52; 27; 138]
# List.map string_of_int [42; 17; 128];;
- : string list = ["42"; "17"; "128"]
# List.fold_left (fun s e -> s + e) 0 [42; 17; 128];;
-: int = 187
# List.iter print_int [42; 17; 128];;
4217128 - : unit = ()
# List.iter (fun n -> print int n; print newline ())
    [42; 17; 128];;
42
17
128
- : unit = ()
# List.iter print_endline (List.map string_of_int [42; 17; 128]);;
42
17
128
- : unit = ()
```

# **Example: Enumerating List Elements**

To transform a list and pass information between elements, use List.fold\_left with a tuple:

Result accumulated in the (I, n) tuple, List.rev reverses the result (built backwards) in the end. Can do the same with a recursive function, but List.fold\_left separates list traversal from modification:

```
# let rec enum (l, n) = function
[] -> List.rev l
| e::tl -> enum ((e, n)::l, n+1) tl
in
enum ([], 0) [42; 17; 128];;
- : (int * int) list = [(42, 0); (17, 1); (128, 2)]
```

# Pattern Matching

A powerful variety of multi-way branch that is adept at picking apart data structures. Unlike anything in C/C++/Java.

A name in a pattern matches anything and is bound when the pattern matches. Each may appear only once per pattern.

## Case Coverage

The compiler warns you when you miss a case or when one is redundant (they are tested in order):

```
# let xor p = match p
  with (false, x) -> x
      | (x, true) -> not x;;
Warning P: this pattern-matching is not exhaustive.
Here is an example of a value that is not matched:
(true, false)
val xor : bool * bool -> bool = <fun>
# let xor p = match p
  with (false, x) -> x
      | (true, x) -> not x
      (false, false) -> false;;
Warning U: this match case is unused.
val xor : bool * bool -> bool = <fun>
```

#### Wildcards

Underscore (\_) is a wildcard that will match anything, useful as a default or when you just don't care.

```
# let xor p = match p
  with (true, false) | (false, true) -> true
      | _ -> false;;
val xor : bool * bool -> bool = <fun>
# xor (true, true);;
- : bool = false
# xor (false, false);;
- : bool = false
# xor (true, false);;
- : bool = true
# let logand p = match p
  with (false, _) -> false
      | (true, x) -> x;;
val logand : bool * bool -> bool = <fun>
# logand (true, false);;
- : bool = false
# logand (true, true);;
- : bool = true
```

## Pattern Matching with Lists

```
# let length = function ( let length = fun p -> match p with
     [] -> "empty"
  | [ ] -> "singleton"
  | [_; _] -> "pair"
  | [_; _; _] -> "triplet"
  | hd :: tl -> "many";;
val length: 'a list -> string = <fun>
# length [];;
- : string = "empty"
# length [1; 2];;
- : string = "pair"
# length ["foo"; "bar"; "baz"];;
- : string = "triplet"
# length [1; 2; 3; 4];;
- : string = "many"
```

# Pattern Matching with when and as

The when keyword lets you add a guard expression:

The as keyword lets you name parts of a matched structure:

```
# match ((3,9), 4) with

(_ as xx, 4) -> xx

| _ -> (0,0);;

- : int * int = (3, 9)
```

# Application: Length of a list

```
let rec length I =
  if I = [] then 0 else 1 + length (List.tl I);;
```

Correct, but not very elegant. With pattern matching,

```
let rec length = function
[] -> 0
| _::tl -> 1 + length tl;;
```

Elegant, but inefficient because it is not tail-recursive (needs O(n) stack space). Common trick: use an argument as an accumulator.

```
let length I =
  let rec helper len = function
      [] -> len
      | _::tl -> helper (len + 1) tl
  in helper 0 l
```

This is the code for the List.length standard library function.

# OCaml Can Compile This Efficiently

#### OCaml source code

```
let length list =
  let rec helper len = function
    []    -> len
    | _::tl -> helper (len + 1) tl
  in helper 0 list
```

- This is a registers
- Pattern matching reduced to a conditional branch
- Tail recursion implemented with jumps
- LSB of an integer always 1

# ocamlopt generates this x86 assembly

```
camlLength helper:
.1101:
  cmpl $1, %ebx
                        # empty?
 ie .L100
  movl 4(%ebx), %ebx # get tail
  addl $2. %eax # len++
  ami
        .1101
.1100:
  ret
camlLength_length:
  movl %eax, %ebx
  movl $camlLength 2, %eax
  movl $1, %eax # len = 0
 jmp
        camlLength helper
```

# **User-Defined Types**

### Type Declarations

A new type name is defined globally. Unlike let, type is recursive by default, so the name being defined may appear in the typedef.

Mutually-recursive types can be defined with and.

```
\begin{array}{ll} \text{type name}_1 = \text{typedef}_1 \\ \text{and name}_{\ \ \overline{\mathcal{F}}} \ \text{typedef}_{\ \ 2} \\ & \vdots \\ \text{and name}_n = \text{typedef}_n \end{array}
```

#### Records

OCaml supports records much like C's structs.

```
# type base = { x : int; y : int; name : string };;
type base = { x : int; y : int; name : string; }
# let b0 = \{ x = 0; y = 0; name = "home" \};
val b0 : base = \{x = 0; y = 0; name = "home"\}
# let b1 = { b0 with x = 90; name = "first" };;
val b1 : base = \{x = 90; y = 0; name = "first"\}
# let b2 = { b1 with y = 90; name = "second" };;
val b2 : base = \{x = 90: v = 90: name = "second"\}
# b0.name;;
- : string = "home"
# let dist b1 b2 =
     let hyp x y = sqrt (float_of_int (x x + y y)) *n
     hyp (b1.x - b2.x) (b1.y - b2.y);
val dist : base -> base -> float = <fun>
# dist b0 b1::
- : float = 90.
# dist b0 b2::
                                                                                 38
-: float = 127.279220613578559
```

# Algebraic Types/Tagged Unions/Sum-Product Types

Vaguely like C's unions, enums, or a class hierarchy: objects that can be one of a set of types. In compilers, great for trees and instructions.

```
# type seasons = Winter | Spring | Summer | Fall;;
type seasons = Winter | Spring | Summer | Fall
# let weather = function
    Winter -> "Too Cold"
  | Spring -> "Too Wet"
  | Summer -> "Too Hot"
  | Fall -> "Too Short";;
val weather : seasons -> string = <fun>
# weather Spring;;
- : string = "Too Wet"
# let year = [Winter; Spring; Summer; Fall] in
  List.map weather year;;
- : string list = ["Too Cold"; "Too Wet"; "Too Hot"; "Too Short"]
```

# Simple Syntax Trees and an Interpreter

```
# type expr =
    Lit of int
  | Plus of expr * expr
  | Minus of expr * expr
  | Times of expr * expr;;
type expr =
    Lit of int
  | Plus of expr * expr
  | Minus of expr * expr
  | Times of expr * expr
# let rec eval = function
    Lit(x) \rightarrow x
  | Plus(e1, e2) -> (eval e1) + (eval e2)
  | Minus(e1, e2) -> (eval e1) - (eval e2)
  val eval : expr -> int = <fun>
# eval (Lit(42));;
-: int = 42
# eval (Plus(Lit(17), Lit(25)));;
-: int = 42
# eval (Plus(Times(Lit(3), Lit(2)), Lit(1)));;
-: int = 7
                                                                          40
```

# Algebraic Type Rules

#### Each tag name must begin with a capital letter

```
# let bad1 = left | right;;
Syntax error
```

# Tag names must be globally unique (required for type inference)

```
# type weekend = Sat | Sun;;

type weekend = Sat | Sun

# type days = Sun | Mon | Tue;;

type days = Sun | Mon | Tue

# function Sat -> "sat" | Sun -> "sun";;

This pattern matches values of type days
but is here used to match values of type weekend
```

# Algebraic Types and Pattern Matching

The compiler warns about missing cases:

```
# type expr =
    Lit of int
  | Plus of expr * expr
  | Minus of expr * expr
  Times of expr * expr;;
type expr =
    Lit of int
  | Plus of expr * expr
  | Minus of expr * expr
  | Times of expr * expr
# let rec eval = function
    Lit(x) \rightarrow x
 | Plus(e1, e2) -> (eval e1) + (eval e2)
| Minus(e1, e2) -> (eval e1) - (eval e2);;
Warning P: this pattern-matching is not exhaustive.
Here is an example of a value that is not matched:
Times (,)
val eval : expr -> int = <fun>
```

## The Option Type: A Safe Null Pointer

Part of the always-loaded core library:

```
type 'a option = None | Some of 'a
```

This is a polymorphic algebraic type: 'a is any type. None is like a null pointer; Some is a non-null pointer. The compiler requires None to be handled explicitly.

```
# let rec sum = function
[] -> 0 (* base case *)
| None::tl -> sum tl (* handle the "null pointer" case *)
| Some(x)::tl -> x + sum tl;; (* normal case *)
val sum : int option list -> int = <fun>
# sum [None; Some(5); None; Some(37)];;
- : int = 42
```

# Algebraic Types vs. Classes and Enums

	Algebraic Types	Classes	Enums
Choice of Types	fixed	extensible	fixed
Operations	extensible	fixed	extensible
Fields	ordered	named	none
Hidden fields	none	supported	none
Recursive	yes	yes	no
Inheritance	none	supported costly	none
Case splitting	simple		simple

An algebraic type is best when the set of types rarely change but you often want to add additional functions. Classes are good in exactly the opposite case.

# **Modules and Compilation**

#### **Modules**

Each source file is a module and everything is public.

# foo.ml (\* Module Foo \*) type t = { x : int ; y : int } let sum c = c.x + c.y

#### To compile and run these,

```
$ ocamlc -c foo.ml
(creates foo.cmi foo.cmo)
$ ocamlc -c bar.ml
(creates bar.cmi bar.cmo)
$ ocamlc -o ex foo.cmo bar.cmo
$ ./ex
333
```

#### bar.ml

```
(* The dot notation
let v = \{ Foo.x = 1 ;
            Foo.y = 2 };;
print_int (Foo.sum v)
(* Create a short name
module F = Foo;;
print int (F.sum v)
(* Import every name from
   a module with "open"
open Foo;;
print_int (sum v)
```

#### Separating Interface and Implementation

#### stack.mli

```
type 'a t
exception Empty
val create: unit -> 'a t
val push : 'a -> 'a t -> unit
val pop : 'a t -> 'a
val top : 'a t -> 'a
val clear: 'a t -> unit
val copy: 'a t -> 'a t
val is empty: 'a t -> bool
val length: 'a t -> int
val iter : ('a -> unit) ->
                      'a t -> unit
```

#### stack.ml

```
type 'a t =
   { mutable c : 'a list }
exception Empty
let create () = \{c = []\}
let clear s = s.c <- []
let copy s = \{ c = s.c \}
let push x s = s.c <- x :: s.c
let pop s =
  match s.c with
     hd::tl -> s.c <- tl; hd
  | [] -> raise Empty
let top s =
  match s.c with
     hd::_ -> hd
   | [] -> raise Empty
let is_empty s = (s.c = [])
let length s = List.length s.c
let iter f s = List.iter f s.c.
```

# A Complete Interpreter in Three Slides

#### The Scanner and AST

#### scanner.mll

#### ast.mli

```
type operator = Add | Sub | Mul | Div

type expr =
Binop of expr * operator * expr
| Lit of int
```

#### The Parser

#### parser.mly

```
%{ open Ast %}
%token PLUS MINUS TIMES DIVIDE EOF
%token <int> LITERAL
%left PIUS MINUS
%left TIMES DIVIDE
%start expr
%type <Ast.expr> expr
%%
expr:
  expr PLUS expr { Binop($1, Add, $3) }
expr MINUS expr { Binop($1, Sub, $3) }
 expr TIMES expr { Binop($1, Mul, $3) }
 expr DIVIDE expr { Binop($1, Div, $3) }
 LITERAL
                       { Lit($1) }
```

### The Interpeter

#### calc.ml

```
open Ast
let rec eval = function
     Lit(x) \rightarrow x
  | Binop(e1, op, e2) ->
        let v1 = eval e1 and v2 = eval e2 in
       match op with
          Add \rightarrow v1 + v2
        | Sub -> v1 - v2
        | Mul -> v1 * v2
        | Div -> v1 / v2
let =
  let lexbuf = Lexing.from_channel stdin in
  let expr = Parser.expr Scanner.token lexbuf in
  let result = eval expr in
  print endline (string of int result)
```

### Compiling the Interpreter

```
S ocamilex scanner.mll # create scanner.ml
8 states, 267 transitions, table size 1116 bytes
$ ocamlyacc parser.mly # create parser.ml and parser.mli
$ ocamlc -c ast.mli # compile AST types
$ ocamle -c parser.mli # compile parser types
$ ocamle -c scanner.ml # compile the scanner
$ ocamlc -c parser.ml # compile the parser
$ ocamlc -c calc.ml # compile the interpreter
$ ocamle -o cale parser.cmo scanner.cmo cale.cmo
$ ./calc
2 * 3 + 4 * 5
26
$
```

# Compiling with ocambuild

```
$ Is
ast.mli calc.ml parser.mly scanner.mll
$ ocambuild calc.native # Build everything
Finished, 15 targets (0 cached) in 00:00:00.
$ Is
ast.mli build calc.ml calc.native parser.mly scanner.mll
$ ./calc.native
2 * 3 + 4 * 5
Ctrl-D
26
$ ocambuild -clean # Remove build and all .native
```

# Exceptions; Directed Graphs

### **Exceptions**

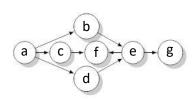
```
# 5 / 0;;
Exception: Division_by_zero.
# try
    5 / 0
  with Division_by_zero -> 42;;
-: int = 42
# exception My_exception;;
exception My exception
# try
    if true then
         raise My exception
    else 0
  with My exception -> 42;;
-: int = 42
```

#### **Exceptions**

```
# exception Foo of string;;
exception Foo of string
# exception Bar of int * string;;
exception Bar of int * string
\# let ex b =
  try
    if b then
       raise (Foo("hello"))
     else
       raise (Bar(42, " answer"))
  with Foo(s) -> "Foo: " ^ s
  | Bar(n, s) -> "Bar: " ^ string of int n ^ s;;
val ex : bool -> unit = <fun>
# ex true;;
- : string = "Foo: hello"
# ex false;;
- : string = "Bar: 42 answer"
```

## Application: Directed Graphs

```
let edges = [
  ("a", "b"); ("a", "c");
  ("a", "d"); ("b", "e");
  ("c", "f"); ("d", "e");
  ("e", "f"); ("e", "g") ]
let rec successors n = function
                           -> []
  | (s, t) :: edges ->
       if s = n then
            t :: successors n edges
        else
            successors n edges
```



```
# successors "a" edges;;
- : string list = ["b"; "c"; "d"]
# successors "b" edges;;
- : string list = ["e"]
```

#### **More Functional Successors**

```
let rec successors n = function

[] -> []

[ (s, t) :: edges ->

if s = n then

t :: successors n edges

else

successors n edges
```

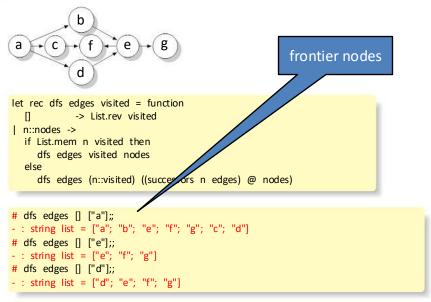
Our first example is imperative: performs "search a list," which is more precisely expressed using the library function List.filter:

```
let successors n edges =
let matching (s,_) = s = n in
List.map snd (List.filter matching edges)
```

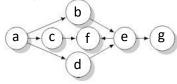
This uses the built-in snd function, which is defined as

```
let snd (_,x) = x
```

## **Depth-First Search**



#### **Topological Sort**



#### Remember the visitor at the end.

```
# tsort edges [] ["a"];;
- : string list = ["a"; "d"; "c"; "b"; "e"; "g"; "f"]

# let cycle = [ ("a", "b"); ("b", "c"); ("c", "a") ];;
val cycle : (string * string) list = [("a", "b"); ...]
# tsort cycle [] ["a"];;
Stack overflow during evaluation (looping recursion?).
```

### **Better Topological Sort**

```
# tsort edges "a";;
- : string list = ["a"; "d"; "c"; "b"; "e"; "g"; "f"]

# tsort edges "d";;
- : string list = ["d"; "e"; "g"; "f"]

# tsort cycle "a";;

Exception: Cyclic "a".
```

# **Standard Library Modules**

#### Maps

Balanced trees for implementing dictionaries. Ask for a map with a specific kind of key; values are polymorphic.

```
# module StringMap = Map.Make(String)::
module StringMap:
  sig
    type key = String.t
    type 'a t = 'a Map.Make(String).t
    val empty: 'a t
    val is empty: 'a t -> bool
    val add : key -> 'a -> 'a t -> 'a t
    val find : key -> 'a t -> 'a
    val remove : key -> 'a t -> 'a t
    val mem : key -> 'a t -> bool
    val iter: (key -> 'a -> unit) -> 'a t -> unit
    val map : ('a -> 'b) -> 'a t -> 'b t
    val mapi : (key -> 'a -> 'b) -> 'a t -> 'b t
    val fold : (key -> 'a -> 'b -> 'b) -> 'a t -> 'b -> 'b
    val compare : ('a -> 'a -> int) -> 'a t -> 'a t -> int
    val equal : ('a -> 'a -> bool) -> 'a t -> 'a t -> bool
  end
```

#### Maps

```
# let mymap = StringMap.empty;;
                                                   (* Create empty map
                                                                            *)
val mymap : 'a StringMap.t = <abstr>
# let mymap = StringMap.add "Douglas" 42 mymap;; ( Add pair*
                                                                            *)
val mymap : int StringMap.t = <abstr>
# StringMap.mem "foo" mymap;;
                                                    (* Is "foo" there?
                                                                            *)
- : bool = false
# StringMap.mem "Douglas" mymap;;
                                               (* Is "Douglas" there?
                                                                            *)
- : bool = true
                                                            (* Get value
# StringMap.find "Douglas" mymap;;
                                                                            *)
-: int = 42
# let mymap = StringMap.add "Adams" 17 mymap;;
val mymap : int StringMap.t = <abstr>
# StringMap.find "Adams" mymap;;
-: int = 17
# StringMap.find "Douglas" mymap;;
-: int = 42
# StringMap.find "Slarti" mymap;;
Exception: Not_found.
```

# Maps

- Fully functional: Map.add takes a key, a value, and a map and returns a new map that also includes the given key/value pair.
- Needs a totally ordered key type. Pervasives.compare usually does the job (returns –1, 0, or 1); you may supply your own.

```
module StringMap = Map.Make(struct
type t = string
let compare x y = Pervasives.compare x y
end)
```

Uses balanced trees, so searching and insertion is O(logn).

#### Depth-First Search Revisited

#### Previous version

```
let rec dfs edges visited = function

[] -> List.rev visited

| n::nodes ->

if L st.mem n isited then

dfs edges visited nodes

else

dfs edges (n::visited) ((successors n edges) @ nodes)
```

was not very efficient, but good enough for small graphs.

Would like faster visited test and successors query.

### Depth-First Search Revisited

#### Second version:

- i use a Map to hold a list of successors for each node
- ; use a Set (valueless Map) to remember of visited nodes

```
module StringMap = Map.Make(String)
module StringSet = Set.Make(String)
```

# Depth-First Search Revisited

```
let top sort map edges =
  (* Create an empty successor list for each node
                                                                   *)
  let succs = List.fold_left
        (fun map (s,d) ->
          StringMap.add d [] (StringMap.add s [] map)
        ) StringMap.empty edges
  in
  (* Build the successor list for each source node
  let succs = List.fold left
        (fun succs (s, d) ->
          let ss = StringMap.find s succs
          in StringMap.add s (d::ss) succs) succs edges
  in
  (* Visit recursively, storing each node after visiting successors
  let rec visit (order, visited) n =
     if StringSet.mem n visited then
        (order, visited)
     else
        let (order, visited) = List.fold left
             visit (order, StringSet.add n visited)
             (StringMap.find n succs)
        in (n::order, visited)
  in
    (* Visit the source of each edge
  fst (List.fold left visit ([], StringSet.empty) (List.map fst edges)
```

# Imperative Features

```
(* ";" means sequencing *)
# 0 ; 42;;
Warning S: this expression should have type unit.
-: int = 42
# ignore 0 ; 42;;
                        (* ignore is a function: 'a -> unit *)
-: int = 42
# () : 42::
                   (* () is the literal for the unit type *)
-: int = 42
# print_endline "Hello World!";; (* Print; result is unit *)
Hello World!
-: unit =()
# print_string "Hello " ; print_endline "World!";;
Hello World!
- : unit = ()
# print_int 42 ; print_newline ();;
42
-: unit =()
# print_endline ("Hello " ^ string_of_int 42 ^ " world!");;
Hello 42 world!
-: unit =()
```

#### **Hash Tables**

```
# module StringHash = Hashtbl.Make(struct
    type t = string
                                            (* type of keys *)
    let equal x y = x = y (* use structural comparison *)
    let hash = Hashtbl.hash
                                  (* generic hash function *)
  end);;
module StringHash:
  sig
    type key = string
   type 'a t
   val create : int -> 'a t
   val clear : 'a t -> unit
   val copy : 'a t -> 'a t
   val add : 'a t -> key -> 'a -> unit
   val remove : 'a t -> key -> unit
   val find : 'a t -> kev -> 'a
    val find_all : 'a t -> key -> 'a list
   val replace : 'a t -> kev -> 'a -> unit
   val mem : 'a t -> kev -> bool
   val iter : (key -> 'a -> unit) -> 'a t -> unit
   val fold: (key -> 'a -> 'b -> 'b) -> 'a t -> 'b -> 'b
   val length : 'a t -> int
  end
```

#### **Hash Tables**

```
# let hash = StringHash.create 17;; (* initial size estimate *)
val hash : '_a StringHash.t = <abstr>
# StringHash.add hash "Douglas" 42;; (* modify the hash table *)
-: unit =()
# StringHash.mem hash "foo";;
                                           (* is "foo" there? *)
- : bool = false
# StringHash.mem hash "Douglas";; (* is "Douglas" there? *)
- : bool = true
# StringHash.find hash "Douglas";;
                                                (* Get value *)
-: int = 42
# StringHash.add hash "Adams" 17;; (* Add another key/value *)
-: unit =()
# StringHash.find hash "Adams";;
-: int = 17
# StringHash.find hash "Douglas";;
-: int = 42
# StringHash.find hash "Slarti";;
Exception: Not_found.
```

#### **Arrays**

```
# let a = [| 42; 17; 19 |];;
                                           (* Array literal *)
val a : int array = [|42; 17; 19|]
# let aa = Array.make 5 0;;
                                        (* Fill a new array *)
val aa : int array = [|0; 0; 0; 0; 0|]
# a.(0);;
                                           (* Random access *)
-: int = 42
# a.(2);;
-: int = 19
\# a.(3);;
Exception: Invalid_argument "index out of bounds".
# a.(2) <- 20;;
                                     (* Arrays are mutable! *)
-: unit =()
# a;;
-: int array = [|42; 17; 20|]
# let 1 = [24; 32; 17];;
val 1 : int list = [24; 32; 17]
# let b = Array.of_list l;;
                                       (* Array from a list *)
val b : int array = [|24; 32; 17|]
# let c = Array.append a b;; (* Concatenation *)
val c : int array = [|42; 17; 20; 24; 32; 17|]
```

### Arrays vs. Lists

8	Arrays	Lists	
Random access	O(1)	O(n)	prepend
Appending	O(n)	O(1)	
Mutable	Yes	No	

Useful pattern: first collect data of unknown length in a list then convert it to an array with Array.of\_list for random queries.

#### **DFS** with Arrays

Second version used a lot of mem, find, and add calls on the string map, each O(logn). (Total: O(nlogn) at least.) Can we do better?

Solution: use arrays to hold adjacency lists and track visiting information.

Basic idea: number the nodes, build adjacency lists with numbers, use an array for tracking visits, then transform back to list of node names.

# DFS with Arrays 1/2

```
let top sort array edges =
  (* Assign a number to each node
  let map, nodecount =
     List.fold left
       (fun nodemap (s, d) ->
         let addnode node (map, n) =
            if StringMap.mem node map then (map, n)
            else (StringMap.add node n map, n+1)
         in
          addnode d (addnode s nodemap)
       ) (StringMap.empty, 0) edges
  in
  let successors = Array.make nodecount [] in
  let name = Array.make nodecount "" in
                                                                              *)
  (* Build adjacency lists and remember the name of each node
  List.iter
     (fun (s. d) ->
       let ss = StringMap.find s map in
       let dd = StringMap.find d map in
       successors.(ss) <- dd :: successors.(ss);
       name.(ss) <- s;
       name.(dd) <- d:
     ) edges;
```

# DFS with Arrays 2/2

```
(* Visited flags for each node
let visited = Array.make nodecount false in
(* Visit each of our successors if we haven't done so yet
(* then record the node *)
let rec visit order n =
  if visited.(n) then order
  else (
    visited.(n) <- true;
    n :: (List.fold left visit order successors.(n))
in
( * Compute the topological order
let order = visit [] 0 in
(* Map node numbers back to node names
List.map (fun n -> name.(n)) order
```