

CSE 3302 Programming Language

Homework2 - Fall 2026

Due Date: Feb.2, 2026, 11:59 PM

Problem1 - 30%

Prove by induction: If $\text{add } n_1 \ n_2 \ n_3$, then $\text{add } n_2 \ n_1 \ n_3$ (the commutative law of addition), where $\text{add } n_1 \ n_2 \ n_3$ is the judgment form for addition defined in the lecture (slide page 23).

(Hint: You may begin by proving the following lemma: If $n \text{ nat}$, then $\text{add } n \ Z \ n$.)

Problem2 - 30%

Prove **Lemma 2** using *induction on the derivation of* $\text{len } l \ n$, instead of *append*. (slide page 35).

Problem3 - 40%

- (a) Give an inductive definition of the judgment form $\text{leq } n_1 \ n_2$, which indicates that n_1 is less than or equal to n_2 , and n_1 and n_2 are defined by judgement form $n \text{ nat}$ in the lecture.
- (b) Prove by induction: If $n_1 \text{ nat}$, $n_2 \text{ nat}$, $\text{leq } n_1 \ n_2$ and $\text{leq } n_2 \ n_1$, then $n_1 = n_2$.

Submission Format: Submit only the **.pdf** version of your homework (typed submissions are preferred; Scanned images must be readable). File must be named **lastname_studentID_hw2.pdf**.