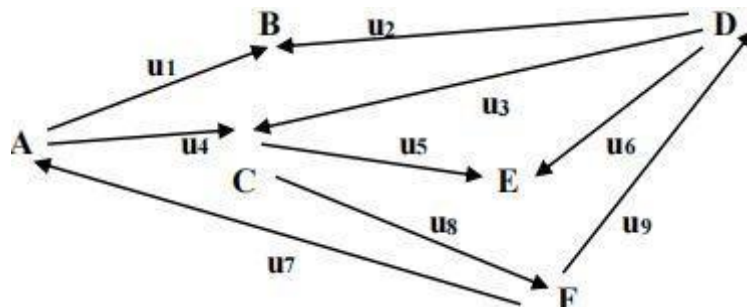


**Exercise1:**

- 1) Let  $G = (X, U)$  be a directed graph with  $X = \{ 1, 2, 3, 4, 5, 6 \}$  and the arcs:  $u_1=(1,2); u_2=(2,3); u_3=(4,3); u_4=(6,4); u_5=(6,5); u_6=(5,1); u_7=(2,5); u_8=(4,2); u_9=(3,5)$  and  $u_{10}=(5,4)$ .

- Plot the graph  $G$ .
- Find the degree of each vertex.
- Give an example of a circuit.

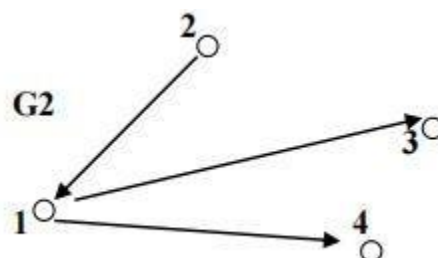
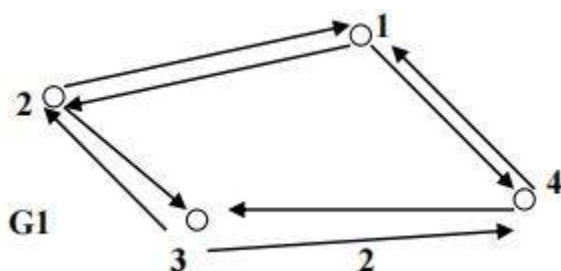
- 2) Let the graph  $G'$  as bellow:



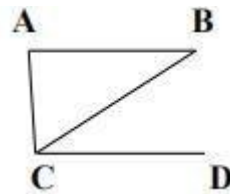
- Is the path:  $\{(AC), (CF), (FD), (DC), (CE)\}$  an elementary path?
  - Is the path:  $\{(AC), (CF), (FA), (AC), (CE)\}$  a simple path?
- 3) From the graph  $G'$ :
- Draw its equivalent undirected graph  $G''=(X, U)$  with  $X=\{ A, B, C, D, E, F \}$  and edges  $u_1; u_2; u_3; u_4; u_5; u_6; u_7; u_8$  and  $u_9$ .
  - Find the degree of each vertex.
  - Give an example of a cycle.
  - Is the chain:  $\{u_4 u_5 u_6 u_9 u_8 u_4\}$  an elementary chain?
  - Is the chain:  $\{u_1 u_2 u_3 u_4 u_7\}$  a simple chain?

**Exercise2:**

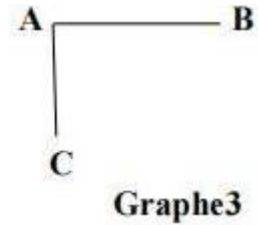
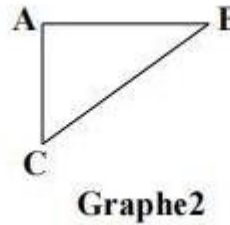
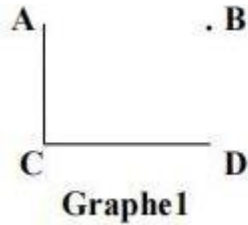
- 1) What is the nature of each graph?



2) Let the undirected graph G be:

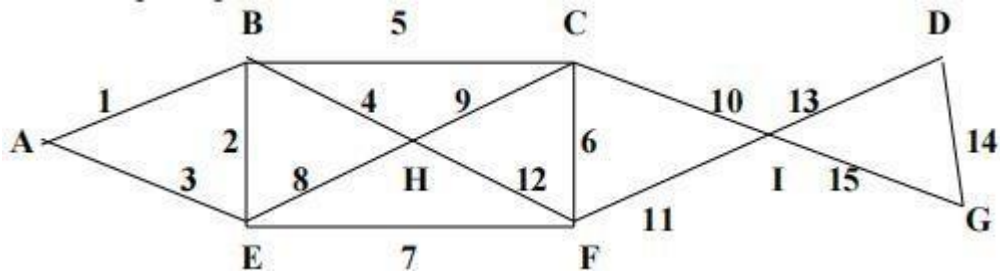


What is the nature of each of the following graphs extracted from G?

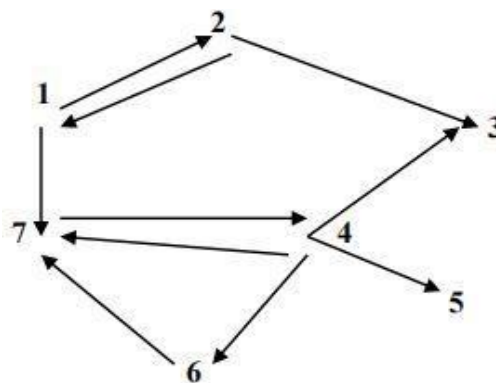


### Exercise3:

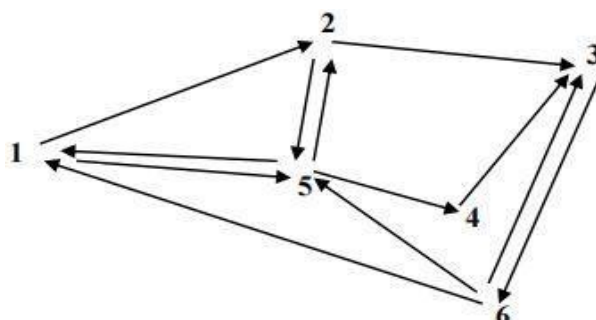
1. Does the following graph admit an Eulerian cycle? If yes, say why and find one?



2. Does the following graph have a Hamiltonian path?



3. Find at least one path and one Hamiltonian circuit in the following graph G':



**Exercise4:**

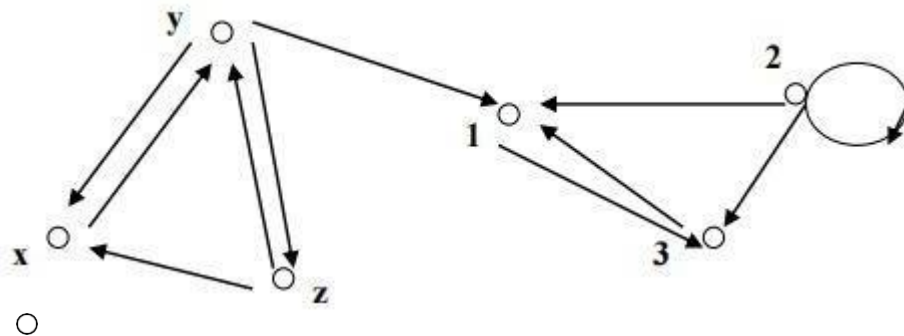
Let  $G$  be an undirected graph of order 10 having 22 edges. It has exactly 5 vertices of degree 3, the others are of degree 4 or 7. How many vertices of degree 4 are there?

**Exercise5:**

1. What is the number of edges of a complete undirected graph  $G = (X, U)$  with  $|X|=n$  and  $|U|=m$ ?

**Exercise6:**

1. Is the following graph a strongly connected graph?



2. Find a reduced graph
3. Show that an undirected, loop-free graph with  $n$  number of vertices and having more than  $(n-1)(n-2)/2$  edges is connected.

**Exercise7:**

1. Propose three different data structures that can be used to represent a graph in a computer's memory.
2. Application to the following graph

