

CS102 – Algorithms and Programming II

Lab Programming Assignment 2

Fall 2016

ATTENTION:

- Feel free to ask questions on Moodle on the Lab Assignment Forum.
- Compress all of the Java program source files (.java) into a single zip file
- The name of the zip file should follow the below convention:
CS102_SecX_Asgn2_YourSurname_YourName.zip
- Replace the variables “YourSurname” and “YourName” with your actual surname and name and X with your Section id (1, 2 or 3).
- Upload the above zip file to Moodle by the deadline before the lab (if not significant points will be taken off). You will get a chance to update and improve your solution by consulting to the TA during the lab. You will resubmit your code once you demo your work to the TA.

GRADING WARNING:

- Please read the grading criteria provided on Moodle.

Q1 [100p.] In this lab, you are going to implement an **Equation** class that represents equations of the form $a = bx + c$

Follow the instructions provided below:

1. Assume a, b and c are integers.
2. Include a constructor that takes the coefficients of the linear equation a, b and c and sets the instance variables accordingly. The constructor should ensure that coefficient b is always non-negative. That is if the b is negative, you should multiply all of the coefficients by -1. For example:

e.g., $-2 = -3x - 1 \Rightarrow 2 = 3x + 1$

3. Include a member method **reduceEquation()** that simplifies the equation. i.e.,

$10 = 5x + 5$ should be stored as $2 = x + 1$

To simplify the coefficients, you should first find the greatest common divisor of them. For example, your values are a, b and c. Let's assume that the $\text{gcd}(a, b, c) = s$. The simplified version of the given equation will be shown as:

$$\frac{a}{s} = \frac{b}{s}x + \frac{c}{s}$$

4. Implement a private **gcd** method that finds the greatest common divisor of two non-negative integers. Mathematically, the gcd of two numbers is defined as the greatest integer that divides both numbers. Use the Euclid's algorithm to implement gcd (See Box 1).

$\text{gcd}(20, 15) = 5$

$\text{gcd}(90, 45) = 45$

$\text{gcd}(8, 3) = 1$

Box 1. Euclid's Algorithm

Euclid's algorithm is a way of calculating the gcd of two numbers. First, let's describe it using an example. We will find the gcd of 36 and 15.

Divide 36 by 15 (the greater by the smaller), getting 2 with a remainder of 6.

Then we divide 15 by 6 (the previous remainder) and we get 2 and a remainder of 3.

Then we divide 6 by 3 (the previous remainder) and we get 2 with no remainder.

The last non-zero remainder (3) is our gcd. Here it is in general:

a/b gives a remainder of r

b/r gives a remainder of s

r/s gives a remainder of t

...

w/x gives a remainder of y

x/y gives no remainder

In this case, y is the gcd of a and b . If the first step produced no remainder, then b (the lesser of the two numbers) is the gcd.

4. Implement a private method `gcd3` that takes three integers and finds their greatest common divisor. This method generalizes the former method `gcd` to three arguments by calling it. **Hint:** Mathematically $\text{gcd}(a,b,c) = \text{gcd}(\text{gcd}(a,b), c)$.

5. Implement two member methods for basic calculations on linear equations.

- **`add(Equation eq2)`** sums two linear equations and return the result as a new equation in a reduced form.
- **`subtract(Equation eq2)`** subtracts `eq2` from the equation for which the method is called on (implicit parameter) and returns the result as an equation in reduced form.

Summation of equations: $(3 = 2x + 1) + (2 = 3x - 1) = (5 = 5x) \Rightarrow (1 = x)$

Subtraction of equations: $(2 = 3x - 4) - (7 = 4x - 1) = (-5 = -x - 3) \Rightarrow (5 = x + 3)$

5. Include a **`toString()`** method that returns a string representation of the equation.

Suppose that the equation format is **$a = bx + c$** .

- If b is 0, then you should return " $a = c$ ".
- If c is 0, then you should return " $a = bx$ ".

6. Implement a class called **`EquationTester`** to test your `Equation` class. You should get the coefficients of the equation from the user on a single line: "2 3 -1".

Example test cases:

```
2431 = 102 x + 595
208 = -368 x + 1276
-7038 = 2646 x + 558
28 = 3 x + 25
```

The expected results:

```
143 = 6 x + 35
-52 = 92 x - 319
-391 = 147 x + 31
28 = 3 x + 25
```

7. Test the addition and subtraction operations. You may prompt the user to enter a, b and c values for two Equation objects. Example input output are given

Sample Runs: (User inputs are shown in **red**.)

```
Enter the value of a, b and c for first equation: 3 2 1
Enter the value of a, b and c for second equation: 2 3 -1
Sum of the equations: 1 = x

Enter the value of a, b and c for first equation: 2 3 -4
Enter the value of a, b and c for second equation: 7 4 -1
Subtraction of the equations: 5 = x + 3
```

IMPORTANT NOTES:

1. Please comment your code according to the documentation and commenting conventions used in the textbook (page 58).