

# CS 240 LAB 4

Finding Factorial in Recursive Way

# Recursive Definition of a Function

To define a function recursively, we should specify

- A rule for constructing new elements of function those can be specified with the function itself (recursive case)
- One or more initial elements of function (base case)
- Recursive calls must move on base condition

# An Example -> Factorial:

- $0! = 1, 1! = 1$  base case
- $n! = n * (n-1)! \text{ for } n > 1$  recursive case
- Thus,  $3 = 3 * 2!$
- $= 3 * 2 * 1!$
- $= 3 * 2 * 1 * 0!$
- $= 3 * 2 * 1 * 1 \quad (= 6)$

# High Level C Code

```
int factorial(int n) {  
    if (n == 0 || n == 1) return 1;  
    return n * factorial(n-1);  
}
```

In another saying;

```
int factorial(int n) {  
    if (n == 0 || n == 1) return 1;  
    int from_stack = factorial(n-1);  
    return n * stack_return;  
}
```

How does recursion work  
inside a computer?

# factorial(3)

- ```
int factorial(int n) {  
  -> if (n == 0 || n == 1) return 1;  
    int from_stack = factorial(n-1);  
    return n * from_stack ;  
}
```

|                                | Address | Value |
|--------------------------------|---------|-------|
| Final Result                   | 20      |       |
| parameter n                    | 300     | 3     |
| result return address          | 301     | 20    |
| return value of factorial(n-1) | 302     |       |

# factorial(3)

- ```
int factorial(int n) {  
    if (n == 0 || n == 1) return 1;  
    ->int from_stack = factorial(n-1);  
    return n * from_stack ;  
}
```

Call factorial(2)

	Address	Value
Final Result	20	
parameter n	300	3
result return address	301	20
return value of factorial(n-1)	302	

# factorial(2)

- ```
int factorial(int n) {  
-> if (n == 0 || n == 1) return 1;  
    int from_stack = factorial(n-1);  
    return n * from_stack ;  
}
```

|                                | Address | Value |
|--------------------------------|---------|-------|
| Final Result                   | 20      |       |
| parameter n                    | 300     | 3     |
| result return address          | 301     | 20    |
| return value of factorial(n-1) | 302     |       |
| parameter n                    | 303     | 2     |
| result return address          | 304     | 302   |
| return value of factorial(n-1) | 305     |       |



# factorial(2)

- ```
int factorial(int n) {  
    if (n == 0 || n == 1) return 1;  
    -> int from_stack = factorial(n-1);  
    return n * from_stack ;  
}
```

Call factorial(1)

	Address	Value
Final Result	20	
parameter n	300	3
result return address	301	20
return value of factorial(n-1)	302	
parameter n	303	2
result return address	304	302
return value of factorial(n-1)	305	

# factorial(1)

- ```
int factorial(int n) {  
-> if (n == 0 || n == 1) return 1;  
    int from_stack = factorial(n-1);  
    return n * from_stack ;  
}
```

STACK UNWIND TIME!

Return to factorial(2)

with 1

|                                | Address | Value |
|--------------------------------|---------|-------|
| Final Result                   | 20      |       |
| parameter n                    | 300     | 3     |
| result return address          | 301     | 20    |
| return value of factorial(n-1) | 302     |       |
| parameter n                    | 303     | 2     |
| result return address          | 304     | 302   |
| return value of factorial(n-1) | 305     | 1     |
| parameter n                    | 306     | 1     |
| result return address          | 307     | 305   |

# factorial(2)

- ```
int factorial(int n) {  
    if (n == 0 || n == 1) return 1;  
    int from_stack = factorial(n-1);  
    ->return n * from_stack ;  
}
```

Return to factorial(3)  
with 2 \* 1

	Address	Value
Final Result	20	
parameter n	300	3
result return address	301	20
return value of factorial(n-1)	302	2
parameter n	303	2
result return address	304	302
return value of factorial(n-1)	305	1
parameter n	306	1
result return address	307	305

# factorial(3)

- ```
int factorial(int n) {  
    if (n == 0 || n == 1) return 1;  
    int from_stack = factorial(n-1);  
    ->return n * from_stack ;  
}
```

Return to main  
with  $3 * 2$

|                                | Address | Value |
|--------------------------------|---------|-------|
| Final Result                   | 20      | 6     |
| parameter n                    | 300     | 3     |
| result return address          | 301     | 20    |
| return value of factorial(n-1) | 302     | 2     |
| parameter n                    | 303     | 2     |
| result return address          | 304     | 302   |
| return value of factorial(n-1) | 305     | 1     |
| parameter n                    | 306     | 1     |
| result return address          | 307     | 305   |

XYZ:

if(.....) goto ABC

goto XYZ

ABC:

if(.....) goto END

goto ABC

END:

goto END

Good Luck 😊