Pairs Trading

MGMT 638: future-Driven Investments: Equity

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Overview

- Find stock pairs that usually track together
- When the relationship is broken:
 - Buy the stock that is cheap compared to the usual relationship
 - Short sell the stock that is expensive compared to the usual relationship
- Hope the usual relationship is restored soon.





Model

- $P_1/P_2 \approx {
 m constant}$
- When the ratio goes above the constant, it tends to come down.
- When the ratio goes below the constant, it tends to go up.

$$\Delta P_1/P_2 = \left\{ egin{array}{ll} + ext{when} \ P_1/P_2 < ext{constant} \ - ext{when} \ P_1/P_2 > ext{constant} \end{array}
ight.$$

-Assume the change is larger when the ratio is further from the constant as

$$\Delta P_1/P_2 = k({
m constant} - P_1/P_2)$$

for a constant k > 0.



• The model is equivalent to

$$\Delta P_1/P_2 = a + bP_1/P_2$$

where $a = k \times \text{constant}$, b = -k.

- Estimate *a* and *b* by linear regression.
- Should get a > 0, b < 0.
- If so, constant = -a/b.
- Hold asset 1 and short 2 when $P_1/P_2 < -a/b {
 m threshold}.$
- Hold asset 2 and short 1 when $P_1/P_2 > -a/b + {
 m threshold}$.

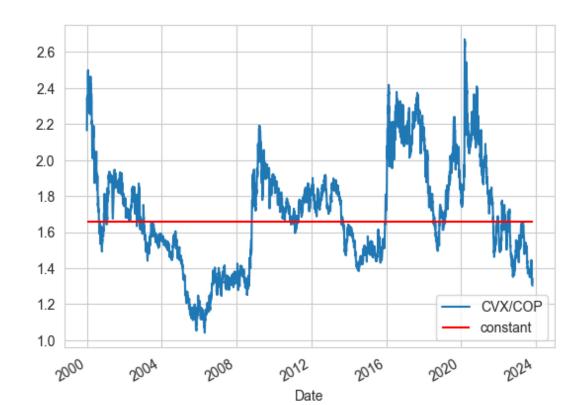
Example

- Chevron (CVX) and Conoco-Phillips (COP) from 2000 on
- Adjusted closing prices from Yahoo Finance
- Compute the price ratio: CVX / COP





```
In [13]: data.ratio.plot(label="CVX/COP")
plt.hlines(
    y=-a/b,
    xmin = data.index[0],
    xmax=data.index[-1],
    color="red",
    label="constant"
)
plt.legend(loc="lower right")
plt.show()
```



Returns

- -a/b = 1.66
- Set threshold = 0.2 as an example
- $\bullet~$ Buy COP and short CVX when CVX / COP is above 1.86
- $\bullet~$ Buy CVX and short COP when CVX / COP is below 1.46





Market Neutrality

- The pairs strategy is an example of a market neutral strategy, meaning its market beta should be approximately zero.
- If it has a return above the risk-free rate, then adding some of it to the market portfolio can improve performance relative to holding the market.
- This is the same as saying that the strategy has a positive alpha.
- It is also the same as saying

Sharpe ratio of strategy > Sharpe ratio of market \times correlation with market

• Get the market return from Ken French's data library.









Avoid Look-Ahead Bias

- ullet Compute the parameter of the strategy (the constant -a/b) from data through 2015
- Test the strategy from 2015 on.





```
In [18]: print(f"mean return of pairs strategy = {252*future.ret.mean():.2%} annualized print(f"correlation of pairs strategy = 6.15% annualized correlation of pairs strategy with market = 10.74%
```





Alpha and Beta

- beta = corr with market excess return x std dev of strategy / std dev of market
- alpha = mean return beta * mean market excess return





```
In [19]: beta = future.ret.corr(future.mkt) * future.ret.std() / future.mkt.std()
    alpha = future.ret.mean() - beta * future.mkt.mean()

    print(f"beta is {beta:.4f}")
    print(f"annualized alpha is {252*alpha:.2%}")

    beta is 0.0011
    annualized alpha is 4.87%
```





Regressions in python

- use statsmodels.formula.api
- smf.ols("model", data).fit().summary()



```
In [20]:
          import statsmodels.formula.api as smf
          smf.ols("ret~mkt", future).fit().summary()
                                 OLS Regression Results
Out[20]:
                                                                        0.012
              Dep. Variable:
                                                      R-squared:
                                           ret
                     Model:
                                          OLS
                                                  Adj. R-squared:
                                                                        0.011
                   Method:
                                 Least Squares
                                                       F-statistic:
                                                                        25.15
                             Wed, 25 Oct 2023
                                               Prob (F-statistic):
                                                                     5.75e-07
                      Time:
                                      12:27:27
                                                  Log-Likelihood:
                                                                       6431.3
          No. Observations:
                                                                  -1.286e+04
                                         2157
                                                            AIC:
                                                             BIC: -1.285e+04
               Df Residuals:
                                         2155
                  Df Model:
           Covariance Type:
                                    nonrobust
                       coef std err
                                          t P>|t|
                                                   [0.025 0.975]
          Intercept 0.0002
                              0.000
                                     0.758
                                                    -0.000
                                            0.448
                                                             0.001
               mkt 0.0011
                               0.000
                                      5.015
                                            0.000
                                                    0.001
                                                             0.002
                Omnibus: 438.977
                                      Durbin-Watson:
                                                            1.951
          Prob(Omnibus):
                              0.000
                                     Jarque-Bera (JB): 11512.699
                    Skew:
                              0.267
                                            Prob(JB):
                                                             0.00
```

Kurtosis:

14.305

Cond. No.

1.20