

# Portfolio Optimization

MGMT 675, AI-Assisted Financial Analysis

Kerry Back, JGSB, Rice University



## Outline for Today

- Download international.xlsx, international\_corrs.xlsx, and us\_developed\_emerging\_rets.xlsx from the Datasets link.
- Examples for frontier and tangency portfolios
  - US, Japan, Germany, France, UK (from Applied Finance)
  - US, Developed, & Emerging (from Applied Finance)
  - ETFs from Yahoo Finance



## Procedure

- Data
  - Upload means, standard deviations, and correlations
  - Or upload returns and calculate historical statistics
  - Or get data online, compute returns, and calculate historical statistics
- Frontier of risky assets
  - Use cvxopt to minimize variance subject to achieving target expected return
- Tangency portfolio
  - Use cvxopt to minimize variance minus risk premium
  - Divide by sum of weights to get tangency portfolio
- Can exclude short sales when using cvxopt for frontier and tangency portfolio
- Can plot assets, frontier, and capital allocation line



## Example 1: Frontier of Risky Assets

- Upload international.xlsx and international\_corrs.xlsx to Julius. Ask Julius to read them.
- Ask Julius to convert the means, standard deviations, and correlation matrix into numpy arrays.
- Ask Julius to compute the covariance matrix as a numpy array.
- Ask Julius to use cvxopt to minimize variance subject to achieving a target expected return.
  - If allowing short sales, tell Julius there are no inequality constraints.
  - If excluding short sales, tell Julius to not allow short sales.
- Ask Julius to repeat for a range of target expected returns and to plot the expected returns and standard deviations.
- Ask Julius to include the expected returns and standard deviations of the country returns in the plot and to label them.



## cvxopt for Frontier Portfolios Allowing Short Sales

- minimize  $(1/2)x'Px$  subject to  $Ax = b$
- $P$  = covariance matrix
  - $x'Px$  is portfolio variance
- $A$  = array with two rows
  - first row = `np.ones(n)`
  - second row = asset expected returns
- $b = \text{np.array}([1, \text{targ}])$ 
  - $Ax = b$  means weights sum to 1 and expected return = targ.
- Julius should figure all of this out. But, Julius might assume you want to exclude short sales.

## cvxopt for Frontier Portfolios Excluding Short Sales

- minimize  $(1/2)x'Px$  subject to  $Ax = b$  and  $Gx \leq h$
- $P$ ,  $A$ , and  $b$  as before
- $G = -\text{np.eye}(n)$  and  $h = \text{np.zeros}(n)$ 
  - $Gx \leq h$  means weights are nonnegative (no shorts)
- Again, Julius should figure this out.

## Example 1: Tangency Portfolio

- Give Julius a number for the risk-free rate.
- Ask Julius to minimize the variance minus the risk premium.
  - If allowing short sales, tell Julius there are no inequality constraints.
  - If excluding short sales, tell Julius to not allow short sales.
- Ask Julius to divide by the sum of the weights to compute the tangency portfolio.
- Ask Julius to include the tangency portfolio and the capital market line on the previous plot.



## cvxopt for Tangency Portfolio

- Minimize  $x'Px - q'x$ 
  - $P = 2$  times covariance matrix (but the 2 is not important)
  - $q =$  risk premia
- No equality constraints
- If no short sales, then  $G = -\text{np.eye}(n)$  and  $h = \text{np.zeros}(n)$
- Then divide by the sum of weights



## Example 2: US, Developed, and Emerging

- Start a new chat.
- Upload `us_developed_emerging_rets.xlsx` and ask Julius to read it.
- Ask Julius to compute the sample means, sample standard deviations and sample correlation matrix as numpy arrays.
- Repeat the frontier and tangency portfolio calculations.



## Online Data

- Julius will normally get some online data without complaining.
  - For example, it will get data from Yahoo Finance and Federal Reserve Economic Data (FRED).
- At other times, Julius will say it has no access to external websites and can only advise.
  - In those cases, it will still produce code that you can run elsewhere.
  - But, it will not be available to debug the code for you.
  - This happens, for example, with the SEC's Edgar site.



## Yahoo's Adjusted Closing Prices

- Yahoo's adjusted closing prices are adjusted for splits and dividends.
- The percent change in the adjusted closing price is the daily close-to-close return including dividends (on ex-dividend dates).
- If we want returns at a different frequency, for example annual returns, then we can either
  - compound the daily returns, or
  - downsample the adjusted closing prices to annual data and compute the percent change of the downsampled data.



## Example 3: ETFs from Yahoo

- Example: ask Julius to use yfinance to get Yahoo adjusted closing prices for
  - SPY = S&P 500
  - VBR = Vanguard small-cap value
  - IEF = Treasury bonds
  - UUP = U.S. dollar bullish
- Ask Julius to downsample prices to end-of-month and compute monthly returns as percent changes in the downsampled prices.
- Ask Julius to compute means, standard deviations, and correlation matrix as numpy arrays.
- Ask Julius to find frontier of risky assets and tangency portfolio as before.

