



MATHEMATICS

GRADE : 10

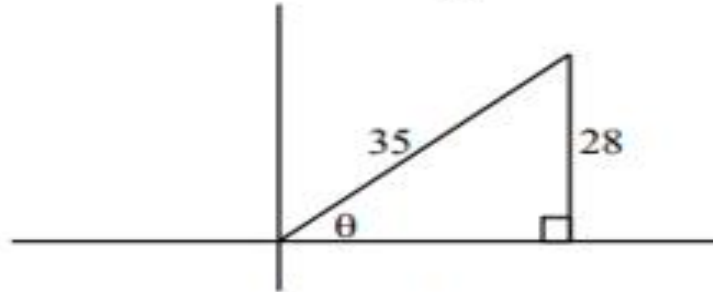
Consoildation

22 October 2021

TRIG 1

QUESTION 3

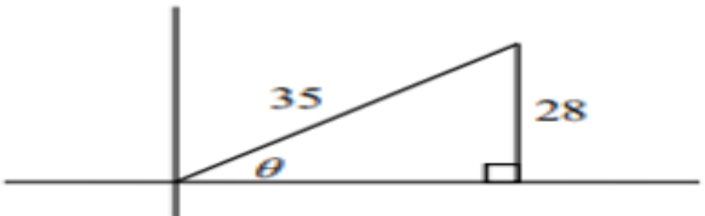
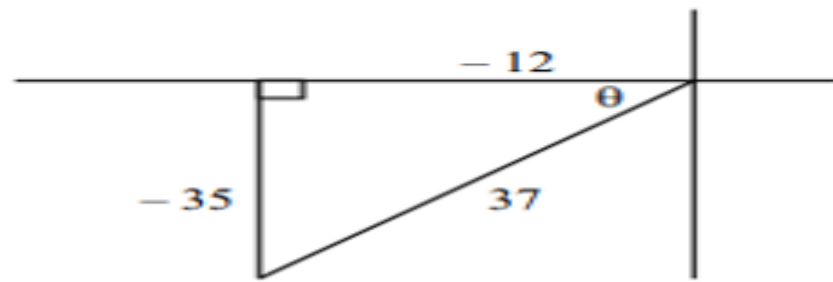
3.1 In the diagram below, the value of $\sin \theta = \frac{28}{35}$



- 3.1.1 Without calculating the value of θ , determine the value of $\cos \theta$. (3)
- 3.1.2 Hence, or otherwise, prove that: $\sin^2 \theta + \cos^2 \theta = 1$ (3)
- 3.2 If $37 \sin \theta + 35 = 0$ and $\tan \theta > 0$, determine with the help of a diagram, the value of $24 \sec \theta - 70 \cot \theta$. (6)
- 3.3 Solve for x , if $x \in [0^\circ; 90^\circ]$. Give your answer correct to 1 decimal place.
- 3.3.1 $8 \cos(x + 10^\circ) = 5$ (3)
- 3.3.2 $\operatorname{cosec} 2x = 2$ (3)
- 3.4 Prove the following without the use of a calculator:
- $$\frac{\sin 30^\circ \times \tan 60^\circ}{\tan 30^\circ \times \cos 60^\circ} = 3 \quad (5)$$

Working area

Solution

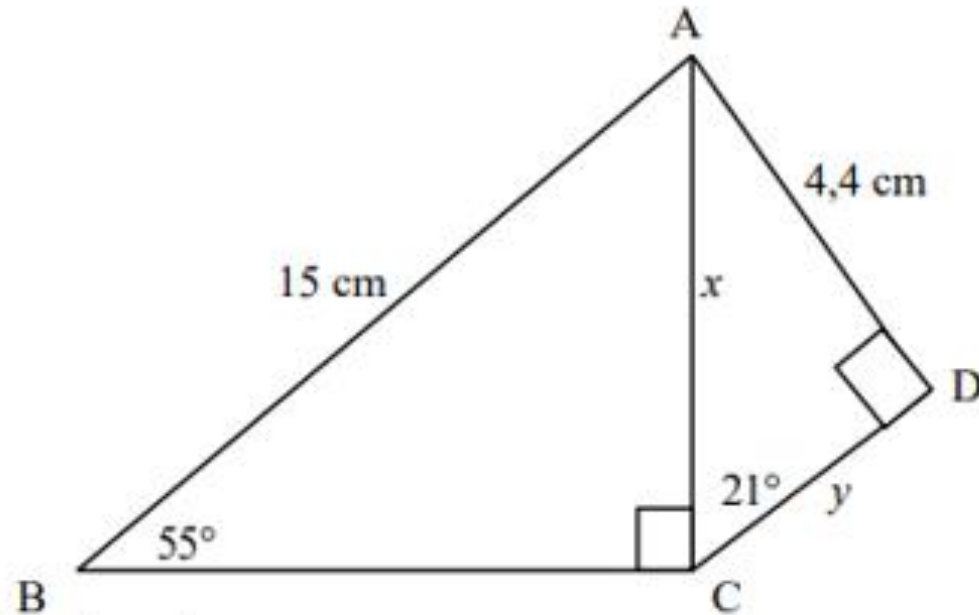
| | | |
|-------|---|--|
| 3.1.1 | $x^2 = 35^2 - 28^2$ $x = 21$ $\therefore \cos \theta = \frac{21}{35}$  | ✓ sub in Pythagoras ✓ $x = 21$ ✓ $\frac{21}{35}$ (3) |
| 3.1.2 | $\sin^2 \theta + \cos^2 \theta = \left(\frac{28}{35}\right)^2 + \left(\frac{21}{35}\right)^2$ $= 1$ $= \text{RHS}$ | ✓ $\left(\frac{28}{35}\right)^2$ ✓ $\left(\frac{21}{35}\right)^2$ ✓ 1 (3) |
| 3.2 | <p>If $37 \sin \theta + 35 = 0$</p> $\therefore \sin \theta = -\frac{35}{37}$ $x^2 = 37^2 - 35^2$ $x = 12$  $24 \sec \theta - 70 \cot \theta$ $= 24\left(\frac{37}{-12}\right) - 70\left(\frac{-12}{-35}\right)$ $= -74 - 24$ $= -98$ | ✓ $\sin \theta = \frac{-35}{37}$ ✓ 3 rd quadrant ✓ x value = -12 ✓ ✓ substitution ✓ answer (6) |

Solution

| | | |
|-------|--|--|
| 3.3.1 | $8\cos(x + 10^\circ) = 5$ $\cos(x + 10^\circ) = \frac{5}{8}$ $x + 10^\circ = 51,32^\circ$ $x = 41,32^\circ$ | <p>✓ $\cos(x + 10^\circ)$</p> <p>✓ $x + 10^\circ$</p> <p>✓ answer</p> <p>(3)</p> |
| | $\sin 2x = \frac{1}{2}$ $2x = 30^\circ$ $x = 15^\circ$ | <p>✓ $\sin 2x = \frac{1}{2}$</p> <p>✓ $2x = 30^\circ$</p> <p>✓ answer</p> <p>(3)</p> |
| 3.4 | $\frac{\sin 30^\circ \times \tan 60^\circ}{\tan 30^\circ \times \cos 60^\circ} = \frac{\frac{1}{2} \times \frac{\sqrt{3}}{1}}{\frac{1}{\sqrt{3}} \times \frac{1}{2}}$ $= 3$ $= \text{RHS}$ | <p>✓ $\frac{1}{2}$</p> <p>✓ $\sqrt{3}$</p> <p>✓ $\frac{1}{\sqrt{3}}$</p> <p>✓ $\frac{1}{2}$</p> <p>✓ answer</p> <p>(5)</p> |

TRIG 2

- 3.5 In the diagram below, $\hat{ACB} = 90^\circ$, $AB = 15 \text{ cm}$, $AD = 4,4 \text{ cm}$, $\hat{B} = 55^\circ$, $\hat{ACD} = 21^\circ$ and $\hat{ADC} = 90^\circ$.



Determine the value of:

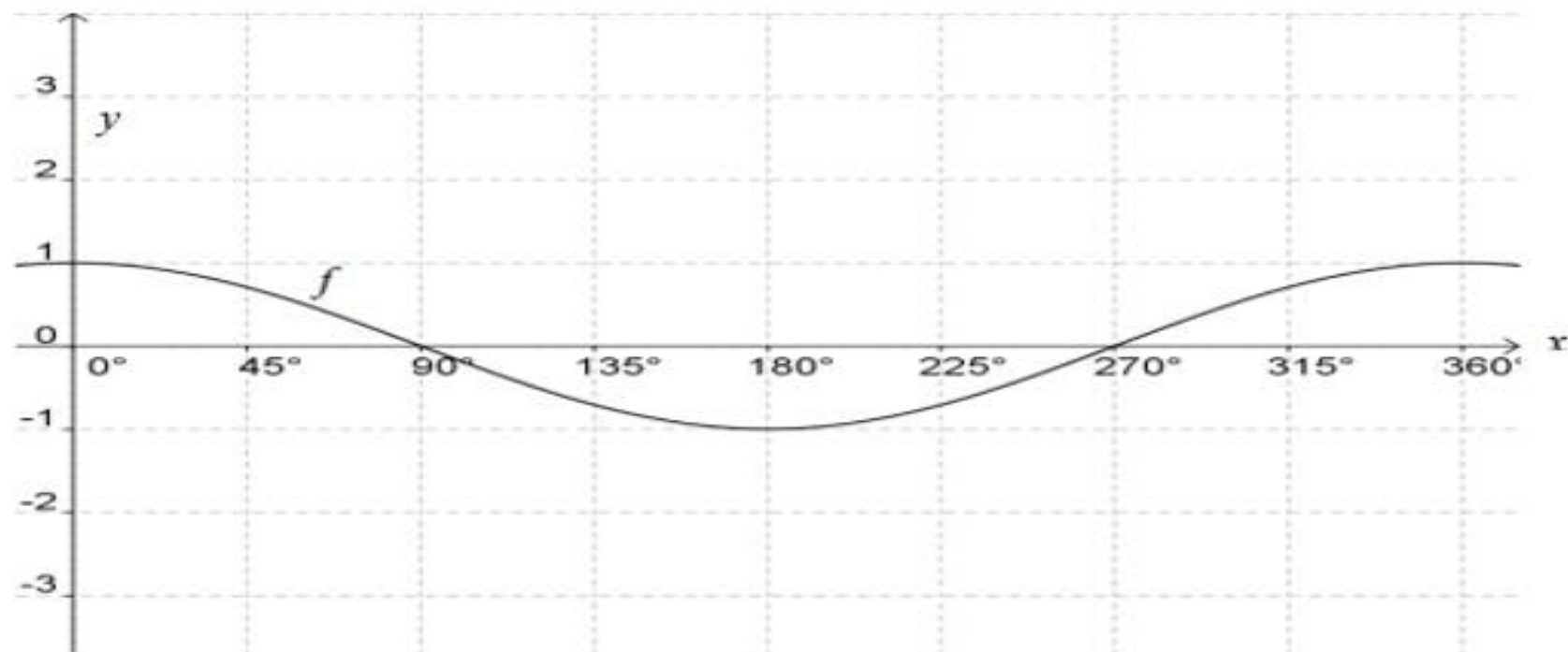
3.5.1 x (2)

3.5.2 y (2)

Working area

QUESTION 4

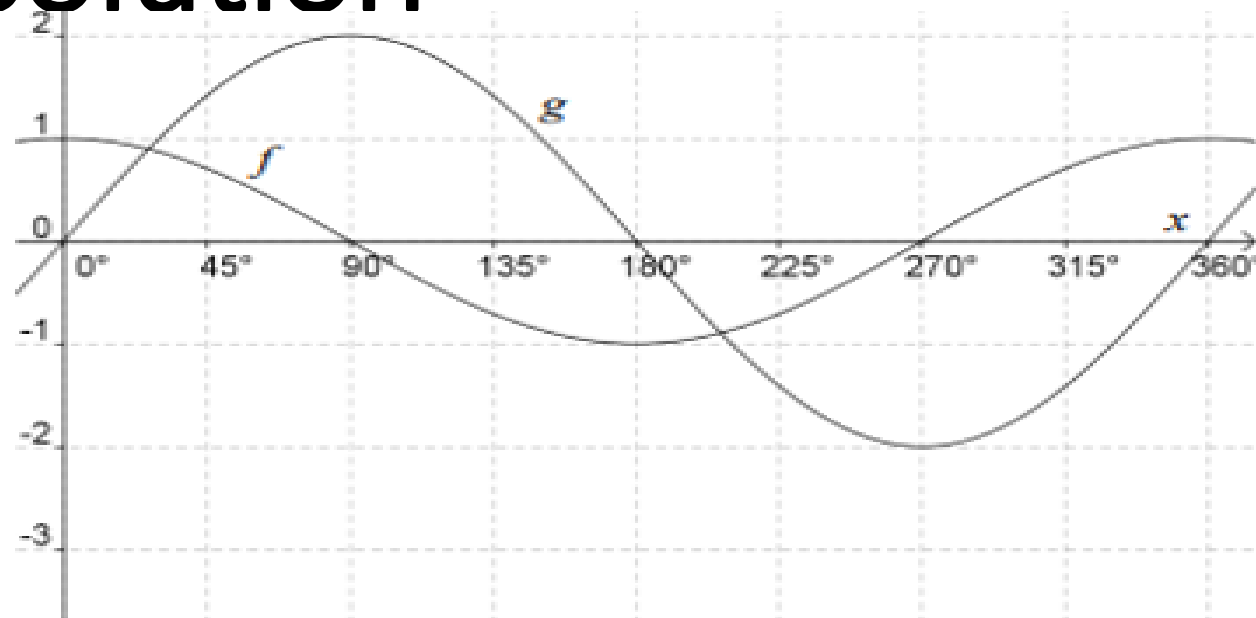
In the diagram below, the graph of $f(x) = \cos x$ is drawn for $x \in [0^\circ; 360^\circ]$



- 4.1 Sketch on the same axis the graph of $g(x) = 2\sin x$ for $x \in [0^\circ; 360^\circ]$. (3)
- 4.2 Write down the period of g . (1)
- 4.3 Write down the range of $m(x)$ if $m(x) = -3f(x) + 1$. (3)
- 4.4 For which value(s) of x is g decreasing? (2)
- 4.5 For which value(s) of x is $f(x) \times g(x) < 0$? (3)

Working area

Solution



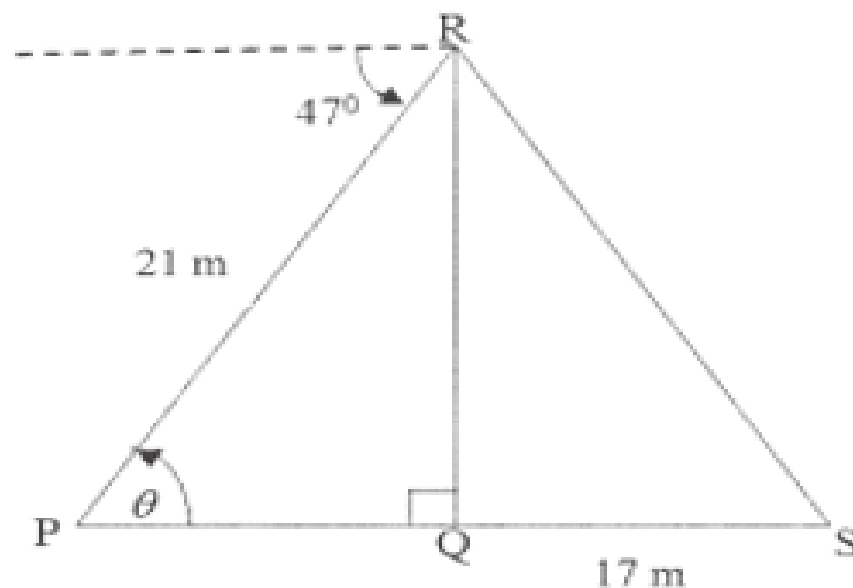
- ✓ intercepts
- ✓ turning pts
- ✓ shape

(3)

| | | |
|-----|---|---|
| 4.2 | period of $g = 360^0$ | ✓ answer (1) |
| 4.3 | range of $m(x)$ if $m(x) = -3f(x) + 1$ range of $-3 f(x)$: $-3 \leq y \leq 3$ range of $m(x)$: $-2 \leq y \leq 4$ | ✓ notation ✓✓ endpoints (3) |
| 4.4 | g decreasing: $90^0 < x < 270^0$ | ✓ notation ✓ endpoints (2) |
| 4.5 | $f(x) \times g(x) < 0$ $90^0 < x < 180^0$ or $270^0 < x < 360^0$ | ✓ notation ✓ endpoints ✓ endpoints (3) |
| | | [12] |

QUESTION 6

RQ is a vertical pole. The foot of the pole, Q, is on the same horizontal plane as P and S. The pole is anchored with wire cables RS and RP. The angle of depression from the top of the pole to point P is 47° . PR is 21 m and QS is 17 m. $\hat{RPQ} = \theta$.



- 6.1 Write down the size of θ . (1)
- 6.2 Calculate the length of RQ. (3)
- 6.3 Hence, calculate the size of \hat{S} . (2)
- 6.4 If P, Q and S lie in a straight line, how far apart are the anchors of the wire cables? (4)
- [10]

Working area

Solution

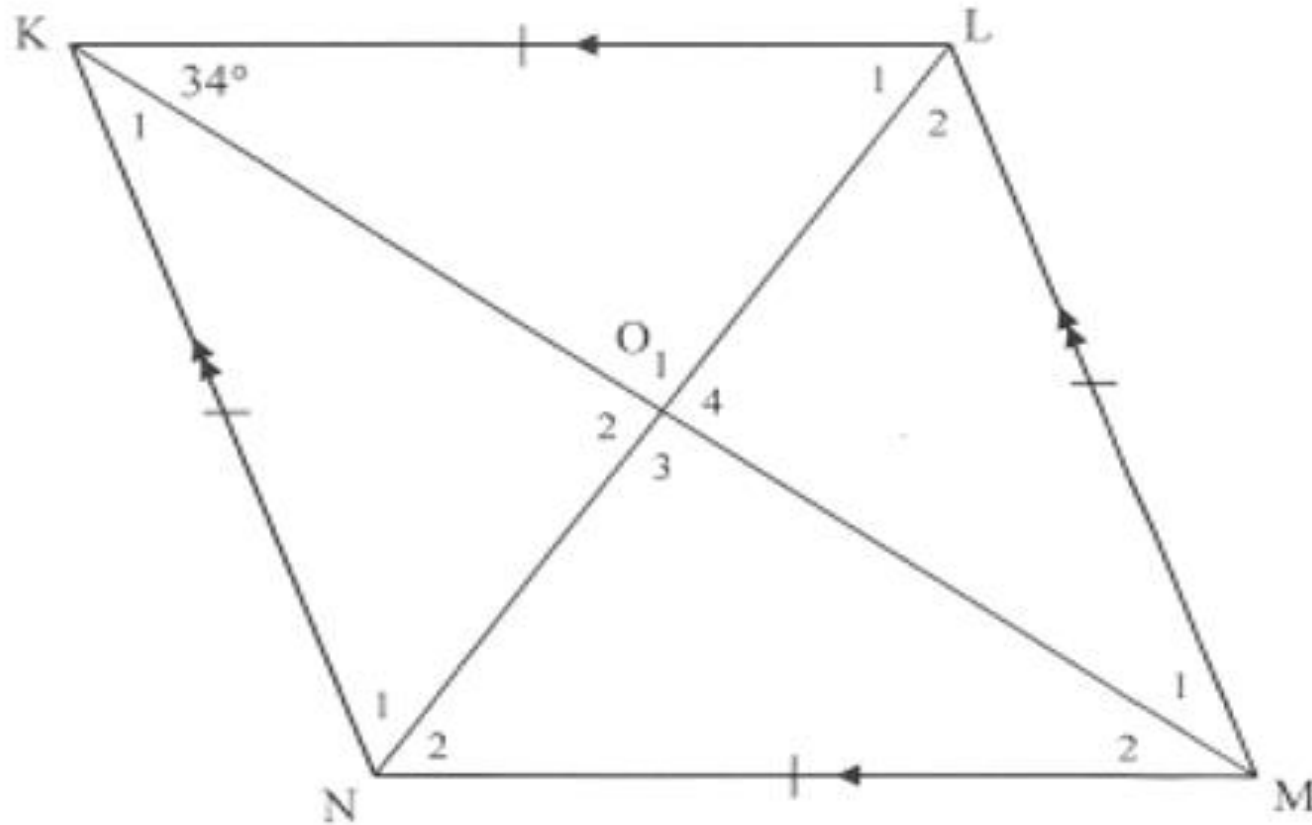
| | | |
|-----|--|--|
| 6.1 | $\theta = 47^\circ$ | ✓ answ./antw. (1) |
| 6.2 | $\sin P = \frac{RQ}{RP}$ $\sin 47^\circ = \frac{RQ}{21}$ $RQ = 21 \sin 47^\circ$ $RQ = 15,36 \text{ m}$ <p>OR/OF</p> $\hat{P}RQ = 43^\circ$ $\cos \hat{P}RQ = \frac{RQ}{RP}$ $\cos 43^\circ = \frac{RQ}{21}$ $RQ = 21 \cos 43^\circ$ $RQ = 15,36 \text{ m}$ | ✓ trig. ratio/trig. verhoud ✓ correct subst./korrekte instelling. ✓ answ./antw. (3) |
| | | <p>OR/OF</p> ✓ trig. ratio/trig. verhoud ✓ correct subst./korrekte instelling. ✓ answ./antw. (3) |

Solution

| | | |
|-----|---|---|
| 6.3 | $\tan S = \frac{RQ}{QS}$ $\tan S = \frac{15,36}{17}$ $\hat{S} = \tan^{-1}\left(\frac{15,36}{17}\right)$ $\hat{S} = 42,10^\circ$ | <p>✓ subst into trig ratio./verv in trig verh</p> <p>✓ answ./antw.</p> <p>(2)</p> |
| 6.4 | <div> $\cos 47^\circ = \frac{PQ}{21}$ $PQ = 21 \times \cos 47^\circ$ $PQ = 14,32$ $PS = 14,32 + 17$ $= 31,32 \text{ m}$ </div> <div> <p>OR/OF</p> $\sin 43^\circ = \frac{PQ}{21}$ $PQ = 21 \times \sin 43^\circ$ $PQ = 14,32$ $PS = 14,32 + 17$ $= 31,32 \text{ m}$ </div> | <p>✓ subst into trig. ratio/verv in trig. verhoud</p> <p>✓ PQ = 14,32 m</p> <p>✓ addition/optel</p> <p>✓ answ./antw.</p> <p>(4)</p> |

QUESTION 8

8.1 KLMN is a rhombus with diagonals intersecting at O. $\angle K = 34^\circ$.



8.1.1 Write down the size of $\angle O_1$. (1)

8.1.2 Calculate the size of $\angle L_1$. (2)

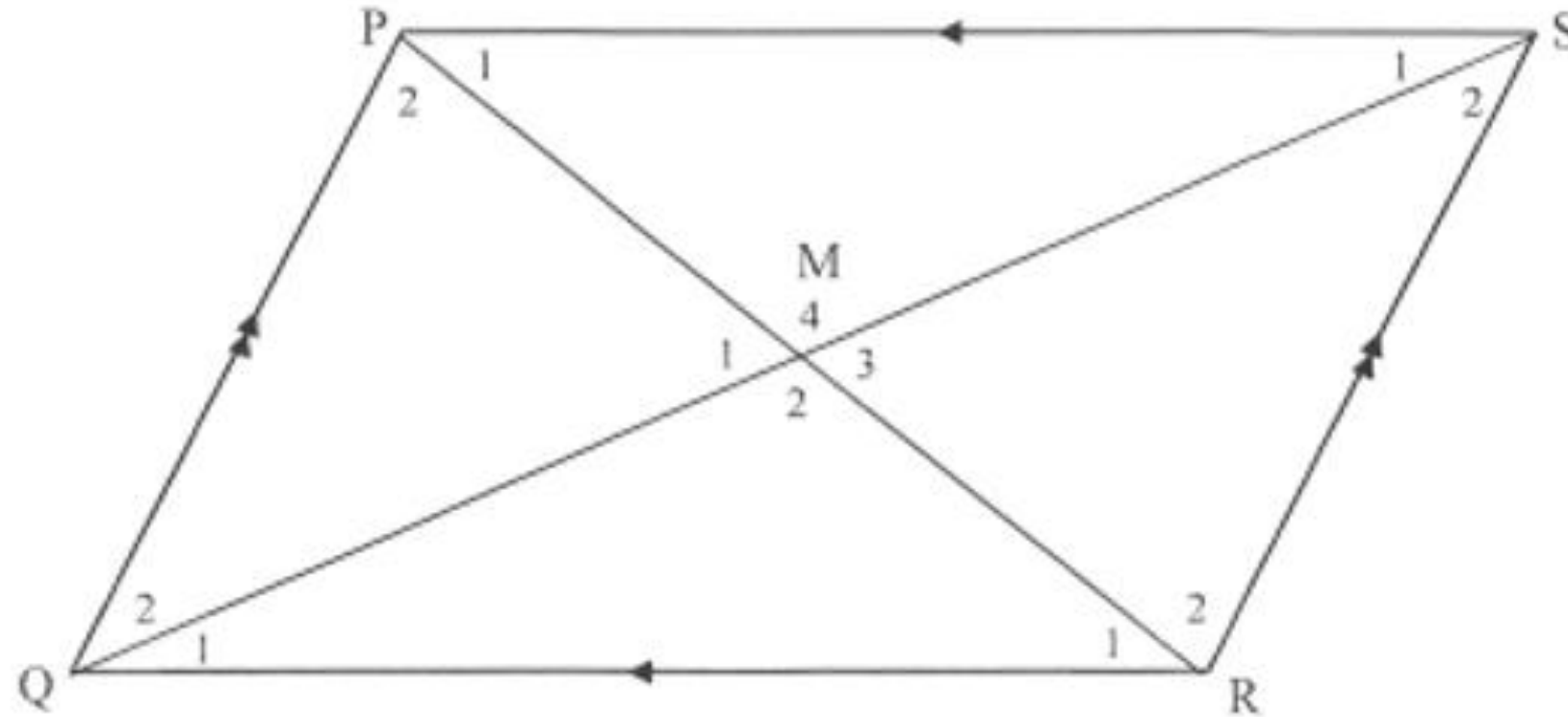
8.1.3 Calculate the size of $\angle KNM$. (2)

Working area

Solution

| | | |
|-------|--|---|
| 8.1.1 | $\hat{O}_1 = 90^\circ$ Diagonal bisect at/ <i>Hoeklyne sny by</i> 90° . | ✓S/R (1) |
| 8.1.2 | $\hat{L}_1 = 180^\circ - (34^\circ + 90^\circ)$ Sum of angles in/ <i>Som van hoeke</i> Δ . $= 56^\circ$ | ✓S ✓answ./antw. (2) |
| 8.1.3 | <p>$\hat{L}_1 = \hat{L}_2 = 56^\circ$ diagonals bisect the/<i>hoeklyne sny die</i> \angles. $\hat{L}_1 + \hat{L}_2 = \hat{N}_1 + \hat{N}_2$ opp. \angles of rhombus/ <i>teenoorst \angleevan die ruit</i> = $\therefore \hat{KNM} = 112^\circ$</p> <p>OR/OF $\hat{K}_1 = 34^\circ$ diagonals bisect the/<i>hoeklyne sny die</i> \angles.</p> <p>$\hat{KNM} + 68^\circ = 180^\circ$ co - int angles $KL \parallel NM$ $\therefore \hat{KNM} = 112^\circ$</p> <p>OR/OF $\hat{N}_2 = 56^\circ$ alt angles $KL \parallel NM$ $\hat{N}_1 = \hat{N}_2 = 56^\circ$ diagonals bisect the/<i>hoeklyne sny die</i> \angles. $\therefore \hat{KNM} = 112^\circ$</p> | <p>✓S/R ✓answ./antw. (2)</p> <p>OR/OF ✓S/R ✓answ./antw. (2)</p> <p>OR/OF ✓S/R ✓answ./antw. (2)</p> |

8.2 Given parallelogram PQRS with diagonals PR and QS intersecting at M.



Prove that the diagonals bisect each other.

(4)

Working area

Solution

8.2

Given/Gegee : $\parallel^m PQRS$ with diagonals/*met hoeklyne PR and/en QS.*

R.P.T : $PM = MR$

Proof/Bewys : In $\triangle PMS$ and/en $\triangle RMQ$

$$1. \hat{P}_1 = \hat{R}_1 \quad (\text{alt./verw. } \angle_s, PS \parallel QR)$$

$$2. \hat{S}_1 = \hat{Q}_1 \quad (\text{alt./verw. } \angle_s, PS \parallel QR)$$

$$3. PS = QR \quad (\text{opp. sides parm are /teenoorst. sye van parm. =})$$

$$\therefore \triangle PMS \equiv \triangle RMQ \quad (\text{AAS})$$

$$\Rightarrow PM = MR \quad \text{and} \quad MS = MQ$$

✓ 1. S/R

✓ 2. S

✓ 3. S/R

✓ congruency/kongruensie (AAS)

(4)

Solution

Given/Gegee $||^m PQRS$ with diagonals/*met hoeklyne*
PR and/en QS.

R.P.T : $QM = MS$

Proof/Bewys : In $\triangle PQM$ and/en $\triangle RSM$

1. $\hat{P}_2 = \hat{R}_2$ (alt./verw. \angle_s , $QP \parallel SR$)
2. $\hat{S}_2 = \hat{Q}_2$ (alt./verw. \angle_s , $SR \parallel PQ$)
3. $PQ = SR$ (opp. sides parm are/teenoorst. sye van parm =)

$\therefore \triangle PQM \equiv \triangle RSM$ (AAS)

$\Rightarrow QM = MS$ and $PM = MR$

✓ 1. S/R

✓ 2. S

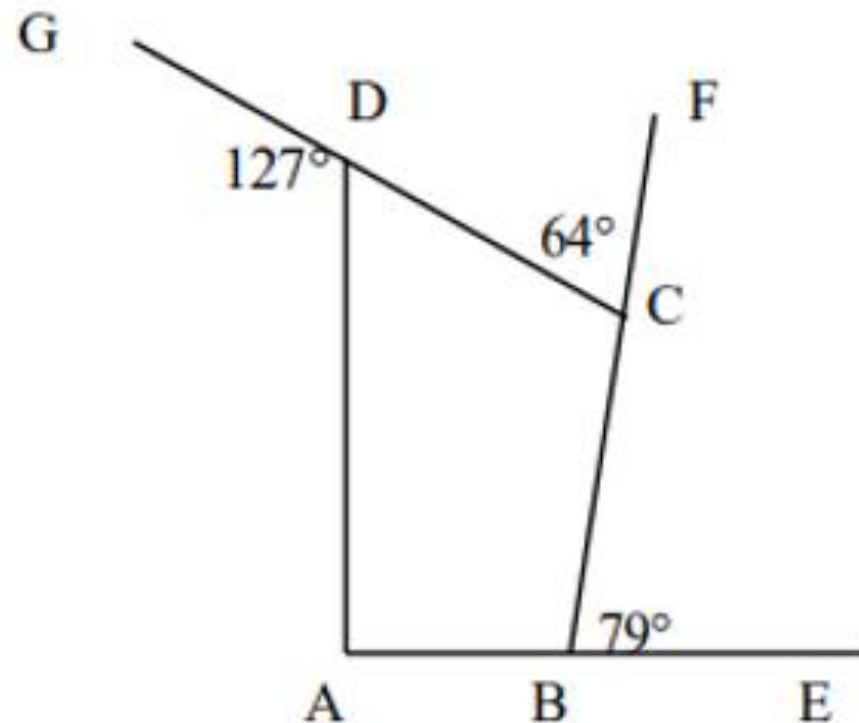
✓ 3. S/R

✓ congruency/kongruensie
(AAS)

(4)

QUESTION 5

- 5.1 The sides of a quadrilateral ABCD are produced such that AB is produced to E, BC is produced to F and CD is produced to G.



If $\angle EBC = 79^\circ$, $\angle FCD = 64^\circ$ and $\angle GDA = 127^\circ$, calculate the value of $\angle BAD$.

Working area

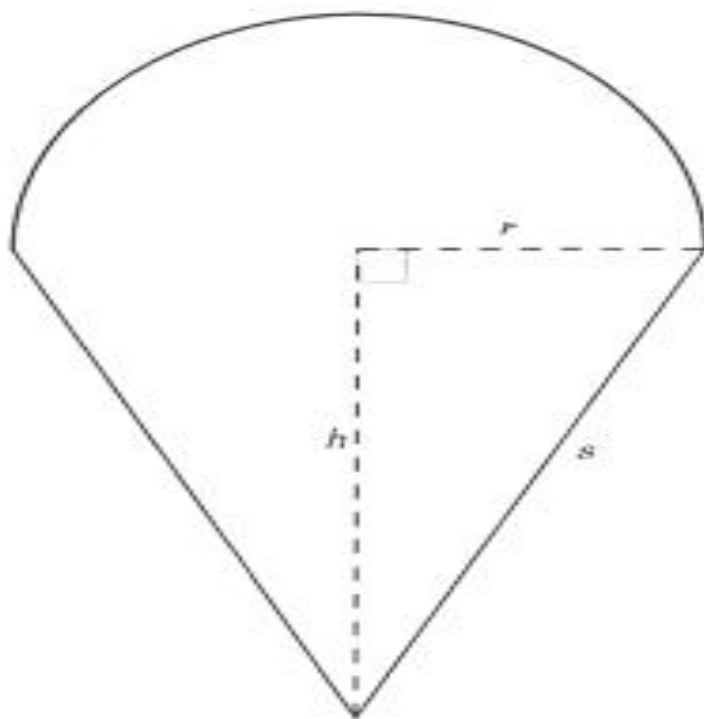
Solution

QUESTION 5

| | | |
|-----|---|---|
| 5.1 | $\hat{ADC} = 53^\circ$ (\angle s on a straight line) $\hat{DCB} = 116^\circ$ (supplementary adj \angle s) $\hat{CBA} = 101^\circ$ (\angle s on a straight line) $\hat{BAD} = 360^\circ - 53^\circ - 116^\circ - 101^\circ$ $= 90^\circ$ (\angle s of a quad $= 360^\circ$) Answer only: full marks, provided one reason is given | \checkmark SR \checkmark SR \checkmark SR \checkmark answer (4) |
|-----|---|---|

QUESTION 7

The diagram below shows the cross-section of a solid made up of a hemisphere placed on top of a right circular cone with radius r and slant height s . The perpendicular height of the cone, h , is 6,5 cm and the volume of the cone is $83,38 \text{ cm}^3$.



Formulae:

$$\text{Surface area of sphere} = 4\pi r^2$$

$$\text{Volume of sphere} = \frac{4}{3}\pi r^3$$

$$\text{Surface area of cone} = \pi r^2 + \pi r s$$

$$\text{Volume of cone} = \frac{1}{3}\pi r^2 h$$

Calculate, correct to TWO decimal places:

7.1 The radius, r , of the cone (2)

7.2 The slant height, s , of the cone (2)

7.3 The surface area of the solid (2)

[6]

Working area

Solution

QUESTION/VRAAG 7

| | | |
|-----|--|--|
| 7.1 | $V = \frac{1}{3} \pi r^2 h$ $83,38 = \frac{1}{3} \times 6,5 \pi r^2$ $r^2 = \frac{3 \times 83,38}{6,5 \pi}$ $r = 3,50 \text{ cm}$ | <p>✓ subst./verv.</p> <p>✓ answ./antw. (2)</p> |
| 7.2 | $s^2 = h^2 + r^2$ $s^2 = 6,5^2 + 3,5^2$ $s = 7,38 \text{ cm}$ | <p>✓ subst./verv.</p> <p>✓ answ./antw. (2)</p> |
| 7.3 | <p>Surface area of the solid/<i>Buite-oppervlakte (Oppervlakarea) van die vaste liggaam</i></p> $= 2\pi r^2 + \pi rs$ $= 2\pi(3,5)^2 + \pi(3,5)(7,38)$ $= 158,12 \text{ cm}^2$ | <p>✓ subst./verv.</p> <p>✓ answ./antw. (2)</p> |
| | | [6] |