

basic education

Department:
Basic Education
REPUBLIC OF SOUTH AFRICA

NATIONAL SENIOR CERTIFICATE

GRADE 10

MATHEMATICS P1

NOVEMBER 2017

MARKS: 100

TIME: 2 hours

This question paper consists of 7 pages.



INSTRUCTIONS AND INFORMATION

Read the following instructions carefully before answering the questions.

- 1. This question paper consists of 7 questions.
- 2. Answer ALL the questions.
- 3. Clearly show ALL calculations, diagrams, graphs, et cetera that you have used to determine the answers.
- 4. Answers only will NOT necessarily be awarded full marks.
- 5. You must use an approved scientific calculator (non-programmable and non-graphical), unless stated otherwise.
- 6. Round off answers to TWO decimal places, unless stated otherwise.
- 7. Diagrams are NOT necessarily drawn to scale.
- 8. Number the answers correctly according to the numbering system used in this question paper.
- 9. Write neatly and legibly.



- 1.1 Given: $q = \sqrt{b^2 4ac}$
 - 1.1.1 Determine the value of q if a = 2, b = -1 and c = -4. Leave your answer in simplest surd form. (2)
 - 1.1.2 State whether q is rational or irrational. (1)
 - 1.1.3 Between which TWO consecutive integers does q lie? (1)
- 1.2 Factorise the following expressions fully:

1.2.1
$$t^2(r-s)-r+s$$
 (3)

1.2.2
$$\frac{x^3 + 1}{x^2 - x + 1} \tag{2}$$

1.3 Simplify the following completely:

1.3.1
$$(2y+3)(7y^2-6y-8)$$
 (2)

1.3.2
$$\frac{3}{x^2 - 9} + \frac{2}{(x - 3)^2}$$
 (3)

1.3.3
$$\frac{3^{t}-3^{t-2}}{2.3^{t}-3^{t}}$$
 (3) [17]

QUESTION 2

- 2.1 Given: 4-2x < 16 where $x \in R$
 - 2.1.1 Solve the inequality.
 - 2.1.2 Hence, represent your answer to QUESTION 2.1.1 on a number line. (1)
- 2.2 Solve simultaneously for x and y:

$$-2x - y = 10$$
 and $3x - 4y = -4$ (4)

2.3 Solve for x:

$$2.3.1 \qquad \frac{x(x-5)}{6} - 1 = 0 \tag{3}$$

$$2.3.2 c = \sqrt{a+2x} (2)$$

Tabelo is currently four times as old as his daughter, Linda. Six years from now, Tabelo will be three times as old as Linda.

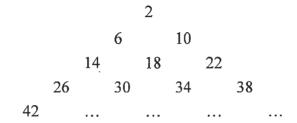
Calculate Linda's age currently.

(4) [16]

(2)

OUESTION 3

- 3.1 Consider the linear sequence: 5; 8; 11; b; 17; ...
 - 3.1.1 Write down the value of b. (2)
 - 3.1.2 Determine the n^{th} term of the sequence. (2)
 - 3.1.3 Calculate the value of the 15th term of the sequence. (2)
 - 3.1.4 Which term in the sequence is equal to 83? (2)
- Consider the number pattern below created by using the numbers of the sequence 2;6;10;14;18;...



- 3.2.1 Calculate the sum of the numbers in the 8th row. (3)
- 3.2.2 Determine the mean of the numbers in the 20th row. (2)

[13]

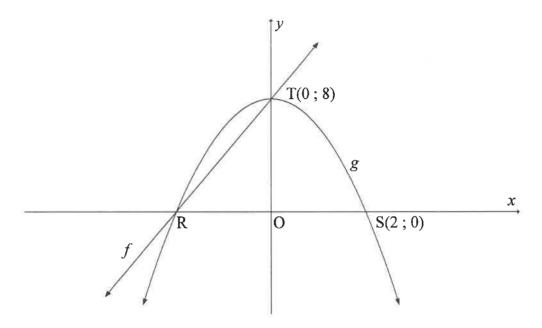
QUESTION 4

- 4.1 Seven years ago, Mrs Grey decided to invest R18 000 in a bank account that paid simple interest at 4,5% p.a.
 - 4.1.1 Calculate how much interest Mrs Grey has earned over the 7 years. (2)
 - 4.1.2 Mrs Grey wants to buy a television set that costs R27 660,00 now. If the average rate of inflation over the last 5 years was 6,7% p.a., calculate the cost of the television set 5 years ago. (3)
 - 4.1.3 At what rate of simple interest should Mrs Grey have invested her money 7 years ago if she intends buying the television set now using only her original investment of R18 000 and the interest earned over the last 7 years?
- 4.2 On a certain day the exchange rate between the US dollar and South African rand is \$1 = R12,91. At the same time the exchange rate between the British pound and the South African rand is £1 = R16,52.
 - Calculate the exchange rate between the British pound and US dollar on that day. (2)

[10]

(3)

The diagram shows the graphs of $g(x) = ax^2 + q$ and f(x) = mx + c. R and S(2; 0) are the x-intercepts of g and T(0; 8) is the y-intercept of g. Graph f passes through R and T.



5.1 Write down the range of g. (1)

5.2 Write down the x-coordinate of R. (1)

5.3 Calculate the values of a and q. (3)

5.4 Determine the equation of f. (3)

5.5 Use the graphs to determine the value(s) of x for which:

5.5.1
$$f(x) = g(x)$$
 (2)

$$5.5.2 x. g(x) \le 0 (3)$$

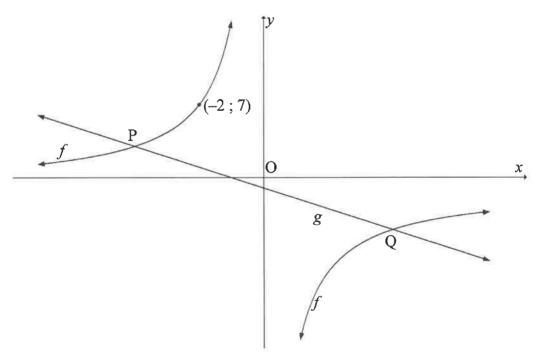
5.6 The graph h is obtained when g is reflected along the line y = 0.

Write down the equation of h in the form $h(x) = px^2 + k$. (2)

[15]

- 6.1 The function $p(x) = k^x + q$ is described by the following properties:
 - $k > 0; k \neq 1$
 - x-intercept at (2;0)
 - The horizontal asymptote is y = -9
 - 6.1.1 Write down the range of p. (1)
 - 6.1.2 Determine the equation of p. (3)
 - Sketch the graph of p. Show clearly the intercepts with the axes and the asymptote. (3)
- The sketch below shows the graphs of $f(x) = \frac{k}{x} + w$ and g(x) = -x 1.

 The graph g is an axis of symmetry of f. The graphs f and g intersect at P and Q.



- 6.2.1 Write down the value of w. (1)
- 6.2.2 The point (-2; 7) lies on f. Calculate the value of k. (2)
- 6.2.3 Calculate the x-coordinates of P and Q. (4)
- 6.2.4 Write down the values of x for which $\frac{-16}{x} > -x$. (2) [16]

Please turn over

- 7.1 Two events, A and B, are complementary and make up the entire sample space. Also, P(A') = 0.35.
 - 7.1.1 Complete the statement: P(A) + P(B) = ... (1)
 - 7.1.2 Write down the value of P(A and B). (1)
 - 7.1.3 Write down the value of P(B). (1)
- 7.2 A survey was conducted among 150 learners in Grade 10 at a certain school to establish how many of them owned the following devices: smartphone (S) or tablet (T).

The results were as follows:

- 8 learners did not own either a smartphone or a tablet.
- 20 learners owned both a smartphone and a tablet.
- 48 learners owned a tablet.
- *x* learners owned a smartphone.
- 7.2.1 Represent the information above in a Venn diagram. (4)
- 7.2.2 How many learners owned only a smartphone? (3)
- 7.2.3 Calculate the probability that a learner selected at random from this group:
 - (a) Owned only a smartphone (1)
 - (b) Owned at most one type of device (2) [13]

TOTAL: 100