

CS283: Assignment 1

January 29, 2024

Due: Monday February 5th, 11:59pm AST
Submit through the **blackboard system**

By turning in this assignment, you agree with the KAUST student code of conduct and declare that all of this is your own work.

Requirements:

- Put all files in a zip file and the file should be named LastnameFirst-name_Assignment1.zip
- It is an individual assignment, independent write up, and submission in your own hand is required for credit.
- The work should be written in a **clear** way
- Late submission will receive credit penalty

1 Problem 1: Generative adversarial networks (60 points)

In this problem, suppose that we will implement a generative adversarial network (GAN) that models a high-dimensional data distribution $p_{data}(x)$, where $x \in \mathbb{R}^n$. To do so, we will define a generator $G_\theta : \mathbb{R}^k \rightarrow \mathbb{R}^n$; we obtain samples from our model by first sampling a k -dimensional random vector $z \sim \mathcal{N}(0, I)$ and then returning $G_\theta(z)$.

We will also define a discriminator $D_\phi : \mathbb{R}^n \rightarrow (0, 1)$ that judges how realistic the generated images $G_\theta(z)$ are, compared to samples from the data distribution $x \sim p_{data}(x)$. Because its output is intended to be interpreted as a probability, the last layer of the discriminator is frequently the sigmoid function

$$\sigma(x) = \frac{1}{1+e^{-x}}$$

There are several common variants of the loss functions used to train a generative adversarial network (GAN). They can all be described as a procedure

where we alternately perform a gradient descent step on $L_D(\phi; \theta)$ with respect to ϕ to train the discriminator D_ϕ , and a gradient descent step on $L_G(\theta; \phi)$ with respect to θ to train the generator G_θ :

$$\min_{\phi} L_D(\phi; \theta) \quad \min_{\theta} L_G(\phi; \theta)$$

In our lecture, we talked about the following losses, where the discriminator's loss is given by:

$$L_D(\phi; \theta) = -\mathbb{E}_{x \sim p_{data}(x)} [\log D_\phi(x)] - \mathbb{E}_{z \sim \mathcal{N}(0, I)} [\log(1 - D_\phi(G_\theta(z)))]$$

and the generator's loss is given by the **minimax loss**:

$$L_G^{minimax}(\theta; \phi) = \mathbb{E}_{z \sim \mathcal{N}(0, I)} [\log(1 - D_\phi(G_\theta(z)))]$$

1. **(20 points)** the minimax loss for L_G suffers from **vanishing gradient** problem. In terms of the discriminator's logits, the **minimax loss** is

$$L_G^{minimax}(\theta; \phi) = \mathbb{E}_{z \sim \mathcal{N}(0, I)} [\log(1 - \sigma(h_\phi(G_\theta(z))))]$$

Show that the derivative of $L_G^{minimax}$ with respect to θ is approximately 0 if $D(G_\theta(z)) \approx 0$, or equivalently, if $h_\phi(G_\theta(z)) \ll 0$. You may use the fact that $\sigma'(x) = \sigma(x)(1 - \sigma(x))$. Why is this problematic for the training of the generator when the discriminator successfully identifies a fake sample $G_\theta(z)$?

2. **(20 points)** To solve this vanishing gradient problem, we usually replace $L_G^{minimax}$ with other loss functions such as non-saturating loss L_G^{nsgan} [1] and more other forms of loss functions can be found in [2]. You may plot different loss functions including minimax loss and non-saturating loss to show the contrast. You also need to explain why non-saturating loss can avoid vanishing gradient problem.

$$L_G^{nsgan}(\theta; \phi) = -\mathbb{E}_{z \sim \mathcal{N}(0, I)} [\log D_\phi(G_\theta(z))]$$

3. **(20 points)** Coding practice: You are going to fill out the missing code blocks in **CS283_homework1_GAN.ipynb** and build a GAN model to convert 1D uniform noise distribution to a uniform 1D normal data distribution. The **readme.txt** is provided for environment setup.

2 KL-Divergence (30 points)

1. **(30 points)** Let $\mu : \mathcal{X} \rightarrow \mathbb{R}^k$, $\sigma : \mathcal{X} \rightarrow \mathbb{R}^k$ and let $q(z|x) = \mathcal{N}(z; \mu(x), (\sigma^2(x)))$. Suppose that $p(z) = \mathcal{N}(z; 0, I)$. Show that

$$D_{KL}(q(z|x) \| p(z)) = \frac{1}{2} \sum_{i=1}^k (\sigma_i^2(x) + \mu(x)_i^2 - 1 - \log \sigma_i^2(x))$$

Note that the KL divergence between two distributions P and Q is defined as

$$D_{KL}(p(x) \| q(x)) = \int p(x) \log\left(\frac{p(x)}{q(x)}\right) dx.$$

3 Creative Adversarial Networks (20 points)

In Creative Adversarial Networks (CANs)[3], an additional loss is added to encourage producing novel images with the loss defined as

$$\begin{aligned} \min_G \max_D V(D, G) = & \mathbb{E}_{x, \hat{c} \sim p_{data}} [\log D_r(x) + \log D_c(c = \hat{c}|x)] + \\ & \mathbb{E}_{z \sim p_z} [\log(1 - D_r(G(z))) - \sum_{k=1}^K \left(\frac{1}{K} \log(D_c(c_k|G(z))) + \right. \\ & \left. (1 - \frac{1}{K}) \log(1 - D_c(c_k|G(z))) \right)], \end{aligned} \quad (1)$$

where x and \hat{c} are a real image and its corresponding art style label from the data distribution p_{data} . $D_r(\cdot)$ is the transformation function that tries to discriminate between real art and generated images. $D_c(\cdot)$ is the function that discriminates between different style categories and estimates the style class posteriors (i.e., $D_c(c_k|\cdot) = p(c_k|\cdot)$).

1. **(10 points)** Comment on the use of Binary Cross Entropy(BCE) in the deviation loss summed up over each style class (i.e. terms in $\sum_{k=1}^K(\dots)$ above). What part of the loss function enables the model not to produce meaningless art images since they may also have high entropy.

2. **(10 points) Bonus*** Why Multiclass Cross Entropy improved the performance over BCE in Holistic-CAN[4] (CAN-H)?

References

- [1] Ian J Goodfellow, Jean Pouget-Abadie, Mehdi Mirza, Bing Xu, David Warde-Farley, Sherjil Ozair, Aaron Courville, and Yoshua Bengio. Generative adversarial nets.
- [2] Mario Lucic, Karol Kurach, Marcin Michalski, Olivier Bousquet, and Sylvain Gelly. Are gans created equal? a large-scale study. In *Proceedings of the 32nd International Conference on Neural Information Processing Systems*, pages 698–707, 2018.
- [3] Ahmed Elgammal, Bingchen Liu, Mohamed Elhoseiny, and Marian Mazzone. Can: Creative adversarial networks, generating” art” by learning about styles and deviating from style norms. *arXiv preprint arXiv:1706.07068*, 2017.
- [4] Othman Sbai, Mohamed Elhoseiny, Antoine Bordes, Yann LeCun, and Camille Couprie. Design: Design inspiration from generative networks. In *Proceedings of the European Conference on Computer Vision (ECCV) Workshops*, pages 0–0, 2018.