27-02-22	1	DATEPAGE_
0 = 1011 (-	Assignment 2	17 18 611
		1 (8 3)
Q1(b) MIE for	multivariate Be	moulli distribution
		J. V. V.
$V(x_j   \theta)$	$(j) = \theta_j^{x_j} (1 - \theta_j)^{1-x_j}$	1 1 1 1 C - 1
=> p/v/n	d 2/10/1-	<del>2</del> 11 ( ) 1 1 1 : : : : : : : : : : : : : : : :
- F ( X   0	$\frac{1}{1} = \frac{1}{1} \frac{\theta_{j}}{1} \frac{(1-\theta_{j})^{2}}{1}$	of (for d-dinensions)
	of the distribution	V
· · · · · · · · · · · · · · · · · · ·	of the resultation	1 d 2 d . 1 V
Q(X) =	$ \begin{array}{c}                                     $	Will be to
The log-	likelihood function	
	V	
F(0) =	= 1 j=1,	- 7; ) ln (1-0;)
The best of the		(1) (=1)
(a) (θ) =	- 1-7;	
7 Oj	$i=1$ $\theta$ ; $1-\theta$ ;	. *
0.14	1= 1 + (1)	-118-178 +
Putting	alsone to 0	-1 9
	$\theta_j = \left( \leq \gamma_{ij} \right) \frac{1}{1}$	
	alone to $0$ $0 = \left( \frac{1}{2} \right) \frac{1}{N}$	W-X(0-1) (6)
	1 . 11 10	
Thue, fort	t j-th dimension	
TAM 5	N	4X - A (9)
MLE		- 1 4 6
71. 211 11	+ MH+ = M M + E+1	
	4 MIN 1 M 1 5 841	
7, + 8 - 2	\$	
	1	

Taking discriminant for sono-one loss. Here, the minimum everor-rate classification is achieved by the function i-th class (1) + ln P(wi) Here  $P(\omega_i) = P(\omega_s)$   $= \lim_{n \to \infty} P(\pi(\omega_i))$ For d-dimensions  $P(X|\omega_i) = 10 + 0 \cdot (1-\theta_i)^{1-x_i}$  i=1Now, for j-th class  $g_{j}(x) = \ln P(x|w_{j})$   $f : P(x|w_{j}) = \lim_{x \to \infty} P(x|w_{j})$   $g_{j}(x) = \lim_{x \to \infty} P(x|w_{j})$  $= \frac{1}{9} \frac{d}{dx} \frac{dx}{(1-\theta_{ij})} = \frac{1-x_{ij}}{1-1} \frac{d}{dx} \frac{dx}{(1-\theta_{ij})}$  $=) \left| \frac{g_{j}(x)}{g_{j}(x)} \right| = \frac{d}{dx} \quad \text{with } \theta_{ij} + (1-\pi_{i}) \ln(1-\theta_{ij})$ 

Tail

10-0-01- + ( :1/K-1) &- :1/K

16)

d=2; N= = 4

OMAP is a 2×1 vector.

 $\theta_{i}^{2} - (2+N)\theta_{i} + \sum_{i=1}^{N} x_{i1} + 1 = 0$ 

 $= \theta_1^2 - 6\theta_1 + 4 = 0$ 

 $=) 0, = 3 \pm \sqrt{5}$ 

Naw,  $\theta_2^2 - (2+N)\theta_2 + \leq \chi_{i2} + 1 = 0$ 

=  $\theta_{1}^{2} - 6\theta_{2} + 2 = 0$ 

 $\Rightarrow \theta_2 = 3 \pm \sqrt{7}$ 

 $\theta_i$  is perobolity, thus  $\theta_i < 1$ 

 $\theta_1 = 3 - \sqrt{5} \approx 0.764$   $\theta_2 = 3 - \sqrt{7} \approx 0.354$ 

Ans.  $\Rightarrow \theta_{MAP} = 3 - \sqrt{5} = 0.764$   $3 - \sqrt{7} = 0.354$ 

	DATEPAGE
Q3.	$X = 2$ 4 $11 = \begin{bmatrix} 2 \end{bmatrix}$
	6 8 7
(a)	$X_{c} = X - \mu = 2 - 3 + 4 - 3 = -1 = -1$
	6-7 8-7 -1 1
	$S_{x_0} = \frac{1}{2} \begin{bmatrix} -1 & 1 & 1 & -1 & -1 \\ -1 & 1 & 1 & 1 \end{bmatrix} = \frac{1}{N} \sum_{i=1}^{N} x_i x_i^T$
	deed e oudto e
	= 1 2 2 7 - [1 1]
	2 2 2 1 1 -1 = 8 =
	If I are eigenvalues of Sx.
	$\det(S_{x_c} - \lambda T) = 0$
	=)del( 111 = 01
	=) Olet 1-2 1 = 01-11 = 01-11
	$= \frac{1 + \lambda}{(\lambda - 1)^2 - 1^2} = 0$
	= = (1-1-1)(1-1+1) = Omission
	$=) \qquad \lambda = 2 \qquad ; \lambda = 0$
	X . N = Y =
1	leigenvalues au [2 and 0]
	Let A be the eigenvector corresponding to b = 2
	Let A be the significant coordinating it 2-2
	$\left(S_{x_{c}}-\lambda I\right)A=0M+V.N=1.$
	7 7 7 0
	$ \begin{vmatrix} -1 & 1 & 0 \\ 1 & -1 & 0 \\ 1 & -1 & 0 \end{vmatrix} = 0 $ $ \begin{vmatrix} -1 & 1 & 0 \\ 1 & -1 & 0 \\ 1 & -1 & 0 \end{vmatrix} = 0 $ $ \begin{vmatrix} -1 & 1 & 0 \\ 1 & -1 & 0 \\ 1 & -1 & 0 \end{vmatrix} = 0 $
1 dl +	$\Rightarrow$ $-q_1 + q_2 = 0 \Rightarrow q_1 = q_2$
1.	2/ 1

	$A = \frac{1}{8} = $
-	B be the eigenvector coverspinding to $\lambda = 0$
11	
	$\lceil 1 \ 1 \rceil \lceil b_1 \rceil = 0$
	$\begin{bmatrix} 1 & 1 \\ b_1 \end{bmatrix} = 0$ $\begin{bmatrix} 1 & 1 \\ b_2 \end{bmatrix} = \begin{bmatrix} 1 & 1 \\ b_3 \end{bmatrix} = \begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix}$
-	$=)$ $b_1 + b_2 = 0 =) b_1 = -b_2$
	= ! 2 2 ! =
	$\Rightarrow B = \begin{bmatrix} -1 \end{bmatrix}$
	I 2 ans sinconvalues of 5x.
	Normalising A and B for PCA
	A = 10 [1] [0 and .B = 1 [-1]
,	1 12 [1/2 ]
	=> U = 1 [1 -1] / 1 K-1 Hab) (=
	$\frac{4}{\sqrt{2}} \left[ \frac{1}{\sqrt{2}} \right] \left[ \frac{1}{$
	Jaking 1 principal component: p = 1
	p = 1
	$=)  \forall =  U_1^{T} \times_{C}$
	Concentres and and a
	= 1 [-1 1] [-2 27 1/6
0 = 7	the children hard 22 is topological sold and A to A
	=> X' = U1.7 + M 1= A (TA-10)
	1= [10] -1
	=11177-2271=17-227=711
	12 12 LIJ = +4 2 L-2 2 L-1 1
	$+\mu$

1 0= (1+X)+ 10(1+E) = 0 1.