1) Complex Fourier Series Consider,

$$x(t) = \sum_{n = -\infty}^{\infty} c_n e^{jnwt} \tag{1}$$

where c_n is the exponential fourier coefficient.

$$c_n = \frac{1}{T} \int_0^T x(t)e^{-jnwt} dt \tag{2}$$

where T is the time period of function x(t).

2) Trigonometric Fourier Series

We can write:

$$e^{jnwt} = cos(nwt) + jsin(nwt)$$
 (3)

Substituting (??) in (??)

$$x(t) = \sum_{n = -\infty}^{\infty} c_n(\cos(nwt) + j\sin(nwt))$$
(4)

$$= a_0 + \sum_{n=1}^{\infty} (a_n \cos(nwt) + b_n \sin(nwt))$$
 (5)

where a_0 , a_n and b_n are trigonometric fourier series.

$$a_0 = c_0 \tag{6}$$

$$=\frac{1}{T}\int_0^T x(t)\,dt\tag{7}$$

$$a_n = 2Re(c_n) \tag{8}$$

$$= \frac{2}{T} \int_0^T x(t) \cos(nwt) dt \tag{9}$$

$$b_n = -2Im(c_n) \tag{10}$$

$$= \frac{2}{T} \int_0^T x(t) \sin(nwt) dt \tag{11}$$