1) Complex Fourier Series Consider,

$$x(t) = \sum_{n = -\infty}^{\infty} c_n e^{j2\pi nft} \tag{1}$$

where c_n is the exponential fourier coefficient.

$$c_n = \frac{1}{T} \int_0^T x(t)e^{-j2\pi nft} dt$$
 (2)

where T is the time period of function x(t).

2) Trigonometric Fourier Series

We can write:

$$e^{j2\pi nft} = \cos(2\pi nftt) + j\sin(2\pi nft) \tag{3}$$

Substituting (3) in (1)

$$x(t) = \sum_{n = -\infty}^{\infty} c_n \left(\cos(2\pi n f t) + j \sin(2\pi n f t) \right) \tag{4}$$

$$= a_0 + \sum_{n=1}^{\infty} (a_n \cos(2\pi n f t)) + (b_n \sin(2\pi n f t))$$
 (5)

where a_0, a_n and b_n are trigonometric fourier series.

$$a_0 = c_0 \tag{6}$$

$$=\frac{1}{T}\int_0^T x(t)\,dt\tag{7}$$

$$a_n = 2Re(c_n) \tag{8}$$

$$=\frac{2}{T}\int_0^T x(t)\cos(2\pi nft)\,dt\tag{9}$$

$$b_n = -2Im(c_n) \tag{10}$$

$$= \frac{2}{T} \int_0^T x(t) \sin(2\pi n f t) dt \tag{11}$$