

Q1

a:

Identity

```
[[0.35542488, 0.35542488],  
[0.71084977, 0.71084977],  
[0.35542488, 0.35542488]]  
[2.36949922],  
[1.42169953],  
[1.42169953]
```

Tanh

```
[[0.25257836, 0.25257836],  
[0.50515672, 0.50515672],  
[0.25257836, 0.25257836]]  
[[2.36636925],  
[1.27085758],  
[1.27085758]]
```

b:

Identity

```
[[0.35566715, 0.35566715],  
[0.71133431, 0.71133431],  
[0.35566715, 0.35566715]]  
[[2.36953466],  
[1.42266861],  
[1.42266861]]
```

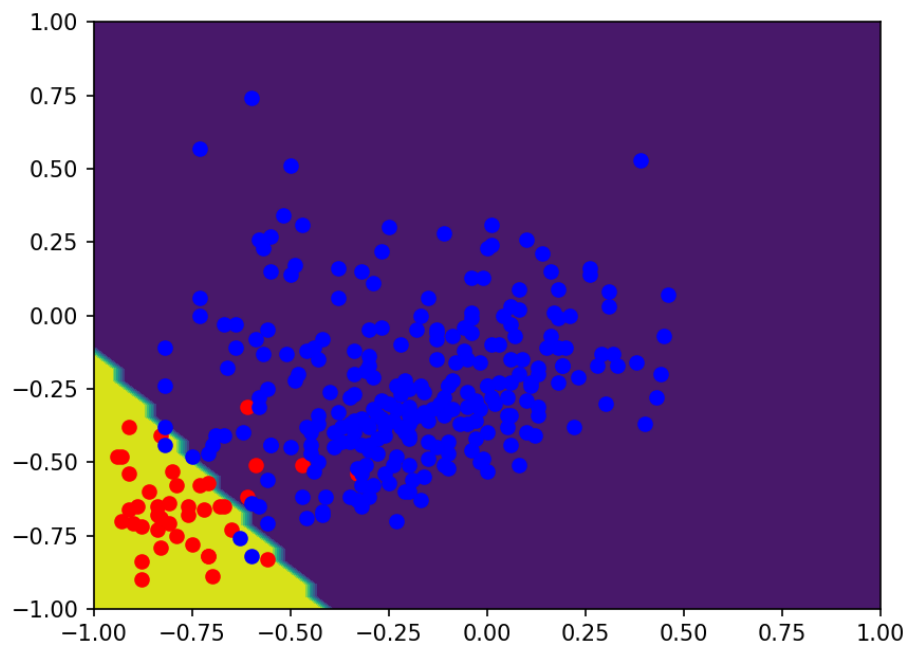
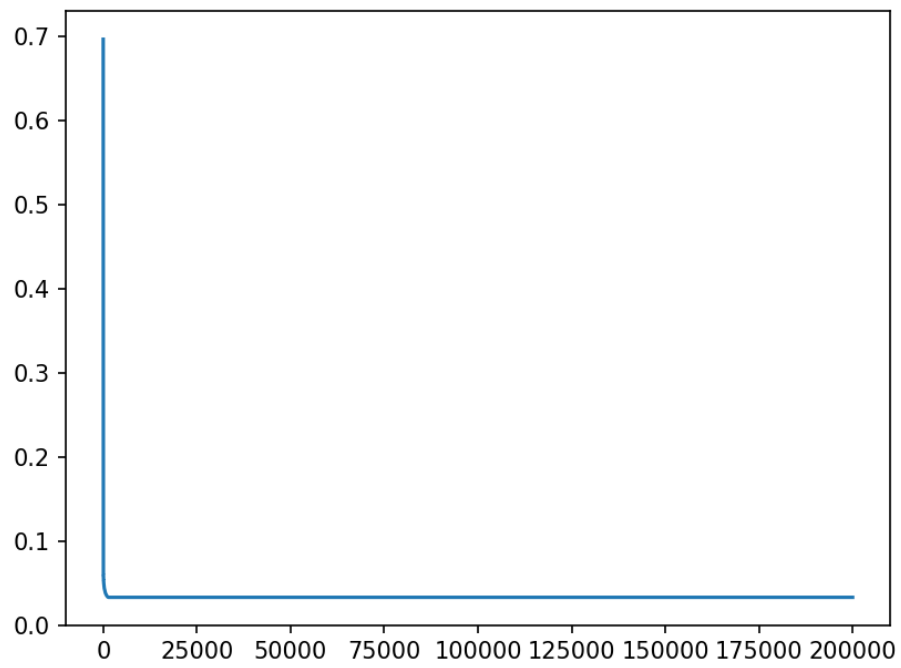
Tanh

```
[0.25251131, 0.25251131],  
[0.50502263, 0.50502263],  
[0.25251131, 0.25251131]]  
[[2.36630271],  
[1.27014818],  
[1.27014818]]
```

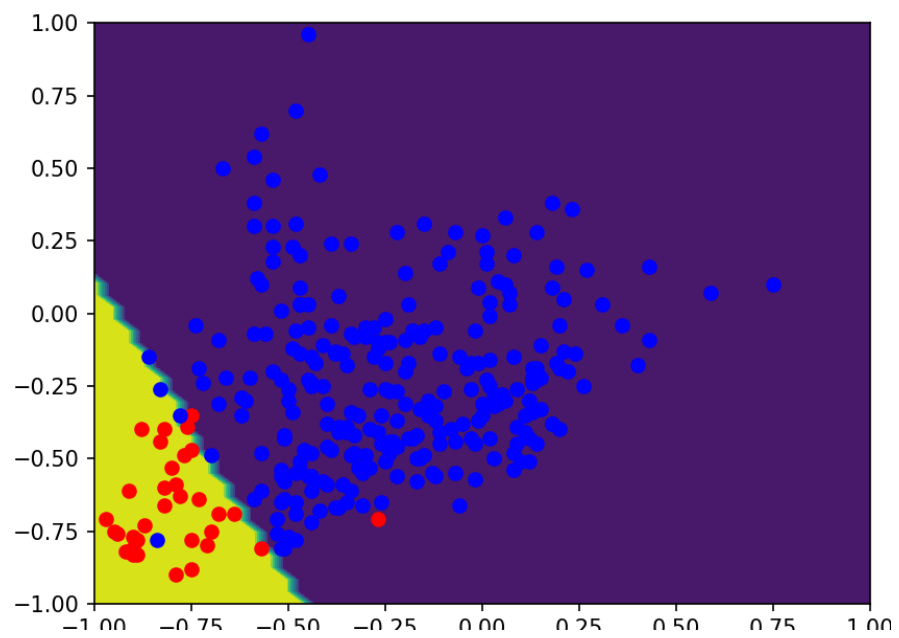
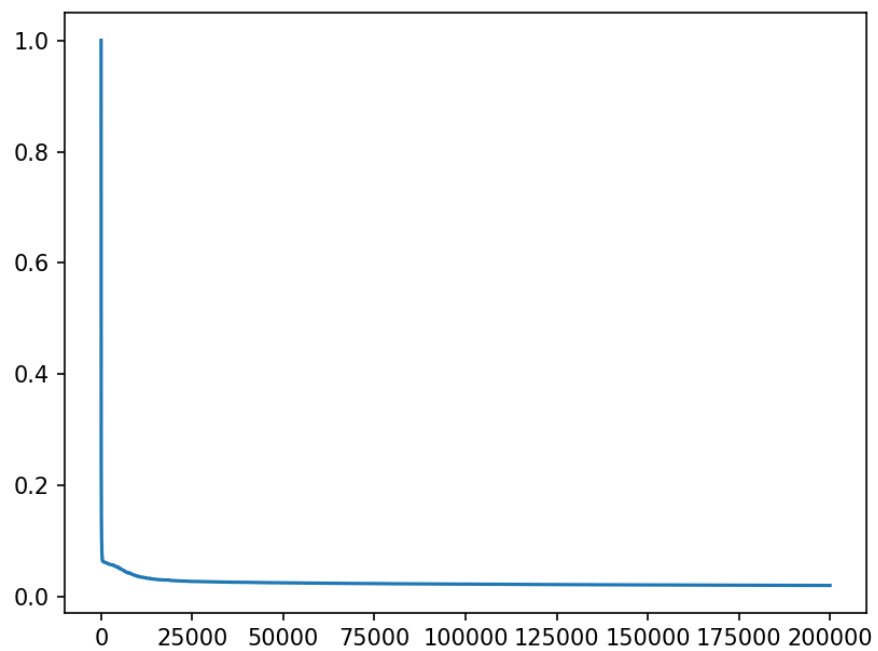
So the results only changed a little.

Q2:

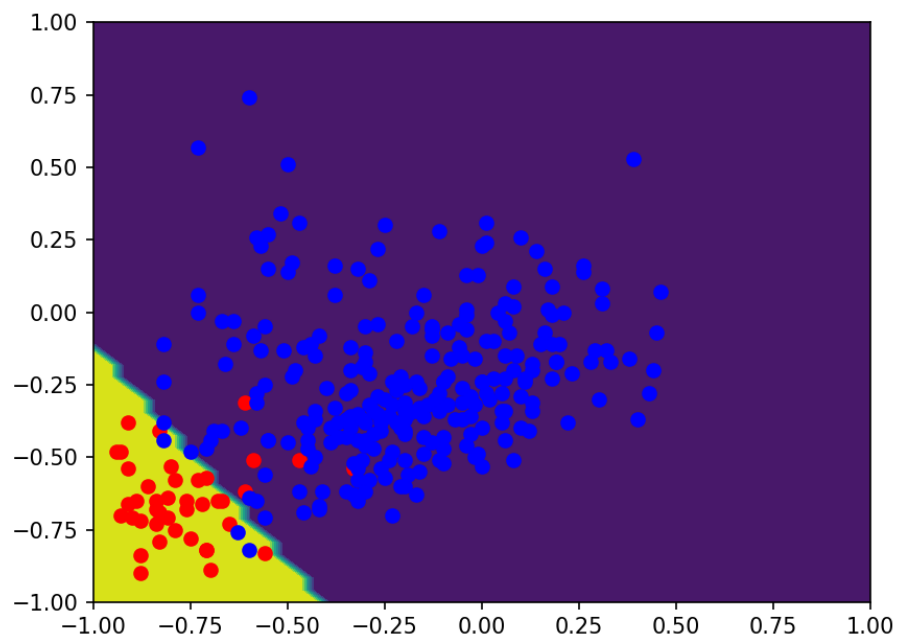
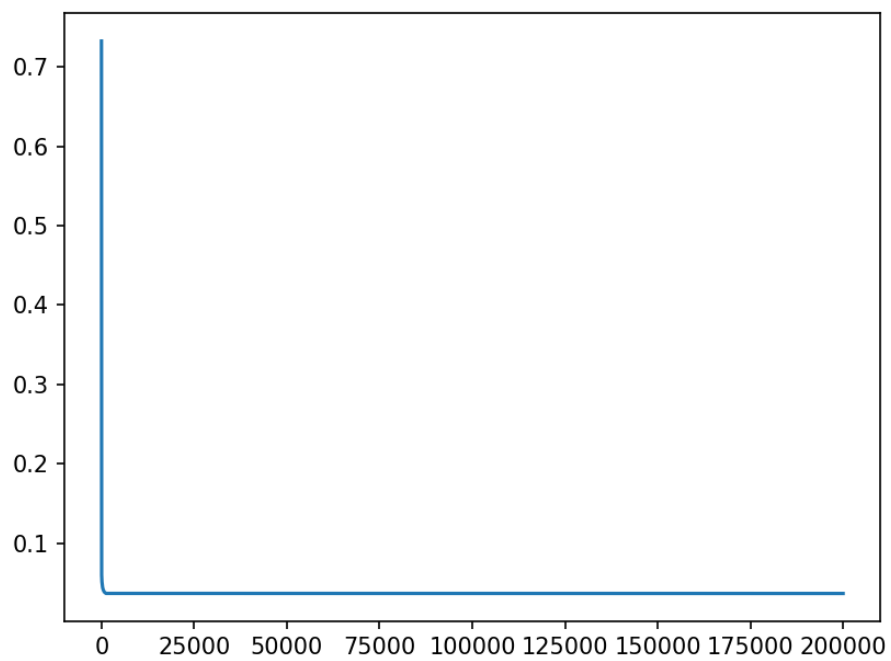
a:



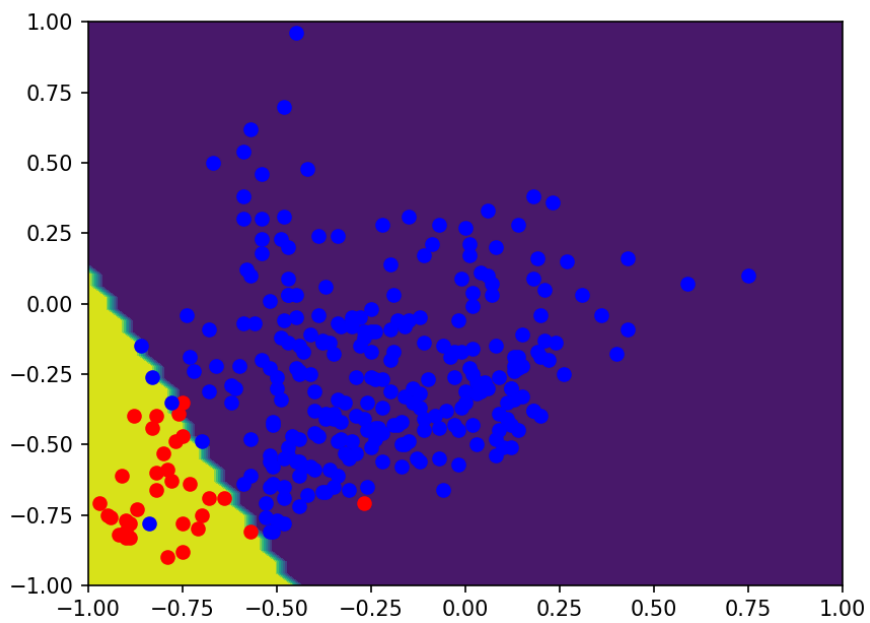
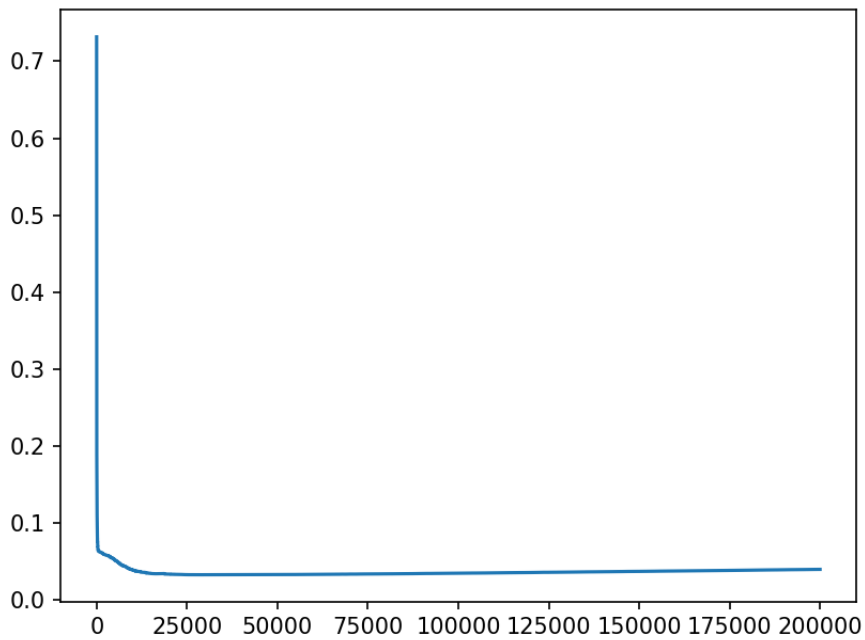
b:



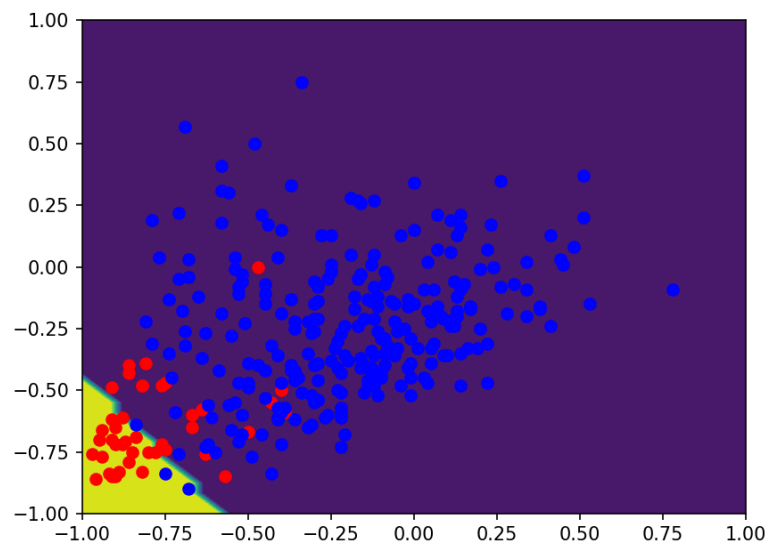
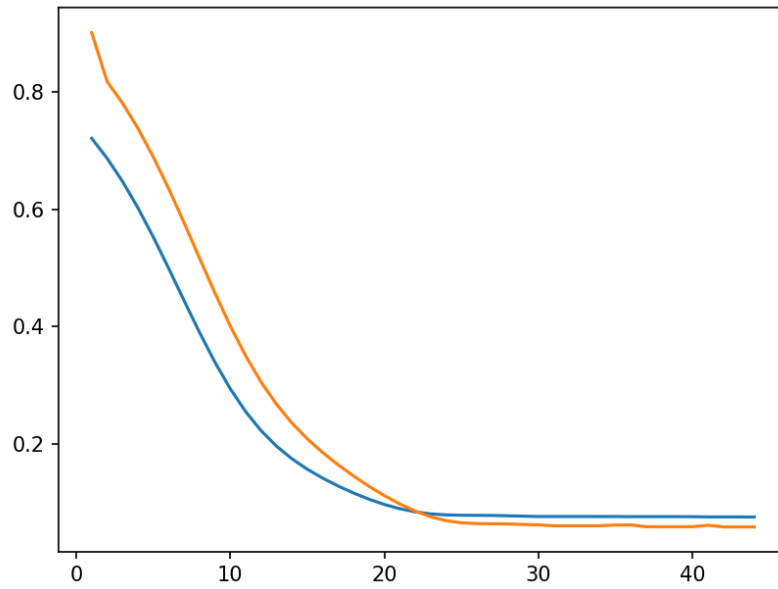
c:  
Gradient Descent



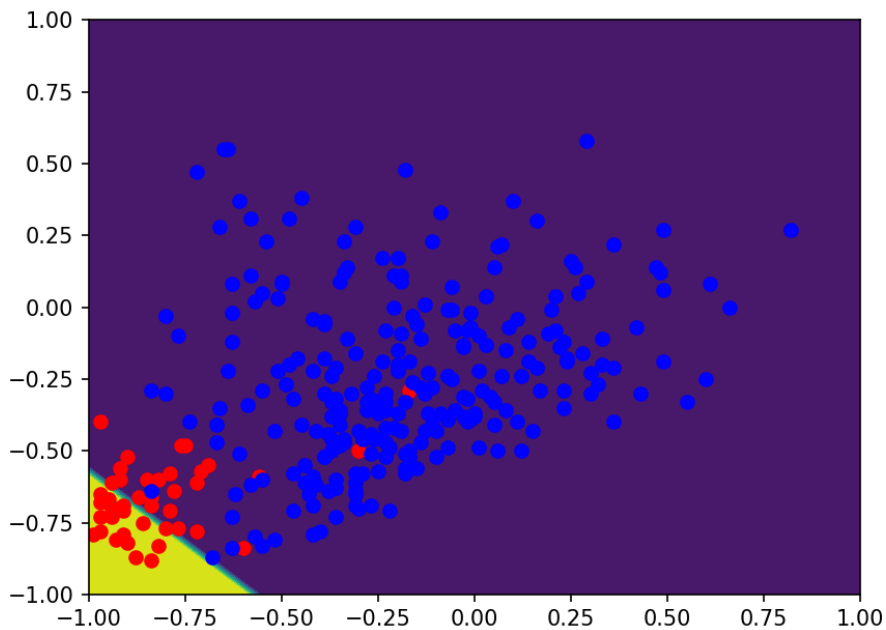
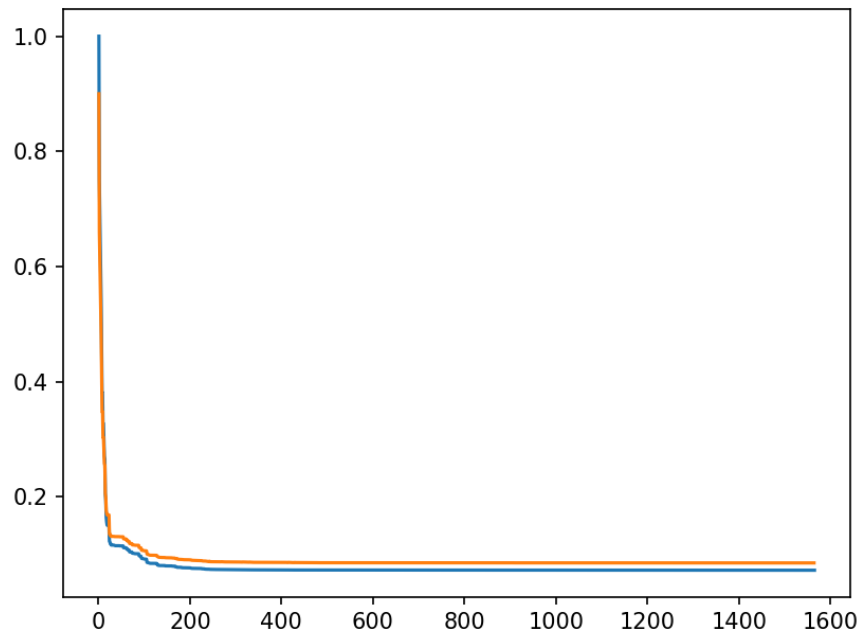
SGD:



d:  
Gradient decent:



SGD:

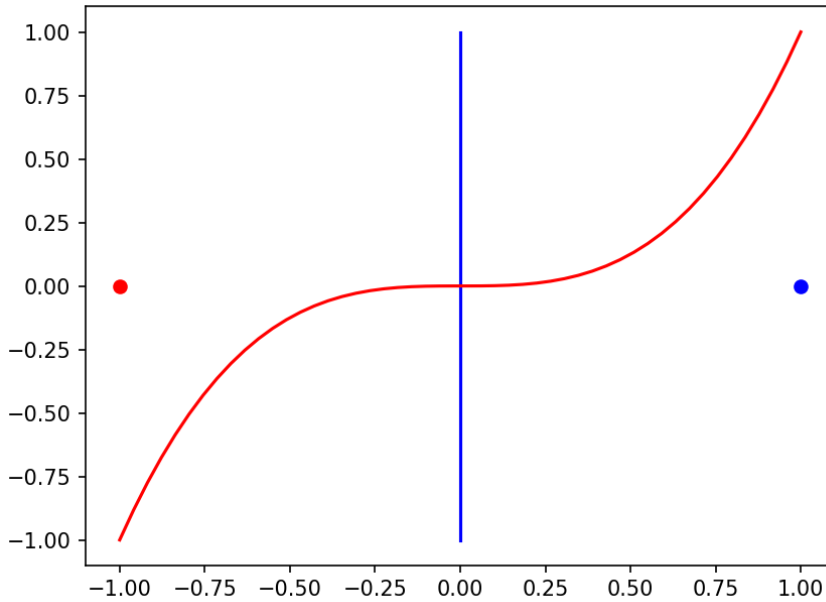


Q3:

a: Since the two points are symmetric about the y axis, the optimal separating hyperplane is just the 'plane' that is the perpendicular bisector of the line segment joining the two points. The optimal separating hyperplane equation is  $g(x) = \text{sign}(x_1)$

b: for the first point,  $z_1 = 1, z_2 = 0$ , for the second point  $z_1 = -1, z_2 = 0$ . Therefore the optimal hyperplane equation  $g(z) = \text{sign}(z_1)$ .

c:



d:

$$z(x)1 = (x1)^3 - x2 \quad z(x)2 = (x1)*(x2)$$

$$z(y)1 = (y1)^3 - y2 \quad z(x)2 = (y1)*(y2)$$

$$z(x) * z(y) = ((x1)^3 - x2) * (y1)^3 - y2 \quad z(x)2 + (x1)*(x2) * (y1)*(y2)$$

$$= (x1)^3 * (y1)^3 - x2 * (y1)^3 - z(x)2 * (x1)^3 + (y1)^3 * (x1)^3 + (x1)*(x2) * (y1)*(y2)$$

e:

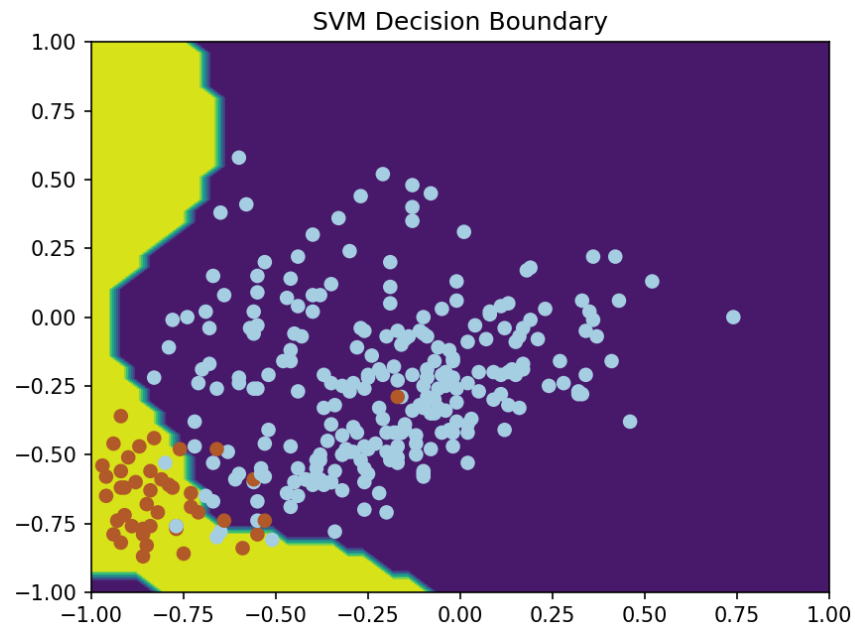
$$g(x) = \text{sign}((x1)^3 - x2) \text{ for any point } (x1, x2)$$

Q4:

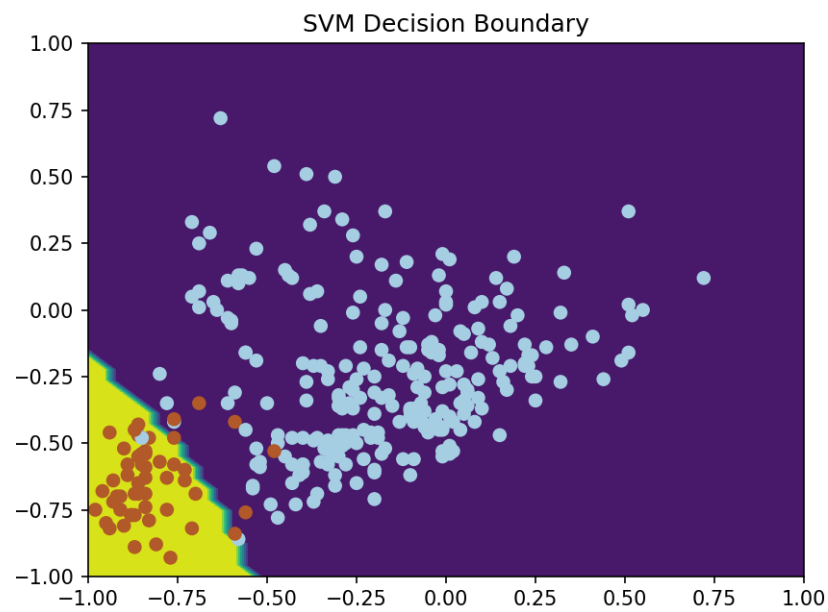
a:

$$C = 100$$



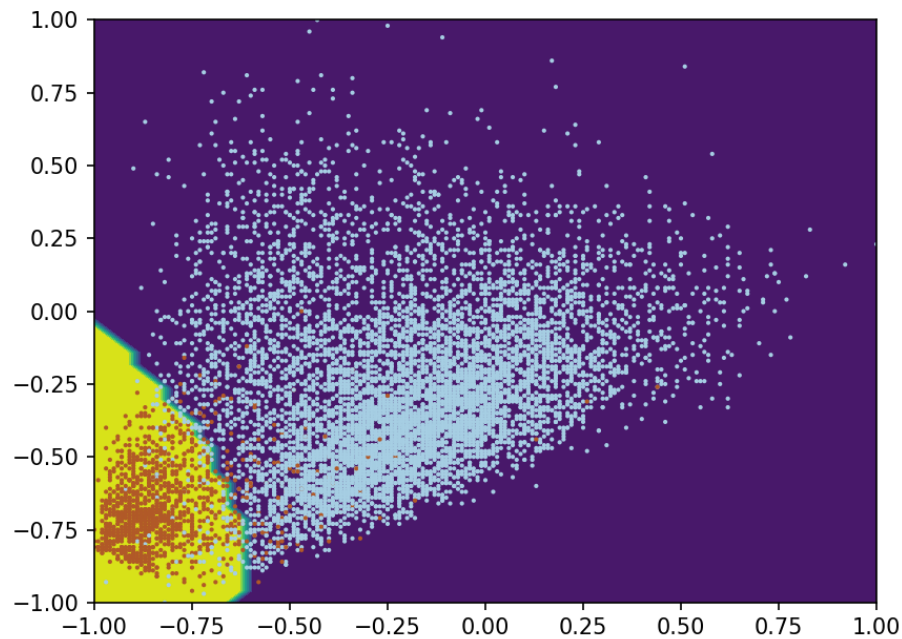


C = 0.01



b: As we can see from the graph, as C gets bigger the decision boundary is getting more complex.

c: C = 0.01



Etest = 0.030117803956434763

Q5: From homework 11, we know:

Etest for Linear model with 8 order polynomial transform is: 0.0316737052678373

Etest for KNN is: 0.030228939764392088

Etest for RBF network is: 0.02967326072460547

From this homework, we know:

Etest for SVM is: 0.030117803956434763

After check etest part on Q2, I got:

Etest for Neural network is: 0.0310086

As we can see all those models have very similar Etest, the highest Etest is only less than 0.002 larger than the lowest Etest. Therefore, I think all of those models perform pretty ok.