

Three numbers are such that the second is 6 less than three times the first, and the third is 2 more than two thirds the first. The sum of the three numbers is 150. Find the largest of the 3 numbers.

Let the first number be x .

Then second number is $3x - 6$ { 6 less than 3 times the first }

Third number is $\frac{2}{3}x + 2$ { 2 more than $\frac{2}{3}$ rd of first }

Sum of all three is 150.

$$\Rightarrow \underline{x + 3x - 6} + \frac{2}{3}x + 2 = 150$$

$$\Rightarrow 4x + \frac{2}{3}x - 6 + 2 = 150$$

$$\Rightarrow \frac{12 + 2}{3}x - 4 = 150 \Rightarrow \frac{14x}{3} = 154$$

$$\Rightarrow x = \frac{3 \times \overset{11}{\cancel{154}}}{14} = \underline{\underline{33}} \rightarrow \text{first number}$$

$$\Rightarrow \text{2nd number} = 3x - 6 = 3 \times 33 - 6 = \underline{\underline{93}}$$

$$\Rightarrow \text{3rd number} = \frac{2}{3}x + 2 = \frac{2}{3} \times 33 + 2 = 22 + 2 = \underline{\underline{24}}$$

So, the largest of the three numbers is 93.

A headset was sold at 212 dollars. If the price included a 6% sales tax, what was the price of headset itself.

Let the original price be x .

$$\text{Sales Tax} = \frac{6}{100} \times x$$

$$\Rightarrow x + \frac{6}{100}x = 212$$

$$\Rightarrow \frac{106}{100}x = 212 \Rightarrow x = \frac{212 \times 100}{106} = 200$$

Thus, price of headset itself was 200 dollars.

Sum of two numbers is 20. If one number is 2 more than half of the other, find the two numbers.

Let the two numbers be x and y .

$$\text{Then } x + y = 20.$$

$$y = 2 + \frac{1}{2}x \quad (2 \text{ more than half of the other})$$

$$\Rightarrow x + 2 + \frac{1}{2}x = 20 \Rightarrow x + \frac{1}{2}x = 18$$

$$\Rightarrow \frac{3}{2}x = 18 \Rightarrow x = \frac{18 \times 2}{3}$$

$$\Rightarrow x = 12$$

$$\Rightarrow y = 2 + \frac{1}{2} \times 12 = 8$$

Thus, the two numbers are 12 and 8.