

**Problem 1.** Find  $dy/dx$ .

1. \*  $y = \cos(x^2)$ .
2.  $y = \left(x + \frac{1}{x}\right)^5$ .
3.  $y = \sqrt{\frac{x}{x+1}}$ .
4.  $y = \sqrt{\frac{1 + \sin x}{1 + \cos x}}$ .
5.  $y = \cot^2(\sin x)$ .
6. \*  $y = \tan^2(4x)$ .
7.  $y \cos x = x^2 + y^2$ .
8.  $x \sin y + y \sin x = 1$ .
9.  $xy = \sqrt{x^2 + y^2}$ .
10.  $\tan(x/y) = x + y$ .

**Problem 2.** Find the equation of tangent and normal lines to the given curve at the given point.

1.  $\sin(x + y) = 2x - 2y$  at  $(\pi, \pi)$ .
2. \*  $x^2 - xy - y^2 = 1$  at  $(2, 1)$  (hyperbola).
3. \*  $x^2 + 2xy + 4y^2 = 12$  at  $(2, 1)$  (ellipse).
4.  $x^2 + y^2 = (2x^2 + 2y^2 - x)^2$  at  $(0, 1/2)$  (cardioid).
5.  $x^{2/3} + y^{2/3} = 4$  at  $(-3\sqrt{3}, 1)$  (astroid).
6.  $y^2(y^2 - 4) = x^2(x^2 - 5)$  at  $(0, -2)$  (devil's curve).

**Problem 3.** Find  $d^2y/dx^2$ .

1.  $x^2 + xy + y^2 = 3$ .
2.  $x^3 - y^3 = 7$ .