

Problem 1. Find whether the following functions are differentiable at the given points.

1. * $f(x) = |x - 1| + |x + 1|$ at $x = -1$ and $x = 1$.

2. $f(x) = \frac{1 - 2x}{3 + x}$ at $x = -3$.

3. $f(x) = |x| + |x - 2|$ at $x = 0$ and $x = 2$.

4. $f(x) = \sqrt{9 - x}$ at $x = 9$.

5. $f(x) = \begin{cases} x^2 + 1 & \text{if } x \leq 1, \\ 3 - x & \text{if } 1 < x \leq 4, \\ \sqrt{x} & \text{if } x > 4, \end{cases}$ at $x = 1$ and $x = 4$.

Problem 2. Use differentiation formulas to differentiate the following functions.

1. * $h(t) = \frac{6t + 1}{6t - 1}$.

2. $f(x) = \frac{\sqrt{x}}{2 + x}$.

3. $g(s) = \frac{s^2 + 1}{s^3 - 1}$.

4. * $f(\theta) = \sec \theta \tan \theta$.

5. $g(\theta) = \theta \cos \theta \sin \theta$.

6. $h(t) = \frac{t \sin t}{1 + t}$.

Problem 3. Find the equations of tangent and normal lines to the following curves at the given point.

1. * $y = x + \sqrt{x}$ at $(1, 2)$.

2. $y = \frac{1}{1 + x^2}$ at $(-1, 1/2)$.

3. $y = \frac{2x}{x + 1}$ at $(1, 1)$.

4. $y = (1 + x) \cos x$ at $(0, 1)$.

Problem 4. Evaluate the following limits.

1. $\lim_{x \rightarrow 0} \frac{\sin 4x}{x \cos x}$.

2. $\lim_{x \rightarrow 0} \frac{\cos x - 1}{2 \sin x}$.