M16600 Lecture Notes

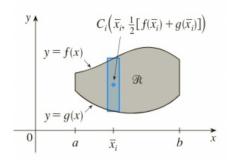
Section 8.3: Center of Mass of Centroid

■ Section 8.3 textbook exercises, page 595: # 29, 30, 32.



Our main objective here is to find the point P on which a thin plate of any given shape balance horizontally as in the figure on the left. This point is called the center of mass of the plate (or the centroid of the plate).

We consider a flat plate (called lamina) that occupies a region \mathcal{R} of the xy-plane.



The center of mass of the region \mathcal{R} is located at the point (\bar{x}, \bar{y}) , where

$$\bar{x} = \frac{1}{A} \int_a^b x [f(x) - g(x)] dx$$

$$\bar{y} = \frac{1}{A} \int_a^b \frac{1}{2} \left([f(x)]^2 - [g(x)]^2 \right) dx$$

Here A is the <u>area</u> of the region \mathcal{R} .

See the discussion on page 600-603 of the textbook for more detail

Example: Find the centroid of the region bounded by the line y = x and the parabola $y = x^2$.