An important Limit

$$\lim_{\theta \to 0} \frac{\sin \theta}{\theta} = 1 .$$

The derivatives of $y = \sin u$, $y = \cos u$:

$$\frac{d}{dx}(\sin x) = \cos x , \qquad \frac{d}{dx}(\sin u) = \cos u \frac{du}{dx} .$$

$$\frac{d}{dx}(\cos x) = -\sin x , \qquad \frac{d}{dx}(\cos u) = -\sin u \frac{du}{dx} .$$

Example 1. Differentiate $y = \sin \sqrt{x^2 + 1}$.

Example 2. Find the derivative of $y = x^2 \cos x^3$.

Example 3. Find the derivative of
$$y = \frac{\sin^2 x}{\sqrt{x}}$$
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