- 1. Let Ω = {1,2,...,6}. Provide 3 distinct σ-fields on Ω.
- 2. Let F, and F2 be two offields on D. Then, prove or disprove:
  - a. F, UFz is a offield on I.
  - b. F, n F2 is a o-field on R.
- 3. Let B denote the  $\sigma$ -field (on B) generated by a collection  $\{(-\infty, \kappa] : \kappa \in \mathcal{R}_{\delta}\}$ . Show that following type of sets belong to B:

  (a)  $(-\infty, \kappa)$  (b)  $(\kappa, +\infty)$  (c)  $[\kappa, +\infty)$  (d)  $[\kappa, \kappa_2]$  (e)  $(\kappa, \kappa_2)$  (f)  $[\kappa, \kappa_2]$  (e)  $(\kappa, \kappa_2)$ .
- 4. Let {ensozo be a sequence of real numbers.

  Define, yn = inf xx & 3n = sup xx.

  xzn
  - a. Prove that lymbaz, and longar converge or diverge, but never oscillate. Hence, limy and lim on is well define.
    - b. Show that  $3 \times n_{n_2}$ , converges to  $\infty$  if and only if  $x = \lim_{n \to \infty} y_n = \lim_{n \to \infty} y_n$ .

lim zn is called lim inf zn and nhao in sup zn.

lim inf 
$$A_n = \{ \omega : \lim_{n \to \infty} f(\omega) = 1 \}$$
.

Show the following:

2. lim inf 
$$A_n = \bigcup_{n \in I} \bigcap_{K = n} A_K (denok by A)$$

5. show that 
$$P(A) \leq \liminf_{n \to \infty} P(A_n)$$
.

7. Show that if 
$$A = A$$
, then define  $\lim_{n \to \infty} A_n = A = A$  and show that  $P(A) = \lim_{n \to \infty} P(A_n)$ .