



Subject: Programming With Python (01CT1309)

Aim: Analysis of Discrete-Time Signals Using Z-Transform

Experiment No: 17

Date:

Enrollment No:92510133028

Aim: Analysis of Discrete-Time Signals Using Z-Transform

IDE:

Install Library

pip install sympy

Example 1:

```
import sympy as sp
# Define symbols
n, z, a = sp.symbols('n z a')
# Define the signal x[n] = a^n * u[n]
x_n = a**n
# Compute the Z-transform
X_z = sp.summation(x_n * z**(-n), (n, 0, sp.oo))
# Print the result
print("Z-transform of x[n] = a^n u[n]:")
sp.pprint(X_z, use_unicode=True)
```

The screenshot shows a Jupyter Notebook cell with the following content:

```
[1]: import sympy as sp
# Define symbols
n, z, a = sp.symbols('n z a')
# Define the signal x[n] = a^n * u[n]
x_n = a**n
# Compute the Z-transform
X_z = sp.summation(x_n * z**(-n), (n, 0, sp.oo))
# Print the result
print("Z-transform of x[n] = a^n u[n]:")
sp.pprint(X_z, use_unicode=True)
```

The output of the cell is:

```
... 1.1s
... Z-transform of x[n] = a^n u[n]:
{ 1           |a|
 { --       for |--| < 1
   a           |z|
   - + 1
   z
{           ∞
 {           n -n
   a · z     otherwise
   |
   n = 0
```



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Example 2:

```
# Define symbols
n, z, a = sp.symbols('n z a')
# Define the signal x[n] = a^n * u[n]
x_n = 2**n
# Compute the Z-transform
X_z = sp.summation(x_n * z**(-n), (n, 0, sp.oo))
# Print the result
print("Z-transform of x[n] = a^n u[n]:")
sp.pprint(X_z, use_unicode=True)
```

```
# Define symbols
n, z, a = sp.symbols('n z a')
# Define the signal x[n] = a^n * u[n]
x_n = 2**n
# Compute the Z-transform
X_z = sp.summation(x_n * z**(-n), (n, 0, sp.oo))
# Print the result
print("Z-transform of x[n] = a^n u[n]:")
sp.pprint(X_z, use_unicode=True)
✓ 0.0s
Z-transform of x[n] = a^n u[n]:
{  
    1      1  
    --      for -- < 1/2  
    2      |z|  
    1 - -  
    z  
}  
{  
    ∞  
    \  
    n -n  
    2 ·z      otherwise  
}  
n = 0
```



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Example 3:

```
import sympy as sp
# Define symbols
n, z = sp.symbols('n z')
# Define the unit step signal u[n]
u_n = 1
# Compute the Z-transform
U_z = sp.summation(u_n * z**(-n), (n, 0, sp.oo))
# Print the result
print("Z-transform of the unit step signal u[n]:")
sp.pprint(U_z, use_unicode=True)
```

```
✓ import sympy as sp
# Define symbols
n, z = sp.symbols('n z')
# Define the unit step signal u[n]
u_n = 1
# Compute the Z-transform
U_z = sp.summation(u_n * z**(-n), (n, 0, sp.oo))
# Print the result
print("Z-transform of the unit step signal u[n]:")
sp.pprint(U_z, use_unicode=True)
✓ 0.0s

Z-transform of the unit step signal u[n]:
{  
    1      1  
    --      --  
    1 - -  
    z      |z|  
    {  
        ∞  
        }  
        }  
        z-n      otherwise  
    n = 0
```



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Example 4:

```
import sympy as sp
# Define symbols
n, z, alpha = sp.symbols('n z alpha')
# Define the signal x[n] = exp(alpha * n) * u[n]
x_n = sp.exp(alpha * n)
# Compute the Z-transform
X_z = sp.summation(x_n * z**(-n), (n, 0, sp.oo))
# Print the result
print("Z-transform of x[n] = exp(alpha * n) u[n]:")
sp.pprint(X_z, use_unicode=True)
```

```
import sympy as sp
# Define symbols
n, z, alpha = sp.symbols('n z alpha')
# Define the signal x[n] = exp(alpha * n) * u[n]
x_n = sp.exp(alpha * n)
# Compute the Z-transform
X_z = sp.summation(x_n * z**(-n), (n, 0, sp.oo))
# Print the result
print("Z-transform of x[n] = exp(alpha * n) u[n]:")
sp.pprint(X_z, use_unicode=True)
✓ 0.0s

Z-transform of x[n] = exp(alpha * n) u[n]:

$$\sum_{n=0}^{\infty} z^{-n} \cdot e^{\alpha \cdot n}$$

n = 0
```



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Example 5:

```
import sympy as sp
# Define symbols
n, z = sp.symbols('n z')
# Define the finite sequence x[n] = {1, 2, 3}
x_n = [1, 2, 3]
# Compute the Z-transform manually
X_z = sum(x_n[i] * z**(-i) for i in range(len(x_n)))
# Print the result
print("Z-transform of the finite sequence {1, 2, 3}:")
sp.pprint(X_z, use_unicode=True)
```

```
import sympy as sp
# Define symbols
n, z = sp.symbols('n z')
# Define the finite sequence x[n] = {1, 2, 3}
x_n = [1, 2, 3]
# Compute the Z-transform manually
X_z = sum(x_n[i] * z**(-i) for i in range(len(x_n)))
# Print the result
print("Z-transform of the finite sequence {1, 2, 3}:")
sp.pprint(X_z, use_unicode=True)
✓ 0.0s

Z-transform of the finite sequence {1, 2, 3}:

$$\frac{2}{z} + \frac{3}{z^2}$$

```

Example 6

```
import sympy as sp
# Define symbols
n, z, omega = sp.symbols('n z omega')
# Define the sinusoidal sequence x[n] = sin(omega * n) * u[n]
x_n = sp.sin(omega * n)
# Compute the Z-transform
X_z = sp.summation(x_n * z**(-n), (n, 0, sp.oo))
```



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Print the result

```
print("Z-transform of x[n] = sin(omega * n) u[n]:")  
sp pprint(X_z, use_unicode=True)
```

```
import sympy as sp  
# Define symbols  
n, z, omega = sp.symbols('n z omega')  
# Define the sinusoidal sequence x[n] = sin(omega * n) * u[n]  
x_n = sp.sin(omega * n)  
# Compute the z-transform  
X_z = sp.summation(x_n * z**(-n), (n, 0, sp.oo))  
# Print the result  
print("Z-transform of x[n] = sin(omega * n) u[n]:")  
sp pprint(X_z, use_unicode=True)
```

✓ 0.0s

Z-transform of x[n] = sin(omega * n) u[n]:

$$\sum_{n=0}^{\infty} z^{-n} \cdot \sin(n \cdot \omega)$$



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Post Lab Exercise:

- Using Python, compute the Z-transform of the sequence $x[n] = 3^n u[n]$.

```
# Using Python, compute the Z-transform of the sequence . x[n] = 3^n * u[n]
import sympy as sp
# Define symbols
n, z = sp.symbols('n z')
# Define the signal x[n] = 3^n * u[n]
x_n = 3**n
# Compute the Z-transform
X_z = sp.summation(x_n * z**(-n), (n,
| 0, sp.oo))
# Print the result
print("Z-transform of x[n] = 3^n u[n]:")
sp.pprint(X_z, use_unicode=True)
```

✓ 0.0s

Z-transform of $x[n] = 3^n u[n]$:

$$\left\{ \begin{array}{ll} \frac{1}{z - 3} & \text{for } |z| < 1/3 \\ \infty & \text{otherwise} \end{array} \right.$$

$n = 0$

- Using Python, compute the Z-transform of the sequence $x[n] = \cos(wn)u[n]$.



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```
# Using Python, compute the z-transform of the sequence x[n] = cos(wn) * u[n]
import sympy as sp
# Define symbols
n, z, omega = sp.symbols('n z omega')
# Define the sinusoidal sequence x[n] = cos(omega * n) * u[n]
x_n = sp.cos(omega * n)
# Compute the z-transform
X_z = sp.summation(x_n * z**(-n), (n, 0, sp.oo))
# Print the result
print("Z-transform of x[n] = cos(omega * n) u[n]:")
sp.pprint(X_z, use_unicode=True)
```

✓ 0.0s

Z-transform of x[n] = cos(omega * n) u[n]:

$$\sum_{n=0}^{\infty} z^{-n} \cdot \cos(n\omega)$$

n = 0

Github: https://github.com/keshvi1234/PWP_experiment