$$Ut t = C^2 U \times \times , \quad 0 \langle X \langle L , t \rangle 0$$

$$(L(0+) = U \langle U + \rangle = 0 \quad t \rangle 0 \quad t$$

$$u(x,0) = u_0$$

$$U(0,t) = U(L,t) = 0 \quad tid \qquad capxikin taxitata$$

$$U(x,0) = U_0(x) \quad U_x(x,0) = U_0(x) \quad x \in (0,L)$$

$$\omega \qquad \text{Gapxikin Deon}$$

$$U(x,t) = \sum_{n=1}^{\infty} \sin\left(\frac{n\pi}{x}\right) \left(\frac{b_n \cos j_n t + b_n \sin j_n t}{x}\right) \quad j_{n=1} = 0.$$



$$b_{n} = \frac{2}{L} \int_{0}^{L} U(x) \sin\left(\frac{n\pi}{L}x\right) dx$$

$$b_{n} = \frac{2}{L} \int_{0}^{L} U(x) \sin\left(\frac{n\pi}{L}x\right) dx$$

$$\int_{0}^{L} U(x) \cos\left(\frac{n\pi}{L}x\right) dx$$

$$\int_{0}^{L} U(x) dx$$

```
\frac{\left(\chi_{L}\alpha_{n}=4\kappa\right)-\frac{1}{n\pi}\frac{1}{2}+\frac{1}{(n\pi)^{2}}\left(\sin\left(n\pi\chi\right)\right)'dx}{2}
                                      = -\frac{1}{\eta \eta} \cdot \left(\frac{1}{2}\right) + \frac{1}{(\eta \eta)^2} \cdot \sin\left(\frac{\eta \eta}{2}\right)
     (year n=4K+2)
                                                                           \frac{1}{2}, n = 4k+1
-\frac{1}{2}, n = 4k+3
0, Siagopetika
• Συγεισφοροί αρτίων:
      \frac{(-\frac{1}{2}n\eta)}{\frac{1}{2}n\eta}, n=4\kappa
                        , διαφορετικά
       Δυνεισφορά Περιττών:
           \frac{1}{2(n\pi)^2}, n=4\kappa+1
+ \frac{-1}{2(n\pi)^2}, n=4\kappa+3
0, S(\alpha (pop ET) \kappa \alpha (pop ET) \kappa \alpha (pop ET)
        και οι δυο σινεισφορές αιφορούν τον όρο \left(\frac{1}{n\pi}\left(\frac{1}{2}\cos(\frac{n\pi}{2})\right)\right)
  · Διατηρώ το αρχικό μου προβηρία και δοκιμάζω
           U(x,t) = \frac{1}{2}(x \pm ct)
              U_{t} = \pm c f'(x \pm c t) [\pm c \cdot \pm c
               Utt = C^2 f''(x \pm Ct)
                Ux = f'(x \pm ct), Ux = f''(x \pm ct)
```

```
Utt = C^2 U \times \times \Longrightarrow C^2 f''(\times \pm ct) = C^2 f''(\times \pm ct)
 O NOTE OPITU,

\frac{U_0(x)}{U_0(x)} = \frac{U_0(x)}{-U_0(x)}, \quad x \in (0, L)

\frac{U_0(x)}{U_0(x+2L)}, \quad S_{LOCIPOPETIKO}

 ETOT KOLVW TOV DO(X) PEPITTA KOL 2L-PEPIOSIKA
  Ομοίως, κάνω και χια την αρχική ταχύτητα.

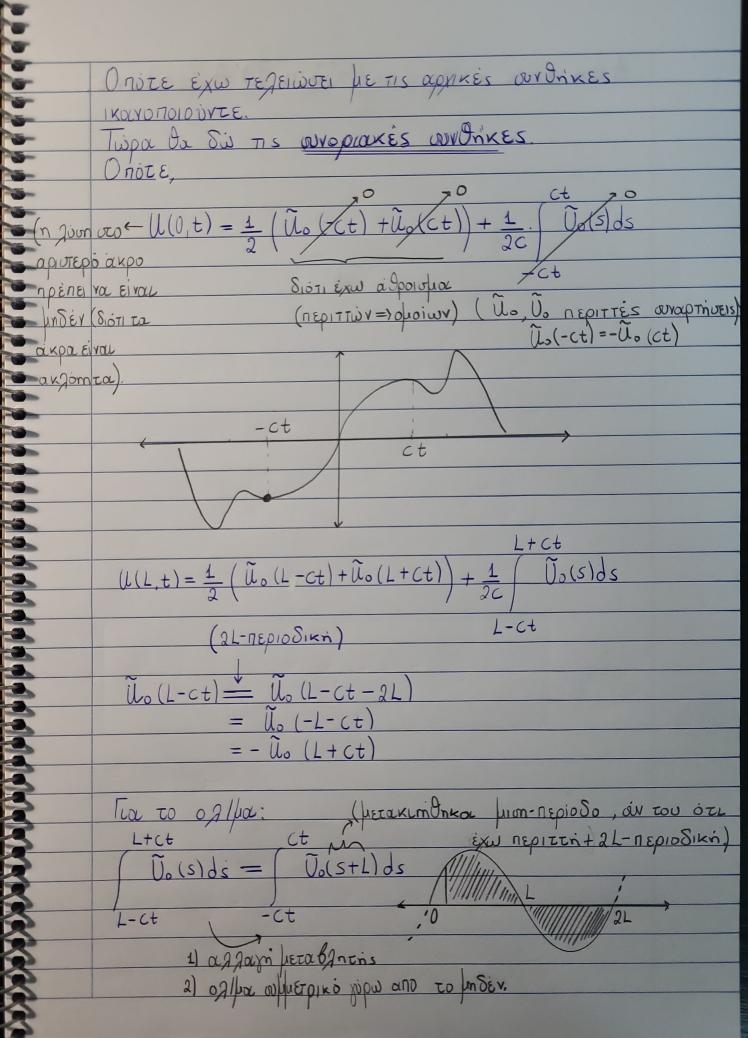
= > \tilde{V}_0: Περιττή + 2L^- περιοδική.
  Monificial Malua Sio R

x+ct
        U(x,t) = \frac{1}{2} \left[ \widetilde{U}_{o}(x-ct) + \widetilde{U}_{o}(x+ct) \right] + \frac{1}{2c} \left[ \widetilde{U}_{o}(s) ds \right]
    αυτο ικανοποιεί την Utt= C2Uxx, χωρίς ομως τις αρχικές συνθ
   θέρω τα μπορώ τα παραχωχίζω ορίτα της μορφής:
 \frac{\partial}{\partial x_{j}} \begin{cases} f(s)ds = \frac{2b}{2x} f(b) - \frac{2\alpha}{2x_{j}} f(\alpha) \\ \frac{\partial}{\partial x_{j}} f(\alpha) = \frac{2\alpha}{2x_{j}} f(\alpha) \end{cases}
Opizw, T := \widehat{U}_{o}(s) ds
Onote,
\frac{2I - C\widetilde{U}_{b}(x+ct) - C\widetilde{U}_{b}(x-ct)}{2t}
 (2) • \frac{2^2T}{2+2} = c^2 \tilde{U}_0'(x+ct) - c^2 \tilde{U}_0'(x-ct)
```

(3)
$$\frac{\Im I}{\Im X} = \tilde{U}_0(X+Ct) - \tilde{U}_0(X-Ct)$$

(4) $\frac{\Im^2 I}{2x^2} = \tilde{U}_0'(X+ct) - \tilde{U}'(X-Ct)$

At anthertaction to (2) kar (4) the application of the extension, enaglished in extension, onote to (1) kar onote to (1) kar



Auti Eiras n gezohem, Noon D'Allembert