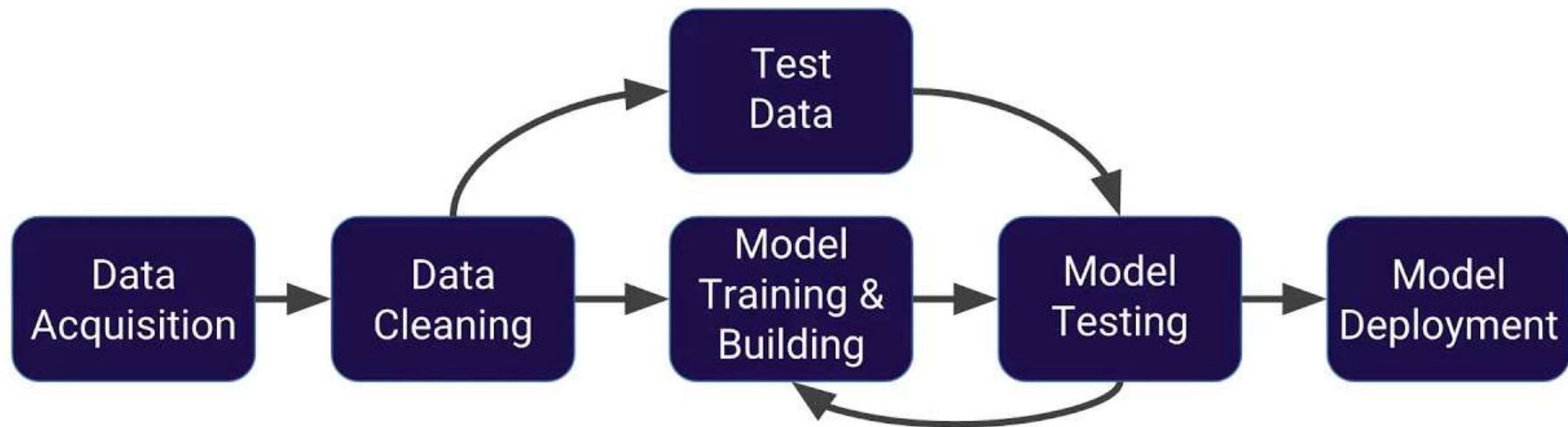


## 1.2

- Basic Components and Key Terminology of Machine Learning,
- Data types
- Training and testing, activation functions,
- Overfitting and under fitting
- Bias- variance Tradeoff.

# Basic Components and Key Terminology of Machine Learning

## Machine Learning Process

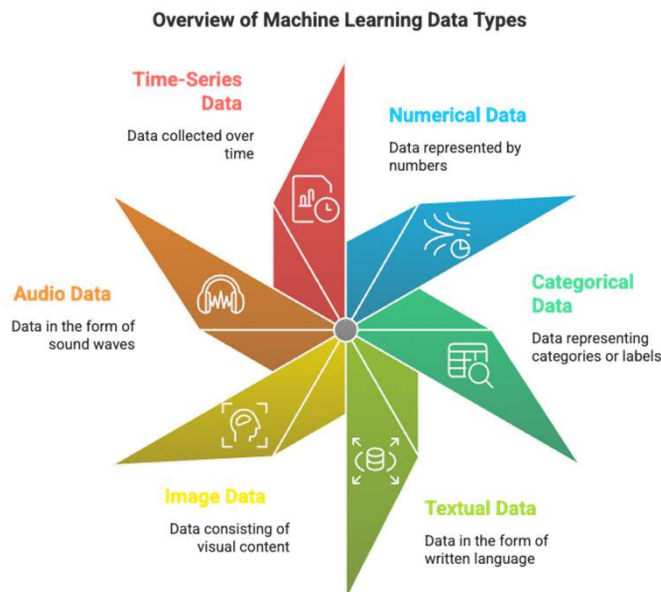


# Key Terminology in Machine Learning

| Term                                  | Definition  |
|---------------------------------------|---|
| Supervised Learning                   | Learning with labeled data (e.g., classification, regression).  |
| Unsupervised Learning                 | Learning patterns from unlabeled data (e.g., clustering, dimensionality reduction).                   |
| Reinforcement Learning                | Learning via rewards and penalties from interactions with an environment.                             |
| Overfitting                           | Model performs well on training data but poorly on unseen data.                                       |
| Underfitting                          | Model is too simple to capture the patterns in data.  |
| Generalization                        | Model's ability to perform well on new, unseen data.  |
| Cross-Validation                      | A method to evaluate model performance by splitting data into multiple subsets.                       |
| Hyperparameters                       | Settings that define the model structure or how it's trained (e.g., learning rate, number of layers). |
| Epoch                                 | One complete pass through the entire training dataset.  |
| Bias                                  | Error due to overly simplistic assumptions in the model.  |
| Variance                              | Error due to model sensitivity to small fluctuations in the training set.                             |
| Confusion Matrix                      | Table used to evaluate the performance of a classification algorithm.                                 |
| Accuracy, Precision, Recall, F1 Score | Metrics used to evaluate model performance.   |

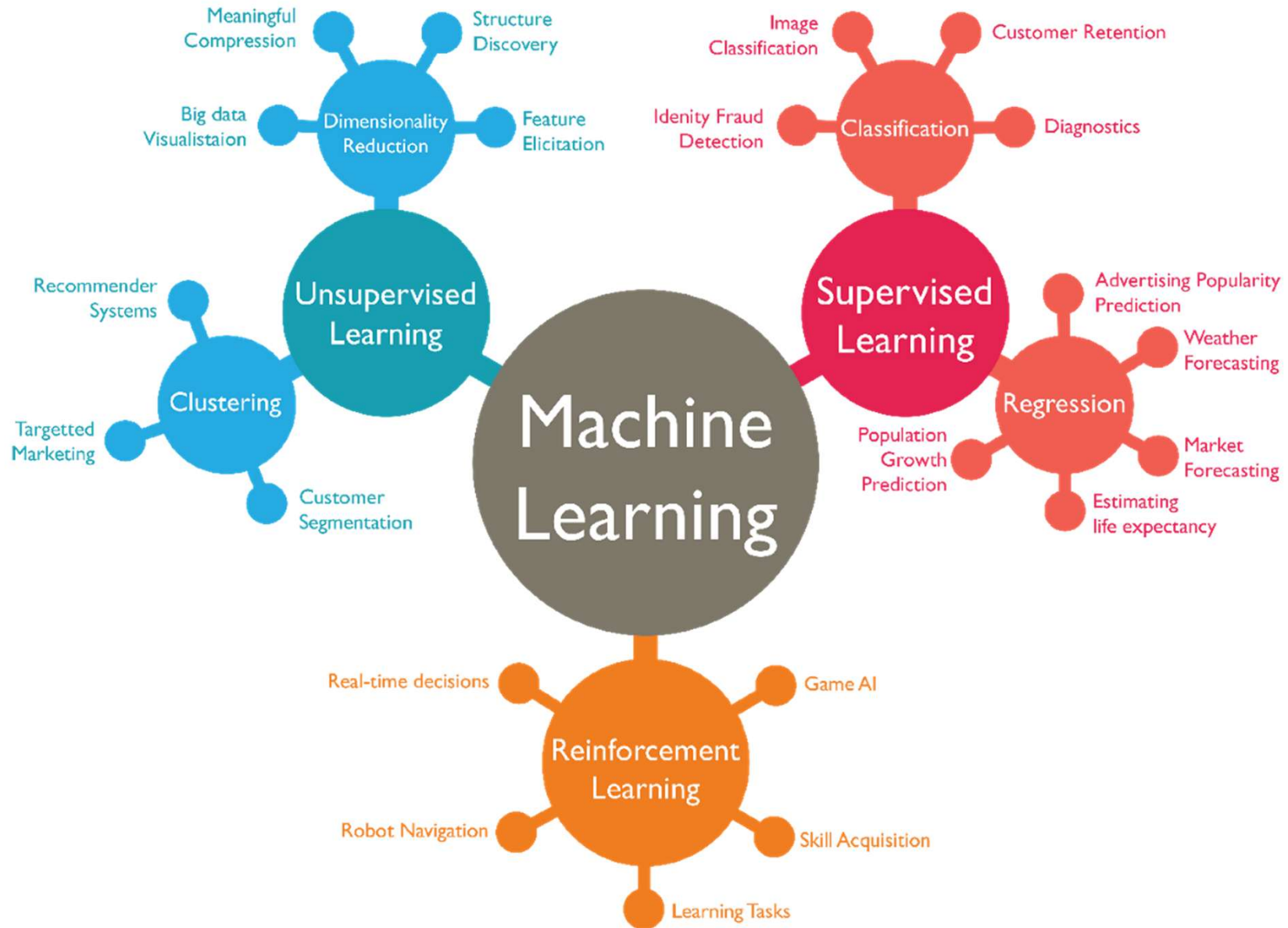
# Data Types in ML

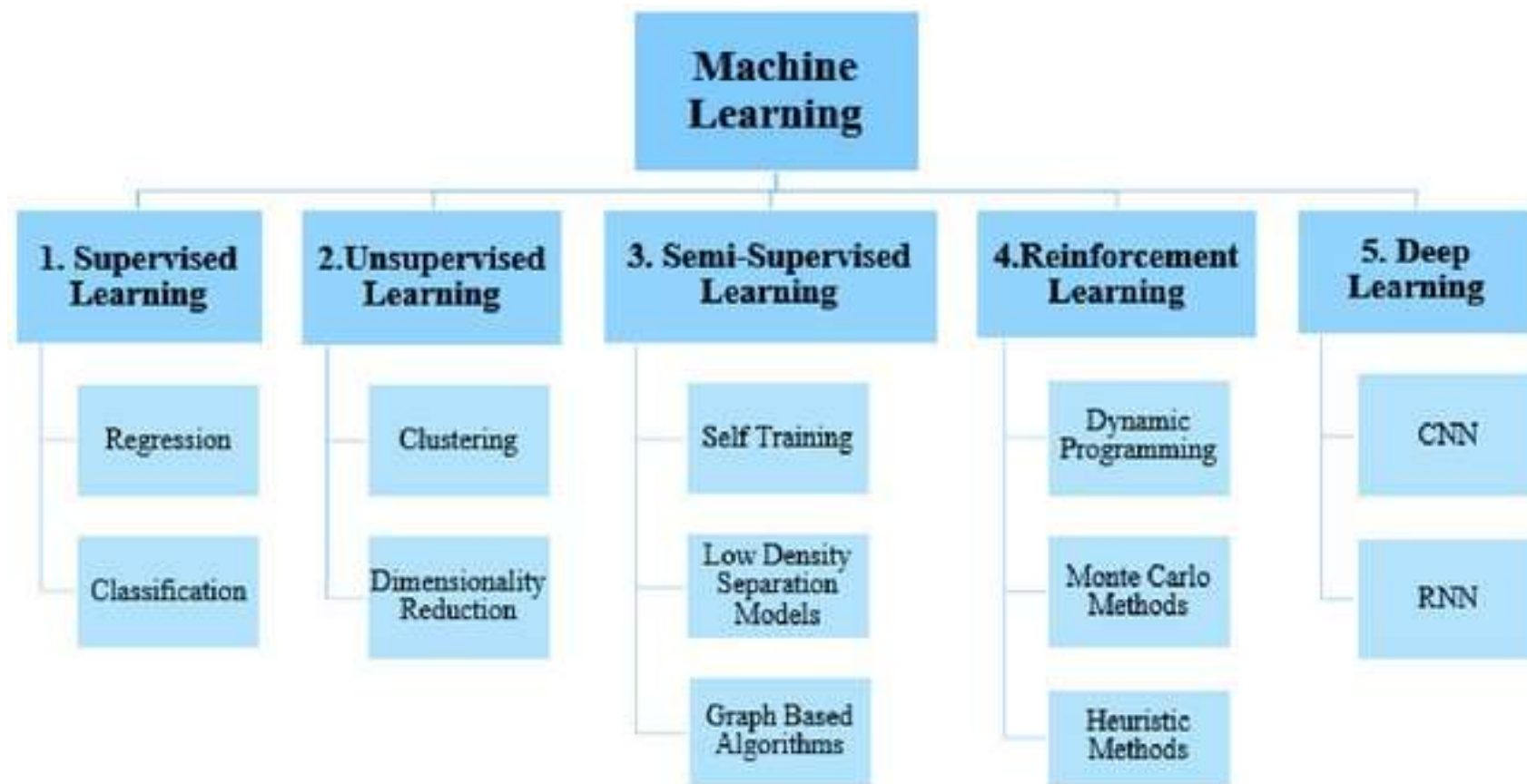
## Types of Data in Machine Learning

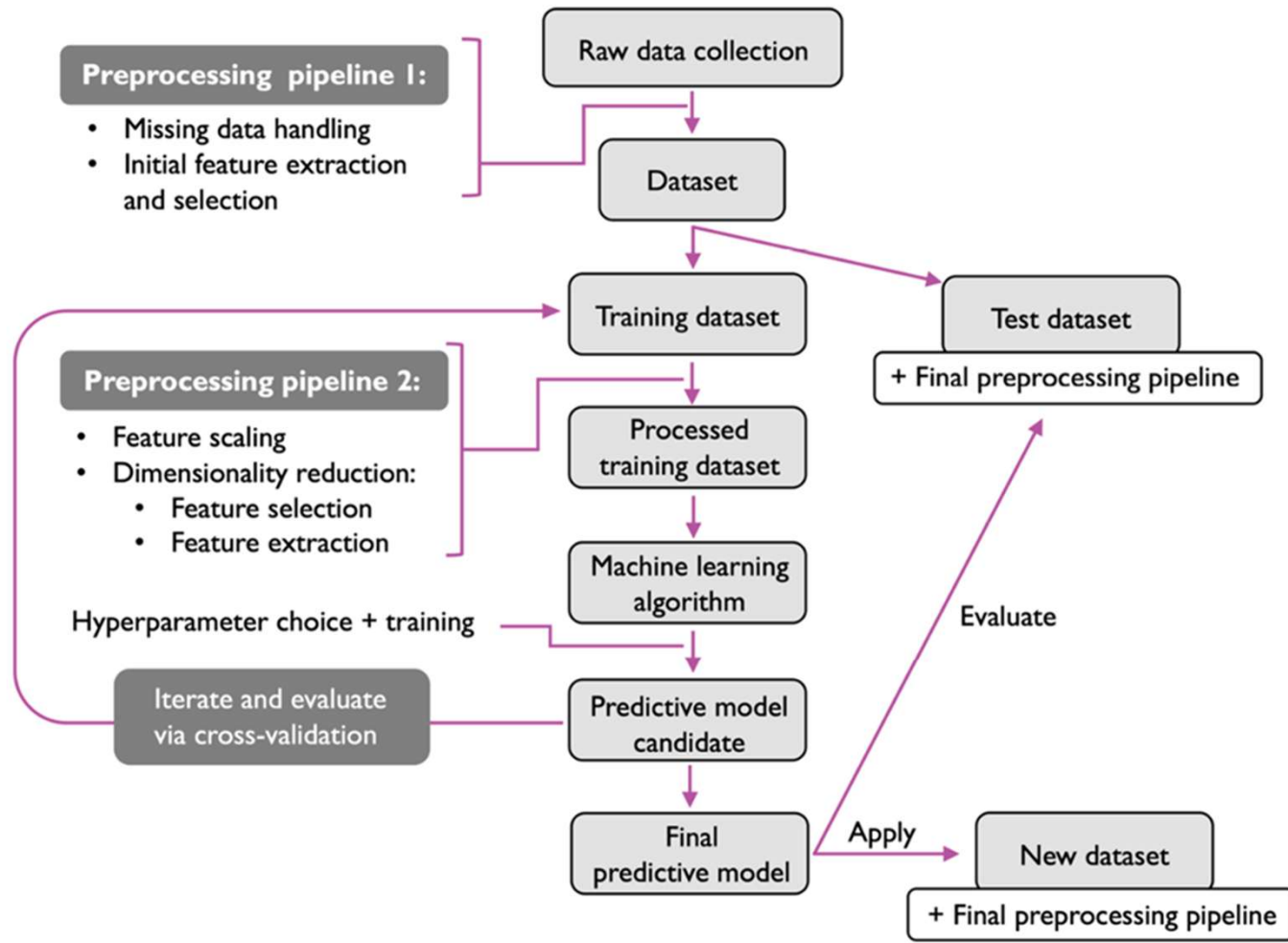


- 1. Structured Data**
  - Data that is organized into rows and columns and is stored in databases or spreadsheets. (e.g., spreadsheets, databases).
  - It follows a fixed schema, making it easy to query and analyze.
  - Examples: Customer databases, sales transactions, student grades, Excel sheets
- 2. Unstructured Data**
  - Data that does not follow a predefined data model or structure.
  - It is harder to analyze and process directly but contains valuable insights when processed with the right tools.
  - Examples: Emails, social media posts, audio files, video recordings, images, and text documents.
- 3. Semi-Structured Data**
  - Data that does not reside in a relational database but still has some structure through tags or markers.
  - It combines elements of both structured and unstructured data.
  - Examples: JSON files, XML documents, HTML pages, log files.
- 4. Quantitative (Numerical) Data**
  - Expressed in numbers; measurable.
  - Types:
    - **Discrete:** Countable (e.g., number of clicks).
    - **Continuous:** Measurable (e.g., temperature, price).
- 5. Qualitative (Categorical) Data**
  - Descriptive; represents categories.
  - Types:
    - **Nominal:** No order (e.g., gender, colors).
    - **Ordinal:** Ordered (e.g., education level, rating scale).
- 6. Time Series Data**
  - Data collected at different time points.
  - Example: Stock prices, weather logs.
- 7. Text Data**
  - Unstructured data in natural language.
  - Example: Tweets, reviews, news articles.
- 8. Image & Video Data**
  - Pixels forming visual content.
  - Used in computer vision tasks like classification, detection, and segmentation.

# Type of Machine learning

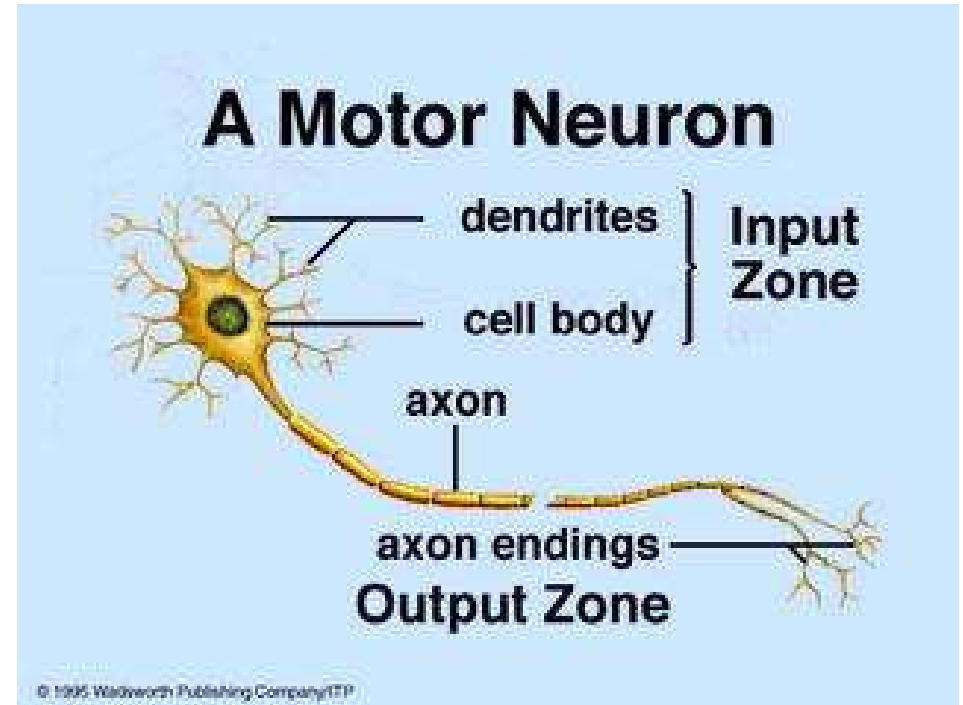






# *Biological Neural Networks*

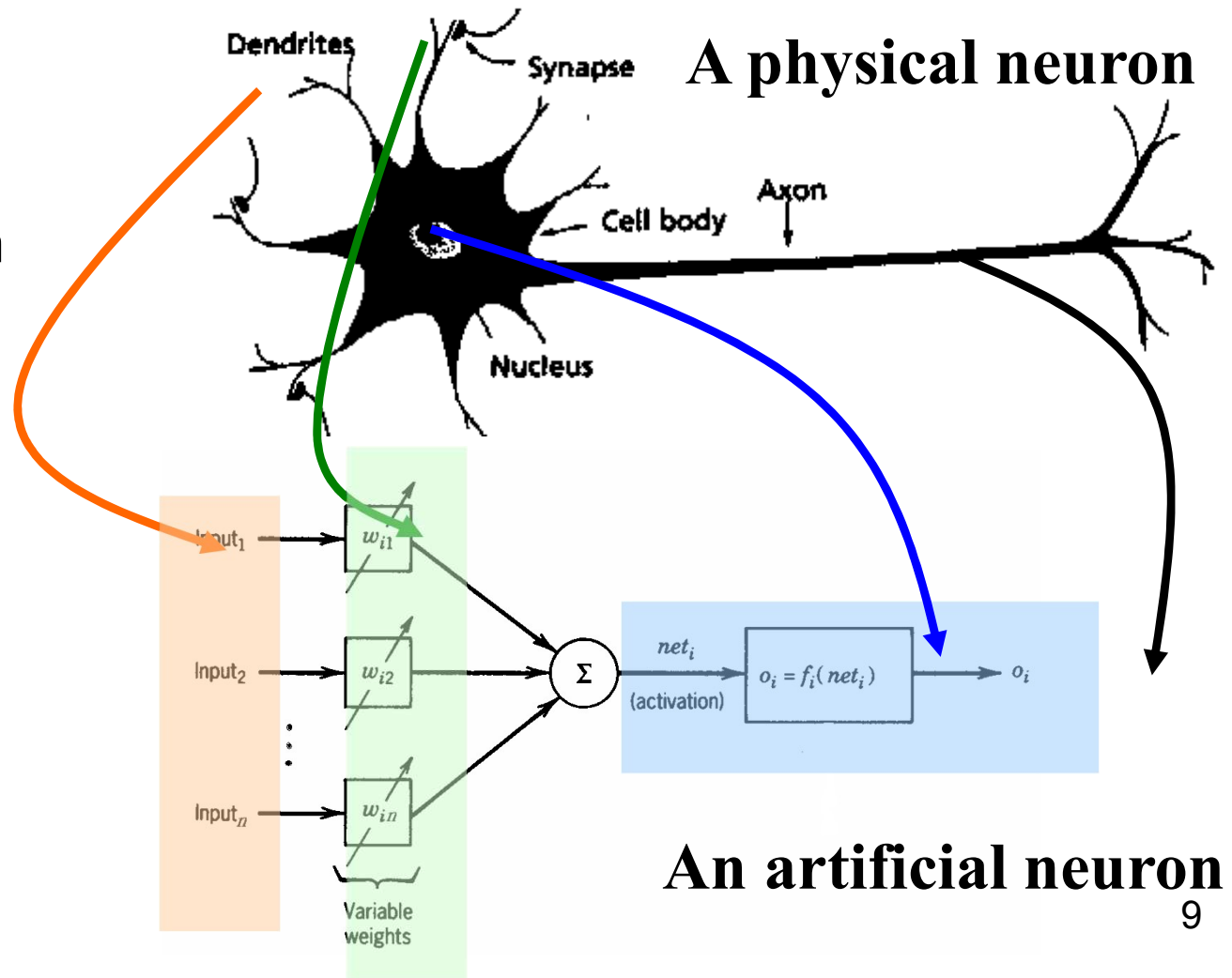
- A biological neuron has three types of main components; dendrites, soma (or cell body) and axon.
- Dendrites receives signals from other neurons.
- The soma, sums the incoming signals. When sufficient input is received, the cell fires; that is it transmit a signal over its axon to other cells.



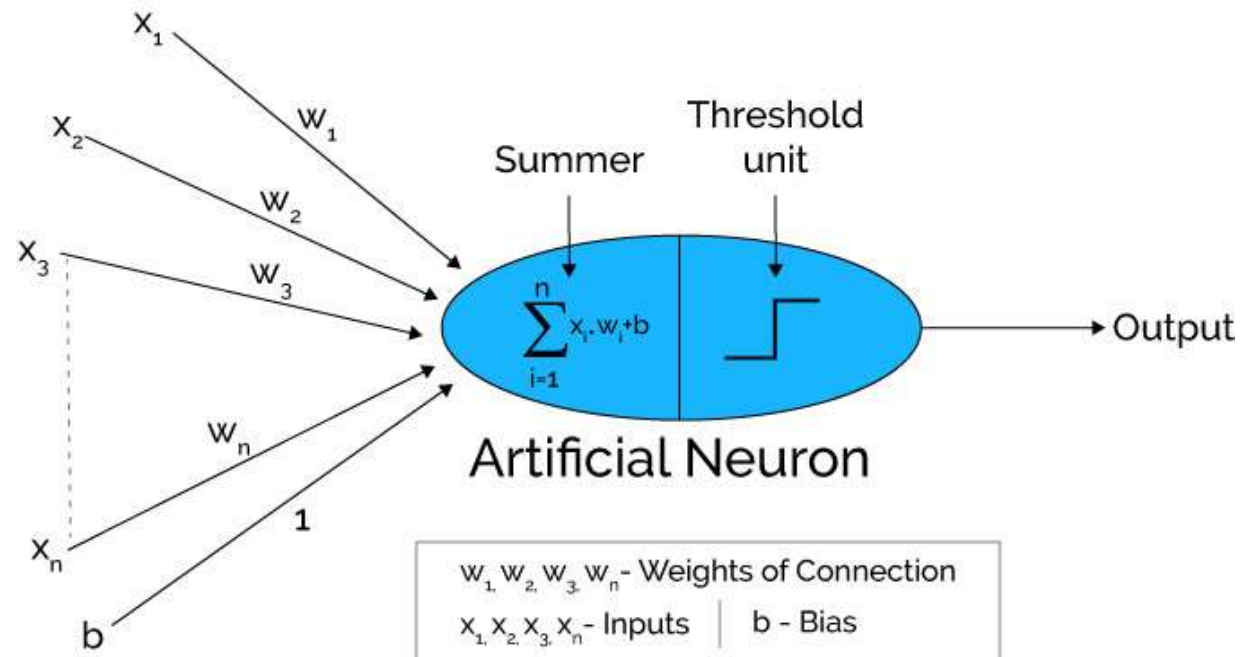
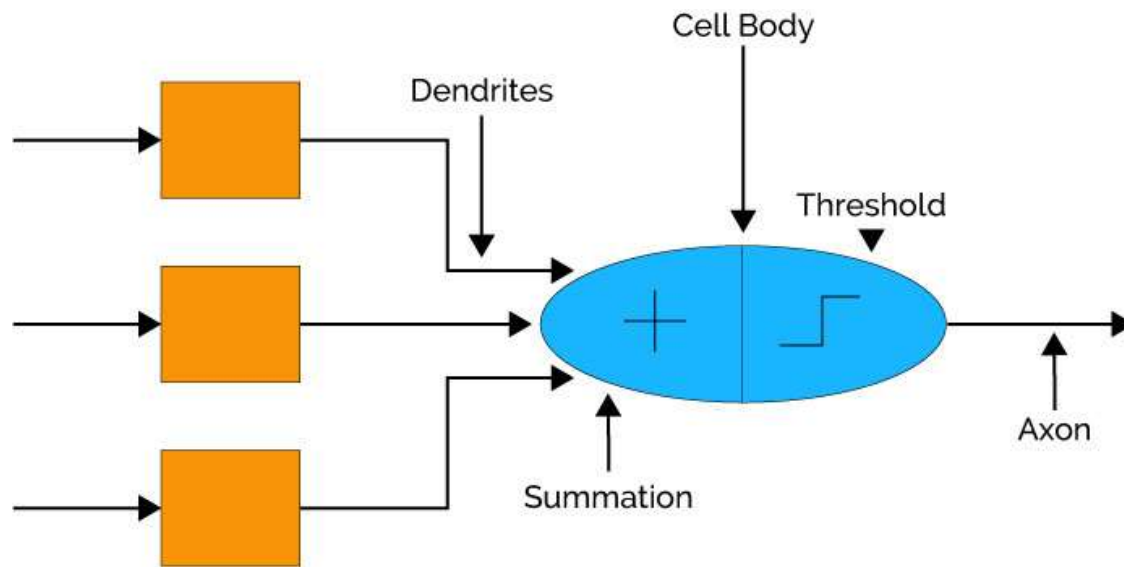


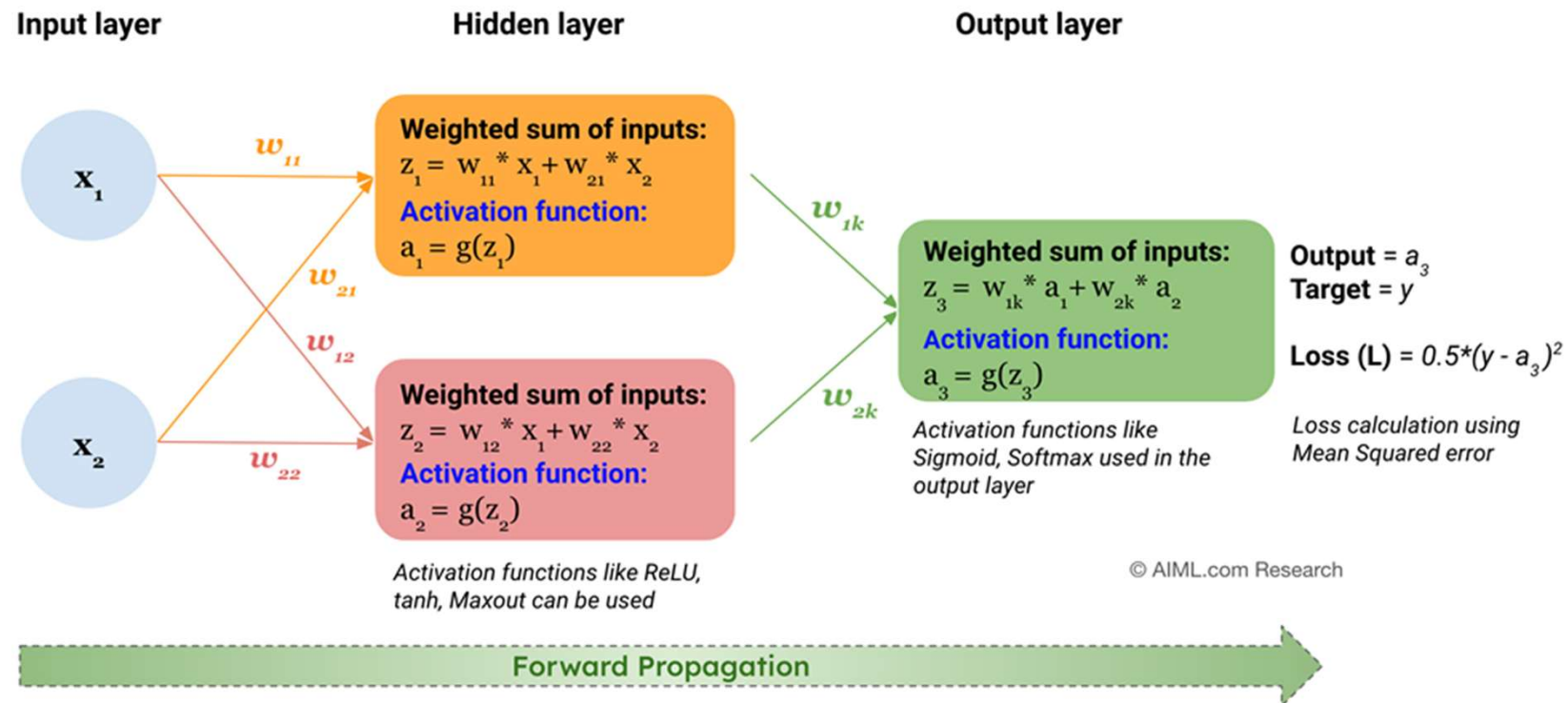
# Artificial Neurons

- From experience: examples / training data
- Strength of connection between the neurons is stored as a weight-value for the specific connection.
- Learning the solution to a problem = changing the connection weights



# *Brain Vs Computer*





Title: Role of Activation Function in a Neural Network

Activation functions serve two main purposes:

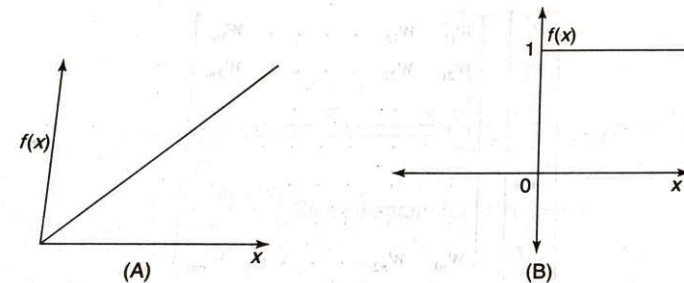
1. **Introduce Non-linearity:** Without non-linearity, a neural network would behave like a linear model, no matter how deep it is. Activation functions allow the network to learn and represent complex, non-linear mappings between inputs and outputs.
2. **Control Neuron Activation:** Activation functions control the firing behavior of neurons. Depending on the activation function's output, a neuron might become activated (output a non-zero value) or remain inactive (output zero).

### 3. Activation Functions

1. *Identity function*: It is a linear function and can be defined as

$$f(x) = x \text{ for all } x$$

The output here remains the same as input. The input layer uses the identity activation function.



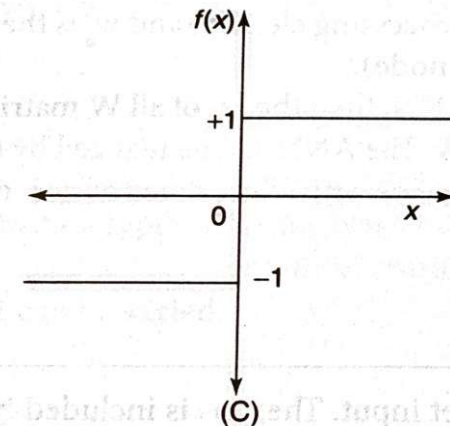
2. *Binary step function*: This function can be defined as

$$f(x) = \begin{cases} 1 & \text{if } x \geq \theta \\ 0 & \text{if } x < \theta \end{cases}$$

where  $\theta$  represents the threshold value. This function is most widely used in single-layer nets to convert the net input to an output that is a binary (1 or 0).

3. *Bipolar step function*: This function can be defined as

$$f(x) = \begin{cases} 1 & \text{if } x \geq \theta \\ -1 & \text{if } x < \theta \end{cases}$$



# 3. Activation Functions

## Sigmoidal Functions

- Bipolar sigmoid function:** This function is defined as

$$f(x) = \frac{2}{1 + e^{-\lambda x}} - 1 = \frac{1 - e^{-\lambda x}}{1 + e^{-\lambda x}}$$

where  $\lambda$  is the steepness parameter and the sigmoid function range is between -1 and +1. The derivative of the function can be

$$f'(x) = \frac{\lambda}{2} [1 + f(x)][1 - f(x)]$$

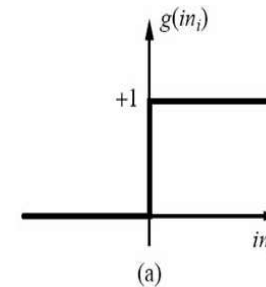
The bipolar sigmoidal function is closely related to hyperbolic tangent function, which is written as

$$h(x) = \frac{e^x - e^{-x}}{e^x + e^{-x}} = \frac{1 - e^{-2x}}{1 + e^{-2x}}$$

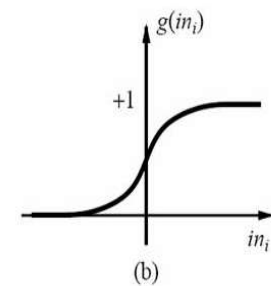
The derivative of the hyperbolic tangent function is

$$h'(x) = [1 + h(x)][1 - h(x)]$$

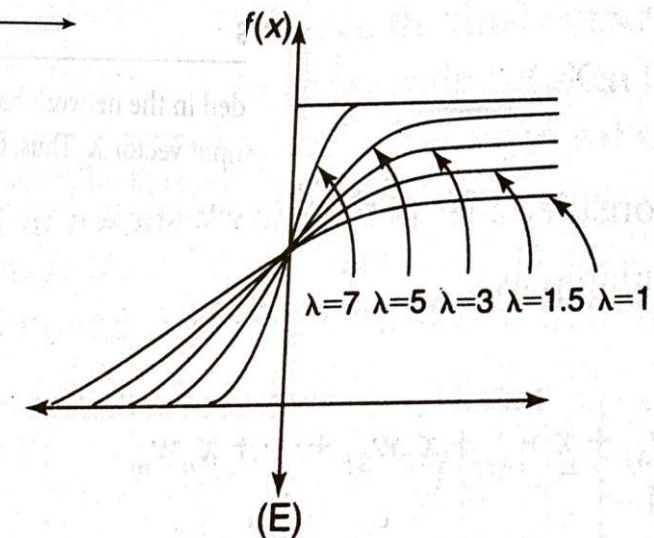
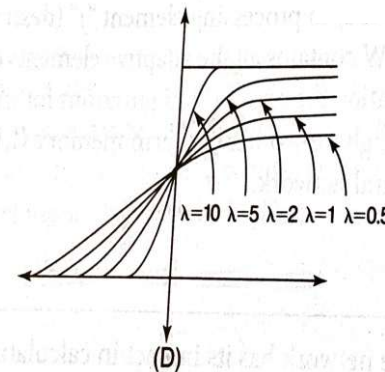
If the network uses a binary data, it is better to convert it to bipolar form and use the bipolar sigmoidal activation function or hyperbolic tangent function.



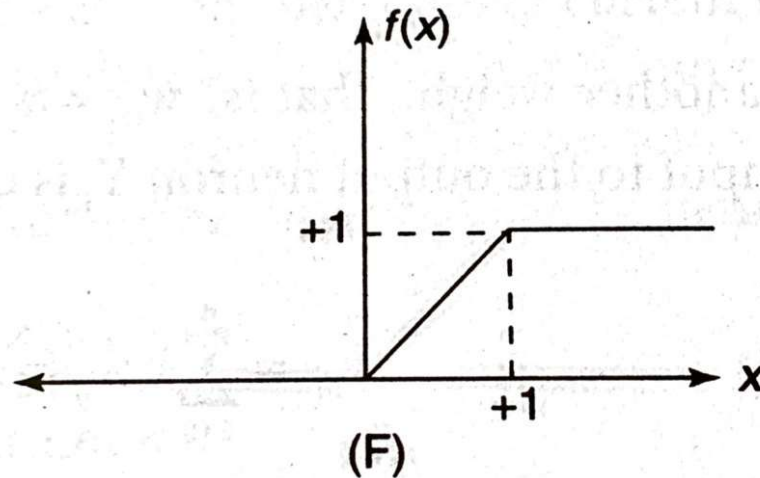
(a) step function



(b) sigmoid function



### 3. Activation Functions



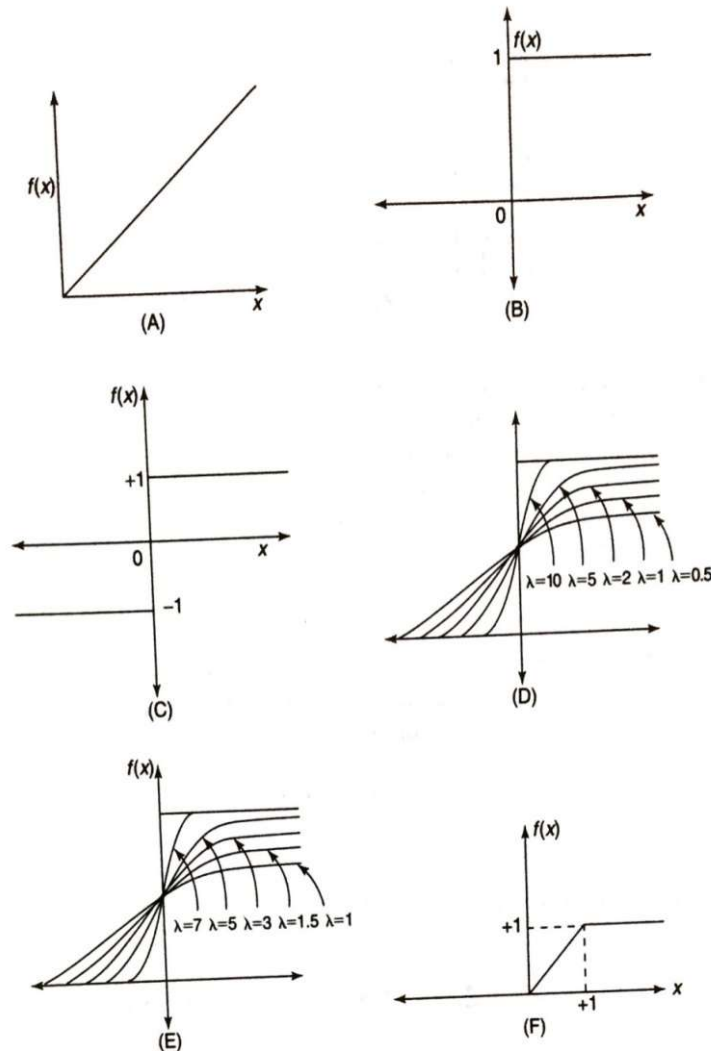
5. *Ramp function*: The ramp function is defined as

$$f(x) = \begin{cases} 1 & \text{if } x > 1 \\ x & \text{if } 0 \leq x \leq 1 \\ 0 & \text{if } x < 0 \end{cases}$$

Figure 2-15(A)–(F) shows all the activation functions.



### 3. Activation Functions



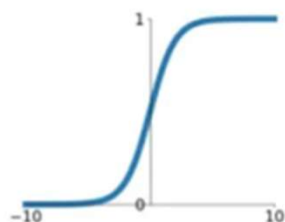
- Identity  
 $f(x) = x$
- Binary step  
 $f(x) = 1$  if  $x \geq \theta$   
 $f(x) = 0$  otherwise
- Binary sigmoid  
 $f(x) = 1 / (1 + e^{-\sigma x})$
- Bipolar sigmoid  
 $f(x) = -1 + 2 / (1 + e^{-\sigma x})$
- Hyperbolic tangent  
 $f(x) = (e^x - e^{-x}) / (e^x + e^{-x})$

**Figure 2-15** Depiction of activation functions: (A) identity function; (B) binary step function; (C) bipolar step function; (D) binary sigmoidal function; (E) bipolar sigmoidal function; (F) ramp function.

# Activation Functions

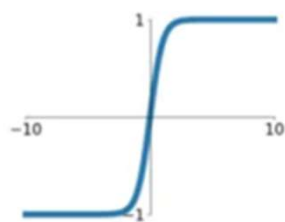
## Sigmoid

$$\sigma(x) = \frac{1}{1+e^{-x}}$$



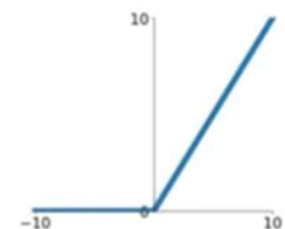
## tanh

$$\tanh(x)$$



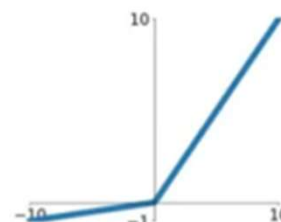
## ReLU

$$\max(0, x)$$



## Leaky ReLU

$$\max(0.1x, x)$$



## Maxout





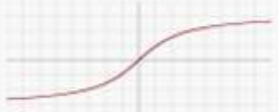



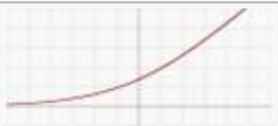
$$\max(w_1^T x + b_1, w_2^T x + b_2)$$

## ELU

$$\begin{cases} x & x \geq 0 \\ \alpha(e^x - 1) & x < 0 \end{cases}$$





| Name  | Plot  | Equation   | Derivative  |
|---|---|--|---|
| Identity                                      |    | $f(x) = x$   | $f'(x) = 1$   |
| Binary step                                   |    | $f(x) = \begin{cases} 0 & \text{for } x < 0 \\ 1 & \text{for } x \geq 0 \end{cases}$               | $f'(x) = \begin{cases} 0 & \text{for } x \neq 0 \\ ? & \text{for } x = 0 \end{cases}$             |
| Logistic (a.k.a Soft step)                    |    | $f(x) = \frac{1}{1 + e^{-x}}$  | $f'(x) = f(x)(1 - f(x))$  |
| TanH  |    | $f(x) = \tanh(x) = \frac{2}{1 + e^{-2x}} - 1$  | $f'(x) = 1 - f(x)^2$  |
| ArcTan  |    | $f(x) = \tan^{-1}(x)$  | $f'(x) = \frac{1}{x^2 + 1}$   |
| Rectified Linear Unit (ReLU)                  |   | $f(x) = \begin{cases} 0 & \text{for } x < 0 \\ x & \text{for } x \geq 0 \end{cases}$               | $f'(x) = \begin{cases} 0 & \text{for } x < 0 \\ 1 & \text{for } x \geq 0 \end{cases}$             |
| Parameteric Rectified Linear Unit (PReLU) [2] |  | $f(x) = \begin{cases} \alpha x & \text{for } x < 0 \\ x & \text{for } x \geq 0 \end{cases}$        | $f'(x) = \begin{cases} \alpha & \text{for } x < 0 \\ 1 & \text{for } x \geq 0 \end{cases}$        |
| Exponential Linear Unit (ELU) [3]             |  | $f(x) = \begin{cases} \alpha(e^x - 1) & \text{for } x < 0 \\ x & \text{for } x \geq 0 \end{cases}$ | $f'(x) = \begin{cases} f(x) + \alpha & \text{for } x < 0 \\ 1 & \text{for } x \geq 0 \end{cases}$ |
| SoftPlus                                      |  | $f(x) = \log_e(1 + e^x)$   | $f'(x) = \frac{1}{1 + e^{-x}}$  |

| Used in layer   | Activation Function                 | Details  | Pros   | Cons  |
|-----------------|-------------------------------------|--|--|---|
| Hidden / Output | <b>Sigmoid</b>                      | $\sigma(x) = 1/(1 + e^{-x})$ <p>Output range: [0,1]</p>                    | <ul style="list-style-type: none"> <li>- Smooth activation that outputs values between 0 and 1, making it suitable for binary classification</li> <li>- Historically popular</li> </ul>  | <ul style="list-style-type: none"> <li>- Vanishing gradient problem due to saturated neurons</li> <li>- Output not zero-centered as sigmoid outputs are always positive</li> <li>- exp() operation is computationally intensive</li> </ul>  |
| Hidden          | <b>Tanh (Hyperbolic tangent)</b>    | $\tanh(x) = \frac{e^x - e^{-x}}{e^x + e^{-x}}$ <p>Output range: [-1,1]</p> | <ul style="list-style-type: none"> <li>- Zero centered outputs that help networks train faster</li> </ul>  | <ul style="list-style-type: none"> <li>- Suffers with vanishing gradient problem when saturated</li> </ul>  |
| Hidden          | <b>ReLU (Rectified Linear Unit)</b> | $f(x) = \max(0, x)$ <p>Output range: [0, ∞)</p>                            | <ul style="list-style-type: none"> <li>- Does not saturate: avoids vanishing gradient issues for positive inputs</li> <li>- Computationally efficient since only certain number of neurons are activated at the same time</li> <li>- Much faster convergence compared to sigmoid/tanh</li> </ul> | <ul style="list-style-type: none"> <li>- Output not zero-centered</li> <li>- Prone to a "dying ReLU" problem, where neurons can get stuck during training and never activate again, leading to a dead neuron that doesn't update its weights.</li> </ul> <p>© AIML.com Research</p> |

| Used in layer   | Activation Function                 | Details  | Pros   | Cons  |
|-----------------|-------------------------------------|--|--|---|
| Hidden / Output | <b>Sigmoid</b>                      | $\sigma(x) = 1/(1 + e^{-x})$ <p>Output range: [0,1]</p>                    | <ul style="list-style-type: none"> <li>- Smooth activation that outputs values between 0 and 1, making it suitable for binary classification</li> <li>- Historically popular</li> </ul>  | <ul style="list-style-type: none"> <li>- Vanishing gradient problem due to saturated neurons</li> <li>- Output not zero-centered as sigmoid outputs are always positive</li> <li>- exp() operation is computationally intensive</li> </ul>  |
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| Hidden          | <b>ReLU (Rectified Linear Unit)</b> | $f(x) = \max(0, x)$ <p>Output range: [0, ∞)</p>                            | <ul style="list-style-type: none"> <li>- Does not saturate: avoids vanishing gradient issues for positive inputs</li> <li>- Computationally efficient since only certain number of neurons are activated at the same time</li> <li>- Much faster convergence compared to sigmoid/tanh</li> </ul> | <ul style="list-style-type: none"> <li>- Output not zero-centered</li> <li>- Prone to a "dying ReLU" problem, where neurons can get stuck during training and never activate again, leading to a dead neuron that doesn't update its weights.</li> </ul> <p>© AIML.com Research</p> |

## Which activation function to choose from?

### Activation function for hidden layers:

- In practice, the choice of activation functions is as follows in order of priority:
- ReLU is the top choice as it is simpler, faster, much lower run time, better convergence performance and do not suffer from [vanishing gradient issues](#)
- Leaky ReLU, PReLU, Maxout and ELU
- tanh
- Sigmoid (not preferred anymore)

### Activation function for output layers:

- Sigmoid for binary classification, multi-label classification
- Softmax for multi-class classification
- Identity / linear function for regression problems

# *Exercise*

- 2 input AND

|   |   |   |
|---|---|---|
| 1 | 1 | 1 |
| 1 | 0 | 0 |
| 0 | 1 | 0 |
| 0 | 0 | 0 |

- 2 input OR

|   |   |   |
|---|---|---|
| 1 | 1 | 1 |
| 1 | 0 | 1 |
| 0 | 1 | 1 |
| 0 | 0 | 0 |

