

4 (a) The  $Cl(E)$  is the set of all the points within  $E$  or on the boundary of  $E$ . Similarly with  $Cl(E^c)$ , it is all the points with  $(E^c)$ , all the points outside of  $E$ , but still contains the points on the boundary of  $E^c$ , also  $E$ . As for  $Int(E)$ , it is the union of all the points within  $E$ . However <sup>not the boundary</sup> if we take the complement of  $Int(E)$ , it is now all the points outside of  $E$  and the boundary points of  $E$ . Hence both  $Cl(E^c)$  and  $Int(E)^c$  both refer to the union of  $E^c$  and the boundary/limit points of  $E$ , and  $\therefore$   

$$Cl(E^c) = Int(E)^c$$

(b) Recall,  $Cl(E)$  is the union of all points within  $E$  and its boundary/limit points.  $Int(E^c)$  is the set of all interior points of the complement of  $E$  (not including limit points). Therefore, if we were to take the complement of  $Int(E^c)$ , it would consist of all the interior points and limit points of  $E$ . Hence  $Cl(E) = Int(E^c)^c$

(c) I'm conflicted with does  $Cl(E) = Cl(Int(E))$ .

The closure of a set includes the limit points, even if they do not with the set. Hence, even though the  $Int(E)$  is only the interior points and not the limit points,  $Cl(Int(E))$  expands to include the limit points as well. Hence  $Cl(E) = Cl(Int(E))$ .

(d)  $Int(E)$  only consists of the interior points.  $Cl(E) = Int(E) + \text{limit points}$ . Therefore if we were to  $Int(Cl(E)) = Int(E) + \text{limit points}$  and the limit points would be excluded because they are not in the intersection. Hence  $Int(Cl(E)) = Int(E)$ .