

KDDM - MidTerm

Q1. Given points:

i.  $A = (0,0,0), B=(0,1,0)$

ii.  $A = (0,1,0), B=(0,0,0)$

The distance formula =  $d(A,B) = ((x_2-x_1)^2 + (y_2-y_1)^2 + (z_2-z_1)^2)^{1/3}$

i.  $d(A,B) = ((0-0)^2 + (0-1)^2 + (0-0)^2)^{1/3}$   
 $= -1$

ii.  $d(A,B) = ((0-0)^2 + (1-0)^2 + (0-0)^2)^{1/3}$   
 $= 1$

Since the distance function must be non negative ( $d(x,y) \geq 0$ ), but here we get the distance as **-1** which violates the non negative property. Hence this is not a valid distance function.

Q2. Probability of travelling to England =  $P(E) = 0.5$

Probability of travelling to Italy =  $P(I)=0.2$

Probability of travelling to Spain =  $P(S)=1-P(E)-P(I)=0.3$

Probability of contracting COVID in each country is proportional to prevalence:

$P(C|E) = 1200/1000000 = 0.0012$

$P(C|I) = 1500/1000000 = 0.0015$

$P(C|S) = 1600/1000000 = 0.0016$

**Probability of contracting COVID while traveling:**

Using the law of total probability:

$$\begin{aligned} P(C) &= P(C|E) P(E) + P(C|I) P(I) + P(C|S) P(S) \\ &= 0.0012 \times 0.5 + 0.0015 \times 0.2 + 0.0016 \times 0.3 \\ &= 0.00138 \end{aligned}$$

So the probability that the employee contracts covid while travelling is **%0.138**

**Given that the employee contracted COVID, what is the probability that they traveled to England**

Using Bayes theorem

$$\begin{aligned}P(E|C) &= P(C|E) \times P(E) / P(C) \\&= 0.0012 \times 0.5 / 0.00138 \\&= 0.4348\end{aligned}$$

So, given that the employee contracted COVID, the probability that they traveled to England is **43.48%**.