

Formulas for set

For any three sets A, B and C

$$n(A \cup B) = n(A) + n(B) - n(A \cap B)$$

If $A \cap B = \emptyset$, then $n(A \cup B) = n(A) + n(B)$

$$n(A - B) + n(A \cap B) = n(A)$$

$$n(B - A) + n(A \cap B) = n(B)$$

$$n(A - B) + n(A \cap B) + n(B - A) = n(A \cup B)$$

$$n(A \cup B \cup C) = n(A) + n(B) + n(C) - n(A \cap B) - n(B \cap C) - n(C \cap A) + n(A \cap B \cap C)$$

Properties of Sets

Commutative Property :

$$A \cup B = B \cup A$$

$$A \cap B = B \cap A$$

Associative Property :

$$A \cup (B \cup C) = (A \cup B) \cup C$$

$$A \cap (B \cap C) = (A \cap B) \cap C$$

Distributive Property :

$$A \cup (B \cap C) = (A \cup B) \cap (A \cup C)$$

$$A \cap (B \cup C) = (A \cap B) \cup (A \cap C)$$

De morgan's Law :

Law of union : $(A \cup B)' = A' \cap B'$

Law of intersection : $(A \cap B)' = A' \cup B'$

Complement Law :

$$A \cup A' = A' \cup A = U$$

$$A \cap A' = \emptyset$$

Idempotent Law And Law of a null and universal set :

For any finite set A

$$A \cup A = A$$

$$A \cap A = A$$

$$\emptyset' = U$$

$$\emptyset = U'$$

These are the basic set of formulas from the set theory.

If there are two sets P and Q,

$n(P \cup Q)$ represents the number of elements present in one of the sets P or Q.

$n(P \cap Q)$ represents the number of elements present in both the sets P & Q.

$$n(P \cup Q) = n(P) + (n(Q) - n(P \cap Q))$$

For three sets P, Q, and R,

$$n(P \cup Q \cup R) = n(P) + n(Q) + n(R) - n(P \cap Q) - n(Q \cap R) - n(R \cap P) + n(P \cap Q \cap R)$$

Symbol	Symbol Name	Meaning	Example
{ }	set	a collection of elements	$A = \{1, 7, 9, 13, 15, 23\}$, $B = \{7, 13, 15, 21\}$
$A \cup B$	union	Elements that belong to set A or set B	$A \cup B = \{1, 7, 9, 13, 15, 21, 23\}$
$A \cap B$	intersection	Elements that belong to both the sets, A and B	$A \cap B = \{7, 13, 15\}$
$A \subseteq B$	subset	subset has few or all elements equal to the set	$\{7, 15\} \subseteq \{7, 13, 15, 21\}$
$A \not\subseteq B$	not subset	left set is not a subset of right set	$\{1, 23\}$

			$\not\subset B$
$A \subset B$	proper subset / strict subset	subset has fewer elements than the set	$\{7, 13, 15\} \subset \{1, 7, 9, 13, 15, 23\}$
$A \supset B$	proper superset / strict superset	set A has more elements than set B	$\{1, 7, 9, 13, 15, 23\} \supset \{7, 13, 15, \}$
$A \supseteq B$	superset	set A has more elements or equal to the set B	$\{1, 7, 9, 13, 15, 23\} \supseteq \{7, 13, 15, 21\}$
\emptyset	empty set	$\emptyset = \{ \}$	$C = \{\emptyset\}$
$P(C)$	power set	all subsets of C	$C = \{4, 7\}$, $P(C) = \{\{\}, \{4\}, \{7\}, \{4, 7\}\}$ Given by 2^s , s is number of elements in set C
$A \not\supset B$	not superset	set X is not a superset of set Y	$\{1, 2, 5\} \not\supset \{1, 6\}$
$A = B$	equality	both sets have the same members	$\{7, 13, 15\} = \{7, 13, 15\}$
$A \setminus B$	relative	objects that belong to A and not to	$\{1, 9,$

or $A-B$	complement	B	$23\}$
A^c	complement	all the objects that do not belong to set A	We know, $U = \{1, 2, 7, 9, 13, 15, 21, 23, 28, 30\}$ $A^c = \{2, 21, 28, 30\}$
$A \Delta B$	symmetric difference	objects that belong to A or B but not to their intersection	$A \Delta B = \{1, 9, 21, 23\}$
$a \in B$	element of	set membership	$B = \{7, 13, 15, 21\}$, $13 \in B$
(a,b)	ordered pair	collection of 2 elements	$(1, 2)$
$x \notin A$	not element of	no set membership	$A = \{1, 7, 8, 13, 15, 23\}$, $5 \notin A$
$ B , \#B$	cardinality	the number of elements of set B	$B = \{7, 13, 15, 21\}$, $ B =4$
$A \times B$	cartesian product	set of all ordered pairs from A and B	$\{3,5\} \times \{7,8\} = \{(3,7), (3,8), (5,7), (5,8)\}$
N_1	natural numbers / whole	$N_1 = \{1, 2, 3, 4, 5, \dots\}$	$6 \in N_1$

	numbers set (without zero)		
N_0	natural numbers / whole numbers set (with zero)	$N_0 = \{0, 1, 2, 3, 4, \dots\}$	$0 \in N_0$
Q	rational numbers set	$Q = \{x \mid x = a/b, a, b \in Z\}$	$2/6 \in Q$
Z	integer numbers set	$Z = \{\dots -3, -2, -1, 0, 1, 2, 3, \dots\}$	$-6 \in Z$
C	complex numbers set	$C = \{z \mid z = a + bi, -\infty < a < \infty, -\infty < b < \infty\}$	$6 + 2i \in C$
R	real numbers set	$R = \{x \mid -\infty < x < \infty\}$	$6.343434 \in R$

Properties of Union of Sets	Properties of Intersection of sets
$A \cup B = B \cup A$ (Commutative law)	$A \cap B = B \cap A$ (Commutative law)
$A \cup (B \cap C) = (A \cup B) \cap (A \cup C)$ (Distributive law)	$(A \cap B) \cap C = A \cap (B \cap C)$ (Associative law)
$A \cup \phi = A$ (Law of identity element, ϕ is the identity of \cup)	$\phi \cap A = \phi, U \cap A = A$ (Law of ϕ and U)
$A \cup A = A$ (Idempotent law)	$A \cap A = A$ (Idempotent law)
$U \cup A = U$ (Law of U)	$A \cap (B \cup C) = (A \cap B) \cup (A \cap C)$ (Distributive law)

Properties of Complement of set:

$$A \cup A' = U$$

$$A \cap A' = \phi$$

$$(A \cup B)' = A' \cap B'$$

$$(A \cap B)' = A' \cup B'$$

$$U' = \phi$$

$$\phi' = U$$

Properties of the intersection of sets operation:

$$A \cap B = B \cap A$$

$$(A \cap B) \cap C = A \cap (B \cap C)$$

$$\phi \cap A = \phi ; U \cap A = A$$

$$A \cap A = A$$

$$A \cap (B \cup C) = (A \cap B) \cup (A \cap C)$$

$$A \cup (B \cap C) = (A \cup B) \cap (A \cup C)$$

Some properties of Union operation:

$$A \cup B = B \cup A$$

$$(A \cup B) \cup C = A \cup (B \cup C)$$

$$A \cup \phi = A$$

$$A \cup A = A$$

$$U \cup A = U$$

Properties of Complement sets

$$P \cup P' = U$$

$$P \cap P' = \Phi$$

Law of double complement : $(P')' = P$

Laws of empty/null set(Φ) and universal set(U), $\Phi' = U$ and $U' = \Phi$.

Cartesian Product of sets

If set A and set B are two sets then the cartesian product of set A and set B is a set of all ordered pairs (a,b), such that a is an element of A and b is an element of B. It is denoted by $A \times B$.

We can represent it in set-builder form, such as:

$$A \times B = \{(a, b) : a \in A \text{ and } b \in B\}$$

Example: set $A = \{1,2,3\}$ and set $B = \{\text{Bat}, \text{Ball}\}$, then;

$$A \times B = \{(1,\text{Bat}), (1,\text{Ball}), (2,\text{Bat}), (2,\text{Ball}), (3,\text{Bat}), (3,\text{Ball})\}$$

Difference of Sets

If set A and set B are two sets, then set A difference set B is a set which has elements of A but no elements of B. It is denoted as $A - B$.

Example: $A = \{1,2,3\}$ and $B = \{2,3,4\}$

$$A - B = \{1\}$$

Links that mentioned in the videos :-

Introduction of set :- <https://youtu.be/Q985NC7B5fs>

Types of set reference :- <https://youtu.be/crQ97zTdS8s>

Operations on set :- <https://youtu.be/IV47aiFpffk>
<https://youtu.be/TZIIUWbklwM>

Laws of set theory :- <https://youtu.be/l8WdCozPTeQ>
<https://youtu.be/HGBLmzHlxJU>

Word problem :- <https://youtu.be/pJ3ed3YCHr4>
<https://youtu.be/CRnh3Vb5BdY>

Example :- <https://youtu.be/Ry2tvyat3Y4>
<https://youtu.be/YSpEA1Cv5VQ>

Other links from nptel :- <https://youtu.be/ISVco9sY-SQ>
<https://youtu.be/je-HLcRBWuM>
<https://youtu.be/rh-Ew15RO04>
<https://youtu.be/wHW-n-friXA>
<https://youtu.be/JbUFP3txlus>
https://youtu.be/nwiuF5hV_5U
<https://youtu.be/71P8JoowR-8>
<https://youtu.be/OBLAbeRvaFE>
https://youtu.be/FF8_CQDABk8
<https://youtu.be/FNTdU1lphg0>
<https://youtu.be/fk0taIB2uhw>

Other youtube links:- <https://youtu.be/YGXM8sNBYo>
<https://youtu.be/byCqdYDDNns>
<https://youtu.be/6RsudHXe6ZM>
https://youtu.be/10Bg_-GYi1c
<https://youtu.be/B3L8ZzrZwzA>

----- Thank-You -----