
Reinforcement Learning - A Browser Based Visualisation Tool

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About this project

Abstract This project will help to explain the temporal difference reinforcement learning process by displaying an agents behaviour, performance and Q-Table (memory) as it interacts within its environment. The application is a browser based visual tool where a user can tweak parameters within a form before running the application. Once the form is submitted it will then make a request to run the application held on a server. Once the script has completed the user will be presented with an animation of the agent moving through its environment. In addition a graph of the agent performance and the q-table will be presented to the user for examination. There are two different temporal difference algorithms for the user to choose from being Q learning, an off policy strategy and SARSA (State Action Reward Action), an on policy strategy. The performance of these two algorithms will be presented to the user for examination within a linear chart. This will aid the user in better understanding the concept of reinforcement learning.

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Chapter 1

Introduction

Reinforcement learning

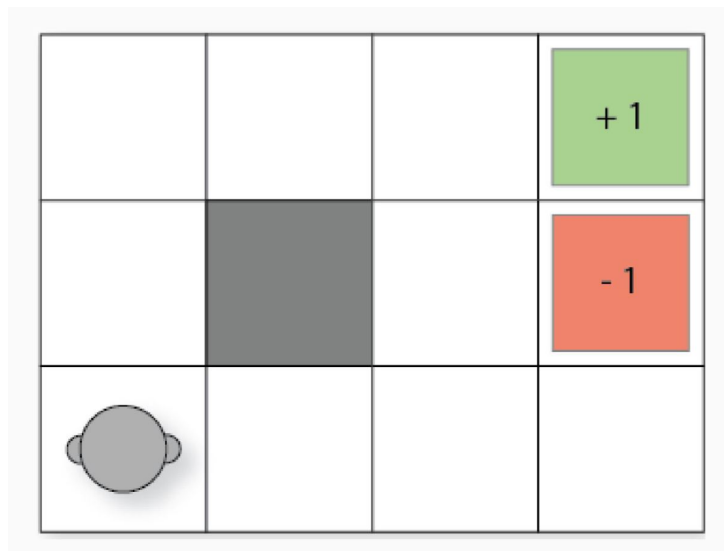


Figure 1.1: Image Source [1]

Reinforcement Learning is an unsupervised machine-learning technique that allows an agent to explore and learn from its environment without any prior knowledge of the domain. An agent transitions from one state to another by choosing an action with the highest reward value. The reward can be either positive or negative based on the decisions made by the agent as it transitions from its current state to the next chosen state.

For example, if a puppy has no knowledge of the sit command it will not perform the desired action on the first attempt. Each time the puppy sits

when commanded its decision is reinforced with a positive treat/reward. If the puppy does not sit the reward is negative (no treat). Eventually after many iterations of training, the dog will associate a treat/reward with that specific command and eventually learn that sitting will get them a treat. The puppy in essence is taking actions to maximise rewards while exploring an unknown environment.

With reinforcement machine learning, this technique is used to train an agent to learn about its environment through trial and error. It will eventually learn the optimal path to a goal after many training episodes have completed.

1.1 Components

This application will have the following reinforcement learning components.

1.2 Markov Decision Process

The Markov decision process has the requirement of being in a present state all future states are independent of past states.

$$P[S_t + 1|S_t] = P[S_t + 1|S_1, \dots, S_t]$$

The above equation simply states that the current state holds all of the past cumulative values where future actions can be decided. Where P is the probability of taking a future action $S_t + 1$ from a current state S_t . Therefore there is no need to keep track of the entire history of the actions taken for every state. The Markov decision process is used in reinforcement learning to allow the agent to only observe it's current state and choose a future action based on the total reward values from previous states observed [2, p. 67].

1.3 Bellmann Equation

$$V(s) = \max_a (R(s, a) + \gamma V(s'))$$

The Bellmann equation is used in conjunction with the Markov decision process where V is a value function, a is an action taken, R is the reward gained, (s, a) represents the state and action taken, γ is the discount factor

(s') is the next state [2, p. 75].

This is a recursive function where the maximum reward for the current state and action is assigned to the next state. A discount factor is applied where the future cumulative rewards are assigned. The closer gamma is to the value one the updated value will be directly related to the adjacent state. With a gamma value closer to zero will take into consideration the future rewards for the next n states.

1.3.1 Agent

The agent is an object within the environment that makes decisions based on its current state space and possible rewards gained by choosing an action. For this application the agent is placed in a two dimensional environment. The possible actions that can be taken by the agent are up, down, left or right.

1.3.2 Episode

An episode is the time from when an agent starts its training to when it has reached a positive or negative terminal state. Within each episode an agent takes time steps where each time step is the transition from its current position to the next within the environment.

1.3.3 Environment

The environment used for this project will be grid world. The grid world domain is a two dimensional grid with the agent's start position at the bottom left of the grid and the goal state at the top right of the grid. In addition there are traps that the agent needs to avoid while travelling from the start state to its goal state. For the purpose of this application a $6 * 6$ two dimensional grid environment will be used. As the script is running the agent will move from one square in the grid to the next adjacent square of up, below, to the left or the right of its current position. As the agent moves through the environment it gains knowledge via reward signals gathered by transitioning from one state to another based on the action taken from its current state.

1.3.4 Epsilon

The Epsilon variable sets the probability of choosing a random action. When set to one it will always choose a random action. If set to .8 it will choose

the a random action 80% of the time. This value is decayed for every episode run to allow for the exploration of the environment.

1.3.5 gamma

The discount factor (Gamma) set to .9 is the immediate reward gained for an action taken. The higher the value the more the agent will take an immediate reward with no concern for future rewards.

1.3.6 alpha

The learning rate (alpha) is a value between zero and one determines how much the Q value is updated for each action taken. It will be .5 for this example.

1.3.7 per step cost

There is a negative reward cost for each step the agent makes in this case -0.04. This will help in getting the best path to the end state.

Q Values

Q values are a weighted score attached to an action of a particular state. The agents next movement is based on theses weighted scores.

Updating Q values

The agent chooses it's action decision based on what highest reward it can get from the next available states.

With the Q Learning algorithm each time step and action taken by the agent the following formulae is used to update the Q values within the Q Table. This is considered an off policy optimistic approach as the maximum value from all possible actions in the next state are use to update the current Q value for the agents action taken

$$Q^{new}(s_t, a_t) \leftarrow Q(s_t, a_t) + \alpha[r_t + \gamma \max_a Q(s_{t+1}, a) - Q(s, a)] \quad [3]$$

This above formulae can be broken can be simplified as:

Q (current state, action) += alpha *[reward + gamma* max value of Q

(next state, all possible actions) – Q (current state, action)]

The SARSA algorithm is considered an on policy pessimistic approach as the Q value is updated from the actual action taken from the current state and the maximum value as Q Learning does. There is just a small difference between the two algorithms but has a significant impact on the behaviour of the agent. This will be evaluated later in the System Evaluation chapter of this document.

$$Q(s_t, a_t) \leftarrow Q(s_t, a_t) + \alpha[r_t + \gamma Q(s_{t+1}, a_{t+1}) - Q(s_t, a_t)] \quad [4]$$

This formulae can be simplified as:

$$Q(\text{current state, action}) += \alpha * [\text{reward} + \gamma * Q(\text{next state, next action}) - Q(\text{current state, action})]$$

1.3.8 Q Table

The Q table is a historic record of the agent's actions taken in a given state. The values held within the Q table are used by the agent to choose the next best state transition. During the first episode all values within the Q table are zero (No knowledge of the environment). With every time step taken the Q table is updated with q values from the above formulae. For brevity the below examples will use a smaller q table rather than the one used for this application. At the beginning of the learning process the Q Table has all zero values meaning it has no prior knowledge of its domain.

State	Action left	Action right	Action up	Action down
1	0	0	0	0
2	0	0	0	0
3	0	0	0	0
4	0	0	0	0
5	0	0	0	0
6	0	0	0	0
7	0	0	0	0
8	0	0	0	0
9	0	0	0	0
10	0	0	0	0
11	0	0	0	0

From its initial state a random action is chosen. If the action chosen is to move up one square to state 5 the Q table is updated using the q learning formulae above which looks like $.5 * -.04 + .9 * 0 - 0 = -0.02$. It then populates the Q table's row of State one's action of moving up to the q value of -0.02.

State	Action left	Action right	Action up	Action down
1	0	0	-0.02	0
2	0	0	0	0
3	0	0	0	0
4	0	0	0	0
5	0	0	0	0
6	0	0	0	0
7	0	0	0	0
8	0	0	0	0
9	0	0	0	0
10	0	0	0	0
11	0	0	0	0

If the Agent decides to move down to state one again the value of moving down from state 5 to state 1 is updated to -0.02 also.

State	Action left	Action right	Action up	Action down
1	0	0	-0.02	0
2	0	0	0	0
3	0	0	0	0
4	0	0	0	0
5	0	0	0	-0.02
6	0	0	0	0
7	0	0	0	0
8	0	0	0	0
9	0	0	0	0
10	0	0	0	0
11	0	0	0	0

When back in state one the agent's best choices (highest value) is down, left or right as they are all 0 and higher the -0.02. This happens for every time step the agent takes. When enough episodes have run, all of the actions of a given state will have a value added including the goal state value. From this the agent will chose the highest value each state as the optimal action to take to the end goal. Once the agent gets to either end state, the episode is terminated and re-run. When episodes are re-run, the Q-Table will continually update until the optimal path is found and minimal updates will be performed.

State	Action left	Action right	Action up	Action down
1	-0.02	-0.02	0.02	-0.02
2	-0.02	-0.05	-0.02	-0.02
3	-0.02	-23	-23	-0.02
4	-0.02	-23	-100	-0.02
5	-0.02	-0.02	10	-0.02
6	-75	-100	1.2	-15
7	0	0	0	0
8	15	75	-0.02	-0.02
9	-0.02	85	-0.02	-0.02
10	-0.02	100	-0.02	-0.02
11	0	0	0	0

The purpose of this application is to demonstrate and explain reinforcement learning through a browser based visualisation tool.

The application will have the following elements on the Browser:

- The agent moving within its environment when the simulation is run. This will be displayed using HTML 5 canvas and represented by a yellow square within the canvas.

- User form input to tweak parameters before each run of the simulation. The parameters that will be available to the user are:
 - The end goal reward
 - The negative trap reward
 - The agent learning rate
 - The learning decay rate
 - The discount factor
 - The Exploration rate
 - The Exploration decay rate
 - The per step reward
 - The maximum number of episodes to be run
 - The maximum number of agent steps per episode
 - Choice of algorithm

Chapter 2

Context

2.1 Overview

The aim of this project is to provide a visual aid that further explains the concept of reinforcement learning. The basic fundamentals of the Q-Learning and SARSA temporal difference algorithms are reasonably straight forward but can seem overly complex and verbose when attempting to verbally explain the topic. This application will help the user visualise where and how the Q-values are stored and how the decision making process is made for the two above algorithms.

2.2 Objectives

The Main objectives of this project are:

- Implement two different temporal difference algorithms SARSA and Q-learning written in python.
- Allow for user interaction via a web page form
- Using Flask server to handle request from the user
- Present the user with data generated by the main python script on the server
- Parsing Json, text and csv files generated via Ajax
- Use the parsed data to animate the agent in HTML canvas
- Google chart for graphing the agent performance

- Generate an dynamic table that updates from the csv file
- Add a heat map to the values of the table as it updates
- Deploying the application to Google Cloud Platform

2.3 Topics Covered

The chapters listed below will have the following elements examined.

- Methodology
This chapter will explain what development process I used along with reasoning the technologies, algorithms and languages chosen.
- Technology Review
This chapter will review each technological element of the application and provide a justification for each technology discussed.
- System Design
The overall architecture will be explained with diagrams of each component of the system supplied.
- System Evaluation
The performance of the overall application will be evaluated here. In addition the limitations of the application discovered while in development will be discussed in detail.
- Conclusion
In this chapter the results of the system evaluation will be discussed along with any new findings that may have occurred.

2.4 Github Repository

The below link is the url to the github repository holding my dissertation and software files.

<https://github.com/kevgleeson78/Reinforcement-Learning>. The contents of this repository are:

- Dissertation folder
This folder holds the latex files for my dissertation developed using Tex Studio

- FlaskApp Folder
This is the main application folder stored on a Flask server when deployed.
- FlaskApp / flaskTest.py
This file is used to serve the main static html page and handle http form requests
- FlaskApp / Environment.py
This file is the main file holding the logic and environment space for the application.
All of the data files are generated from here once run.
- FlaskApp / app.yaml
This file is used to deploy the application to a Google Cloud App engine instance.
- FlaskApp / requirements.txt
This file is used to declare what resources are needed from the application to run on Google Cloud
- FlaskApp / Static / JavaScript
Each of the files contained within this folder are the main JavaScript files controlling the HTML canvas environment, Google Chart and Q-Table data.
- FlaskApp / Static / Css
The folder holding the styling script for the html pages
- FlaskApp / Static / gif
The folder holding the gif animation for the loading page
- FlaskApp / Static / Data
The folder holding the agents position coordinates as a .txt file
A csv file for the agents Q-Table values A json file for the agent rewards gained for each algorithm
- FlaskApp / Templates
This folder contains the the initial html page, the waiting page and result page. These pages are served to the view when http requests are made by the user.

Chapter 3

Methodology

3.1 Initial Planning

At the beginning of this project the over all problem set was broken down into the following areas to allow for a more manageable modular development process:

3.1.1 Initial Meetings

After an initial meeting with Dr. Patrick Mannion a high level view of the project was explored. This gave me a grasp of what components would be needed for the high level structure of the project. The different components identified were:

- The Environment should be a two dimensional grid
- Environment constraints are in the form of a grid world game where the agent will attempt to navigate to an end goal state and avoid any traps present in the grid.
- Front end technologies used should be JavaScript based.
- User interactivity via a form
- Server side functionality to handle form requests

On further meetings with my project supervisor Mr. Martin Hynes the concepts were further broken down into fine grain units of work with initial milestones set for each phase of development.

3.1.2 Which area of reinforcement learning?

After viewing lectures for Temporal Difference Reinforcement Learning I decided that the Q-Learning algorithm would be best suited to the grid world environment. If time permitted I would then implement the SARSA algorithm for a comparison between the performance of the two algorithms. The reason I chose these two algorithms for comparison was they are very similar in design but have vastly different outcomes depending on the environment the agent is in.

3.1.3 Mockup of application

Reinforcement learning

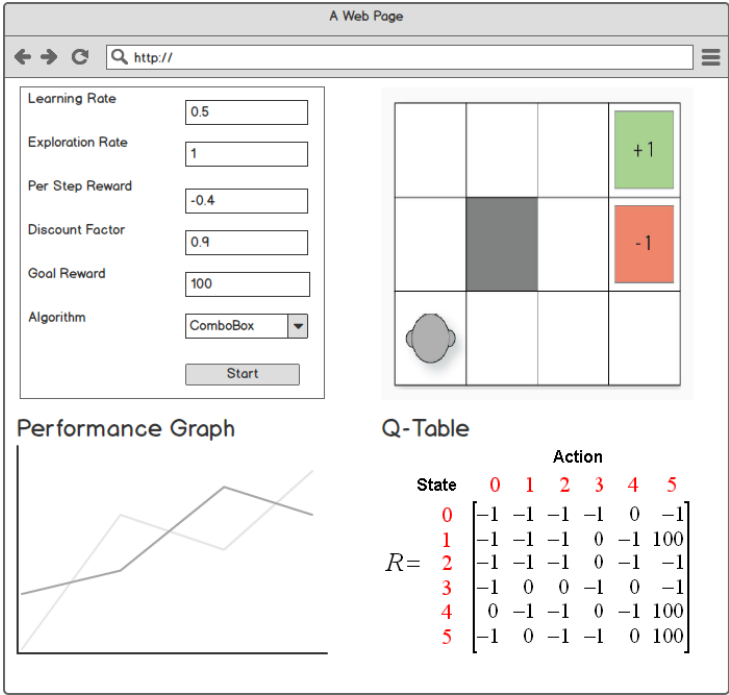


Figure 3.1

3.1.4 User Requirements gathering

On meeting with Mr. Hynes the following user requirements were gathered from the mock up created and the high level components identified from the initial meeting with Dr. Patrick Mannion.

- When the application is launched the user should be presented with a form.
- The form should have input parameters the user can alter
- The user should have the ability to submit the form
- Once the form has been submitted the result page should be displayed
- Once the result page is displayed the user should be presented with:
 - The grid world environment
 - The agent moving within the environment
 - The Q-Table should be presented with updates as the agent moves from one state to another
 - A performance chart of the agents rewards for each episode
 - The type of Algorithm chosen above the form
 - The form on the result page should have the same parameters chosen when the form was originally submitted from the home page.
 - The user should have the ability to change the saved parameters and resubmit the form for a new view of the simulation
 - The layout should be responsive to all devices
- The user should have the ability to access the application deployed to the cloud

3.2 Mile Stones

Once the user requirements were identified the following mile stones were then set for the initial development of the application.

- Front end mock-up
- Requirements gathering
- Set up development environment
- Small scale command line prototype
- Write agent positional coordinates to text file

- Stream agent positional coordinates as raw data to web page
- Create HTML canvas grid environment
 - Create Agent object within canvas grid
 - Animate agent object in canvas from coordinate text file
- Write the total reward gained for each episode out to a Json file
- Display the reward Json file data in a linear chart
- Write out the Q-table to a csv file for each step the agent takes
- Read the csv file via an ajax request
- Display the csv file data to a table
- Clear the table after each step of the simulation
- Create a front end form for user input
- Data binding of form post request to variables held in Environment.py(main script)
- Data persistence of user input between requests
- Performance testing
- Cloud deployment

3.3 Selection criteria of Technologies

After the initial user requirements gathering the following technologies were then researched and chosen to begin the development of the application.

3.3.1 Programming Languages

Java had been considered as the main language but after consideration python was chosen for the ability to rapidly prototype small versions of the system allowing for an agile iterative approach to development.

The possibility of a purely front end JavaScript application was also explored but cross browser compatibility of the scripts needed was a major issue that indicated a different approach was needed. However JavaScript would be used for the front end of the application.

3.3.2 Integrated Development Environment

The IDE chosen for the development of the application is IntelliJ with the pyCharm plug-in. This plug-in is compatible with all of the frameworks needed for setting up the development environment. Git capabilities are also within the IDE allowing for tracking changes, committing and managing merge conflicts.

3.3.3 Server Side

For server side programming and scripting the Flask python framework was chosen. Flask is a light weight package that allows for the rapid deployment and development of web applications.

The Django python framework was also considered but it was decided that it was not necessary to have a fully blown MVC model seeing as the application has in essence only three pages of Home page, Training Page and result Page.

When testing a simple hello world application Django generated a project that was almost twice the size of a flask application with little or no difference in performance. For this reason Flask was chosen.

3.3.4 Front End

For the front end of the application all of the data will be presented within a web browser. The frameworks used for this application are HTML canvas for drawing the grid world environment and animating the agent around this space.

JQuery will be used to make ajax requests to retrieve the files from the server containing the relevant data needed.

D3.js was investigated for charting the agent performance but problems with the data rendering incorrectly were identified as a potential sign for an alternative method of displaying the data.

Google charts has been successfully tested and chosen for displaying the agent performance within the environment.

A table will be used to display the Q-Table values from the generated csv file. The JavaScript library "Hottie" will be used to display the data within the table cells as a heat map based on the range of values from the highest to the lowest value.

3.3.5 Cloud Deployment

Initially Heroku was chosen for the cloud platform for the application to run on. However there was a problem with the server timing out after 20 seconds once a request has been made. Since the main script can take up to 30 seconds to complete this was a major issue.

The Google cloud application platform was investigated as an alternative solution and while there is a time out limit in place this can be altered if needed. For this reason the Google Cloud application platform was chosen for deploying the application.

3.4 Scheduled meetings

Scheduled meetings were held with Mr. Martin Hynes every week to evaluate the progress of assigned tasks along with any problems encountered. These meetings were in the form of the scrum methodology where a quick overview of my progress was presented. In addition any problems I had were discussed along with what tasks needed to be done for the next scrum meeting. These new tasks identified were then assigned for the following week to complete.

3.5 Development Approach

An iterative development approach was used throughout the construction of this application. The first task was to develop a basic prototype that demonstrated the basic concepts of the algorithm Q-Learning. Once implemented this prototype will be the foundation for each additional feature added with the start of a new iteration.

3.6 Testing

No test suites were used to test this application however there was considerable manual testing done with each iteration completed. Any major bugs found that would stop the development of the project while testing were fixed right away. Minor bugs found such as layout issues could be addressed at a later date as they did not have a detrimental impact on the progress of the project. This testing strategy would be used for every small new feature added while developing.

3.7 Use of GitHub

Github was used to track my progress of the project. While this is a solo project github would still need to be used for version control allowing for the roll back of the system in the event of a new feature causing unwanted behaviour.

Chapter 4

Technology Review

The following sections in this chapter will discuss the various technologies used to develop this application.

4.1 Python

The main programming language chosen for this application is Python. Python is a high level programming language that allows for the rapid development of a software system from prototyping to final system deployment [5]. As python is a high level programming language a significant amount of the low level functionality is isolated from the user. There are many different libraries within the python domain and need to be imported as needed. For example to get the maximum value back from an array we simply use the `argmax` function from the `numpy` package.

```
import numpy as np

num_list = [1,2,3,4,5]

max_num = np.argmax(num_list)

print(max_num)
```

This will return 5 as the maximum argument within the array without the need for a loop or element comparison that some other languages would require.

To reverse a string in python slices can be used [6]. This notion is extremely powerful as we can access any element or group of elements within a list.

Start at the end of the string and work back to the beginning

```
txt = "Hello World"[::-1]
print(txt)
```

output
dlroW olleH

The philosophy behind python is to keep everything as simple and as readable as possible [7]. One rule of python is that all code must be properly indented. If code is not indented correctly the compiler will throw an error. In the below example the compiler will throw an error due to no indentation within the defined function. All code with this function must be indented.

```
import numpy as np
num_list = [1,2,3,4,5]
#Incorrect Indentation
def max_element(x)
max_num = np.argmax(x)
return max_num
```

```
max_element(num_list)
```

Below is the correct format.

```
import numpy as np
num_list = [1,2,3,4,5]
#Correct Indentation
def max_element(x)
    max_num = np.argmax(x)
    return max_num
```

```
max_element(num_list)
```

This enforces a coding style promoting the easier readability of source code. Another unenforced guideline is that all code blocks should have one line of white space separation like below.

```
import numpy as np

num_list = [1,2,3,4,5]

#Correct Indentation
```

```
def max_element(x)

    max_num = np.argmax(x)
    return max_num

max_element(num_list)
```

This philosophy in conjunction with the powerful high level functionality of the Python programming language allows for the rapid development and prototyping of a software system. Three Python packages of Pandas, Numpy and Flask were used for the development of this application and will be discussed in the subsequent sections below.

4.1.1 Pandas Data Frame

The pandas Data Frame is used to convert a Python dictionary or list into a tabular format. In the below example a dictionary is presented with the keys of 'Key1' and 'Key2'. Each of these keys have an array containing four elements as the value. [8]

```
import pandas as pd

d = {'Key1': [1., 2., 3., 4.],
     'Key2': [4., 3., 2., 1.]}
```

The above dictionary can then be converted to a data frame using the following command.

```
df = pd.DataFrame(d)
```

This will convert the dictionary into the following tabular format.

	one	two
0	1.0	4.0
1	2.0	3.0
2	3.0	2.0
3	4.0	1.0

From here the table can be queried with specific data displayed using slices.

```
df.loc[1:3]
```

This will access rows one, two and three inclusively.

	one	two
1	2.0	3.0
2	3.0	2.0
3	4.0	1.0

This package is a powerful data manipulation tool that enables the rapid creation of customised data in the structure needed.

4.1.2 Numpy

The Numpy Python package is used to rapidly create and manipulate ndarray multi dimensional arrays. Arrays can be created with a dynamically generated range of values and may be reshaped to any dimension needed. A one dimensional array can be reshaped into an n dimensional array. Inversely a multidimensional array can be flattened to a one dimensional array with ease. Some of the functionality of the Numpy package is documented below. [9]

Creating a one dimensional array.

```
import numpy as np

#Create a 1D array
a = np.array([1,2,3,4])
```

Creating a two dimensional array.

```
import numpy as np

#Create a 2D array
a = np.array([(1,2,3,4),(5,6,7,8)])
```

When the elements of an array are unknown but the size has been identified the array can be initialised with default place holder values.

np.zeros fills an array of a chosen size with zero value place holders. The below example creates a two dimensional zero filled array of 3 rows and four columns.

```
import numpy as np

np.zeros( (3,4) )
```

```
## Output
```

```
[[ 0.,  0.,  0.,  0.],  
 [ 0.,  0.,  0.,  0.],  
 [ 0.,  0.,  0.,  0.]]
```

Alternatively the array can be populated with one's for place holders.

```
import numpy as np
```

```
np.ones( (3,4) )
```

```
## Output
```

```
[[ 1, 1, 1, 1],  
 [ 1, 1, 1, 1],  
 [ 1, 1, 1, 1]]
```

If the requirement is to initialise the array with random noise the empty function can be used. This function generates random 64 bit float point integers for each element within the array.

```
import numpy as np
```

```
np.empty( (2,3) )
```

```
## Output
```

```
[[ 3.73603959e-262,  6.02658058e-154,  6.55490914e-260],  
 [ 5.30498948e-313,  3.14673309e-307,  1.00000000e+000]]
```

A sequence of number can be generated using the range function. The function takes three parameters, the starting lower range number, the non-inclusive upper range number and the incremental value.

```
import numpy as np
```

```
np.arange( 0, 10, 2 )
```

```
## Output
```

```
[0,2,4,6,8]
```

If the need to generate subdivided values the linspace function can be used. The function takes three parameters, the lower bound value, the upper bound inclusive value and the number of divisional values between the lower and upper bounds.

```
import numpy as np
```

```
np.linspace( 0, 2, 9 )
```

```
## Output
```

```
[ 0. ,  0.25,  0.5 ,  0.75,  1.  ,  1.25,  1.5 ,  1.75,  2. ]
```

Arrays can also be reshaped to what ever dimensions needed using the reshape function. The parameters passed to this function are the rows and columns of the new array.

```
import numpy as np
```

```
b = np.arange(9)
```

```
## Output of One dimensional array
```

```
[0,1,2,3,4,5,6,7,8]
```

```
b.reshape(3,3)
```

```
## Output
```

```
[[ 0,  1,  2]
 [ 3,  4,  5]
 [ 6,  7,  8]]
```

4.1.3 Flask

Flask is a micro framework for building web applications using the python programming language. Flask is considered a micro framework as it has the minimum amount of required functionality needed to begin building a web application. When first run there is only the main flask file that contains the following code [10].

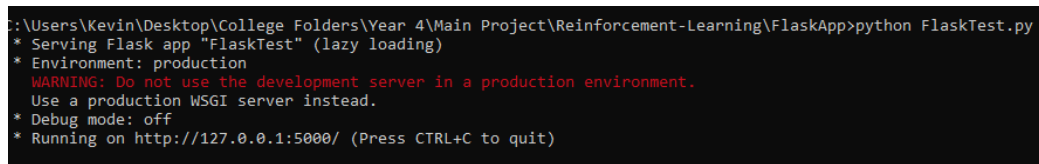
```
from flask import Flask
app = Flask(__name__)

@app.route('/')
def hello_world():
    return 'Hello, World!'

if __name__ == "__main__":
    app.run()
```

This file handles all request resources sent from the browser with the above file handling a single url resource of the root address of the application and return a simple text message. This allows for the creation of custom resources that can have any response we need i.e a html page, result of a calculation or running a entire python script and then returning the result to the user in the response body [10].

When this file is run from the command line a server is started and run locally on port :5050 by default.



```

.:Users\Kevin\Desktop\College Folders\Year 4\Main Project\Reinforcement-Learning\FlaskApp>python FlaskTest.py
* Serving Flask app "FlaskTest" (lazy loading)
* Environment: production
  WARNING: Do not use the development server in a production environment.
  Use a production WSGI server instead.
* Debug mode: off
* Running on http://127.0.0.1:5000/ (Press CTRL+C to quit)

```

Figure 4.1

The user enters the address of `http://127.0.0.1:5050` into their browser and a web page is severed from the root resource of the application with the simple message "hello world".

The following folder structure is used within a flask project.

The parent project folder

Root folder\

The main http routing script

FlaskApp.py

A python file that can be called

PythonScript.py

For deployment of application

DeploymetFile.yaml

Declares the application python requirements at deploy time

RequirementsFile.txt

For the staicly served files

Static Folder\

JavaScript Folder\

file1.js

filw2.js

file3.js

Css folder\

style.css

Data Folder\

```
Data1.txt
Data2.csv
Data3.json
Data4.xml
# For the html templates sent back in the response body
Templates Folder\
    home.html
    result.html
    pooling.html
```

4.2 REST Architecture

The Representational State Transfer Protocol (REST) is an architectural design philosophy that is used to acquire resources held on a server via HTTP Requests/Responses. The REST architecture is known as stateless whereby the server holds no information about the client's session state. The session state is held locally by the client. The server only receives a client request, then sends a response back to the client with the resources requested. Resources can be in the form of text, image or html files etc. A client request is in the form of a URL with "address.com" being the physical address of the server and "/resource-request" the actual resource needed to be sent back within the response body [11].

<https://address.com/resource-request>

The main http request methods used within the REST architecture are:

- GET should be used to retrieve an existing resource held on the server.
- POST should be used to create a resource on the server.
- PUT should be used to update a resource held on the server.
- DELETE should be used to remove a resource from the server.

Note that should is used in describing the four methods above. As rest is not a standard but rather a set of guidelines to follow, the above methods can be used for different functionality but would not be considered a restful application.

4.3 JavaScript

JavaScript is a client side browser based scripting language. It can be used to dynamically update information on a static web page in the form of tabular data, 2D/3D animations or session based user information [12], this will be discussed further in the following subsequent subsections. JavaScript can also be used to manipulate html elements with event listeners. In the below example [13] an onClick event listener is used to change the font size of the text contained with the html paragraph element. The element is accessed by document.getElementById('demo'). This parses the document object model DOM of the html file and locates the element with the id of 'demo'. From here ('demo').style.fontSize='35px' alters the text style font size to 35 pixels. This is all done dynamically via a click event on the web page allowing for the local client side real time manipulation of browser data.

```
<!DOCTYPE html>
<html>
<body>

<h2>What Can JavaScript Do?</h2>

<p id="demo">JavaScript can change the style of an HTML element.</p>

<button type="button" onclick="document.getElementById('demo')
    .style.fontSize='35px'">Click Me!</button>

</body>
</html>
```

4.3.1 AJAX

Asynchronous JavaScript and XML (AJAX) is a front end browser technology which allows for the retrieval of server side data asynchronously without altering the view or behaviour of the web page. When an asynchronous request is made to the server it simply waits until a response has been returned and can then process the returned data. This method can be used to request specific files held on the server then run any data processing needed once the files have been returned. AJAX also has the ability to only update partial segments of a web page without reloading the entire page. [14]

In the below example [15] there is a h1 heading with the text "The XMLHttpRequest Object" along with a button holding an onClick event listener.

When the button is clicked within the browser the loadDoc() JavaScript function is called.

Within the loadDoc function the onreadystatechange method waits for a http message of 4 and 200 response from the server which indicates the message has been sent correctly. From there the response text from the "ajax info" file is bound to the div with the id of demo changing the on screen text to the text held within the file.

```
<!DOCTYPE html>
<html>
<body>

<div id="demo">
<h1>The XMLHttpRequest Object</h1>
<button type="button" onclick="loadDoc()">Change Content</button>
</div>

<script>
function loadDoc() {
var xhttp = new XMLHttpRequest();
xhttp.onreadystatechange = function() {
if (this.readyState == 4 && this.status == 200) {
document.getElementById("demo").innerHTML =
this.responseText;
}
};
xhttp.open("GET", "ajax_info.txt", true);
xhttp.send();
}
</script>

</body>
</html>
```

4.3.2 Google Charts

The Google charts API is a JavaScript charting library that allows for the creation of numerous types of charts to be generated within a browser window. For the purpose of this project a line chart is used to display the agent rewards gained over time. Scalable Vector Graphics (SVG) are used to render

the chart image within the browser [16].

To create a line chart:

- The library must be imported along with an empty div to hold the final rendered image of the chart [16].

```
<script type="text/javascript" src="https://www.gstatic.com/charts/loader.js">
</script>
<div id="chart_div"></div>
```

- The line chart package is loaded from the library.
- A callback function then used to load the drawBasic() function.

```
google.charts.load('current', {packages: ['corechart', 'line']});
google.charts.setOnLoadCallback(drawBasic);
```

The drawBasic() function has the following elements

- A data table is first instantiated to hold all of the columns, rows and data. Then columns are created with declared data types and a name. [16]

```
function drawBasic() {

var data = new google.visualization.DataTable();
data.addColumn('number', 'X');
data.addColumn('number', 'Dogs');
```

- The numerical data is then added to the data table as rows. The data is represented by a two dimensional JavaScript array [16].

```
data.addRow([
[0, 0], [1, 10], [2, 23], [3, 17], [4, 18], [5, 9],
[6, 11], [7, 27], [8, 33], [9, 40], [10, 32], [11, 35],
[12, 30], [13, 40], [14, 42], [15, 47], [16, 44], [17, 48],
[18, 52], [19, 54], [20, 42], [21, 55], [22, 56], [23, 57],
[24, 60], [25, 50], [26, 52], [27, 51], [28, 49], [29, 53],
[30, 55], [31, 60], [32, 61], [33, 59], [34, 62], [35, 65],
[36, 62], [37, 58], [38, 55], [39, 61], [40, 64], [41, 65],
[42, 63], [43, 66], [44, 67], [45, 69], [46, 69], [47, 70],
[48, 72], [49, 68], [50, 66], [51, 65], [52, 67], [53, 70],
[54, 71], [55, 72], [56, 73], [57, 75], [58, 70], [59, 68],
[60, 64], [61, 60], [62, 65], [63, 67], [64, 68], [65, 69]
]);
```

- Within the options object the chart can be customised. Below names are then given to the horizontal and vertical. axis [16]

```
var options = {
  hAxis: {
    title: 'Time'
  },
  vAxis: {
    title: 'Popularity'
  }
};
```

- Finally the container div for the chart is identified and the chart.draw method is called with the data array and personalised options as parameter arguments. [16]

```
var chart = new google.visualization.LineChart(
  document.getElementById('chart_div'));
```

```
chart.draw(data, options);
```

This will result in a rendered line chart SVG image to the browser. [16]

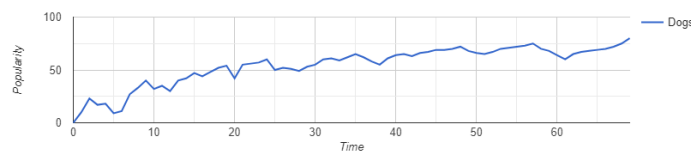


Figure 4.2: Goolge Line Chart

4.3.3 Hottie heat mapping JavaScript Library

Hottie is an open source heat mapping JavaScript library used to colour code data being generated. Any number of colour transitions can be used to represent low to high values within a dataset. The values in between low to high will have a gradient value based on the highest/ lowest value within the dataset. [17]

The hottie.js library is a used via JQuery and has the ability to colour code html tabular data based on the numerical values held within each table cell. The below example is a simple html table with some floating point values inserted into the table cells. The table has an ID of "myTable" for data access via JQuery. [18]

```

<table id="myTable">
  <tr>
    <td>2.59</td><td>0.68</td><td>1.35</td>
    <td>1.35</td><td>2.03</td><td>1.60</td>
  </tr>
  <tr>
    <td>1.39</td><td>0.70</td><td>1.22</td>
    <td>1.08</td><td>1.00</td><td>2.12</td>
  </tr>
  <tr>
    <td>2.87</td><td>0.59</td><td>1.22</td>
    <td>0.57</td><td>1.08</td><td>3.00</td>
  </tr>
  <tr>
    <td>0.99</td><td>0.25</td><td>0.48</td>
    <td>0.50</td><td>0.99</td><td>1.77</td>
  </tr>
</table>

```

Using JQuery a handle is gained on the table via the ID of "myTable". Three transitional hex colour values are then set from low (red), medium (red + green) to high (green). [18]

```

$("#myTable td").hottie({
  colorArray : [
    "#63BE7B",
    "#FBE983",
    "#F8696B"
  ]
});

```

The resulting cell values within the html table now have colour codes mapped to them based on the lowest (red) to highest (green) values. Every value in between the lower and upper bound will have a mixture of the two colours. The amount of colour mix is dependant on the current value within the cell and how close it is to the lowest/highest value. [17] [18]

2.59	0.68	1.35	1.35	2.03	1.60
1.39	0.70	1.22	1.08	1.00	2.12
2.87	0.59	1.22	0.57	1.08	3.00
0.99	0.25	0.48	0.50	0.99	1.77

Figure 4.3

4.3.4 HTML Canvas

The html canvas element is used to draw graphics via JavaScript and render the result within a browser page.

All of the drawing commands are written in JavaScript then sent to the empty canvas element for the resulting image to be rendered by the browser. Below is a simple example of a line drawn using html canvas. [19]

The attributes the canvas element have are the with and height of the canvas view, the ID and optional styling if needed [20].

```
<canvas id="myCanvas" width="200"
        height="100" style="border:1px solid #000000;">
</canvas>
```

To draw the line firstly a handle is gain on the canvas element with the ID of "myCanvas".

The context of the canvas is then declared as a two dimensional drawing.

The moveTo() method tells the browser where to start the drawing with 0,0 being the x,y coordinates. The x,y coordinates 0,0 start at the top left of the canvas which is not the conventional position of bottom left.

The lineTo() method states where to draw a line along the x,y coordinates. In the below example a line is drawn 200 pixels along the x axis and 100 pixels along the y axis giving the result of a diagonal line from the top left to the bottom right of the containing canvas. [20, 19]

```
var c = document.getElementById("myCanvas");
var ctx = c.getContext("2d");
ctx.moveTo(0, 0);
```

```
ctx.lineTo(200, 100);  
ctx.stroke();
```

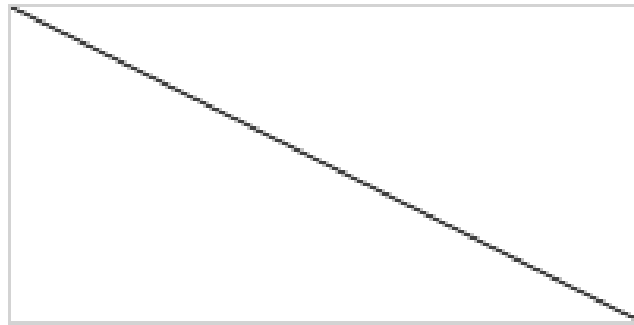


Figure 4.4

4.4 Bootstrap

Bootstrap is a CSS framework library that allows for the rapid development of a fully responsive front end user interface.

All css is pre-written with pre-defined class/id names.

To utilise the Bootstrap framework all that is required is to assign the html elements a class name or ID matching the class names or ID within the Bootstrap CSS file [21]. In the below example a simple grid layout is used by declaring three types of div with the class names of:

- "container" the wrapper class that controls the responsiveness of all containing divs.
- "row" the class that identifies a section of the horizontal view within the browser.
- "col-sm" the class that identifies each column. col-sm is used in this example but the width can be set by adding a value at the end of the class name. col-sm-12 will give the column a full width of the browser window. If no numeric value is given the column width is decided by dividing the number of col class names by 12. In the below example each column is assigned a width of four as there are three divs with the class name of "col-sm".

```

<div class="container">
  <div class="row">
    <div class="col-sm">
      One of three columns
    </div>
    <div class="col-sm">
      One of three columns
    </div>
    <div class="col-sm">
      One of three columns
    </div>
  </div>
</div>

```

The above BootStrap html will produce the following result in a browser view on a desktop at full screen [22].

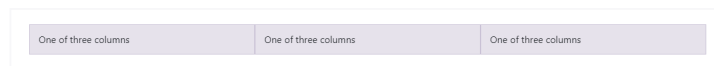


Figure 4.5

The below image is a view of the same BootStrap html viewed on a mobile device [22].

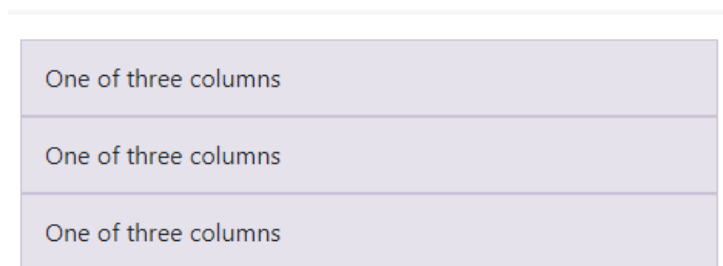


Figure 4.6

4.5 Json

JavaScript Object Notation (Json) is a language independent text based representation of a data object. This allows for the marshalling and un-marshalling of data to an object across many different programming languages. The Json data is written to a file with the .json extension and

usually held on a server. The .json file contents are plain text, which are interpreted by a programming language requesting the file from the server. Once the file has been received the data can be un-marshalled to the language specific object [23]. In the below example a JavaScript object will be used to explain the process.

The .json file structure has a parent container node named performance. Within this parent node there are two child nodes with key value pairs. The key for each object is named timeStep and reward with numerical values as the value for each key. [24]

```
{"Performance": [  
  { "timeStep":1, "reward":45 },  
  { "timeStep":2, "reward":100 }  
]}
```

When the file is requested from the server it needs to be parsed so it can be read as a JavaScript object.

```
var obj = JSON.Parse(demo.json);
```

The variable obj is now converted to a JavaScript object array and can be used as needed within the browser to display the relevant data.

```
["Performance",  
 [  
   "timeStep"  
   [  
     1  
   ]  
 ],  
 [  
   "reward"  
   [  
     45  
   ]  
 ],  
 [  
   "timeStep"  
   [  
     2
```



```

    ]
  ],
  [
    "reward"
    [
      100
    ]
  ]
]

```

4.6 CSV

A Comma Separated Value (CSV) file is used for storing data in a tabular format. Each new line within the file represents a new data entry. CSV files can be used to store multiple data types within the same file. It is then up to the program opening the file to interpret the data as needed. Below is a simple example of some numerical data entries within a csv file. [25]

```

1,30,80,300
2,59,67,-59
3,40,22,21

```

To parse this data an ajax call to a server can be used to request the file needed. [26]

```

$.ajax({
  type: "GET",
  url: "static/Data/test.csv",
  dataType: "text",
  cache: false,
  async: true,
  success: function(data) {
    // Array of data
    var data =data;

    $('table').append('<tr class="data"><td>'+data[0] +
      '</td><td>'+data[1]+'</td><td>'+data[2] +
      '</td><td>'+data[3]+'</td></tr>');

  }

});

```

In the above example once the csv file has been received from the server the data is placed into an array and appended to a html table for rendering the data to the browser page within a table cells [26].

4.7 Google Cloud App Engine

The Google Cloud app engine is used to deploy and host web applications to a live server.

In the below example a python flask application is used, however a number of different languages can be used for deployment.

The following requirements are needed to deploy an application to Google Cloud App Engine.

- Create App Engine instance: A new project is needed as a container for the application [27].



Figure 4.7

- A locally created Flask project as discussed within the flask section of this chapter.
- app.yaml file: This file contains the configuration settings for the application declaring the programming language, Version number, libraries used, static directories and the main flask file name [28].

```
runtime: python27
api_version: 1
threadsafe: true

libraries:
- name: ssl
  version: latest

handlers:
- url: /static
  static_dir: static
- url: /.*
script: main.app
```

- requirements.txt file: This file declares the different dependencies that are needed for the application to run. In the below example the flask and Werkzeug versions are declared [28].

```
Flask==0.12.4  
Werkzeug<0.13.0,>=0.12.0
```

- Google Cloud SDK: The Google SDK must be installed locally to enable the deployment of the project to the app engine. Once the SDK has been installed open the command line tool and change to the root directory of the project folder. Once inside the directory type the following command to deploy the application [28].

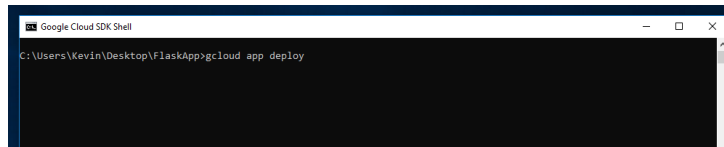


Figure 4.8

Once the deployment has completed the application will be available at app-name.appspot.com. [28]

Chapter 5

System Design

This chapter will examine the overall architecture and individual system components. These will be discussed at a high level view for the main structure of the system. The major functional components will then be broken down into a more fine grain view for examination. In addition the interaction between the components will be explained in further detail.

5.1 System Architecture

This system is client server based architecture with all of the system resources held on a server. The client interacts with the server via a resource http requests. When the client first enters the root URL of the application address a request is made for the "Index.html" web page. If found the index page along with any other JavaScript or CSS files are sent back to the browser for rendering.

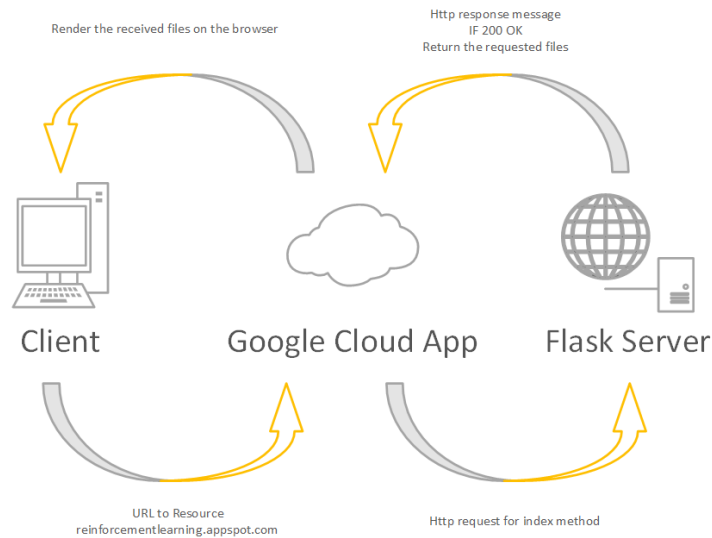


Figure 5.1: Architectural Diagram

In the following images the server will be launched locally. A request will be then sent to the server for the root resource. Finally the home page will be sent back to the browser to render the page to the user.

```
C:\Users\Kevin\Desktop\College Folders\Year 4\Main Project\Reinforcement-Learning\FlaskApp>python FlaskTest.py
* Serving Flask app "FlaskTest" (lazy loading)
* Environment: production
  WARNING: Do not use the development server in a production environment.
  Use a production WSGI server instead.
* Debug mode: off
* Running on http://127.0.0.1:5000/ (Press CTRL+C to quit)
```

Figure 5.2: Starting the server

The above image is the flask server running and listening for requests at `http://127.0.0.1:5000/`.

Once the URL has been entered to the address bar of the browser. The resource root method is called in the main Flask server file.

```
@app.route('/')
def index():
    # Return the main home page when the route resource is requested
    return render_template('index.html')
```

The above root method returns the `index.html` file within the response body to be read by the browser.

If everything is ok and all resources can be retrieved a status message of 200 is sent to the browser.

```
* Debug mode: off
* Running on http://127.0.0.1:5000/ (Press CTRL+C to quit)
127.0.0.1 - - [22/Apr/2019 16:20:32] "GET / HTTP/1.1" 200 -
```

Figure 5.3: http 200

Finally the home page is rendered to the user.

Reinforcement Learning

Home

Parameters

Grid Type:

Algorithm:

Epsilon:

Epsilon Decay:

Gamma:

Alpha:

Alpha Decay:

Number of Episodes:

Max number of steps:

Per Step cost:

Goal Reward:

Trap Reward:

Figure 5.4: Rendered Home Page

When the highlighted url is entered to the browser address. The index html page is sent back to the browser along with any CSS and JavaScript files needed.

This example is a brief introduction of the overall architecture of the application. A more in depth investigation of each system component will be discussed in the next chapter.

5.2 System Components

The following subsections will explain how each component operates within the application.

5.2.1 Environment File

The environment.py python file holds all of the agent logic, environment space, algorithmic operations and file creation for the application.

Grid Item Variables

There are four environment objects within each grid of an agent, a trap, an empty space and the goal. These are represented by single characters and are placed within the grids below as needed.

```

"""
Declare Agent, Goal, Empty and trap chars.
To be used for the environment space
"""
AGENT = 'A'
GOAL = 'G'
EMPTY = '*'
TRAP = '#'

```

Environment Grid Types

For this application the user can choose which grid they want to use for the agent to explore. Below there is a grid initialised to all empty characters and a further two grids of different configurations.

```

"""
Initialise the initial grid with all empty variables.
"""
grid = [
[EMPTY, EMPTY, EMPTY, EMPTY, EMPTY, EMPTY],
[EMPTY, EMPTY, EMPTY, EMPTY, EMPTY, EMPTY],
[EMPTY, EMPTY, EMPTY, EMPTY, EMPTY, EMPTY],
[EMPTY, EMPTY, EMPTY, EMPTY, EMPTY, EMPTY],
[EMPTY, EMPTY, EMPTY, EMPTY, EMPTY, EMPTY],
[EMPTY, EMPTY, EMPTY, EMPTY, EMPTY, EMPTY],
]
"""
The Cliff environment.
"""
grid_cliff = [
[EMPTY, EMPTY, EMPTY, EMPTY, EMPTY, EMPTY],
[EMPTY, EMPTY, EMPTY, EMPTY, EMPTY, EMPTY],

```

```

[EMPTY, EMPTY, EMPTY, EMPTY, EMPTY, EMPTY],
[EMPTY, EMPTY, EMPTY, EMPTY, EMPTY, EMPTY],
[EMPTY, EMPTY, EMPTY, EMPTY, EMPTY, EMPTY],
[AGENT, TRAP, TRAP, TRAP, TRAP, GOAL],
]
"""
The standard environment.
"""
grid_standard = [
[EMPTY, EMPTY, EMPTY, EMPTY, EMPTY, GOAL],
[EMPTY, EMPTY, EMPTY, EMPTY, EMPTY, TRAP],
[EMPTY, EMPTY, TRAP, EMPTY, EMPTY, EMPTY],
[EMPTY, EMPTY, TRAP, EMPTY, TRAP, EMPTY],
[EMPTY, EMPTY, EMPTY, EMPTY, TRAP, EMPTY],
[AGENT, EMPTY, EMPTY, EMPTY, EMPTY, EMPTY],
]

```

Depending on which grid the user has chosen the empty grid gets assigned to the chosen grid.

```

if environment_form == "grid_cliff":
    grid = grid_cliff

if environment_form == "grid_standard":
    grid = grid_standard

```

State Class

The State class is used to keep track of the agents position once the script has run.

```

class State:
    # Initialise the class variables of grid and agent position
    def __init__(self, grid, agent_pos):
        self.grid = grid
        self.agent_pos = agent_pos

    def __eq__(self, other):
        return isinstance(other, State) and self.grid == other.grid \
        and self.agent_pos == other.agent_pos

```


Hyper Parameters

The hyper parameters below are taken from the submitted form apart from the MIN ALPHA value. This value is used to ensure that the alpha value will not fall below zero when decaying after each episode.

```
#The max number of episodes
N_EPISODES = int(epochs_form)
# Set the maximum number of steps per episode
MAX_EPISODE_STEPS = int(max_steps_form)
MIN_ALPHA = 0.0001
# Learning rate value
alpha = float(alpha_form)
# Future reward value
gamma = float(gamma_form)  # .8
# Random action probability
eps = float(epsilon_form)  # .09
# Decay the alpha value for every completed episode
alphaDecay = float(alpha_form_decay)
# Set an array of equal values deviding alpha by the number of episodes.
alphas = np.linspace(alpha, MIN_ALPHA, N_EPISODES)
# The random action decay rate for every completed episode.
epsilon_decay = float(epsilon_form_decay)
```

Agent Actions

The agent actions of up, down, left and right are given numerical values and placed in an array named actions. This will later be used by the choose action function.

```
UP = 0
DOWN = 1
LEFT = 2
RIGHT = 3
ACTIONS = [UP, DOWN, LEFT, RIGHT]

start_state = State(grid=grid, agent_pos=[5, 0])
```

Choosing Agent Actions

This method checks if the epsilon value is greater than a randomly generated floating point number between 0 and 1. With the epsilon value at .8 there is an 80% chance of the agent choosing a random action. This will force the

agent to explore the environment and seek out all possible paths to the goal. This values decays after each episode gradually minimising the chance of the agent choosing a random choice.

```
# Choosing an action based on the epsilon value
def choose_action(state):
    if random.uniform(0, 1) < eps:
        # choose a random action of up, down , left or right.
        return random.choice(ACTIONS)
        # If epsilon is less than the random number choosed the maximun
        # value for the next state.
    else:
        return np.argmax(q(state))
```

Defining Agent Actions

The below code is a snippet of a method that move the agent position. It checks the action taken of up, down left or right and moves the agent in the direction needed.

```
# A deep copy of the state classs agent position to prevent
# an unwanted change in data.
p = deepcopy(state.agent_pos)
if action == UP:
    # Move up and Limit the movement to the top of the grid
    p[0] = max(0, p[0] - 1)
elif action == DOWN:
    # Move down and limit the movement to the bottom of the grid
    p[0] = min(len(state.grid) - 1, p[0] + 1)
elif action == LEFT:
    # Move left and limit the movement to the far left of the grid
    p[1] = max(0, p[1] - 1)
elif action == RIGHT:
    # Move right and limit the movement to the far right of the grid
    p[1] = min(len(state.grid[0]) - 1, p[1] + 1)
```

Checking the agent position

In the below code snippet the agent position is checked for a Trap of a Goal. (Empty and Agent have been omitted for brevity). If the agent is occupying either of these grid items a final reward is given and the episode is terminated. A new episode is started if the maximum number of episodes has not been exceeded.

```

# Condition to check if the grid item is a trap
if grid_item == TRAP:
    # assign the reward signal from the value set in hte form
    reward = int(trap_reward)
    # done to end the iteration
    is_done = True
    # palce the agent back to the start position
    new_grid[p[0]][p[1]] += AGENT
    # Check if the goal has been reached
elif grid_item == GOAL:
    # assign the reward value set from the front end form
    reward = int(goal_reward)
    # Set the episode to done to restart another new episode
    is_done = True

```

Q-Table

The Q-Table is a dictionary that is initialised to all zero values when the script is first run.

```

# Q-Table dictionary
q_table = dict()
# set the state to zeros within the Q-Table
q_table[state] = np.zeros(len(ACTIONS))

```

Q-Learning Algorithm

The Q-Learning algorithm is defined as an off policy strategy whereby the current q values are partially updated from the next state maximum q value. With this implementation of the Q-Learning algorithm there is an outer loop for every episode. The inner loop is every time step for each episode. With each iteration of the inner loop the Q-Table is updated with the Q-Learning formula as discussed in chapter one

$$Q^{new}(s_t, a_t) \leftarrow Q(s_t, a_t) + \alpha[r_t + \gamma \max_a Q(s_{t+1}, a) - Q(s, a)] \quad [3].$$

This updates the current sates value for the action taken based on the maximum value of all actions in the next state. The inner loop continues until it either reaches the maximum number of steps set by the user or a terminal state has been reached.

```

for e in range(N_EPISODES):
    state = start_state
    # Inner loop for executing every step of the agent within each episode.

```

```

for _ in range(MAX_EPISODE_STEPS):
    # choose an action for each step taken
    action = choose_action(state)
    # assign the returned parameters from the act function
    (next_state, reward, done) = act(state, action)
    # assign the returned decay rate to alpha and epsilon from
    # the check_terminal_state function
    alpha, eps = check_terminal_state(done, alpha, eps)
    """
    Q-Learning Algorithm
    """
    # Get the max value from the next action used for updating the
    # current states q value.
    max_next_action = np.max(q(next_state))
    # Formula for Q Learning
    #  $Q(s, a) = Q(s, a) + \alpha[r + \gamma * \max_{a'} Q(s, a') - Q(s, a)]$ 
    # The above formula has been broken into three statements
    target = reward + gamma * max_next_action
    end_eq = target - q(state)[action]
    q(state)[action] += alpha * end_eq
    # add to total reward
    total_reward += reward
    # The next new state assigned to the current state.
    state = next_state
    # Increment the number of steps
    number_of_steps += 1
    if done:
        break

```

SARSA Algorithm

The SARSA and Q-Learning algorithms look almost identical at first glance but the way in which the q values are updated are very different. The SARSA algorithm $Q(s_t, a_t) \leftarrow Q(s_t, a_t) + \alpha[r_t + \gamma Q(s_{t+1}, a_{t+1}) - Q(s_t, a_t)]$ [4] is defined as on policy whereby its q value is partially updated based on the next state and next action unlike Q-Learning using the maximum q value from the next state. The inner and outer loops are similar to the Q-Learning example above, with the difference being an action is chosen at the start of every episode and the next action is chosen from the next state only. The next state and next action are also updated within the inner loop. The difference in performance between the two algorithms will be examined in

the next chapter.

```

if algorithm_form == "sarsa":
    # Start the outer episode loop
    for e in range(N_EPISODES):
        # Get the initial start state of the agent
        state = start_state
        # Choose an action
        # This differs from the q learning algorithm
        # An action is chosen at the start of every episode
        action = choose_action(state)
        # Inner loop for every agent time step
        for _ in range(MAX_EPISODE_STEPS):
            # assign the returned parameters from the act function
            (next_state, reward, done) = act(state, action)

            # the next action based on the next random or max state
            # This differs from q learning as the q table is update just by this action
            # not the max value of all possible next actions
            next_action = choose_action(next_state)
            # For decaying alpha and epsilon
            alpha, eps = check_terminal_state(done, alpha, eps)
            # Formula for SARSA
            #  $Q(s,a) = Q(s,a) + \alpha[r + \gamma Q(s',a') - Q(s,a)]$ 
            # Broken down into three statements
            target = reward + gamma * q(next_state)[next_action]
            eq_end = target - q(state)[action]
            q(state)[action] += alpha * eq_end
            # Set the current action to the next action
            action = next_action
            # set the current state to the next state
            state = next_state
            # add the current reward to the total reward
            total_reward += reward
            # increment the number of steps
            number_of_steps += 1
        if done:
            break

```

Writing Agent Position to File

For each step the agent takes the coordinates are written to a text file using the open python method.

```
completeName = os.path.join('static/Data', 'agentPos.txt')
# Open the file or create one if it doesn't exist
f = open(completeName, 'w+')
```

From there the agent position can be written out to a text file wherever is needed using the f.write python method.

```
f.write('%d,' % p[0])
f.write('%d,' % p[1])
```

As the algorithms are episodic the agent x,y coordinates will be written out to a text file for every step the agent takes. This file can then be read via JavaScript to animate a shape representing the agent within a HTML canvas. In addition the file will be overwritten when a new request has been made ensuring that only the latest data is present.

Writing Q-Table Values to CSV File

To store the Q-Table values as they are being generated the dictionary holding the Q-Table is converted to a python list and then a pandas data frame. Once the Q-Table is represented as a data frame it can be converted and written to a csv file. This allows the data to be displayed within a HTML table and updated as needed. A new version of the Q-Table is appended to the csv file for every step the agent takes within the inner loop of the Q-Learning or SARSA algorithms. This supplies complete history of every q value update as the algorithm runs. Terminal states were removed from the q table as they were all zero and of no use for the front end table data.

```
# check for a row in the dictionary that sums to zero
# If it does sum to zero store in empty keys
empty_keys = {k: v for k, v in q_table.items() if sum(v) == 0}
# iterate through empty_keys
for k in empty_keys:
    # delete all rows with zeros
    del q_table[k]
# open the Q-Table csv file is it exists. If it doesn't exist create one.
with open('static/Data/Q_Table.csv', 'a', newline='') as f1:
    #Write out and append to a dataframe the q table values
    f1.write(pd.DataFrame(list(q_table.values())).to_csv(header=None))
```

Writing Rewards to Json File

With each episode completed:

- The total rewards gained are stored in a list array

```
q_learning_list = []
q_learning_list.append(total_reward)
```

- The list is converted to a pandas data frame

```
df = pd.DataFrame(q_learning_list).
```

- The data frame is converted to Json

```
df.to_json()
```

- The Json data is written out to a Json file using pandas toJson() method

```
with open('static/Data/q_learning.json', 'w') as al:
    # write the dataframe out to a json file
    al.write(df.to_json())
```

5.2.2 Data Files

When the script has completed the following files are created:

Q_Learning.json:

The data is structured with each episode number and total reward gained as key value pairs.

```
{"0":{"0":-119.0,"1":-106.0,"2":-110.0,"3":-118.0,"4":-110.0,"5":-178.0}}
```

Agent_Pos.txt:

Within this file every multiple of two values represent the x, y coordinates of the agent position. These values will be later split into tuples for animating a shape representing the agent.

```
5,0,5,0,4,0,4,0,3,0,4,0,3,0,2,0
```

Q_Table.csv:

The contents of this file holds the q-table values for every step the agent has taken for the duration of the chosen algorithm. The below data is the final q-table of the csv file with the state number and q values for each states action. This table is a representation of the final step the agent has taken.

The file generated can be very large depending on how many episodes the user has selected. With every time step the agent takes within each episode a new version of the below table is appended to the csv file. Each time the script is run the file is deleted and then recreated to ensure that the latest data is only present.

State	Up	Down	Left	Right
0	22.52511999999982	15.312135367563133	14.289668672248755	-99.71113772079485
1	3.960936623865009	13.617460700938727	17.95734718463899	29.40639999999984
2	-1.878271117634098	-2.012313902784331	-1.8815576932847637	15.243839125901262
3	-1.5295742726218287	-0.6651108864555006	-1.453991195638845	-1.3454791885513238
4	-1.3298856168452398	-1.3782276976507892	-1.4810440112176881	-1.4009042382447756
5	-1.3404449880448084	-1.236788766027146	-1.2436143067994825	-1.2819022725009503
6	-1.257981734927635	-1.3173966251263058	-1.4462891399381745	-1.301105125926431
7	-1.0987670989925822	-1.2414790942150584	-1.125976271967187	-0.9656125664425864
8	-1.1551614289269732	-0.9918947873425943	-1.0312728318577251	-1.0777704347717376
9	-0.8293603632964249	-1.0161329114408177	-0.85828502336085	-1.0220599125373369
10	-0.98961	-0.7783057291019736	-0.7112311527378622	-0.748887226749499
11	-0.8319	-0.7464912046893787	-0.582	-0.582
12	-0.582	0.05138677455413032	-0.8028881891543086	-0.534987435270541
13	-0.7853614648496994	-0.7543131835324851	5.5357476588926735	-0.7267475254392772
14	-0.6374463101903487	30.48445789559959	-0.04147787369938402	-0.1835066667305324
15	6.1008142164208214	59.57216742404885	3.578987325960474	20.15045848281535
16	-0.7489549628955137	73.3921476146162	14.899340036798916	-0.49569258876485467
17	44.1636518774165	99.99999999999994	54.92054424745762	68.95364044676266
18	-0.796333333789363	0.5075142332201901	-0.7683226310600988	-0.582
19	-1.1213878960723254	-1.0917344464410255	-1.0386342926259675	2.0537214318666543
20	-0.9174273822373968	-0.34233859769154196	-1.2038302558215905	-0.8684927436176264
21	-0.9418047973287629	-1.4207538670916309	-1.214509420128951	-1.0517542749162405
22	11.488866076827776	-99.9707299730268	14.315620732267625	38.007999999999846
23	-1.5425145779800709	27.980085861161136	0.1955682559630758	-1.407294795583535
24	-1.238480339898809	34.474084517089224	-1.5855723303517113	1.3381376892739045
25	-1.3411399964853334	-1.3097183035656783	-1.1600550530407983	-1.394592539382078
26	0.5247675921814534	7.51784556502975	3.8684041759256216	30.338944504641102
27	13.204714294782987	-92.83844051173776	32.35995431002325	62.19999999999989
28	19.127847414768297	-98.95976848214123	21.905625961034534	48.75999999999987
29	-1.0351164988463812	2.054113774404443	-0.6847721449750789	11.755097177999282
30	32.17905547303044	-96.73690973090974	29.987489972815574	78.9999999999999

5.2.3 index.html

: Holds the home page with a form for the user to submit. The input fields available to the user are the choice of algorithm and hyper parameters all of which will be bound to the variables held in the environment.py file.

The screenshot shows a web browser window with the address bar displaying '127.0.0.1:5000'. The page title is 'Reinforcement Learning'. Below the title is a navigation bar with a 'Home' button. The main content area is titled 'Parameters' and contains a form with the following fields:

- Grid Type: Clib (dropdown)
- Algorithm: Q-Learning (dropdown)
- Epsilon: 1 (text input)
- Epsilon Decay: 99 (text input)
- Gamma: 8 (text input)
- Alpha: 3 (text input)
- Alpha Decay: 9 (text input)
- Number of Episodes: 100 (text input)
- Max number of steps: 20 (text input)
- Per Step cost: -1 (text input)
- Goal Reward: 100 (text input)
- Trap Reward: -100 (text input)

A 'Submit' button is located at the bottom right of the form.

Figure 5.5

To bind the form parameters to the environment python script variables, each form input field is given an id.

```
<input id="max_steps" name="max_steps" type="number" min="20"
max="100" step="20" value="20" class="form-control">
```

When the form is submitted the form data is sent as a post request and the run method is requested on the servers flask application file.

```
<form class="form-horizontal" action="/run" method="post">
```

Within the flask application file the run method is called and each form input field is bound to the variables within the environment.py file. The waiting.html page is then returned to the browser for rendering.

```
@app.route('/run', methods=['GET', 'POST'])
def test():
    if request.method == 'POST':
        environment.environment_form = request.form.get('grid_type')
```

```

environment.algorithm_form = request.form.get('algorithm')
environment.episodes_form = request.form.get('episode')
environment.max_steps_form = request.form.get('max_steps')
environment.per_step_cost = request.form.get('per_step_cost')
environment.goal_reward = request.form.get('goal_reward')
environment.gamma_form = request.form.get('gamma')
environment.epsilon_form = request.form.get('epsilon')
environment.epsilon_form_decay = request.form.get('epsilon_decay')
environment.alpha_form = request.form.get('alpha')
environment.alpha_form_decay = request.form.get('alpha_decay')
environment.trap_reward = request.form.get('trap_reward')
return render_template('waiting.html')

```

5.2.4 waiting.html

: The waiting page is simply holds an animated gif image that displays until the script has completed running. In the background of this page JavaScript is used to send a get request for the run resource. This will run the environment.py file and return a message of 'done' once the file has completed running.

```

# The first request made once teh form has been submitted
@app.route('/run', methods=['GET', 'POST'])
def test():
    if request.method == 'GET':
        # Call the init function from the environment.py script
        environment.init()
        return 'done'

```

JavaScript is used to ping the server for a return message of "done". Once the message has been successfully returned the success resource is then requested.

```

if (request.status === 200 && request.responseText === 'done') {
    window.location = '/success';
}

```

Finally the flask application file returns the result.html page to the browser for rendering. In addition the form input field values are stored in variables that can be used within template holders in the result.html page. This keeps the from data submitted by the user on the home page. This can then be inserted to the form on the result page so the user does not need to remember the original settings. This allows for the tweaking of some parameters and

rerunning the application to view the difference in performance. Some of the form input variables have been omitted for brevity.

```
@app.route('/success', methods=['GET', 'POST'])
def dealy():
    var0 = environment.environment_form
    var1 = environment.algorithm_form
    var2 = environment.epsilon_form
    return render_template("result.html", var0=var0, var1=var1, var2=var2)
```

5.2.5 result.html

: This file displays all of the rendered data from the files generated by the environment.py file with the following UI elements.

The performance chart uses Google line chart JavaScript library to access the Json files via an Ajax request. There are two files requested, the SARSA and Q-Learning Json file generated by environment.py when run.

Google Chart

```
// Make ajax call
$.ajax({
    //Request the q learning json file
    url: "/static/Data/q_learning.json",
    dataType: "json",
    // Clear cache for new data after each request
    cache: false,
    async: true,
    success: function (data) {

    var data2 = data;

    $.ajax({
        //Request the sarsa json file
        url: "/static/Data/sarsa.json",
        dataType: "json",
        cache: false,
        async: true,
        success: function (data1) {
```

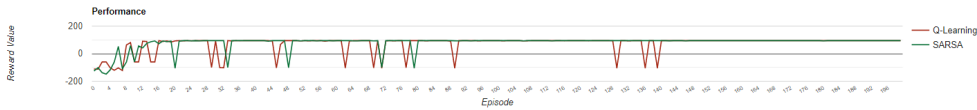


Figure 5.6: Performance Chart

Bootstrap framework

The Bootstrap framework was used to style and set the layout of the page elements. The html tags were given bootstrap id and class names to enable the forms, canvas elements and charts a responsive design. Below in a image of the result page with the from compressed to a button that will slide down when clicked. the chart and grid have also resized to fit the browser size.

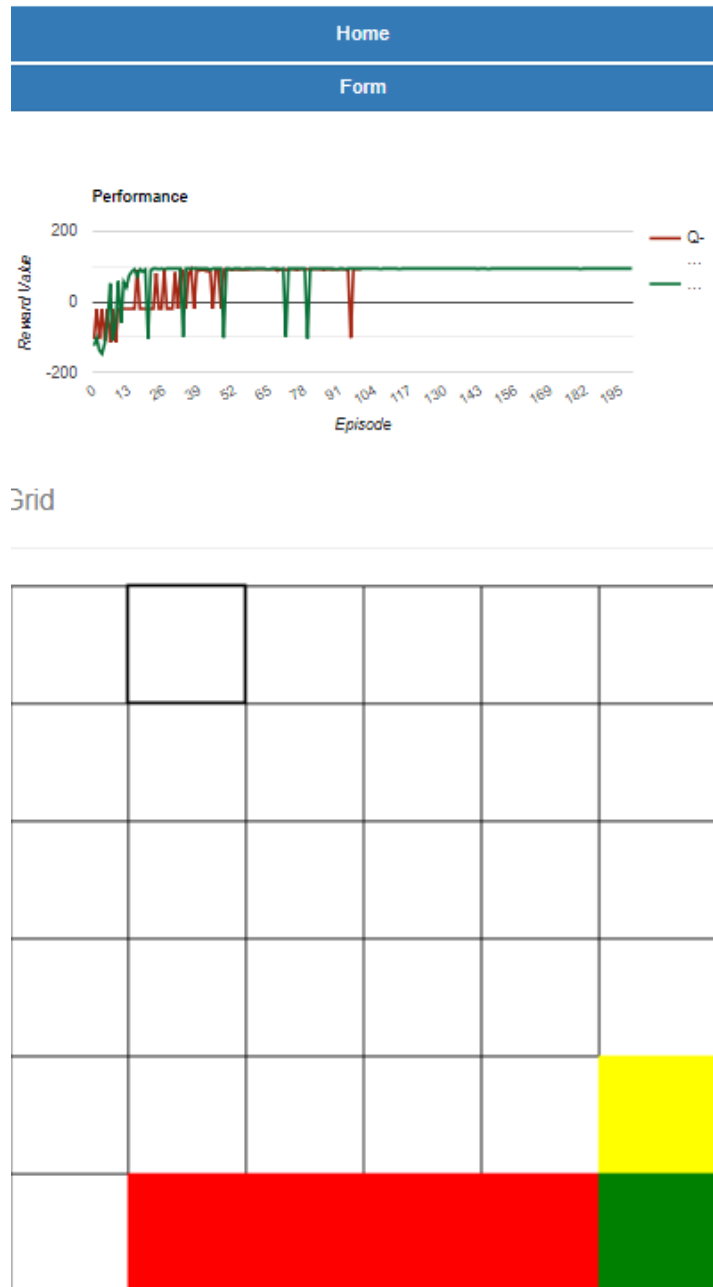


Figure 5.7

Html Canvas

The below grid environment uses the HTML canvas to animate the agent from one grid coordinate to the next. The agent position is read from the text file generated by the environment.py script.

```
//request the agent position text file from the server
url: "/static/Data/agentPos.txt",
dataType: "text",
cache: false,
async: true,
success: function (data)
```

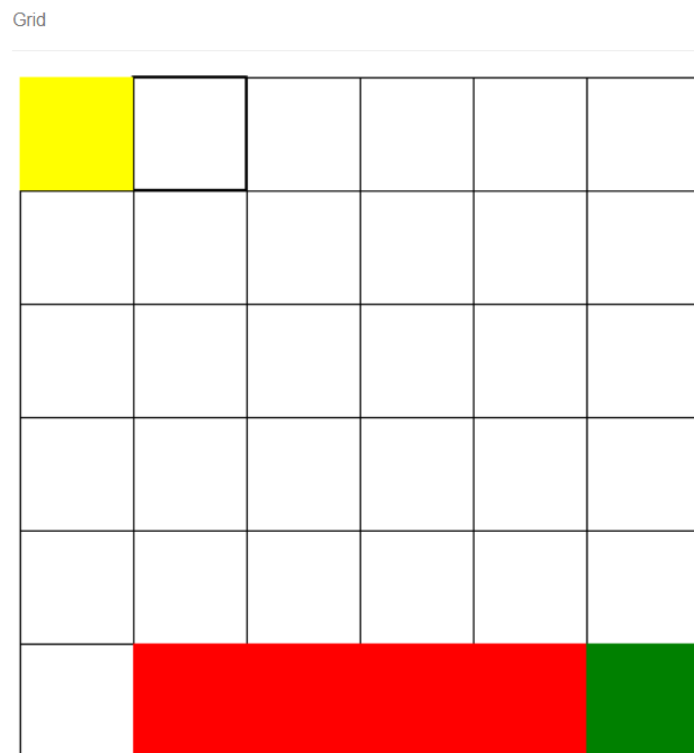


Figure 5.8: Grid Environment

Animation of the agent is achieved by a time out function where the canvas is redrawn with the agents updated position.

```
for(let i=0; i<arr.length -2; i+=2){
// Time out function for animating the agent
window.setTimeout(function () {
```

```

// Get the x, y coordinates
x1 = arr[i];
y1 = arr[i+1];
// Clear the canvas after each frame is rendered
context.clearRect(0, 0, 650, 650);
// Call the draw board function
drawBoard();
// Check the grid type set by the form input
// Flask template variable is used to get the value in the result page
if(grid_type == "grid_standard") {
drawShape(5, 0, 'green');
drawShape(5, 1, 'red');
drawShape(4, 3, 'red');
drawShape(4, 4, 'red');
drawShape(2, 2, 'red');
drawShape(2, 3, 'red');
drawShape(y1, x1, 'yellow');
}
// Set the frame rate of hte animation
}, i * 50);

```

Q-Table Data update

The below image of the Q-Table is populated from the Q_Table.csv data. The file is requested via an ajax request to the server. Once the file is accessed the data is parsed and fed to a html table. To update the table the data is cleared at every zero index (new q table).

Q-Table

State	UP	Down	Left	Right	Agent Pos
0	22.1773253	-2.4509339	-2.4763362	-67.8354884	5,0
1	-0.5342945	1.2106974	-0.1355992	29.2379704	4,0
2	-1.5789511	-61.6472848	2.0342724	37.9204296	4,1
3	-1.4493946	-1.4720294	-1.5655000	-1.3793400	3,1
4	-1.3244453	-1.2612907	-1.4380969	-1.3502950	2,1
5	-1.2694297	-1.1806022	-1.2202219	-1.2172792	1,1
6	-1.1948964	-1.2050199	-1.2572985	-1.2064564	0,1
7	-1.7224178	8.8228914	-1.7290263	-1.7127011	3,0
8	-1.4942970	-1.5805811	-1.5216638	-1.5607638	2,0
9	-1.3619570	-1.4590299	-1.3399212	-1.3106478	1,0

Figure 5.9: Q-Table

```

// Timeout for parsing the array of data
window.setTimeout(function () {
// Get every 5th column for each row

```

```

for(j=0; j< (result[i].length-1) / 5; j++){
  // Store the 5 columns in array
  csvRowCheck = result[i].slice(j * 5, (j + 1) * 5);
  // Clear the data after every zero index
  // Allows for updating the data after every frame
  if(csvRowCheck[0]==0){
    $('<td>').remove();
  }
  // Add the data to the html table on the result page
  // Truncating the point decimal places to 7 to save space on the page.
  $('<table>').append('<tr class="data"><td>'+csvRowCheck[0] +
    '</td><td>'+csvRowCheck[1].toFixed(7) +
    '</td><td>'+csvRowCheck[2].toFixed(7) +
    '</td><td>'+csvRowCheck[3].toFixed(7) +
    '</td><td>'+csvRowCheck[4].toFixed(7) +
    '</td><td>'+arrays[j]+ '</td></tr>');

```

Hottie Library

The values within the q-table are also colour coded from low (red) to high (green) this was achieved by using the Hottie JavaScript library. The table data is accessed via JQuery selectors and the cells colour is based on these numerical values from low to high.

```

// The Hottie framework to heatmap the values in the table as they update
// Adapted from : https://github.com/DLarsen/jquery-hottie
$("#q_table td:not(:first-child, :last-child)").hottie({
  colorArray : [
    "#F8696B",
    "#FBE983",
    "#63BE7B",
    "#63BE7B",
    "#63BE7B",
    "#63BE7B"
  ]
});

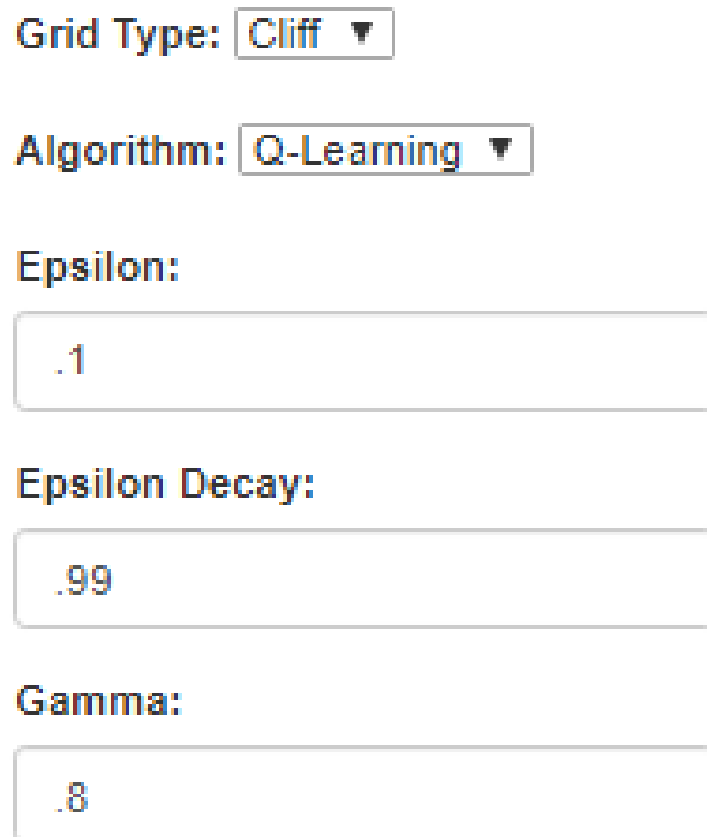
```

Form Data Persistence

The form data submitted on the home page or the result page is persisted across requests. This is achieved via flask parameter templates. var2 is the second parameter returned from the success resource within the flask

application file. There are eleven other parameters that have been omitted to keep the below example concise.

```
<input id="epsilon" name="epsilon" type="number"
min="0" max="1" step=".1"
value="{ { var2 } }" class="form-control">
```



Grid Type:

Algorithm:

Epsilon:

Epsilon Decay:

Gamma:

Figure 5.10: Data kept from home page

5.3 Sequence Digram

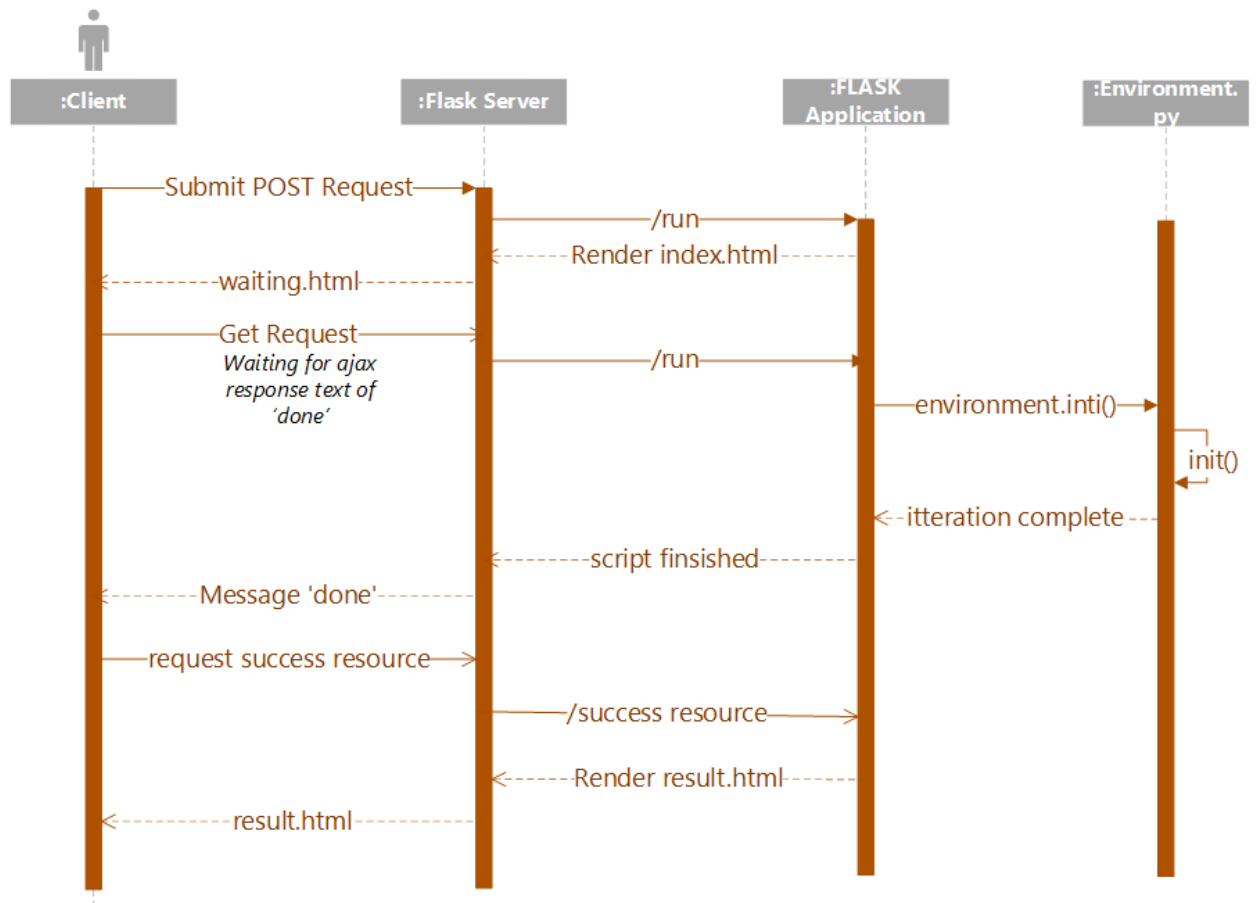


Figure 5.11

5.4 Deployment

To deploy the local development environment to a instance of a Google Cloud Application. The files app.yaml and requirements.txt are needed for pushing the application files to the Google application instance.

The yaml file contains the configuration information for the application including the programming language, environment type, time out limit for the server and the flask application file name.

```
runtime: python
env: flex
```

```
entrypoint: gunicorn -t 120 -b :$PORT FlaskTest:app
runtime_config:
python_version: 3
```

The requirements text file declares what python packages the application will use.

```
Click==7.0
Flask==1.0.2
gunicorn==19.9.0
itsdangerous==1.1.0
Jinja2==2.10
MarkupSafe==1.1.0
Werkzeug==0.14.1
numpy==1.15.1
pandas==0.23.4
```

Once an empty application instance has been created on Google cloud platform the locally held files are ready to be pushed to the cloud for deployment. The Google sdk command line interface is used with the following command.

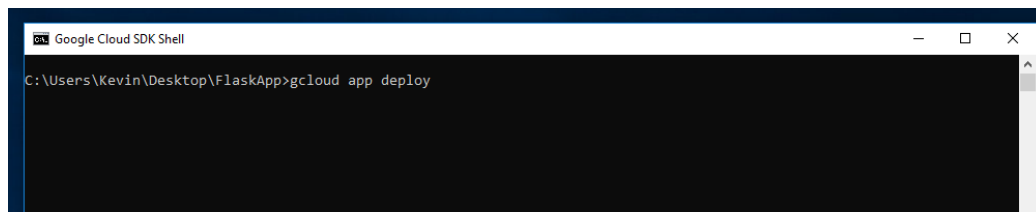


Figure 5.12

Once completed the application is now live and available to anyone who wishes to access the application.

Chapter 6

System Evaluation

From the objectives identified in the introduction of this document the systems performance will be examined and documented in this chapter.

6.1 Implementing SARSA and Q-learning

The difference between the SARSA and Q-Learning algorithms should be evident once the algorithms have completed. The SARSA algorithm should take a longer path to the goal state but have less instances of falling into a negative trap state. The resulting graph should show over time that q-learning gains a higher end reward but has more negative trap rewards than SARSA. Below is an image of the performance graph of both algorithms using the same input parameters.

- 6.2** Flask server to handle requests
- 6.3** Parsing Json, text and csv files via Ajax
- 6.4** Agent animation HTML canvas
- 6.5** Generate dynamic table
- 6.6** Add a heat map to the values of table cells
- 6.7** Deployment to the Google Cloud Platform

Chapter 7

Conclusion

About three pages.

- Briefly summarise your context and ob-jectives (a few lines).
- Highlight your findings from the evalua-tion section / chapter and any opportuni-ties identified.

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