

## 3 Linear Regression in Scikit-learn

### 3.1 Explore Scikit-learn Dataset

#### 3.1.1 Get n\_features and n\_samples

Number of features in the Boston dataset is: 13

Number of samples in the Boston dataset is: 506

#### 3.1.2 Find best fitted feature

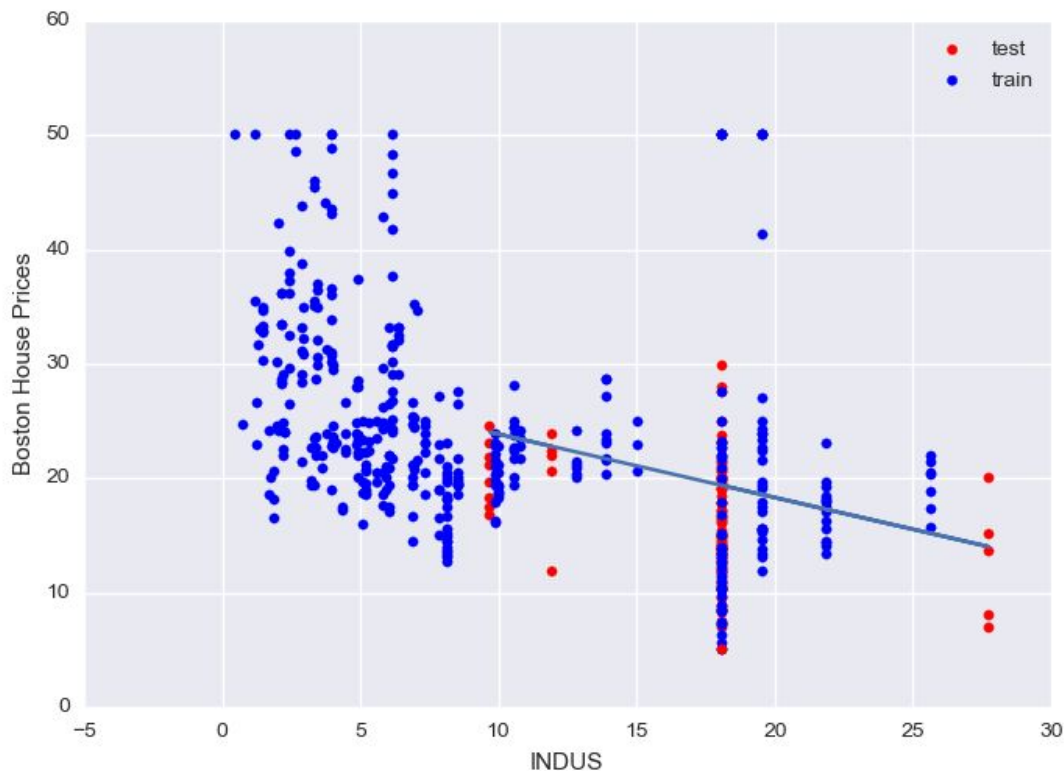
Best fitted feature name is: INDUS

Best fitted model score is: 0.20596851298

#### 3.1.3 Calculate the loss function

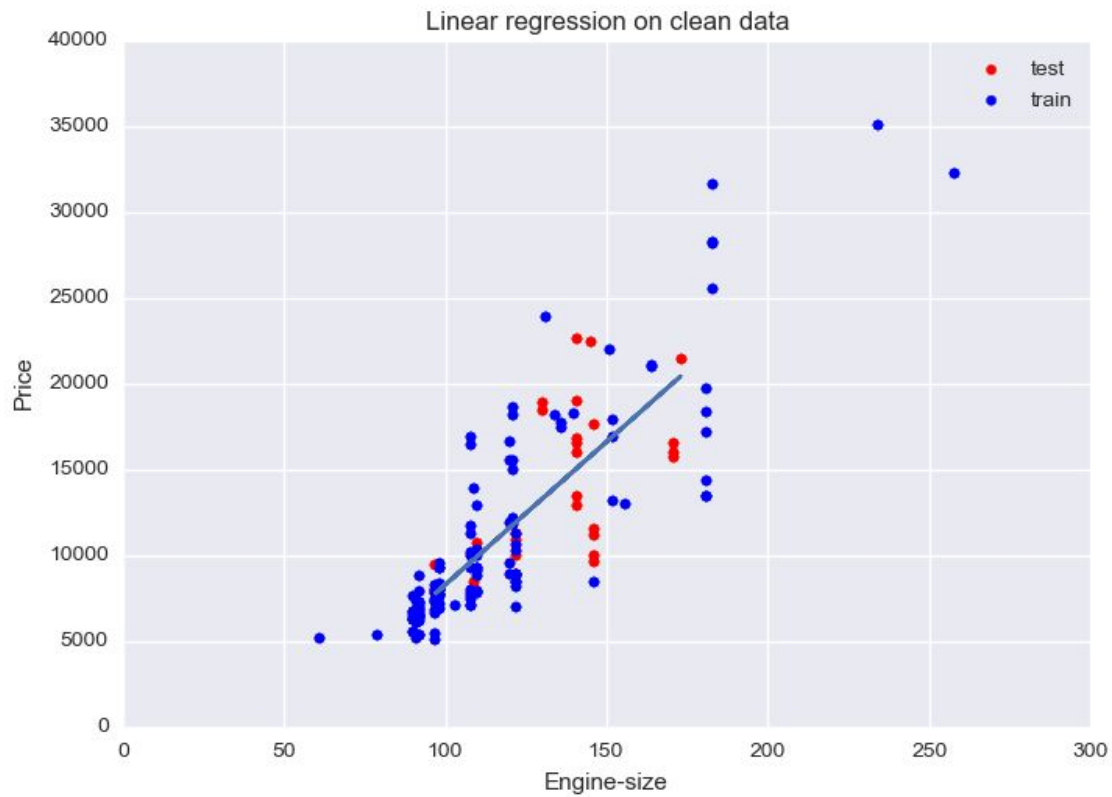
Value of the loss function for the best fitted model is: 18.5645355697

#### 3.1.4 Plot the predictions and test data



## 3.2 Explore Raw Dataset

### 3.2.3 Linear regression on the cleaned data



Price prediction for engine size equals to 175 is: 20793.532819

### 3.2.4 Linear regression on the standardized data



### 3.2.5 Linear regression with multiple features

Parameter theta calculated by normal equation:

```
[[ -4.51028104e-17]
```

```
 [ 8.62451816e-01]
```

```
 [ 7.36117228e-02]]
```

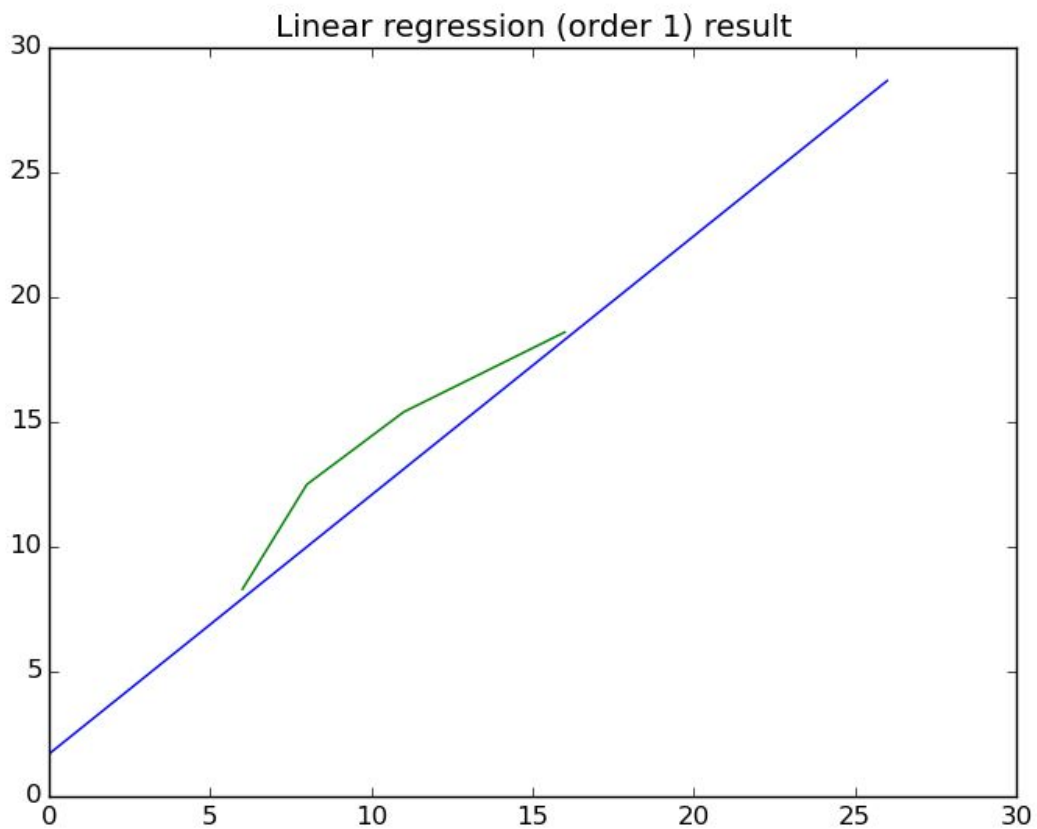
Parameter theta calculated by SGD: [-0.00054594] , [ 0.72440641 -0.00671158]

## 3.3 Understand Regularization

### 3.3.1 LR regression on polynomial data

$$y_1 = 1.7 + 1.0375x$$

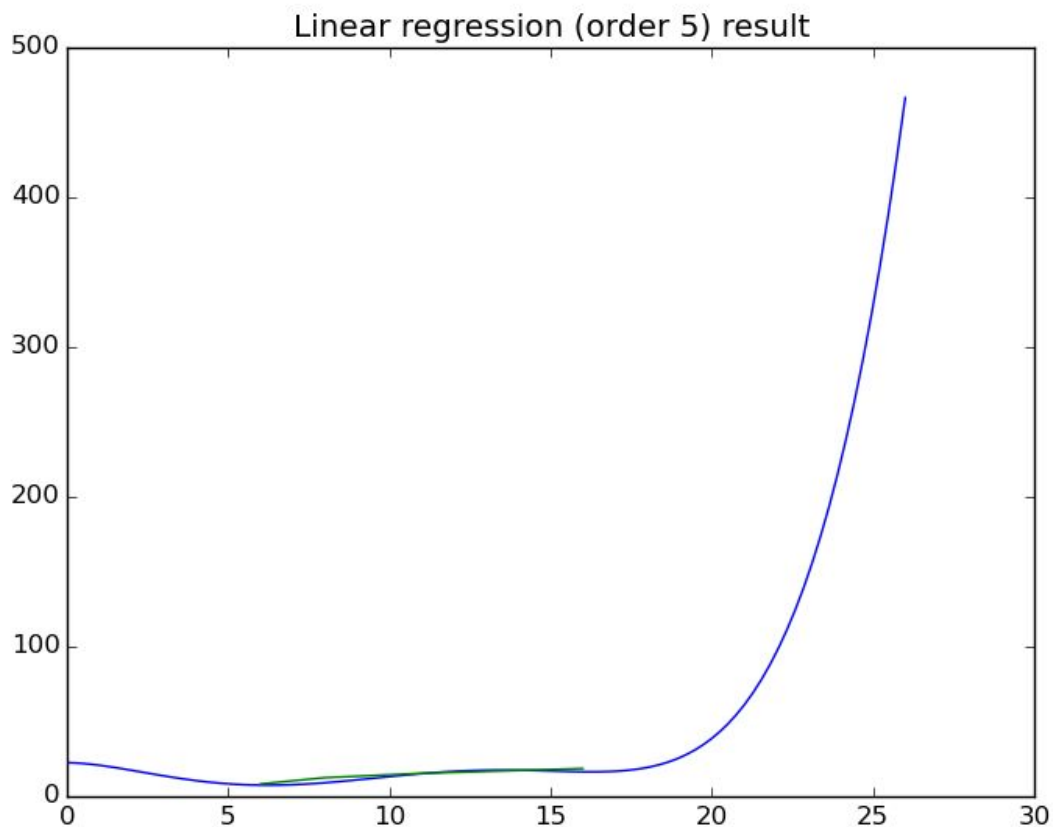
Linear regression (order 1) model score is: 0.79629076087



### 3.3.2 Polynomial regression on training data

$$y_2 = (22.51893655) + (2.34036485e-11)x + (-3.45575425e-01)x^2 + (-1.69531630e+00)x^3 + (3.41630495e-01)x^4 + (-2.28934322e-02)x^5 + (5.09722747e-04)x^6$$

Linear regression (order 5) score is: 0.706486295693



### 3.3.3 Ridge Regression

$$y_3 = (8.04794217) + (0.00000000e+00)x + (-7.08628224e-02)x^2 + (-3.45903785e-01)x^3 + (8.79869408e-02)x^4 + (-6.15336314e-03)x^5 + (1.36225166e-04)x^6$$

Ridge regression (order 5) score is: 0.82053974087

### 3.3.4 Comparisons

The model with the highest score is: Ridge Regression

Ridge model can prevent over-fitting: Yes

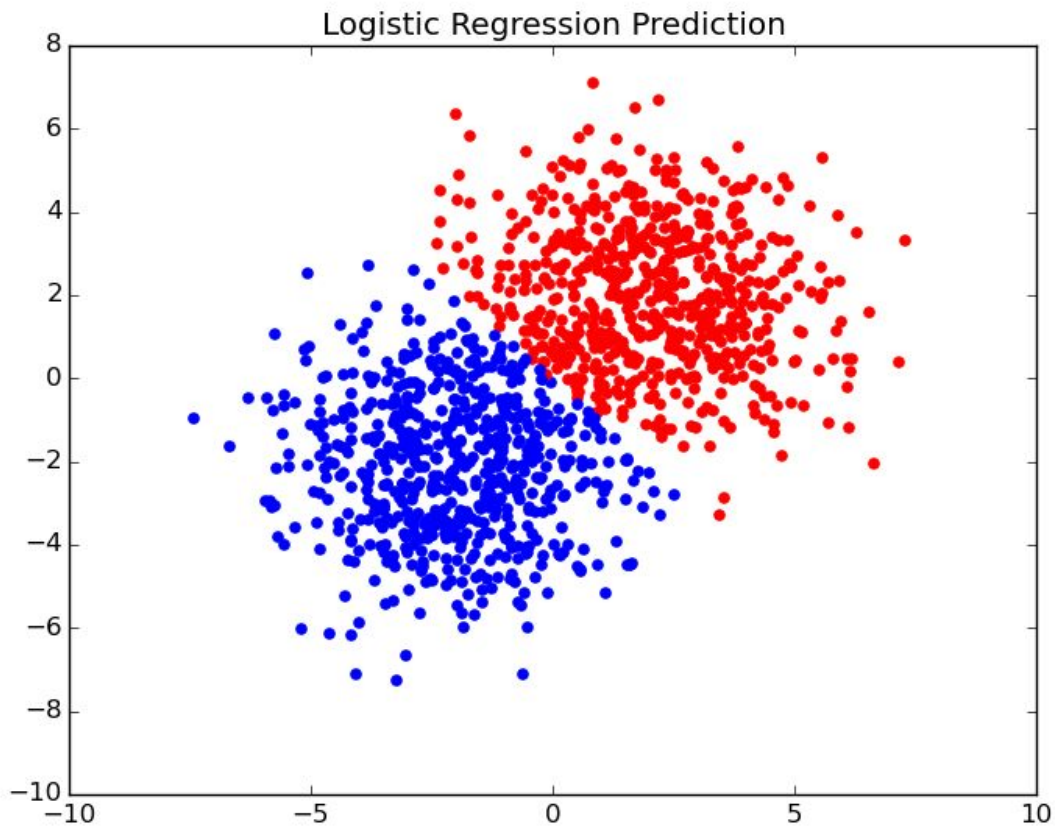
Ridge model is nearly equivalent to LR model (order 5) if alpha = 0: Yes

A larger alpha results in a larger coefficient for  $x^4$ : Yes

## 4 Linear Discrimination/Classification

### 4.1 Binary Classification

The predictions only have 0 and 1: Yes



### 4.2 Classification Statistics

Number of wrong predictions is: 73