Assignment 8 – Part 2 Set 9.6 - 4, 12, 18

- A camera shop stocks eight different types of batteries, one of which is type A7b. Assume there are at least 30 batteries of each type.
 - a. How many ways can a total inventory of 30 batteries be distributed among the eight different types?
 - b. How many ways can a total inventory of 30 batteries be distributed among the eight different types if the inventory must include at least four A76 batteries?

4.a.)
$$\binom{30+8-1}{30} = \binom{37}{30} = \frac{37!}{30!7!} = \frac{37*36*35*34*33*32*31}{7*6*5*4*3*2*1} = 10,295,472$$

4.b.)
$$\binom{26+8-1}{26} = \binom{33}{26} = \frac{33!}{26!7!} = \frac{33*32*31*30*29*28*27}{7*6*5*4*3*2*1} = 4,272,048$$

In 10–14, find how many solutions there are to the given equation that satisfy the given condition.

12. $y_1 + y_2 + y_3 + y_4 = 30$, each y_i is a nonnegative integer.

12.)
$$\binom{10+4-1}{10} = \binom{13}{10} = \frac{13!}{10!3!} = \frac{13*12*11}{3*2*1} = 286$$

- A large pile of coins consists of pennies, nickels, dimes, and quarters.
 - a. How many different collections of 30 coins can be chosen if there are at least 30 of each kind of coin?
 - b. If the pile contains only 15 quarters but at least 30 of each other kind of coin, how many collections of 30 coins can be chosen?
 - c. If the pile contains only 20 dimes but at least 30 of each other kind of coin, how many collections of 30 coins can be chosen?
 - d. If the pile contains only 15 quarters and only 20 dimes but at least 30 of each other kind of coin, how many collections of 30 coins can be chosen?

18.a.)
$$\binom{30+4-1}{30} = \binom{33}{30} = \frac{33!}{30!3!} = \frac{33*32*31}{3*2*1} = 5,456$$

18.b.) $\binom{33}{30} - \binom{15+4-1}{15} = 5456 - \frac{18!}{15!3!} = 5456 - \frac{18*17*16}{3*2*1} = 5456 - 816 = 4640$
18.c.) $\binom{33}{30} - \binom{10+4-1}{10} = 5456 - \frac{13!}{10!3!} = 5456 - \frac{13*12*11}{3*2*1} = 5456 - 286 = 5170$
18.d.) $5456 - 816 - 286 = 4354$