#### Lecture 7: Model Evaluation I

## COMP90049 Introduction to Machine Learning

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# Roadmap

#### So far

- Instance-based classification with KNN
- Probabilities and probabilistic modeling
- Optimization and MLE
- Probabilistic classification with Naive Bayes

#### Today... Evaluation

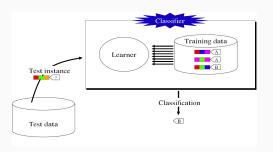
- How do we know that we succeeded in learning?
- Evaluation paradigms
- Evaluation methods



# Classification Evaluation

## The Nature of "Classification"

- Input: set of labelled training instances; set of unlabelled test instances
- Model: an estimate of the underlying target function
- Output: prediction of the classes of the test instances





#### **Goal 1: Model Evaluation**

#### Our goal (in a supervised Machine Learning framework):

- Have a perfect model?
  - Not necessarily clear what that means
  - More difficult than necessary
- · Make predictions that are correct!
- Train and test machine learning models based on the limited data available
- Estimate the *true* performance on any data based on the errors made on the limited labelled data available

## **Goal 2: Model Selection**

# Choosing the best model from a number of possibilities

- Different machine learning algorithms
- Different parameterizations for the same algorithm
- Different training parameters
- Other considerations: Efficiency, explainability, fairness, ...



# **Evaluation Strategies**

# **Evaluating Classification I**

#### Main idea:

- Train (build model) using training data
- Test (evaluate model) on test data

But often, we just have data — a collection of instances



# **Evaluating Classification II**

#### An obvious strategy, which is highly **not recommended**:

- Use all of the instances as training data
  - Build the model using all of the instances
- Use all of the (same) instances as test data
  - Evaluate the model using all of the instances

"Testing on the training data" tends to grossly over-estimate classifier performance.

Effectively, we are telling the classifier what the correct answers are, and then asking whether it can come up with the correct answers.



#### **Holdout**

One solution: Holdout evaluation strategy

- Each instance is randomly assigned as either a training instance or a testing instance
- Effectively, the data is **partitioned** no overlap between datasets
- Evaluation strategy:
  - Build the model using (only) the training instances
  - Evaluate the model using (only) the (different) test instances

Very commonly used strategy; typical split sizes are approximately 50–50, 80–20, 90–10 (train, test)

Source(s): Tan et al. [2006, pp 186-7]



#### **Holdout**

## **Advantages**

- simple to work with and implement
- · fairly high reproducability

#### **Disadvantages**

- · size of the split affects estimate of the model's behaviour:
  - lots of test instances, few training instances: learner doesn't have enough information to build an accurate model
  - lots of training instances, few test instances: learner builds an accurate model, but test data might not be representative (so estimates of performance can be too high/too low)



# Repeated Random Subsampling

# Slower, but somewhat better solution: Repeated Random Subsampling

- Like Holdout, but iterated multiple times:
  - A new training set and test set are randomly chosen each time
  - Relative size of training-test is fixed across iterations
  - New model is built each iteration
- Evaluate by averaging (chosen metric) across the iterations



# **Repeated Random Subsampling**

### Advantages:

averaging Holdout method tends to produce more reliable results

#### Disadvantages:

- more difficult to reproduce
- slower than Holdout (by a constant factor)
- wrong choice of training set-test set size can still lead to highly misleading results (that are now very difficult to sanity-check)

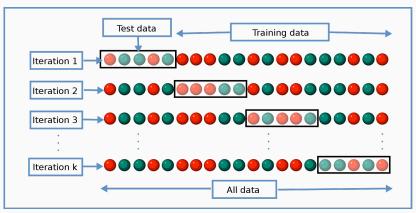


## Usually preferred alternative: Cross-Validation

- Data is progressively split into a number of partitions m (≥ 2)
- Iteratively:
  - One partition is used as test data
  - The other m-1 partitions are used as training data
- Evaluation metric is aggregated across m test partitions
  - This could mean averaging, but more often, counts are added together across iterations



#### Usually preferred alternative: Cross-Validation



https://en.wikipedia.org/wiki/Cross-validation\_(statistics)#/media/File:K-fold\_cross\_validation\_EN.svg



Why is this better than Holdout/Repeated Random Subsampling?

- Every instance is a test instance, for some partition
  - Similar to testing on the training data, but without dataset overlap
  - Evaluation metrics are calculated with respect to a dataset that looks like the entire dataset (i.e. the entire dataset)
- Takes roughly the same amount of time as Repeated Random Subsampling (but see below)
- Very reproducible
- Can be shown to minimise bias and variance of our estimates of the classifier's performance (more on this in Evaluation II)



#### How big is *m*?

- Number of folds directly impacts runtime and size of datasets:
  - Fewer folds: more instances per partition, more variance in performance estimates
  - More folds: fewer instances per partition, less variance but slower
- Most common choice of m: 10 (occasionally, 5)
  - Mimics 90-10 Holdout, but far more reliable
- Best choice: m=N, the number of instances (known as Leave–One–Out Cross–Validation):
  - · Maximises training data for the model
  - Mimics actual testing behaviour (every test instance is treated as an individual test "set")
  - · Way too slow to use in practice



#### **Inductive Biases and No Free Lunch**

A learner that makes no a priori assumptions regarding the identity of the target concept has no rational basis for classifying any unseen instances"

[Mitchell, 1997, Ch. 2.7.3]

#### The No Free Lunch Theorem (Wolpert and Macready, 1997)

- Intuition: You don't get something for nothing. You won't get a good classifier (or any ML algorithm) without making assumptions.
- Averaged across all possible problems, the performance of any two algorithms is identical.
- $\rightarrow$  If algorithm A does well on p1 it necessarily performs worse on some p2
  - Averaged across all classification problems, the generalization error on a held-out test set of any two classifiers is identical. There is no universally superior classifier.



#### **Inductive Biases and No Free Lunch**

A learner that makes no a priori assumptions regarding the identity of the target concept has no rational basis for classifying any unseen instances"

[Mitchell, 1997, Ch. 2.7.3]

- Inductive Learning Hypothesis: Any hypothesis found to approximate
  the target function well over (a sufficiently large) training data set will
  also approximate the target function well over unseen test examples.
- Assumptions must be made about the data to build a model and make predictions (inductive biases)
  - → Different assumptions will lead to different predictions



#### Stratification

- Typical inductive bias in our evaluation framework (n.b. independent of model): Stratification
  - → Assume that class distribution of unseen instances will be the same as distribution of seen instances
- When constructing Holdout/Cross–Validation partitions, ensure that training data and test data **both** have same class distribution as dataset as a whole





**Evaluation Measures** 

#### Error E

The fraction of incorrect predictions.

$$E = \frac{1}{N}(1 - I(y_i, \hat{y}_i)), where \quad I(a, b) \begin{cases} 1, & \text{if } a == b \\ 0, & \text{otherwise} \end{cases}$$

Error rate reduction: ERR =  $\frac{E_0 - E}{E_0}$ 



### Error E

The fraction of incorrect predictions.

$$E = \frac{1}{N}(1 - I(y_i, \hat{y}_i)), where \quad I(a, b) \begin{cases} 1, & \text{if } a == b \\ 0, & \text{otherwise} \end{cases}$$

Error rate reduction:  $\text{ERR} = \frac{E_0 - E}{E_0}$ 

Outlook	Temperature	Humidity	Windy	Actual	Classified
overcast	cool	normal	TRUE	yes	
sunny	mild	high	FALSE	no	
sunny	cool	normal	FALSE	yes	
rainy	mild	normal	FALSE	yes	
sunny	mild	normal	TRUE	yes	no
overcast	mild	high	TRUE	yes	no
overcast	hot	normal	FALSE	yes	yes
rainy	mild	high	TRUE	no	yes



# **Two Types of Errors**

#### **Contingency Tables**

$\downarrow y,  \hat{y} \rightarrow$	1	0
1	true positive (TP)	false negative (FN)
0	false positive (FP)	true negative (TN)

## Not all Errors are equal

- Some problems want to strongly penalize false negative errors e.g.,
- Other problems want to strongly penalize false positive errors,
- Attach a "cost" to each type of error



# **Accuracy**

$\downarrow y, \hat{y} \rightarrow$	1	0
1	true positive (TP)	false negative (FN)
0	false positive (FP)	true negative (TN)

Accuracy: The basic evaluation metric

$$Accuracy = \frac{Number of correctly labelled test instances}{Total number of test instances} = \frac{TP + TN}{TP + FP + TN + FN}$$

- Same as 1 − E
- Quantifies how frequently the classifier is correct



# **Accuracy**

Outlook	Temperature	Humidity	Windy	Actual	Classified
sunny	hot	high	FALSE	no	
sunny	hot	high	TRUE	no	
overcast	hot	high	FALSE	yes	
rainy	mild	high	FALSE	yes	
rainy	cool	normal	FALSE	yes	
rainy	cool	normal	TRUE	no	
overcast	cool	normal	TRUE	yes	
sunny	mild	high	FALSE	no	
sunny	cool	normal	FALSE	yes	
rainy	mild	normal	FALSE	yes	
sunny	mild	normal	TRUE	yes	no
overcast	mild	high	TRUE	yes	yes
overcast	hot	normal	FALSE	yes	yes
rainy	mild	high	TRUE	no	yes



# **Accuracy**

4 test instances; 2 correct predictions, 2 incorrect predictions

Accuracy = 
$$\frac{\text{Number of correctly labelled test instances}}{\text{Total number of test instances}}$$
  
=  $\frac{2}{4} = 50\%$ 



#### **Precision and Recall**

$\downarrow y, \hat{y} \rightarrow$	1 (interesting)	0 (uninteresting)
1 (interesting)	true positive (TP)	false negative (FN)
0 (uninteresting)	false positive (FP)	true negative (TN)

## With respect to just the interesting class:

 Precision: How often are we correct, when we predict that an instance is interesting?

$$Precision = \frac{TP}{TP + FP}$$

 Recall: What proportion of the truly interesting instances have we correctly identified as interesting?

$$\textbf{Recall} = \frac{\textit{TP}}{\textit{TP} + \textit{FN}}$$



#### **Precision and Recall**

Precision/Recall are typically in an **inverse relationship**. We can generally set up our classifier, so that:

- The classifier has high Precision, but low Recall
- The classifier has high Recall, but low Precision

But, we want **both** Precision and Recall to be high. A popular metric that evaluates this is **F-score**:

$$F_{\beta} = \frac{(1+\beta^2)PR}{\beta^2P + R}$$

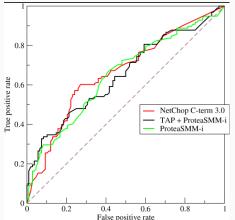
$$F_{1} = \frac{2PR}{P + R}$$



# Capturing trade-offs between different objectives

## Receiver Operating characteristics (ROC-curve)

- Goal: Maximize the area under the ROC curve: (a) minimize the false alarms and maximize the true alarms
- History: trade off between false alarms and true alarms in signal processing





X-axis: percentage of false positives
 Y-axis: percentage of true positives

# Many other Metrics!

		Predicted co	ndition		
	Total population	Predicted Condition positive	Predicted Condition negative	Prevalence = $\frac{\Sigma \text{ Condition positive}}{\Sigma \text{ Total population}}$	
True condition	condition positive	True positive	False Negative (Type II error)	True positive rate (TPR), Sensitivity, $Recall = \frac{\Sigma \text{ True positive}}{\Sigma \text{ Condition positive}}$	False negative rate (FNR), Miss rate $= \frac{\Sigma \text{ False negative}}{\Sigma \text{ Condition positive}}$
	condition negative	False Positive (Type I error)	True negative	False positive rate (FPR), Fall-out $= \frac{\Sigma \text{ False positive}}{\Sigma \text{ Condition negative}}$	True negative rate (TNR), Specificity (SPC) = $\frac{\Sigma}{\Sigma}$ True negative $\frac{\Sigma}{\Sigma}$ Condition negative
	Accuracy (ACC) =	$\begin{aligned} & \text{Positive predictive value (PPV), Precision} \\ & = \frac{\Sigma \text{ True positive}}{\Sigma \text{ Test outcome positive}} \end{aligned}$	False omission rate (FOR) $= \frac{\Sigma \text{ False negative}}{\Sigma \text{ Test outcome negative}}$	Positive likelihood ratio (LR+) = $\frac{TPR}{FPR}$	Diagnostic odds ratio (DOR) = $\frac{LR+}{IR-}$
	$\frac{\Sigma \text{ True positive} + \Sigma \text{ True negative}}{\Sigma \text{ Total population}}$	False discovery rate (FDR) $= \frac{\Sigma \text{ False positive}}{\Sigma T}$	Negative predictive value (NPV) $= \frac{\Sigma \text{ True negative}}{\Sigma True \text{ negative}}$	Negative likelihood ratio (LR-) = $\frac{FNR}{TNR}$	Diagnostic odds ratio (DOA) = LR-

#### From Wikipedia:

https://en.wikipedia.org/wiki/Sensitivity\_and\_specificity



For a multi-class problem, assume an **Interesting** class (I) and several **Uninteresting** classes (U1, U2, ...).

			Predict	ed	
		1	U1	U2	
	1	TP	FN	FN	
Actual	U1	FP	TN	TN	
	U2	FP	TN	TN	

A multi-class Confusion Matrix.

Typically, all classes are "interesting" in a multi-class context.



- The natural definition of Accuracy still makes sense in a multi-class context,
- The technical definition behaves strangely: re-interprets the multi-class problem as a special case of a two-class problem, namely One-vs-Rest
- Precision/Recall/F-Score are all calculated per-class, and must be averaged:
- macro-averaging: calculate P, R per class and then average

$$\begin{aligned} & \operatorname{Precision}_{M} & = & \frac{\sum_{i=1}^{c} \operatorname{Precision}_{i}}{c} \\ & \operatorname{Recall}_{M} & = & \frac{\sum_{i=1}^{c} \operatorname{Recall}_{i}}{c} \end{aligned}$$



- The natural definition of Accuracy still makes sense in a multi-class context,
- The technical definition behaves strangely: re-interprets the multi-class problem as a special case of a two-class problem, namely One-vs-Rest
- Precision/Recall/F-Score are all calculated per-class, and must be averaged:
- micro-averaging: combine all test instances into a single pool

$$\begin{aligned} & \text{Precision}_{\mu} & = & \frac{\sum_{i=1}^{c} TP_{i}}{\sum_{i=1}^{c} TP_{i} + FP_{i}} \\ & \text{Recall}_{\mu} & = & \frac{\sum_{i=1}^{c} TP_{i}}{\sum_{i=1}^{c} TP_{i} + FN_{i}} \end{aligned}$$



- The natural definition of Accuracy still makes sense in a multi-class context,
- The technical definition behaves strangely: re-interprets the multi-class problem as a special case of a two-class problem, namely One-vs-Rest
- Precision/Recall/F-Score are all calculated per-class, and must be averaged:
- weighted averaging: calculate P, R per class and then average, based on the proportion of instances in that class

Precision<sub>W</sub> = 
$$\sum_{i=1}^{c} \operatorname{Precision}_{i} \times (\frac{n_{i}}{N})$$
  
Recall<sub>W</sub> =  $\sum_{i=1}^{c} \operatorname{Recall}_{i} \times (\frac{n_{i}}{N})$ 



# How to average your predictions?

- Macro average treats all classes equal: emphasizes small classes.
   Micro average is dominated by large classes.
- Macro-averaged F-score: is it the F-score of macro-averaged P (over classes) and macro-averaged R (over classes)? Or the macro-average (over classes) of the F-score for each class?
- If we are doing Repeated Random Subsampling, and want weighted-averaged Precision, do we average the weighted Precision (over classes) for each iteration of Random Subsampling? or do we take the weighted average (over classes) of the Precision averaged over the iterations of Subsampling? Or the weighted average over the instances aggregated over the iterations?

**Model comparison** 

### Baselines vs. Benchmarks

- **Baseline** = naive method which we would expect any reasonably well-developed method to better
  - e.g. for a novice marathon runner, the time to walk 42km
- Benchmark = established rival technique which we are pitching our method against
  - e.g. for a marathon runner, the time of our last marathon run/the world record time/3 hours/...
- "Baseline" often used as umbrella term for both meanings



# The Importance of Baselines

 Baselines are important in establishing whether any proposed method is doing better than "dumb and simple"

"dumb" methods often work surprisingly well

- Baselines are valuable in getting a sense for the intrinsic difficulty of a given task (cf. accuracy = 5% vs. 99%)
- In formulating a baseline, we need to be sensitive to the importance of positives and negatives in the classification task

limited utility of a baseline of unsuitable for a classification task aimed at detecting potential sites for new diamond mines (as nearly all sites are unsuitable)



### **Random Baseline**

Method 1: randomly assign a class to each test instance

• Often the only option in unsupervised/semi-supervised contexts

**Method 2:** randomly assign a class to each test instance, weighting the class assignment according to  $P(C_k)$ 

- · Assumes we know the prior probabilities
- · Alleviate effects of variance by:
  - running method N times and calculating the mean accuracy OR
  - arriving at a deterministic estimate of the accuracy of random assignment = ∑<sub>i</sub> P(C<sub>i</sub>)<sup>2</sup>



# Zero-R (Zero rules)

# Also known as majority class baseline

- Method: classify all instances according to the most common class in the training data
- The most commonly used baseline in machine learning
- Inappropriate if the majority class is FALSE and the learning task is to identify needles in the haystack

Outlook	Temperature	Humidity	Windy	y (Play)	ŷ
sunny	hot	high	FALSE	no	
sunny	hot	high	TRUE	no	
overcast	hot	high	FALSE	yes	
rainy	mild	high	FALSE	yes	
rainy	cool	normal	FALSE	yes	
rainy	cool	normal	TRUE	no	
overcast	cool	normal	TRUE	yes	
sunny	mild	high	FALSE	no	?



# One-R (One Rule)

#### Introduction

- Select one attribute and use it to predict an instance's class
- Test each attribute, and select the one with the smallest error rate
- Each attribute-specific test is often called "Decision stump" (more on that in the Trees lecture)

#### Intuition

 If there is a single, simple feature with which we can classify most of our features correctly – do we really need a sophisticated machine learner?



# One-R pseudo-code

For each attribute

For each value of the attribute, make a rule:

- (i) count how often each class appears
- (ii) find the most frequent class
- (iii) make the rule assign that class to this value

Calculate the error rate of the rule

Choose the rules with the smallest error rate

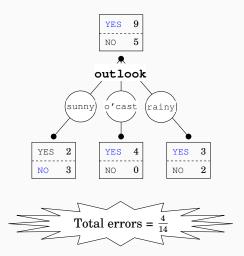


# Weather dataset

Outlook	Temperature	Humidity	Windy	Play
sunny	hot	high	FALSE	no
sunny	hot	high	TRUE	no
overcast	hot	high	FALSE	yes
rainy	mild	high	FALSE	yes
rainy	cool	normal	FALSE	yes
rainy	cool	normal	TRUE	no
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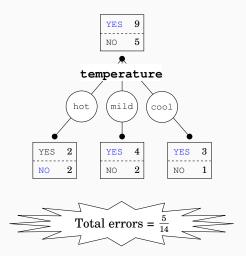


# Attribute Option 1 (outlook)



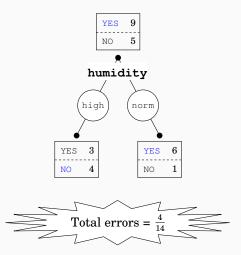


# Attribute Option 2 (temperature)



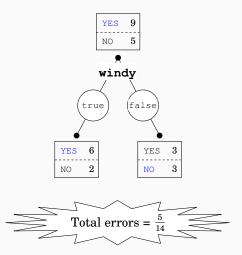


# Attribute Option 3 (humidity)





# Attribute Option 4 (windy)





### **One-R: Reflections**

# Advantages:

- simple to understand and implement
- · simple to comprehend the results
- · surprisingly good results

# Disadvantages:

- unable to capture attribute interactions
- bias towards high-arity attributes (attributes with many possible values)



# Summary

# **Today**

- How do we set up an evaluation of a classification system?
- What are the measures we use to assess the performance of the classification system?
- What is a baseline? What are some examples of reasonable baselines to compare with?

#### **Next lecture**

Feature Selection



#### References

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