

Passive SSH Key Compromise via Lattices

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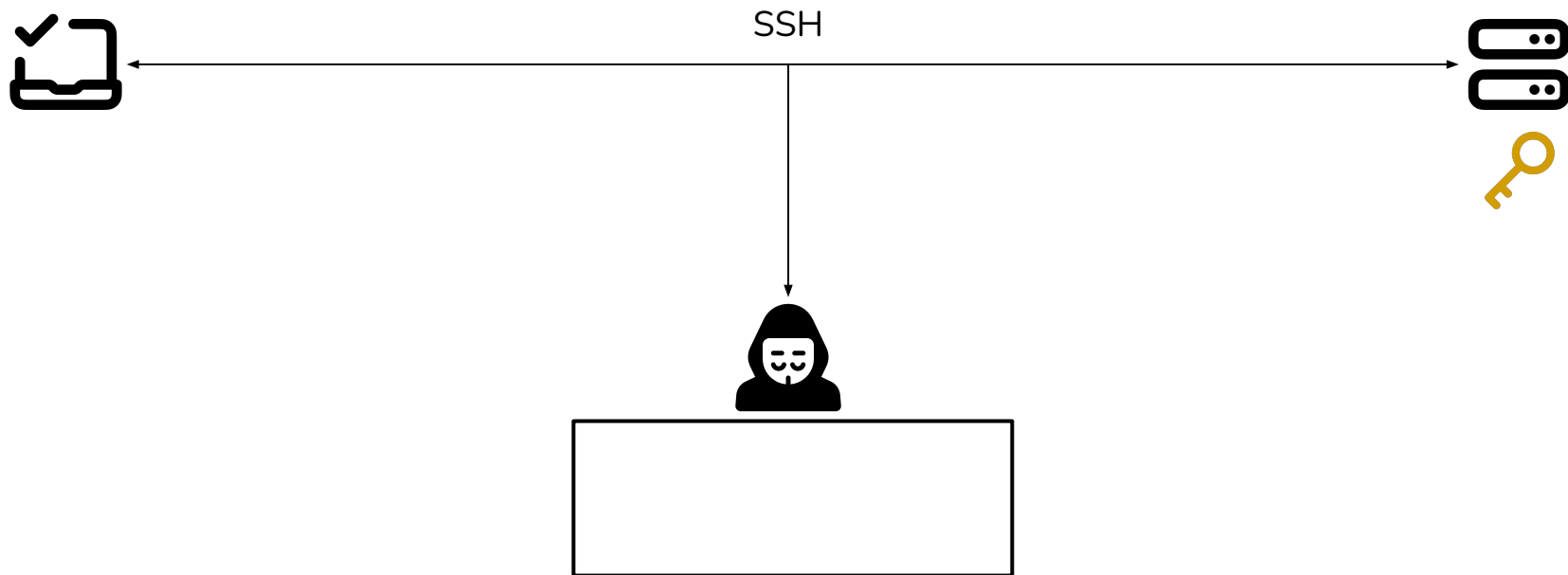
ACM CCS, November 2023

Overview

1. Can faulty RSA signatures reveal the private SSH host key to eavesdroppers?

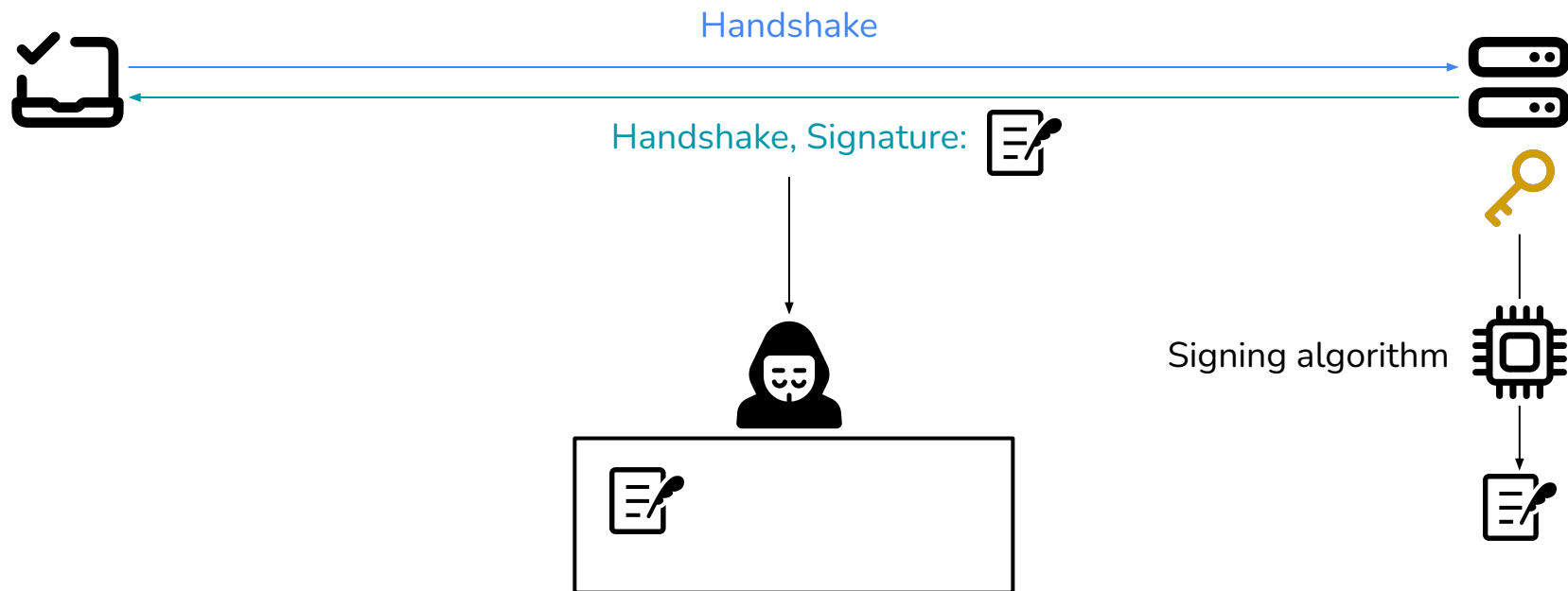
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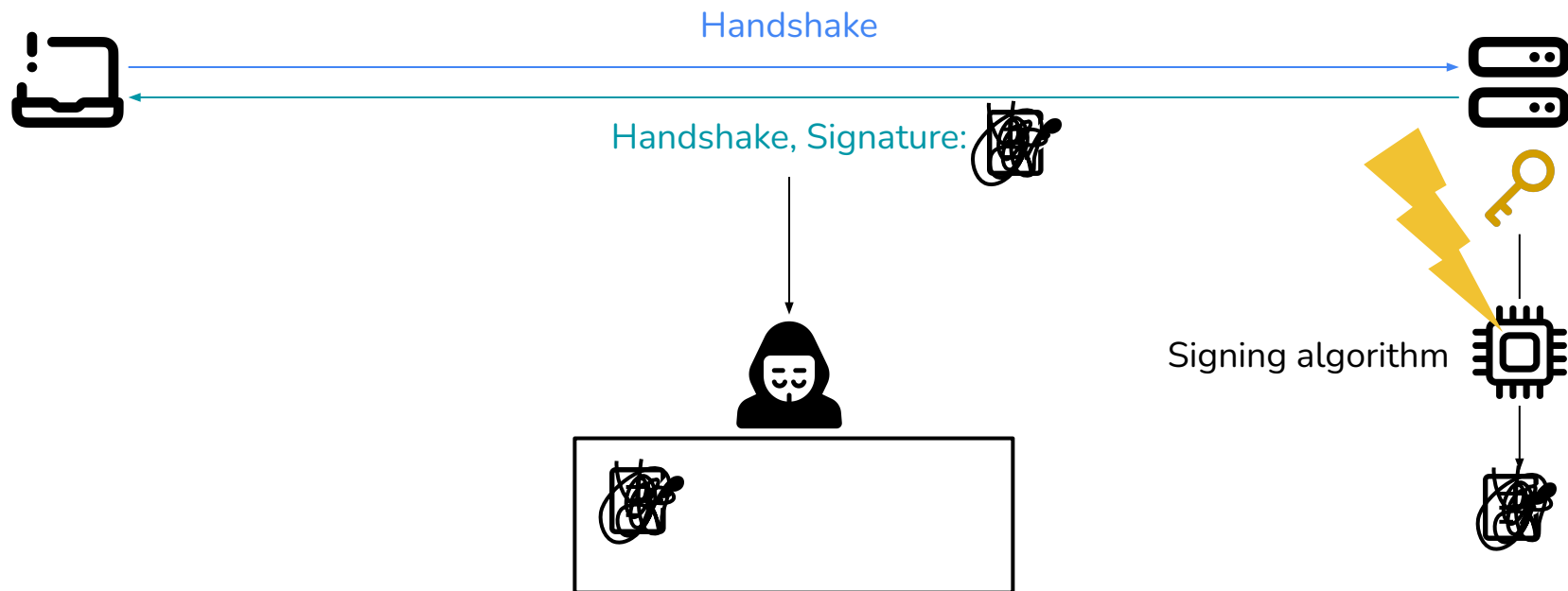
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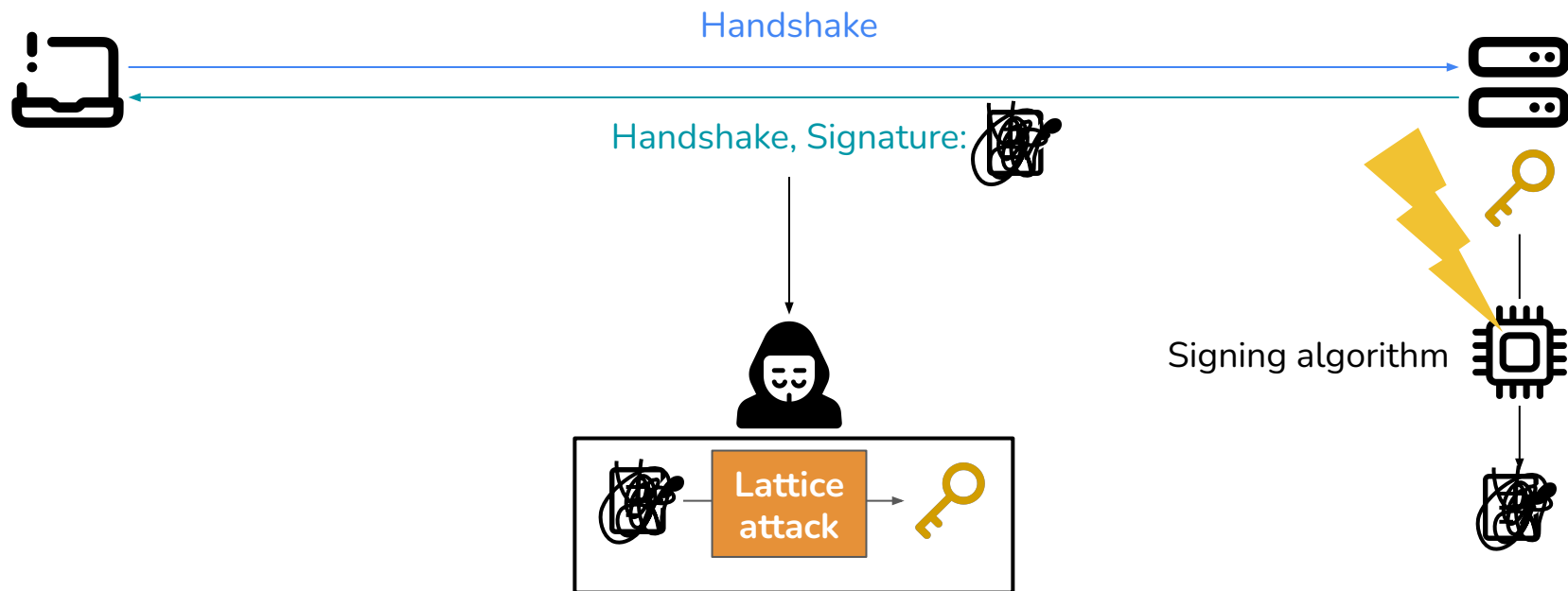
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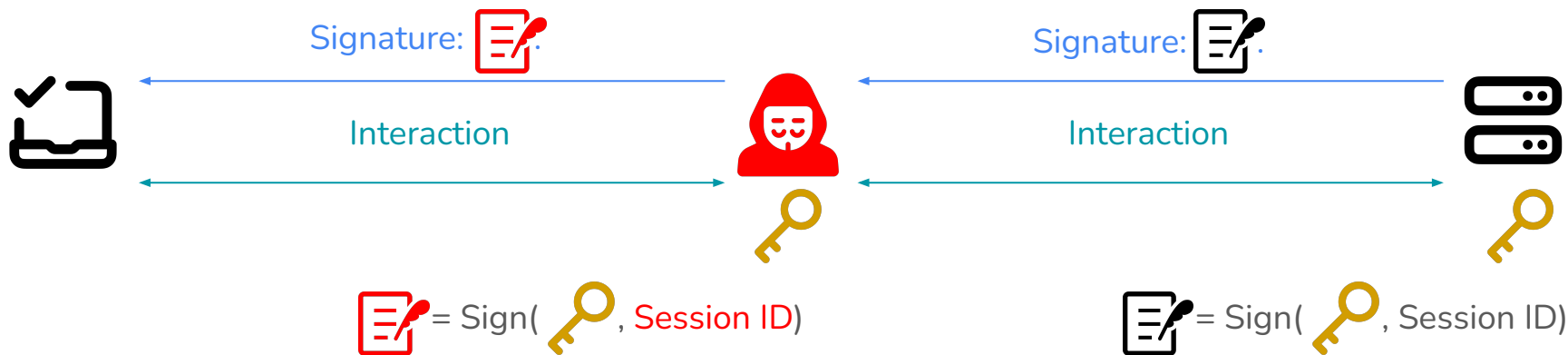
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Implications of host key compromise

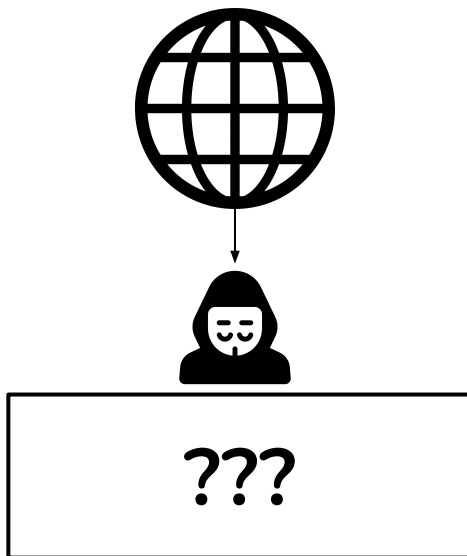
Active attacker with the key can impersonate the server

- Can then intercept and arbitrarily tamper with connection



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1. Can faulty RSA signatures reveal the private SSH host key to eavesdroppers?
2. Are such keys leaked frequently over the internet?



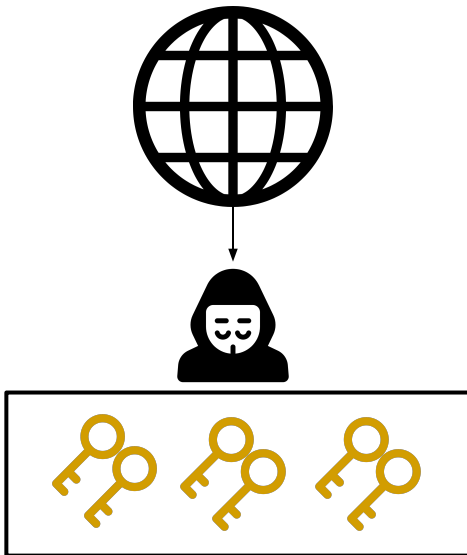
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2. Are such keys leaked frequently over the internet?

We analyzed **3.2 billion** SSH signatures on the internet

(1.2 billion *RSA signatures*)

4,962 signatures:
Revealed **private keys**



History of signature fault attacks

1996-97

[Len96], [BDL97]: Error in RSA signature can reveal private key

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Practical signature fault attack on **TLS** in **active setting**

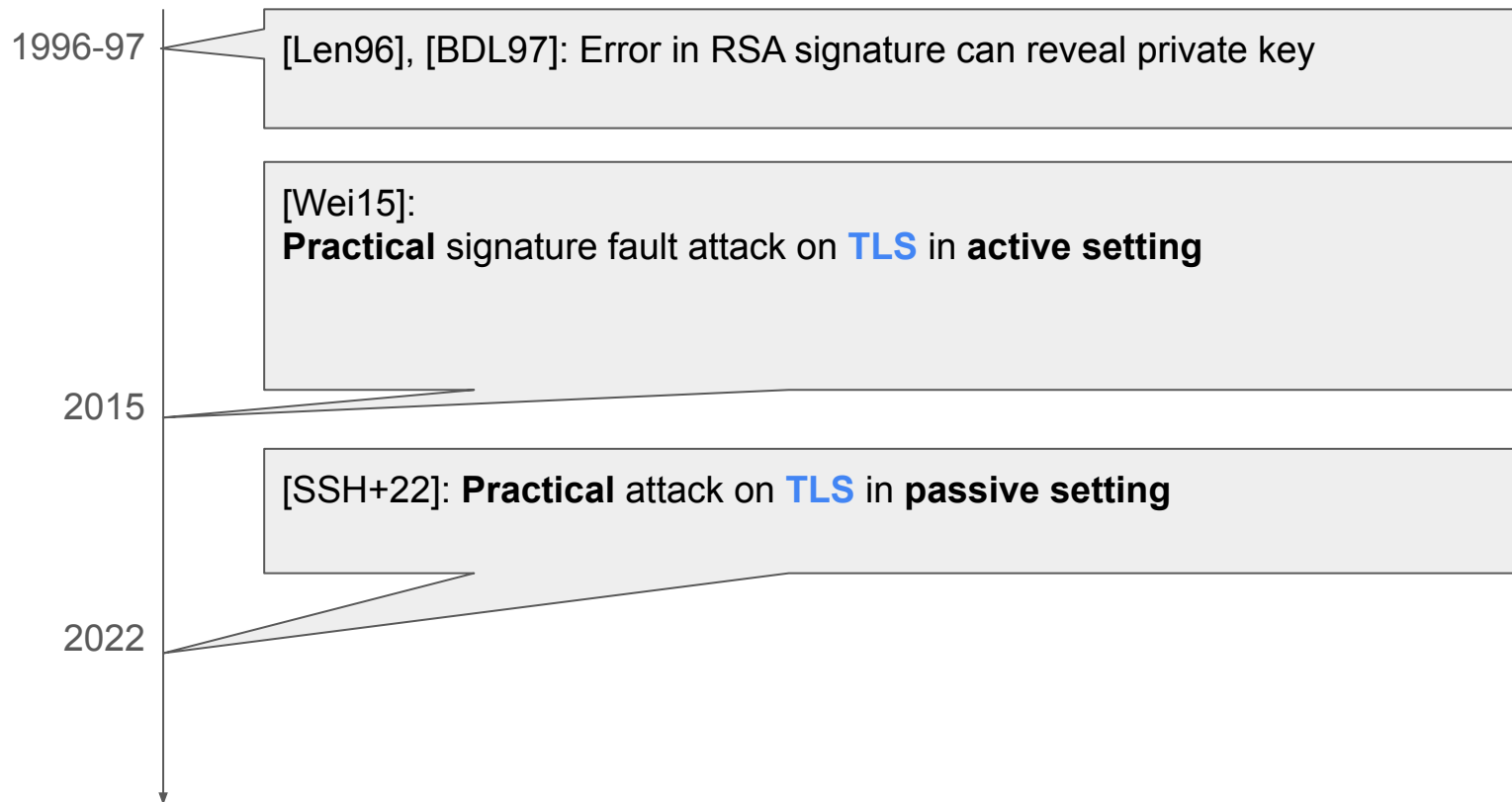
Believed **SSH** is not exploitable in **passive setting**

2015

[SSH+22]: **Practical** attack on **TLS** in **passive setting**

2022

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(only if signed message is **fully known**)

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Message hash includes **DH shared secret** → unknown to eavesdropper

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Message fully computable by eavesdropper

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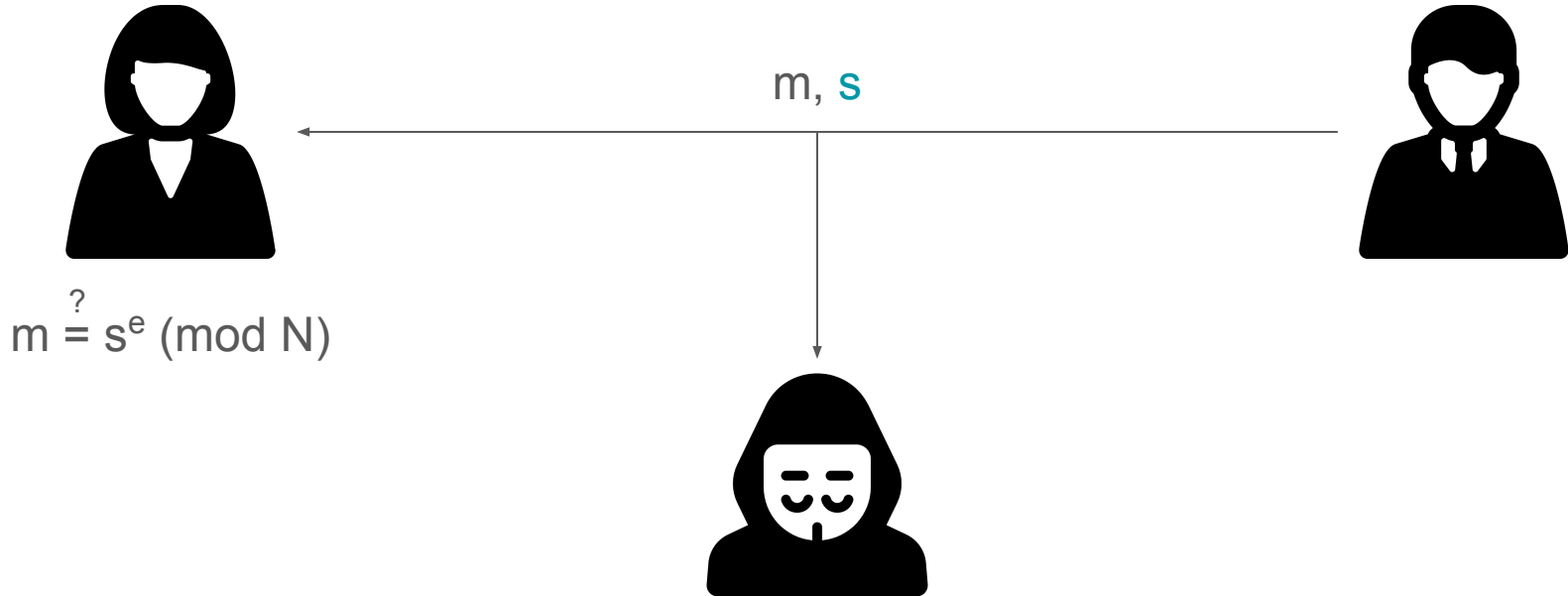
Textbook RSA signing

Public key = (N, e)

Private key = (p, q, d)

$N = pq, d = e^{-1} \pmod{\phi(N)}$

$s = m^d \pmod{N}$



Textbook RSA signing with CRT optimization

Private key = (p, q, d_p, d_q)

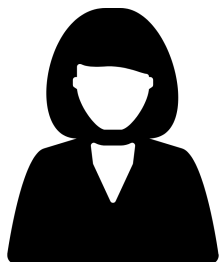
$N = pq, d = e^{-1} \pmod{\phi(N)}$

Public key = (N, e)

$$s_p = m^{d_p} \pmod{p}$$

$$s_q = m^{d_q} \pmod{q}$$

m, s



$$m \stackrel{?}{=} s^e \pmod{N}$$



RSA-CRT signing, with a **fault**

Private key = (p, q, d_p, d_q)

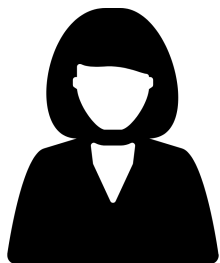
$N = pq, d = e^{-1} \pmod{\phi(N)}$

Public key = (N, e)

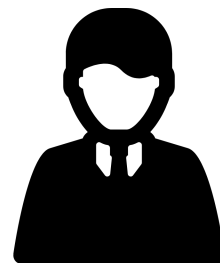
$$s_p = m^{d_p} \pmod{p}$$

$$s_q \neq m^{d_q} \pmod{q}$$

m, s'



$$m \stackrel{?}{=} s^e \pmod{N}$$

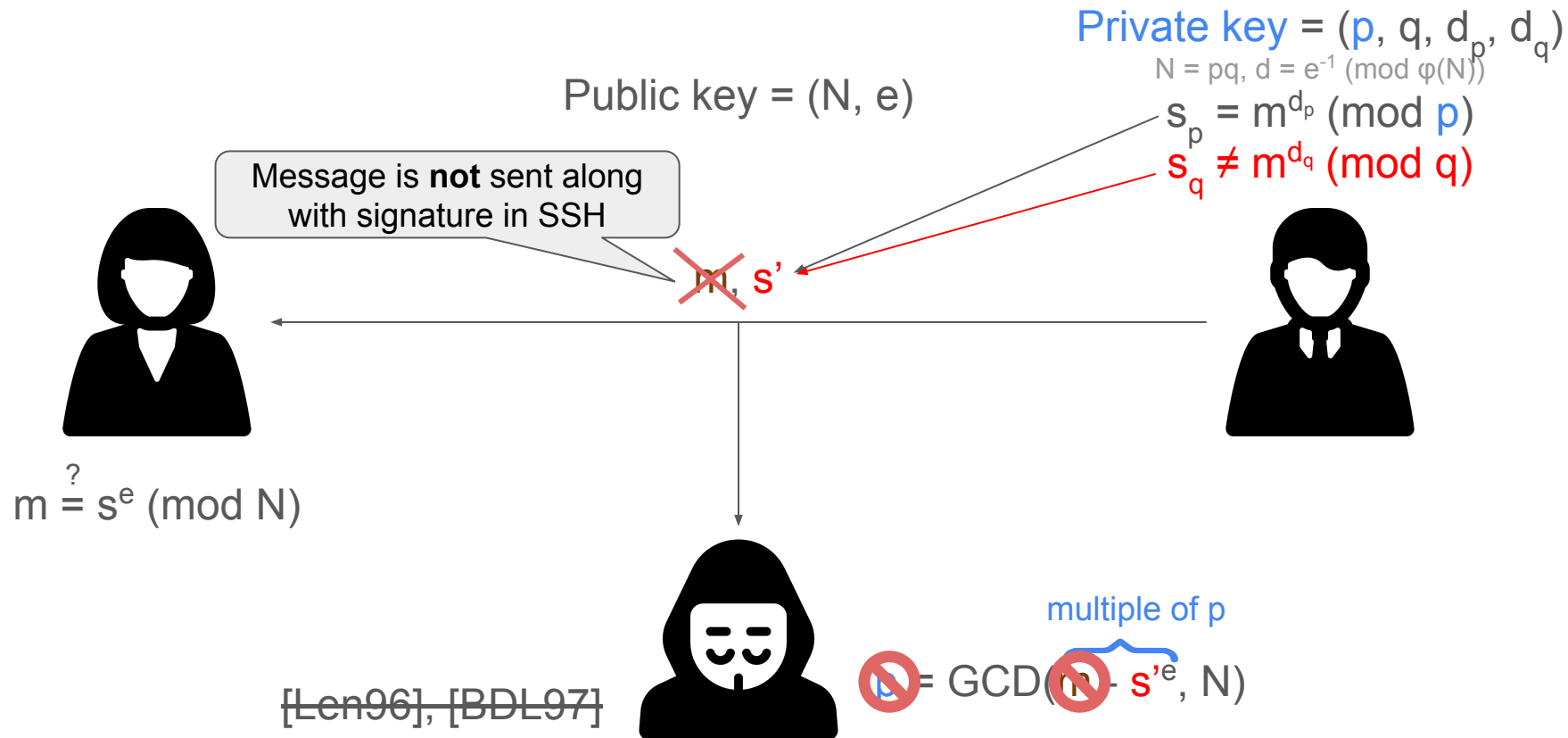


[Len96], [BDL97]

multiple of p

$$p = \text{GCD}(\overbrace{m - s'^e}^{\text{multiple of } p}, N)$$

RSA-CRT **fault** in SSH



PKCS#1 v1.5 RSA signature padding

Message format for SSH:

$m = 0x0001FF \dots FF00 \{ \text{hash algorithm} \} \{ \text{hash} \}$

- **Padding** is deterministic and known to the attacker
- Attacker knows almost all of message m , except for the **hash**

RSA-CRT **fault** in SSH, passive attack

Public key = (N, e)

Private key = (p, q, d_p, d_q)

$N = pq, d = e^{-1} \pmod{\phi(N)}$

$s_p = m^{d_p} \pmod{p}$

$s_q \neq m^{d_q} \pmod{q}$

s'

Message format for SSH: (PKCS#1 v1.5)

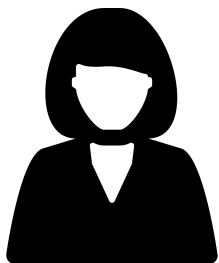
$m = 0x0001FF...FF00 \{algorithm\} \{hash\}$

known small unknown

Knows that $m = \widehat{a} + \widehat{r}$

$p = \text{Approx-GCD}(\widehat{a} - s'^e, N)$

[CJK+09]



Lattice attack

Message format for SSH: (PKCS#1 v1.5)
 $m = 0x0001FF \dots FF00 \{\text{hash algorithm}\} \{\text{hash}\} < N$

Experimented with attacking faulty SSH signatures:

- Generated instances that correspond to SSH parameter choices
 - e.g., RSA-2048, SHA-256

For all common parameter choices (RSA modulus length $> 4 \times$ hash length):

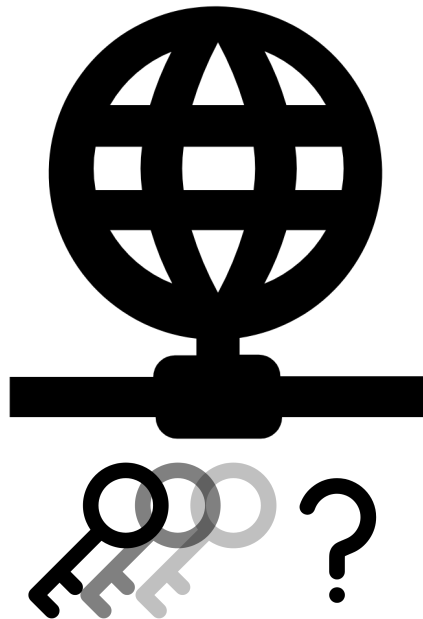
- Attack averages under 0.2 seconds per signature
- Recovers correct key for every generated signature

Key leakage in the wild

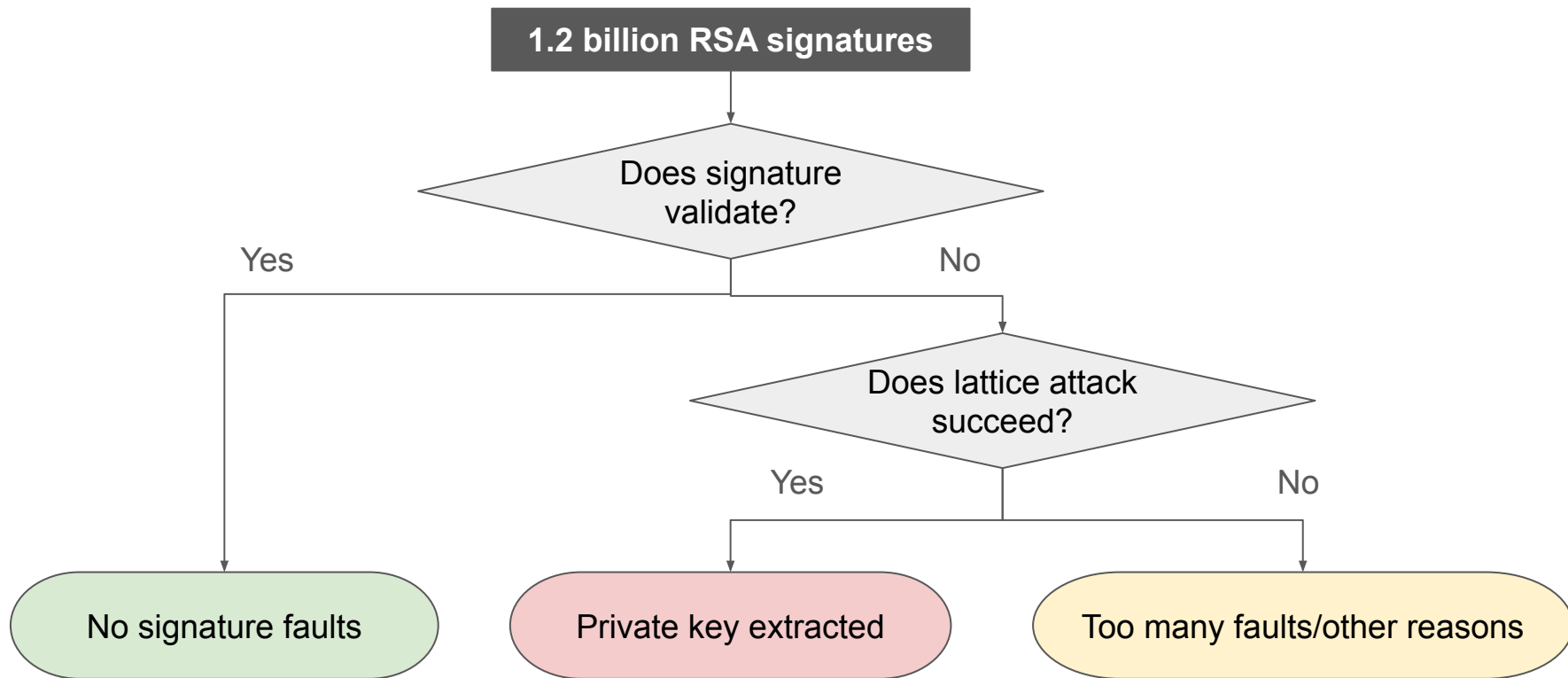
How frequently do keys leak on the internet?

We analyzed data from:

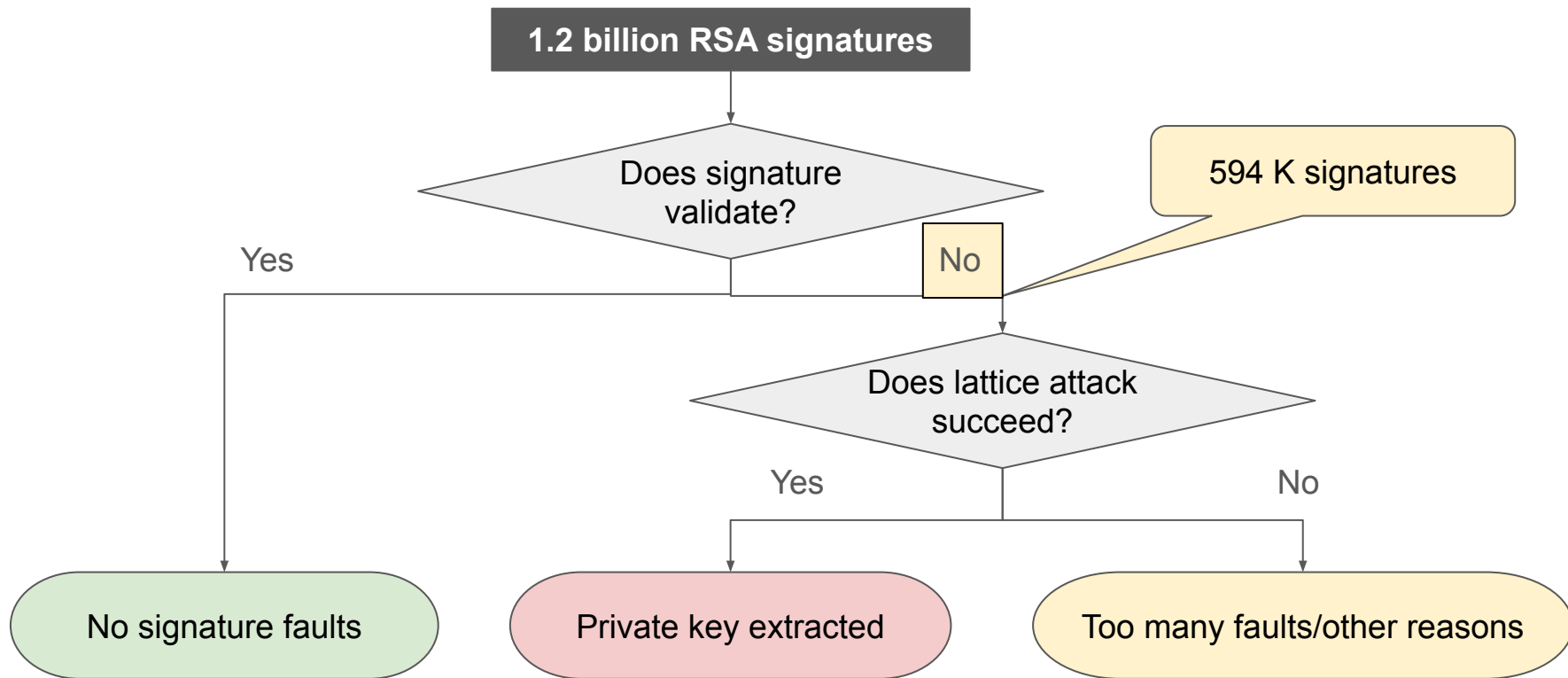
- Zmap scans performed at UCSD
- Passive network traffic through UCSD
- Censys
- University of Michigan



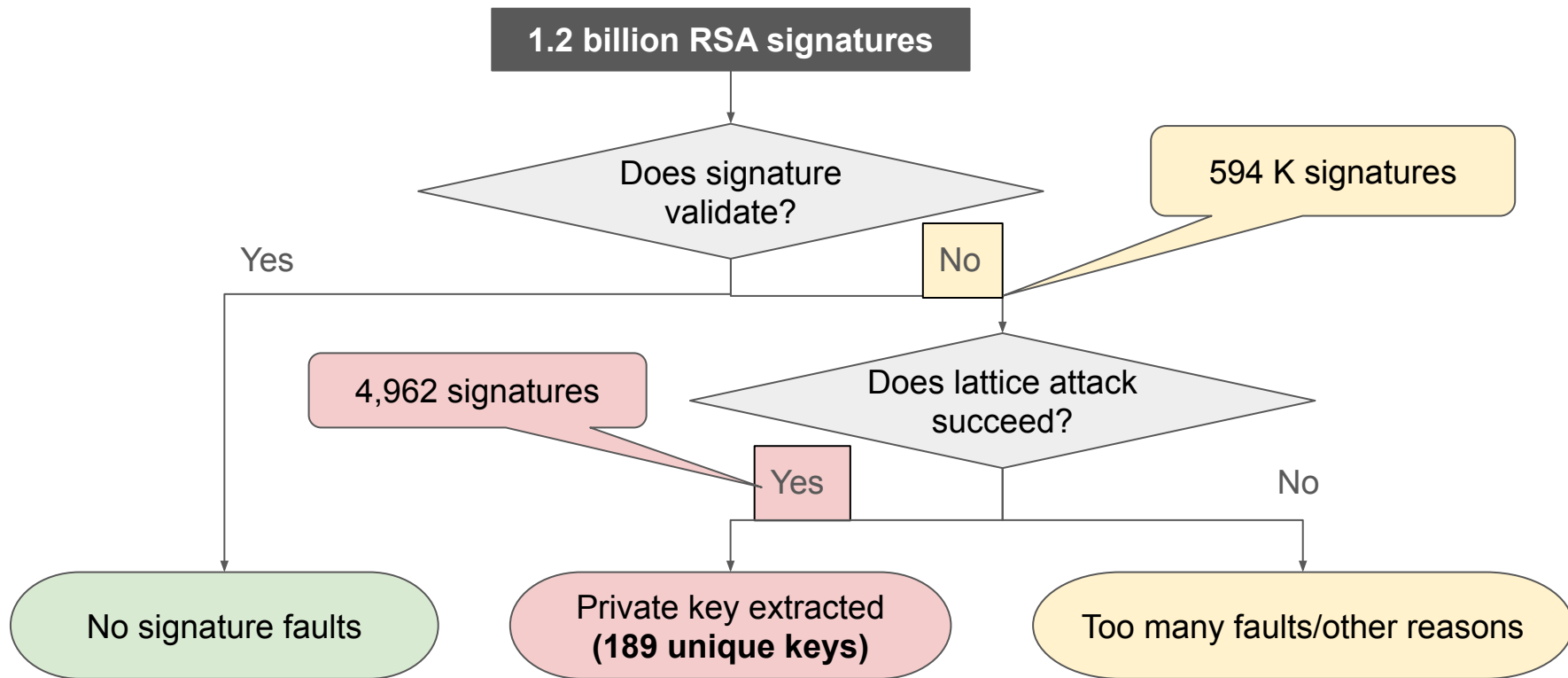
Analysis



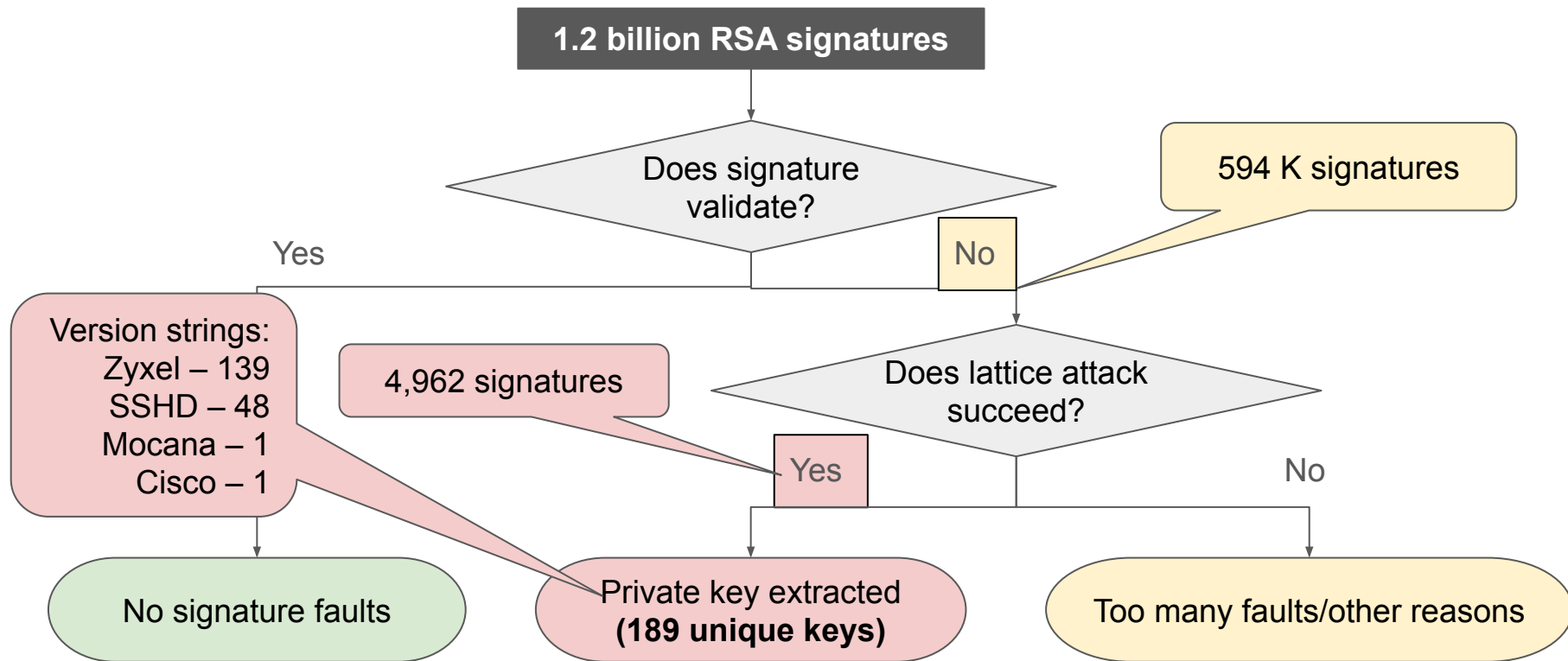
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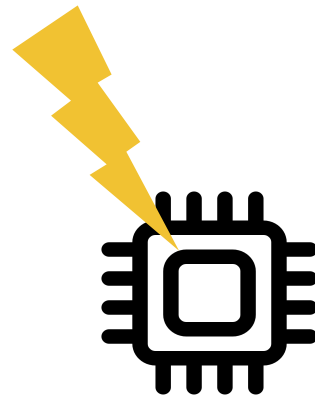
Lessons

Hypothesis: signature faults originate from hardware failures

Include random hardware faults in the threat model

Countermeasure: Validate signatures before sending

- OpenSSL and derivatives include this check
- Vulnerable implementations we observed do not have this countermeasure



Future directions

- SSH: Collect `rsa-sha2-*` signatures
 - Potentially more vulnerable hosts are out there
- Collect more data passively
- Study similar key leaks on IPsec
 - Our visibility into IPsec hosts is limited

Summary

A single faulty signature reveals the private SSH host key to eavesdroppers

- Private host key allows attacker to later impersonate server
- About 1 out of 1 million analyzed signatures on the internet are vulnerable

We disclosed the vulnerability to device vendors:

- Mitigations confirmed for Cisco, Zyxel, and Hillstone Networks
- Unable to contact Mocana

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<https://ia.cr/2023/1711>

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ACM CCS, November 2023



References

- [BDL97]: Dan Boneh, Richard A. DeMillo, and Richard J. Lipton. 2001. On the Importance of Eliminating Errors in Cryptographic Computations. *Journal of Cryptology* 14, 2 (March 2001), 101–119. <https://doi.org/10.1007/s001450010016>
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