

# Data-Driven Contextual Modeling for 3D Scene Understanding

Yifei Shi<sup>a</sup>, Pinxin Long<sup>c</sup>, Kai Xu<sup>a,c,\*</sup>, Hui Huang<sup>b,c</sup>, Yueshan Xiong<sup>a</sup>

<sup>a</sup>*HPCL, National University of Defense Technology*

<sup>b</sup>*Shenzhen University*

<sup>c</sup>*Shenzhen VisuCA Key Lab / SIAT*

## Abstract

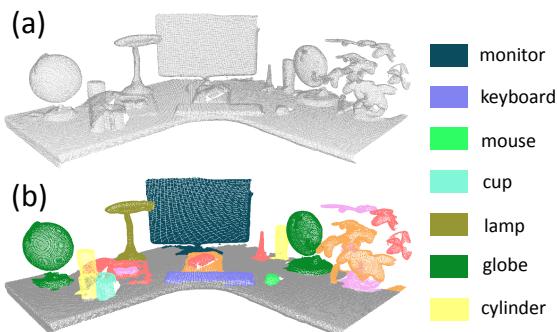
The recent development of fast depth map fusion technique enables the realtime, detailed scene reconstruction using commodity depth camera, making the indoor scene understanding more possible than ever. To address the specific challenges in object analysis at subscene level, this work proposes a data-driven approach to modeling contextual information covering both intra-object part relations and inter-object object layouts. Our method combines the detection of individual objects and object groups within the same framework, enabling contextual analysis without knowing the objects in the scene *a priori*. The key idea is that while contextual information could benefit the detection of either individual objects or object groups, both can contribute to object extraction when objects are unknown.

Our method starts with a robust segmentation and partitions a subscene into segments, each of which represents either an independent object or a part of some object. A set of classifiers are trained for both individual objects and object groups, using a database of 3D scene models. We employ the multiple kernel learning (MKL) to learn per-category optimized classifiers for objects and object groups. Finally, we perform a graph matching to extract objects using the classifiers, thus grouping the segments into either an object or an object group. The output is an object-level labeled segmentation of the input subscene. Experiments demonstrate that the unified contextual analysis framework achieves robust object detection and recognition over cluttered subsenes.

**Keywords:** Scene understanding, object recognition, contextual modeling, data-driven approach

## 1. Introduction

\*Corresponding author: kaixu@nudt.edu.cn



**Figure 1:** Scene understanding by our method. (a): The input point cloud of a table-top scene. (b): The labeling result (legends show semantic labels in color).

With the rapid development of 3D sensing techniques, the digitalization of large-scale indoor scenes has become unprecedently accessible to a wide range of applications. Among the most exciting and promising applications, robot-operated exploration and interaction over unknown indoor environment would benefit significantly from the availability of high-quality and realtime acquired 3D geometry information [1]. Such 3D information can not only improve robot navigation and exploration, but more importantly, facilitate efficient robot-scene interaction with fine-grained understanding of scene objects. The latter may support highly complex robot tasks such as room cleaning.

Motivated by the high demand, extensive research has been devoted to the understanding of scanned indoor scenes. Most existing works on scene understanding focus on large-scale objects, such as furniture, as well as their spatial layout [2, 3, 4, 5, 6], since the analysis

is usually limited by the quality and resolution of input scans. Recent advances in volumetric scan fusion technique (such as KinectFusion [7]) has made it possible to reconstruct quality and detailed scenes from scans captured by commodity depth camera (e.g. Microsoft Kinect and Asus Xtion). The dense point clouds processed by KinectFusion can well capture small scale objects such as household objects, which enables detailed understanding at a subscene level, e.g. many objects placed a tabletop; see Figure 1.

Object analysis at subscene level is arguably much more challenging than that at whole scene level. *Firstly*, unlike furnitures which are usually sparsely distributed in an indoor scene, household objects are often highly cluttered due to the limited space of supporting surfaces [8]. For example, a tabletop scene is typically cluttered with many on-table objects. *Secondly*, repetition of objects, which is ubiquitous among furnitures and has been extensively exploited in previous works [3, 5], may not be as commonly seen among household objects. For example, the objects placed on a table are mostly unique within the subscene. *Thirdly*, from the acquisition point of view, smaller objects are often more sensitive to scanning imperfection. These challenges make the existing methods, dealing with large-scale furniture layout, unsuitable for the object analysis of small-scale subscenes.

To address these challenges, it seems a natural option is to fully utilize the inter-object relations, or contextual information. However, a key prerequisite for contextual scene analysis is that all objects are segmented and labeled with semantic tags [9], which is apparently infeasible for an unsegmented scene. Essentially, context is defined with objects. Without knowing objects, how can we utilize contextual information to help the identification of objects? In this work, we try to tackle this problem through integrating the discovery of both individual objects and object groups into a unified framework. While the former involves grouping parts into an object, which detects individual objects, the latter amounts to finding structure groups [10] composed of multiple objects, which can actually enhance or reinforce the detection and recognition of objects within the structure group. The key idea is that contextual information could benefit the detection of either individual objects or object groups, when objects are unknown. However, both can contribute to object extraction.

To enable such unified framework, we take a data-driven approach equipped with several key procedures. First, we propose a robust segmentation method to partition a indoor scene into segments which each represents either

an independent object or a part of some object. We then train a set of classifiers for both individual objects and object groups, based on a database of 3D scene models. To improve the classification accuracy, we employ multiple kernel learning (MKL) [11] to learn per-category optimized SVM classifiers for various objects and object groups. Finally, we perform a graph matching to extract objects using the classifiers, thus grouping the segments into either an object or an object group. The input of our algorithm is an indoor scene point cloud, and the output is an object-level labeled segmentation of the input scene. Experiments demonstrate the robust performance for both segment extraction and object recognition on several subscenes.

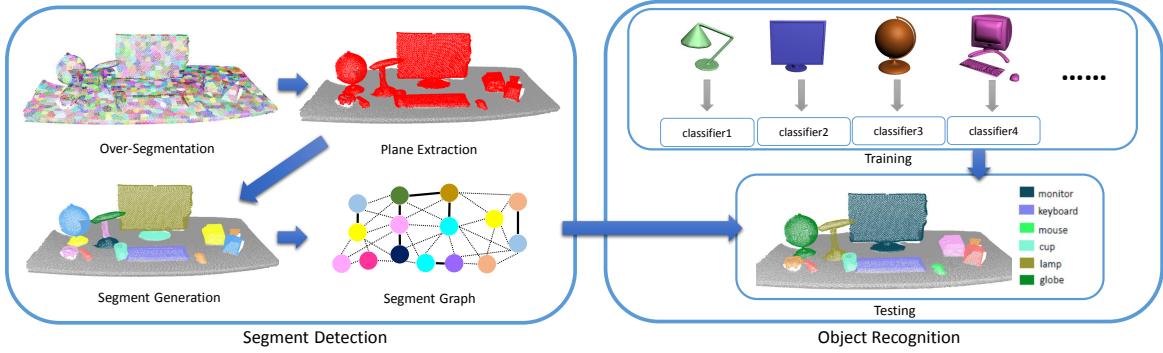
Our approach possesses two key features compared with previous methods. First, we perform a segmentation process before recognition, which leads to robust handling of cluttered scenes. Second, instead of solving the recognition of individual objects and object groups as two separate problems, we encode features of both individual objects and object layout into a unified classifier via contextual modeling.

## 2. Related Work

Scene understanding is a long-standing research topic which has received extensive research from both computer vision and computer graphics community. We mainly review those works which take 3D point clouds as input.

*Point cloud segmentation.* Mesh segmentation is a fundamental shape analysis problem in computer graphics, for which both heuristic methods [12] and data-driven approach [13] have been extensively studied over the years. On the other hand, the segmentation of 3D point clouds remains to be a challenging problem.

There are three kinds of methods for point cloud segmentation [14]. The first type is based on primitive fitting [3, 15, 5]. It is hard for these methods to deal with objects with complex shape. The second kind of techniques is the region growing method. Nan et al. [2] propose a controlled region growing process which searches for meaningful objects in the scene by accumulating surface patches with high classification likelihood. Berner et al. [16] detect symmetric regions using region growing. Another line of methods formulates the point cloud segmentation as a Markov Random Field (MRF) or Conditional Random Field (CRF)



**Figure 2:** An overview of our algorithm. We first over-segment the scene and extract the supporting plane on the patch graph, then segment the scene into segments and represent the whole scene using a segment graph (a). To obtain the contextual information, we train a set of classifiers for both single objects and object groups using multiple kernel learning (b). The classifiers are used to group the segments into objects or object groups (c).

problem [4, 17, 14]. A representative random field segmentation method is the min-cut algorithm [17]. The method extracts foreground from background through building a KNN graph over which min-cut is performed. The shortcoming of min-cut algorithm is that the selection of seed points relies on human interaction. We extend the min-cut algorithm by first generating a set of object hypotheses via multiple binary min-cuts and then selecting the most probable ones based on a voting scheme, thus avoiding the seed selection.

*Object recognition.* Recently, the development of commodity RGB-D cameras has opened many new opportunities for 3D object recognition and scene recognition [18, 19]. With the ever-growing amount of 3D models becoming available, data-driven approach starts to play an important role in 3D object recognition and has gained great success [20].

Nan et al. [2] propose a search-classify approach to scene understanding by interleaving segmentation and classification in an iterative process. Li et al. [6] propose scene reconstruction by retrieving objects from a 3D model database. Song et al. [21] render database models from hundreds of viewpoints and train an exemplar-SVM classifier for each of them to achieve object recognition. Their method overcomes several difficulties in object recognition, such as the variations of texture, illumination, etc. Chen et al. [22] utilize contextual information for indoor scene understanding. Small objects and incomplete scans can be recognized with the help of contextual relationships learned from database objects. Our method lends itself to cluttered indoor scene analysis through integrating segmentation and recognition

into a single framework, which leads to a better performance when dealing with close-by objects than the contour-based method of [22].

Another line of analysis method is unsupervised learning based on the presence of repetitions or symmetries in indoor scenes [3, 5, 23]. A limitation of such approaches is that such repetitive patterns are less common in subscenes dominated by household objects, e.g., a tabletop scene.

*Plane extraction.* Plane extraction from point cloud is another important topic in scene understanding. For example, planes can be used to improve the reconstruction of arbitrary objects containing both planar and non-planar regions [24].

Perhaps the most widely used approach for plane extraction is RANSAC based plane fitting [15]. This method scales well with respect to the size of the input point cloud and the number of planes. Mattausch et al. [5] utilize planar patches as a compact representation of the point cloud of an indoor scene, which facilitates efficient repetition detection in a large-scale scene point cloud. Zhang et al. [24] perform plane extraction to delineate non-planar objects. Plane extraction has also been performed in the analysis of RGB-D data [25, 26]. These works trim the plane boundary and convert the input data into a compact polygonal representation. Recently, Monszpart et al. [27] propose to reconstruct the raw scan of man-made scenes into an arrangement of planes with both local fitting and global regularization.

### <sup>177</sup> 3. Overview

<sup>178</sup> The input of our algorithm is a 3D point cloud of indoor  
<sup>179</sup> scene acquired and fused by KinectFusion. Our goal is  
<sup>180</sup> to detect objects in the scene and recognize their seman-  
<sup>181</sup> tic categories automatically. Our method proceeds in  
<sup>182</sup> two stages. First, we segment the point cloud into seg-  
<sup>183</sup> ments representing potential objects. Second, to achieve  
<sup>184</sup> object extraction and recognition, we propose a joint es-  
<sup>185</sup> timation of individual objects and object groups, as well  
<sup>186</sup> as their semantic categories.

<sup>187</sup> *Segment detection.* In the first stage, we segment the  
<sup>188</sup> input scene (Figure 2 (a)). Specifically, we first over-  
<sup>189</sup> segment the entire scene and build a patch graph. We  
<sup>190</sup> then extract the supporting plane with a method inte-  
<sup>191</sup> grating RANSAC primitive fitting into graph-cut. Af-  
<sup>192</sup> ter plane extraction, the remaining points are grouped  
<sup>193</sup> into isolated groups. Within each group, we generate  
<sup>194</sup> segments via a robust segmentation algorithm, which  
<sup>195</sup> takes both geometry and appearance information into  
<sup>196</sup> account. Based on the segmentation, we represent the  
<sup>197</sup> entire scene as a segment graph with two types of edges  
<sup>198</sup> representing direct spatial adjacency (solid lines in Fig-  
<sup>199</sup> ure 2) and spatial proximity (dashed lines) between two  
<sup>200</sup> segments, respectively.

<sup>201</sup> *Object extraction and recognition.* In the second phase,  
<sup>202</sup> we extract objects via recognizing both individual ob-  
<sup>203</sup> jects and object groups within a unified framework,  
<sup>204</sup> based on the above segment graph representation.

<sup>205</sup> In an off-line stage, we train per-category optimized  
<sup>206</sup> SVM classifiers with multiple kernel learning for both  
<sup>207</sup> objects and object groups. The classifiers are trained  
<sup>208</sup> using 3D database models. Each 3D model is first con-  
<sup>209</sup> verted into 3D point cloud using virtual scanning and  
<sup>210</sup> segmented using the method mentioned above. We then  
<sup>211</sup> extract features from the corresponding segment graph  
<sup>212</sup> and train classifiers based on the graph.

<sup>213</sup> In the online stage, we extract objects or object groups  
<sup>214</sup> from the segment graph of the input scene, through  
<sup>215</sup> searching for the subgraph matching corresponding to  
<sup>216</sup> the occurrence of database objects and object groups.  
<sup>217</sup> Once a matched subgraph is found, we use the cor-  
<sup>218</sup> responding SVM classifier to estimate the probability  
<sup>219</sup> of the match. Finally, we solve a labeling optimiza-  
<sup>220</sup> tion which minimizes the overall matching cost for all  
<sup>221</sup> matching probabilities.

### <sup>222</sup> 4. Segment detection

<sup>223</sup> Our goal is to partition the input scene into segments  
<sup>224</sup> which each represents either an independent object or  
<sup>225</sup> a part of an object. In order to segment objects from  
<sup>226</sup> cluttered scenes, we propose an unsupervised segment  
<sup>227</sup> detection approach to detect segments in 3D scene.

<sup>228</sup> Specifically, we first over-segment the input point cloud  
<sup>229</sup> into a set of patches (Sec. 4.1) and detect the supporting  
<sup>230</sup> plane (Sec. 4.2). We then group the remaining patches  
<sup>231</sup> to extract potential objects or parts (Sec. 4.3) and rep-  
<sup>232</sup> resent them as a segment graph (Sec. 4.4). See Algo-  
<sup>233</sup>rithm 1 for an overview of our method.

#### <sup>234</sup> 4.1. Patch graph generation

<sup>235</sup> We first over-segment the entire scene  $S$  into sev-  
<sup>236</sup> eral patches, using the method in [28]. We build a  
<sup>237</sup> patch graph based on the patches, denoted with  $G_p =$   
<sup>238</sup>  $(\mathcal{V}_p, \mathcal{E}_p)$ , where  $\mathcal{V}_p$  and  $\mathcal{E}_p$  represent the patches and  
<sup>239</sup> the near-by relations within the patches, respectively.  
<sup>240</sup> Specifically, the near-by relations are determined by  
<sup>241</sup> comparing the nearest distance between two patches  
<sup>242</sup> with a threshold.

Essentially, our segment detection algorithm is a graph-  
cut based approach. The most vital component for  
graph-cut method is the definition of smooth term. In  
this section, the smooth terms for all graph-cut opti-  
mization are identical, which we first define here:

$$E_s(x_u, x_v) = w_c \cdot E_c + w_p \cdot E_p + w_n \cdot E_n, \quad (1)$$

<sup>243</sup> where  $x_u, x_v$  are two adjacent patches.  $E_c, E_p, E_n$  are  
<sup>244</sup> the differences between two adjacent patches in terms of  
<sup>245</sup> color, planarity and normal.  $w_c, w_p, w_n$  are the weights.

$E_c$  and  $E_p$  are computed based on the chi-square dis-  
tance of the color and planarity histogram between  $u$   
and  $v$ , we normalize them to  $(0, 1)$ . It is worth mention-  
ing that the planarity histogram are computed as fol-  
low: first compute the least-square plane for a patch,  
then built a histogram for distances of all points in the  
patch to the plane. The formulation for  $E_n$  is different  
for convex and concave situations. Specifically, the for-  
mulation is:

$$E_n(x_u, x_v) = 1 - \eta(1 - \cos \theta_{u,v}), \quad (2)$$

<sup>246</sup> where  $\theta_{u,v}$  is the angle between the average normals of  
<sup>247</sup> patch  $P_u$  and  $P_v$ . For  $\eta$ , we take 0.01 (a small value) if  
<sup>248</sup> the two adjacent patches form a convex dihedral angle

---

**Algorithm 1** :Segment Detection.

---

**Input:** scene  $S$

**Output:** segment graph  $G_s$

- 1:  $G_p \leftarrow \text{OverSegment}(S);$
  - 2:  $S \leftarrow \text{PlaneExtract}(S, G_p);$  //extract plane
  - 3:  $\mathcal{H} \leftarrow \text{SegHypGen}(S, G_p);$  //generate seg. hypo.
  - 4:  $T \leftarrow \text{SegHypSelect}(\mathcal{H});$  //select seg. hypo.
  - 5:  $G_s \leftarrow \text{SegGraGen}(T);$  //generate seg. graph
  - 6: **return**  $G_s;$
- 

249 and 1 otherwise, to encourage cuts around a concave  
250 region [29].

251 Our smooth term takes both geometry (planarity and  
252 normal) and appearance (color) factors into considera-  
253 tion, thus makes the patches belong to different objects  
254 can be detected easily.

255 *4.2. Supporting plane extraction*

256 Supporting plane is usually the largest object in most  
257 subscenes of an indoor scene, such as tables, beds,  
258 shelves, etc. The extraction of supporting plane is es-  
259 pecially useful since it makes the detection of objects  
260 on top of the supporting plane easier. Therefore, the  
261 first step of our segment generation is supporting plane  
262 extraction. For this task, perhaps the most straightfor-  
263 ward approach is RANSAC based primitive fitting [15].  
264 Since the objects placed on the supporting plane may be  
265 very small or thin, setting a hard threshold for point-to-  
266 plane distance may cause a lot of false positives. We  
267 therefore improve this method by adding a graph-cut  
268 optimization, to robustly segment on-top objects from  
269 the supporting plane.

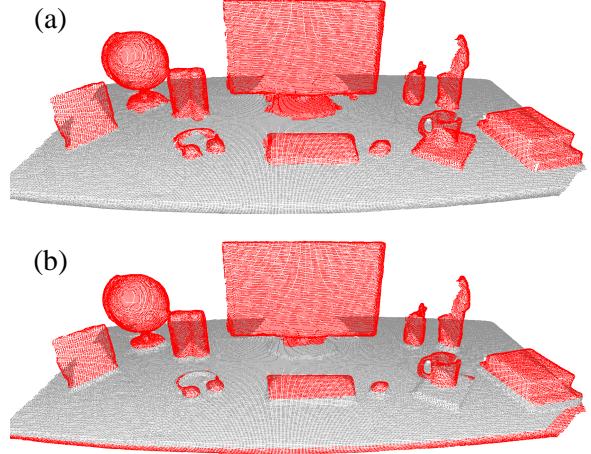
We try to assign each patch a binary label, denoted by  $X = [x_1, \dots, x_n]$  with  $x_i \in \{0, 1\}$ .  $x_i = 1$  if patch  $P_i$  lies in the plane, and  $x_i = 0$  otherwise. We formulate the labeling problem as graph cuts over the patch graph:

$$E(X) = \sum_{u \in \mathcal{V}_p} E_d(x_u) + \sum_{(u,v) \in \mathcal{E}_p} E_s(x_u, x_v), \quad (3)$$

where the data term is defined as:

$$E_d(x_u) = \begin{cases} \delta, & \text{if } x_u = 1 \\ (1 - \frac{p}{p_{max}}) \cdot (1 - \frac{d}{d_{max}}) \cdot \cos \theta_{u,l}, & \text{if } x_u = 0 \end{cases}$$

270 where  $\delta$  is a constant value,  $d$  the distance between the  
271 center of  $u$  to the plane, and  $p$  the planarity of the patch.  
272  $d_{max}$  and  $p_{max}$  is the maximum distance and planarity,  
273 respectively. We compute  $p$  as the average distance



**Figure 3:** Plane extraction from the point cloud of a tabletop scene by using our method (a) and RANSAC based primitive fitting (b), respectively. While our method can segment out the supporting plane accurately, RANSAC missed some points due to the thin objects.

274 of all the points in patch  $P_u$  to its corresponding least-  
275 square fitting plane.  $\theta_{u,l}$  is the angle between the average  
276 normal of  $P_u$  and the normal of the plane.

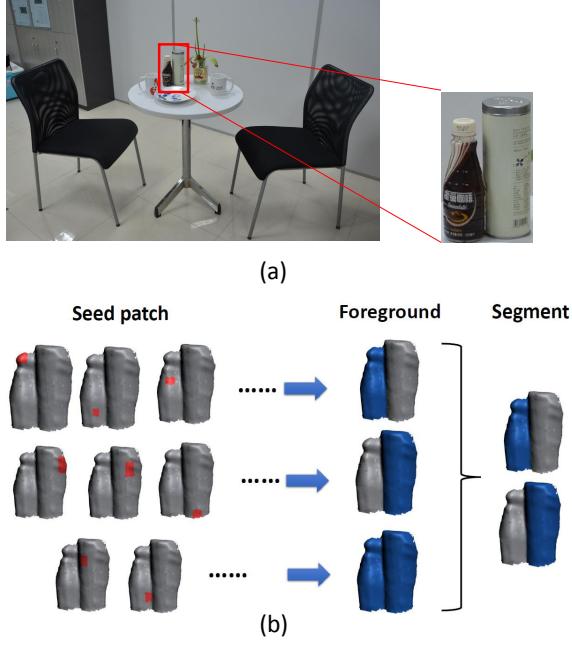
277 Figure 3 (a) demonstrates the segmentation results of  
278 our method. As a comparison, the RANSAC based  
279 primitive fitting can also get the majority of points cor-  
280 rectly, but it fails when dealing with small and thin ob-  
281 jects, as is shown in Figure 3 (b).

282 *4.3. Segment generation*

283 *Segment hypothesis generation.* After plane removal,  
284 object extraction only amounts to segmenting the iso-  
285 lated groups of patches on top of the supporting plane  
286 into individual objects. To solve the problem, we pro-  
287 pose to first generate a set of segment hypotheses and  
288 then select the most prominent ones based on a voting  
289 algorithm.

290 We first update the patch graph  $G_p$  by removing the  
291 nodes belonging to the extracted plane. Based on the  
292 updated patch graph, we generate segment hypothese-  
293 ses by performing several times of binary graph cut,  
294 where the foreground corresponds to potential objects  
295 or prominent parts.

Different from other graph cut method, we do not se-  
296 lect foreground seed heuristically. Instead, we use every  
297 patch as seed and perform binary graph cuts for multiple



**Figure 4:** Illustration of our segment detection method. The scene is composed of two bottles stuck together on a round table (a). We use every patch as seed to generate many foreground hypotheses and then select the most prominent ones (b).

times, generating many candidate foregrounds. In each binary cut, we select one patch as foreground seed but do not prescribe any seed for background. This is performed by introducing a background penalty for each non-seed patch [30]. Specifically, we select one patch, denoted by  $P_s$ , labeling it as foreground  $x_s = 1$ , and minimize over binary patch labels  $X = [x_1, \dots, x_n]$ ,  $x_i \in \{0, 1\}$  ( $n$  is the number of patches) the following parametric energy function:

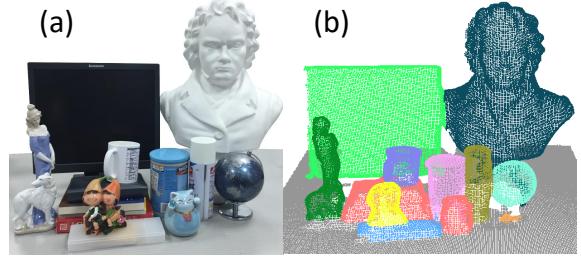
$$E^\lambda(X) = \sum_{u \in \mathcal{V}_p} E_d^\lambda(x_u) + \sum_{(u,v) \in \mathcal{E}_p} E_s(x_u, x_v), \quad (4)$$

where the data term is defined as:

$$E_d^\lambda(x_u) = \begin{cases} \infty, & \text{if } x_u = 0 \text{ and } u = s \\ 0, & \text{if } x_u = 1 \text{ and } u = s \\ 0, & \text{if } x_u = 0 \text{ and } u \neq s \\ f_u, & \text{if } x_u = 1 \text{ and } u \neq s \end{cases}$$

$$f_u = \begin{cases} k(d(P_s, P_u) - \lambda), & \text{if } d(P_s, P_u) > \lambda \\ 0, & \text{otherwise.} \end{cases}$$

$f_u$  is the background penalty which penalizes a non-seed patch which is distant from the foreground seed.



**Figure 5:** Segment detection from the point cloud of a highly cluttered scene (a) by using our method (b). The input data has a lot of close-by objects and the back view is not scanned, which makes the segmentation quite challenging. Our method can segment out most objects accurately.

<sup>298</sup>  $d(P_s, P_u)$  is the distance between the centers of patch  $P_s$  and  $P_u$ . We use  $k = 2.0$  for a steep penalty to quickly <sup>299</sup> reject those patches whose distance to  $P_s$  is larger than <sup>300</sup>  $\lambda$  to be labeled as foreground. The parameter  $\lambda$  controls <sup>301</sup> the range, centered around the foreground seed, within <sup>302</sup> which one seeks for foreground patches. Instead of us- <sup>303</sup> ing a hard threshold on this range, we slide  $\lambda$  from 0 to <sup>304</sup>  $\ell_d$  (the diagonal length of the bounding box of the entire <sup>305</sup> scene) and find the first point where the total cut cost <sup>306</sup> drops significantly (up to 50%) and take the resulting <sup>307</sup> cuts as the segmentation result. The smooth term is the <sup>308</sup> same as the one used for plane extraction in Eq. (1). <sup>309</sup>

<sup>310</sup> Once we select every patch as seed and perform graph <sup>311</sup> cut for each of them, we can obtain a set of foreground <sup>312</sup> segments. To filter out the redundancy, we cluster <sup>313</sup> the foreground segments using non-parametric mean- <sup>314</sup> shift [31]. The similarity between two segments, de- <sup>315</sup> noted as  $S$  and  $T$ , is measured by the Jaccard index, i.e., <sup>316</sup>  $s(S, T) = |S \cap T| / |S \cup T|$ . For example, as is shown <sup>317</sup> in Figure 4 (b), selecting the seed patches in the same <sup>318</sup> row will lead to identical foregrounds, thus these fore- <sup>319</sup> grounds will cluster together after the mean-shift pro- <sup>320</sup> cessing, as the Jaccard index is high. For each cluster, <sup>321</sup> we choose the cluster center as the segment hypothesis <sup>322</sup> for that cluster. As a result, we obtain a pool of  $k$  hypo- <sup>323</sup> thetic segments,  $\mathcal{H} = \{H_i\}_{i=1}^k$ .

*Segment hypothesis selection.* The set of hypotheses may overlap with each other, making the labeling of patches ambiguous. To select good hypotheses without relying on heuristics or supervision, we propose a multi-class Markov random field (MRF) segmentation with object label selection, which minimizes the follow-

ing energy function:

$$E(L) = \sum_{u \in \mathcal{V}_p} E_d(l_u; P_u) + \sum_{(u,v) \in \mathcal{E}_p} E_s(l_u, l_v), \quad (5)$$

324 over the labeling for all patches:  $L = [l_1, \dots, l_n], l_i \in$   
 325  $\{1, \dots, k\}$ .

The data term  $E_d(l_u; P_u)$  is defined as the likelihood that the patch  $P_u$  belongs to a particular segment hypothesis. For instance, for patch  $P_u$  and hypothesis  $H_i$ , we define the data term as the frequency of  $P_u$  being covered by the hypotheses in  $H_i$ :

$$E_d(H_i; P_u) = -\ln(t(P_u, C_i) / \sum_j t(P_u, C_j)), \quad (6)$$

326 where  $t(P_u, C_i) = |\{P_u \subset H_j | H_j \in C_i\}|$  is the presence  
 327 times of patch  $P_u$  in cluster  $C_i$ . The smooth term is also  
 328 the same as the one in Eq. (1)).

329 The data term selects a label for each patch based on a  
 330 consensus voting by all foreground clusters: The larger  
 331 a foreground cluster is, the more probable that its cor-  
 332 responding segment hypothesis represents an indepen-  
 333 dent object, since the object is proposed by many binary  
 334 segmentations. Figure 4 depicts our segment detection  
 335 algorithm and Figure 5 demonstrates the segmentation  
 336 results over a highly cluttered scene.

#### 337 4.4. Segment graph generation

338 To deal with the recognition for both object and object  
 339 group, we represent the entire scene as a segment graph  
 340  $G_s = (\mathcal{V}_s, \mathcal{E}_s)$ , where  $\mathcal{V}_s$  represents the segments we  
 341 detected in the input scene and  $\mathcal{E}_s$  encodes the relation-  
 342 ship between two segments. We use two kinds of edges  
 343 to describe relations in  $G_s$ . If the shortest distance be-  
 344 tween two segments is less than a small threshold  $t_s$ , we  
 345 use a *connection edge* to link them, that means the two  
 346 segments contact with each other and probably belongs  
 347 to the same object. If the shortest distance between two  
 348 segments is large than the small threshold but less than  
 349 a larger threshold  $t_l$ , we use a *proximity edge* to con-  
 350 nect them, which means they are in the same supporting  
 351 plane and has the potential to constitute a object group.  
 352 The two kinds of edges represent the contextual infor-  
 353 mation for intra-object part relations and inter-object  
 354 object layouts, respectively.  $t_l$  is selected as slightly  
 355 larger than the largest bounding box diagonal length of  
 356 all object groups in the database. Figure 2 shows an  
 357 illustration the segment graph of the given input scene.

## 358 5. Object Recognition

### 359 5.1. Training

360 When recognizing a scene containing multiple objects,  
 361 human perception is predominantly affected by three  
 362 levels of prior knowledge [32]: the shape information  
 363 of individual parts, the part composition of individual  
 364 objects, and the contextual relationship among object  
 365 groups. In our object recognition procedure, we en-  
 366 code all these knowledge in an unified model and recog-  
 367 nize objects and object groups simultaneously. Specif-  
 368 ically, we train per-category optimized SVM classifiers  
 369 for all kinds of objects and object groups, and then uti-  
 370 lize these classifiers to test the category of the input seg-  
 371 ments. Here, an object group is refer to a group of ob-  
 372 jects whose co-occurrence is frequently seen in an in-  
 373 door scene category [33]. For example, the monitor-  
 374 keyboard-mouse combo is frequently seen in office.

375 *Data Preparation.* To learn the model from the  
 376 database of 3D scene models, the first step is to convert  
 377 the database models (training data) into point cloud rep-  
 378 resentation, which is compatible against the input (test  
 379 data), and extract features from the point clouds.

380 First, we download a set of 3D CAD models of house-  
 381 hold objects, denoted by  $\{\Gamma_i\}$ , from the internet. Each  $\Gamma_i$   
 382 contains the models belonging to the same shape cate-  
 383 gory. Second, we collect indoor scene models from the  
 384 dataset of [9] and [10]. In order to obtain object groups  
 385 which are not only frequently occurring but also seman-  
 386 tically significant, we extract local substructures  $\{\Phi_i\}$   
 387 from the dataset as the focal points defined in [33]. Each  
 388  $\Phi_i$  contains the substructures belonging to the same se-  
 389 mantic group.

390 We then perform virtual scanning for all models/groups  
 391 in  $\{\Gamma_i\}$  and  $\{\Phi_i\}$ , similar to [2]. Such virtual scan could  
 392 mimic the real situation of object clutter or incomple-  
 393 te scan, making the training data more suitable for learn-  
 394 ing a generalizable recognition model. After the virtual  
 395 scanning, we compute segment graphs using the method  
 396 described in Sec. 4 for object groups in  $\{\Phi_i\}$ . For in-  
 397 dividual objects in  $\{\Gamma_i\}$ , we perform the same process  
 398 except for table extraction. The label of each virtu-  
 399 ally scanned point is determined by aligning the point cloud  
 400 with the original 3D CAD models and transferring the  
 401 labels based on closest point search.

*Classifier Learning.* We compute two kinds of features  
 for our SVM classifier: node features and edge features.

---

**Algorithm 2** :Training.

---

**Input:** object set  $\{\Gamma_i\}$  and object group set  $\{\Phi_i\}$   
**Output:** classifiers  $C$

```

1: for all  $\Gamma_i$  do
2:   for all  $\gamma_j$  in  $\Gamma_i$  do
3:      $\gamma_j \leftarrow \text{VirtualScan}(\gamma_j);$ 
4:   end for
5:    $g_i \leftarrow \text{ConstructSegGraph}(\Gamma_i);$ 
6:    $c_i^\gamma \leftarrow \text{MKL}(g_i);$ 
    //train SVM for each single object category
7: end for
8: for all  $\Phi_i$  do
9:   for all  $\phi_j$  in  $\Phi_i$  do
10:     $\phi_j \leftarrow \text{VirtualScan}(\phi_j);$ 
11:   end for
12:    $g_i \leftarrow \text{ConstructSegGraph}(\Phi_i);$ 
13:    $c_i^\phi \leftarrow \text{MKL}(g_i);$ 
    //train SVM for each object group category
14: end for
15: return  $C = \{c_i^\gamma\}_{i=1}^m + \{c_i^\phi\}_{i=1}^n;$ 

```

---

For each node, we voxelize its bounding box and extract features of shape, normal and volume as described in [21]. In addition, we estimate the oriented bounding box (OBB) for each object and measure its anisotropy:

$$c_l = \frac{s_1 - s_2}{(s_1 + s_2 + s_3)}, c_p = \frac{2(s_2 - s_3)}{(s_1 + s_2 + s_3)}, c_s = \frac{3s_3}{(s_1 + s_2 + s_3)} \quad (7)$$

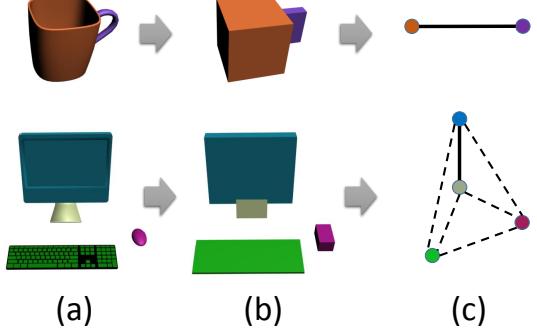
where  $s_1, s_2, s_3$  are the three scales of the OBB with  $s_1 > s_2 > s_3 \geq 0$ . For each edge, we compute the layout similarity [33] as its feature:

$$\gamma(p, q) = \frac{d_H(\text{obb}(p), \text{obb}(q))}{dl(p) + dl(q)}, \quad (8)$$

$$\rho(p, q) = \text{angle}(\mathbf{v}_{\text{dir}}(p, q), \mathbf{v}_{\text{upright}}), \quad (9)$$

The two features measure the distance and direction between two objects, respectively.

We compute features and learn pre-category optimized SVM classifiers for each category of individual objects in  $\{\Gamma_i\}$  and object groups in  $\{\Phi_i\}$ . Positive examples are the models from the two datasets, while negative ones are generated by using the method in [21] for individual objects and the method in [22] for object groups. In addition, we associate a triplet  $(n_n, n_c, n_p)$  with each classifier, where  $n_n, n_c$  and  $n_p$  represent the number of segments, edges and proximity edges, respectively. This triplet is used to perform a coarse matching based on the triplet, before testing with the classifier.



**Figure 6:** The generation of object and object group. The input is a segmented object or object group (a). We compute the OBB for each part (b) and connect them into a graph (c). The solid and the dashed lines in (c) are connection and proximity edge, respectively.

415 **Multiple Kernel Learning.** Kernel method has been  
416 successfully applied into many learning areas, while the  
417 results of these methods are heavily dependent on the  
418 selection of kernels. Instead of choosing a single ker-  
419 nel, it is better to have a set of kernels and use the com-  
420 bination of them [11]. Since our features are computed  
421 for both individual objects and their relations, it is espe-  
422 cially desirable to combine several kernels and to allow  
423 the classifiers to choose their optimized kernels, in order  
424 to reduce their bias [34]. The idea is to use a combina-  
425 tion of basic kernels  $k(\mathbf{x}, \mathbf{y}) = \sum w_i \cdot k_i(\mathbf{x}, \mathbf{y})$  rather than  
426 a specific kernel in SVM. The basic kernels could be  
427 linear kernel, Gaussian kernel, polynomial kernel, etc.

428 Figure 7 illustrates the architecture of our MKL-based  
429 classification. Given the segment graph of an individual  
430 object or an object group, we first represent it in the fea-  
431 ture space spanned with six kinds of features. We then  
432 transform the data from feature space to kernel space us-  
433 ing several predefined kernels. By computing the opti-  
434 mized weights for each kernel space, we obtain the final  
435 MKL classifier. The procedure for training the classi-  
436 fiers is detailed in Algorithm 2.

437 **5.2. Testing**

438 **Data Preprocessing.** The segments in scenes acquired  
439 by Kinect or any other commodity depth camera are  
440 usually noisy and low-quality, making the recogni-  
441 tion quite difficult. Therefore, we first surface reconstruc-  
442 tion [35] to form a watertight surface for each segment,  
443 and then compute features as described in Sec. 5.1.

---

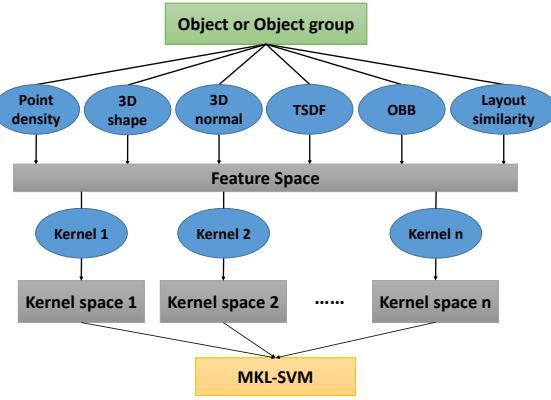
**Algorithm 3** :Testing.

---

**Input:** classifiers  $C$  and segments  $T$   
**Output:** segments label  $X$

- 1: **for all**  $c_i$  in  $C$  **do**
- 2:   **if** Matching( $c_i, T$ ) **then**
- 3:      $cost_i \leftarrow$  ComputeProbability( $c_i, T$ );
- 4:   **end if**
- 5: **end for;**
- 6:  $X \leftarrow$  ComputeLabel( $\{cost_i\}_{i=1}^k$ );  
//compute label for all segments
- 7: **return**  $X$ ;

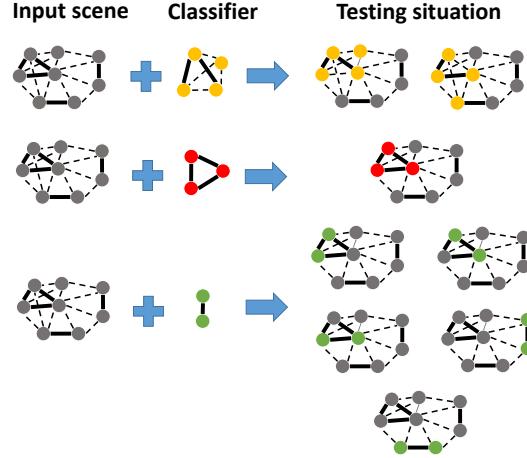
---



**Figure 7:** The architecture of our MKL-based classifier. Given an object or a object group, we compute its features and map it into several kernel spaces with several basic kernels. The MKL-SVM classifier is learned by computing the optimized weight for each kernel.

444 *Labeling Optimization.* To extract objects and object  
445 from the segment graph, we search from the seg-  
446 ment graph of the input scene for the subgraphs cor-  
447 responding to the occurrences of database objects and  
448 object groups. Graph matching can be formulated as  
449 quadratic assignment problem, which is known to be  
450 NP-hard, so an exhaustive search over the whole graph  
451 leads to high computational cost.

452 In our method, the graph matching is performed as fol-  
453 lows. For each MKL classifier, we first use the associ-  
454 ated triplet  $(n_n, n_c, n_p)$  to filter subgraph matchings. A  
455 subgraph is filtered if any one of the three terms is dif-  
456 ferent from that of the classifier. For the remaining sub-  
457 graphs, we use the learned MKL classifiers to test if it  
458 belongs to the corresponding category and record the  
459 probability if yes. The probability will be used as the  
460 labeling cost which penalizes the mislabeling in the fol-  
461 lowing optimization.



**Figure 8:** The matching strategy of our algorithm. Given a segment graph of the input scene on the left, we use all the three classifiers to test the occurrence of the corresponding subgraph. The testing samples are shown on the right. Note that some connection edge in the first row can be turned into a proximity one to allow more matchings.

462 After applying all classifiers, we detect all the potential  
463 objects or object groups in the input scene. The graph  
464 matching strategy is illustrated in Figure 8. Note that we  
465 allow a connection edge to be converted into a proximity  
466 one to produce more matchings. The rationale of this is  
467 that some segments not belonging to the same object  
468 could be linked by connection edges mistakenly due to  
469 small mutual distance.

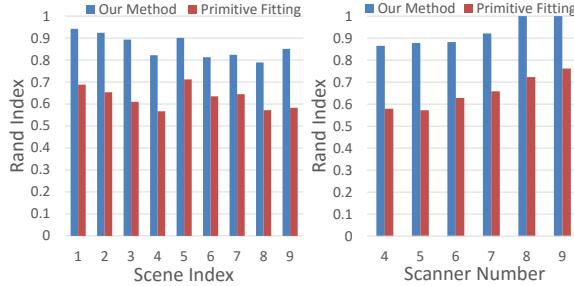
Next, we solve a labeling optimization which minimizes the overall matching cost computed from all the matching probability. The final labeling,  $X$ , for all segments of the input scene is computed by:

$$X = \operatorname{argmin}_X \sum_{c_i \in C} D(X, c_i) \quad (10)$$

where:

$$D(X, c_i) = \begin{cases} 0, & \text{if recognized subgraph by } c_i \text{ is labeled correctly in } X \\ \text{cost}(X, c_i), & \text{otherwise.} \end{cases}$$

470 where  $\text{cost}(X, c_i)$  is the labeling cost penalizing the  
471 wrong labeling of the subgraph detected by the classifier  
472  $c_i$ . We found it suffices to solve this labeling optimiza-  
473 tion using a combinatorial search over all labeling pos-  
474 sibilities since the possible labeling for each segment  
475 is limited after the classifier filtering and testing. The



**Figure 9:** Segmentation comparison against the RANSAC based primitive fitting method [15]. Left: Comparison over nine test scenes. Right: Results of our method and the RANSAC-based one over scene #2 with increasing number of scans.

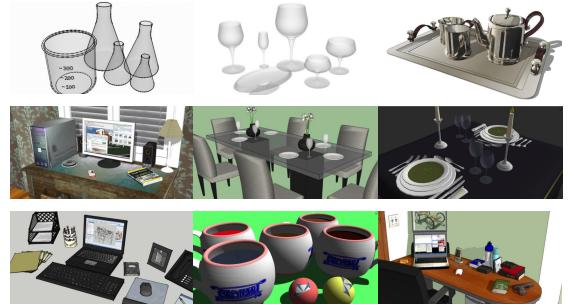
476 whole testing process for object and object group detection is described in Algorithm 3.

## 478 6. Results and Evaluation

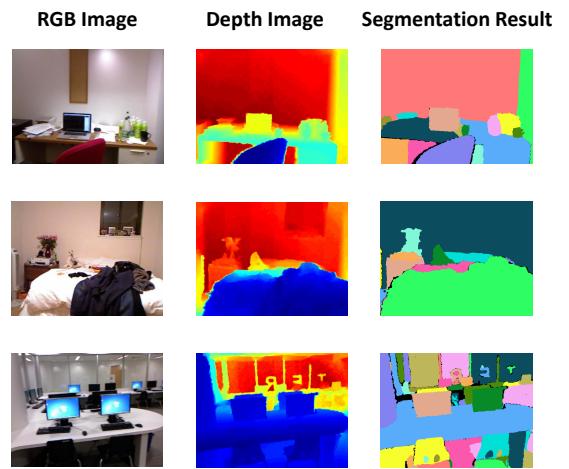
479 We test our method on both real-world and virtually 480 scanned scenes. A gallery of results is shown in Figure 481 18. We first describe the experimental setting of our 482 method and then evaluate our method in two aspects, 483 i.e., the segment detection and the object recognition.

484 *Experimental Setting.* Our method is implemented us- 485 ing C++ and run on a desktop PC with an Intel I5-3750 486 CPU (quad core, 3.4GHz) and Nvidia GeForce GTX 487 460 graphics card. We scan a few indoor scenes using a 488 Microsoft Kinect. We also use the Washington scene 489 dataset [36] acquired by an ASUS Xtion PRO LIVE 490 RGB-D sensor. The parameter settings are provided be- 491 low. Patch size (diameter): 8cm for NYU-Depth V2 492 dataset and 4cm for others;  $w_c$ ,  $w_p$ , and  $w_n$  in 1: 0.2, 493 0.3, and 0.5, respectively;  $\delta$  for table extraction: 0.95 494 for all datasets;  $t_s$  and  $t_l$  for segment graph construc- 495 tion: 3cm and 50cm, respectively; Poisson iso-point 496 sampling density: 2cm; basic kernels for MKL (we use 497 SimpleMKL [37]): five Gaussian kernels and two poly- 498 nomial kernels.

499 *Segment Detection.* We test our segment detection al- 500 gorithm on nine tabletop scenes downloaded from the 501 Internet (Figure 10) and virtually scanned. We compare 502 our method with the RANSAC-based primitive fitting 503 method in [15]. The Rand Index [38] is used as the 504 evaluation criterion. We perform six tests on each scene



**Figure 10:** The test scenes used in segmentation evaluation.



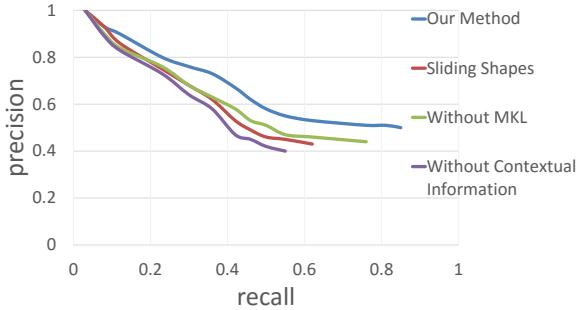
**Figure 11:** The segmentation results our algorithm over the scenes from the NYU-Depth V2 dataset. Our method can segment most objects correctly in the highly cluttered scenes.

505 with different number of scan and quality and take the 506 average Rand Index. In the virtual scanning, the virtual 507 scanners are positioned around the scene being scanned 508 and oriented to the center of the scene. The plot in Fig- 509 ure 9 (left) show that the Rand Index of our method is 510 higher than that of the RANSAC-based method over the 511 nine test scenes. We also evaluate how scan quality 512 would affect the segmentation results with the varying 513 number of scans for scene #2; see Figure 9 (right).

514 We also test our segmentation approach on NYU-Depth 515 V2 dataset. A significant feature of the depth images is 516 that the point cloud is of low resolution, making our seg- 517 mentation infeasible. In order to tackle this kind of in- 518 put, we made some changes over our algorithm. Given 519 an RGB-D image and its camera parameters, we first

	Primitive fitting[16]	Support relation[9]	Our method
Rand Index	61.8%	78.7%	76.4%

**Figure 12:** A comparison of the segmentation accuracy (Rand Index) of the methods in [15] and [8] and ours on the NYU-Depth V2 dataset.



**Figure 13:** Precision-recall curves for object recognition. Comparison is made between our method and the other three methods by testing on the database in [36].

520 project the 2D points into 3D space to reconstruct a 3D  
521 scene. We skip the table extraction process and detect  
522 the segments for the near-camera points (distance less  
523 than 2m) using our method, and cluster the rest distant  
524 points using Euclidean cluster extraction [39].

525 We test our method on a selected subset of the NYU-  
526 Depth V2 dataset as in [22], which contains 45 living  
527 rooms and offices. Some results of our algorithm are  
528 shown in Figure 11. We compare our method with the  
529 support relation based method in [8] and the RANSAC-  
530 based one in [15]. The segmentation Rand Index mea-  
531 sures for the three methods are shown in Figure 12. The  
532 support relation based method slightly outperforms our  
533 method, due to the incorporation of the high-level prior.

534 *Object Recognition.* Our recognition database contains  
535 900 objects in 18 categories and 10 kinds of object  
536 groups. We test our object recognition method on two  
537 scanned scene datasets. The first one is several real-  
538 world scenes such as office, meeting room, and lab-  
539 oratory, scanned by ourselves and the second dataset  
540 from [36]. The scenes contain a variety of object cat-  
541 egories with noisy and low quality scans.

542 Figure 18 demonstrates the results on six indoor scenes.  
543 The semantic labels are shown using distinct colors,  
544 while the contextual information is illustrated with red

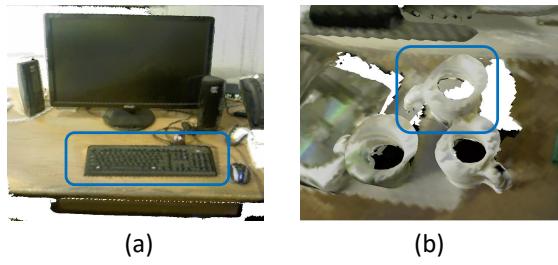
545 dots and dashed lines. The majority of objects can be  
546 recognized correctly, benefiting from the contextual in-  
547 formation. The geometric ambiguity between different  
548 categories of objects, such a keyboard and a book, are  
549 resolved with the help of contextual information. Some  
550 segments are correctly segmented but not successfully  
551 recognized due to capability of our recognition model  
552 learned from the limited model database. This can be  
553 improved by collecting more data and training a more  
554 powerful model.

555 We evaluate our method on the database of [36] con-  
556 taining 58 indoor scenes collected using KinectFusion.  
557 We compare to three alternative methods: the sliding  
558 shapes [21], a reduced version of our method by us-  
559 ing linear SVM classifiers, and a reduced method with-  
560 out using contextual information. The precision-recall  
561 curves for recognition are plotted in Figure 13. It is  
562 obvious that our method outperforms sliding shapes,  
563 thanks to the object-group-level analysis and the MKL  
564 classifiers in our method. The reduced method with-  
565 out contextual information is slightly inferior to sliding  
566 shapes. This is because sliding shapes use a plethora  
567 of classifiers, which is three orders of magnitude more  
568 than what our method uses.

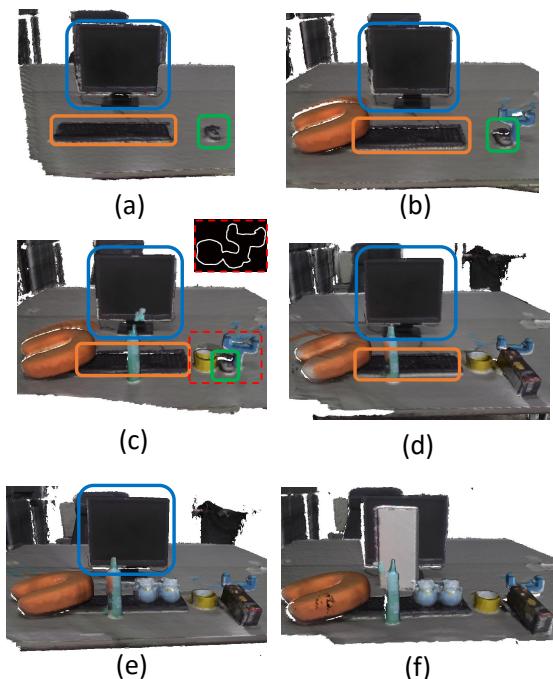
569 As demonstrated in Figure 14, our method benefits from  
570 the contextual information in two ways. First, context  
571 helps to eliminate recognition ambiguity. For example,  
572 the object in Figure 14 (a) can either be a book or a  
573 keyboard, which is correctly recognized with the help  
574 of the monitor-keyboard-mouse combo. Second, con-  
575 text can enhance the recognition ability under low data  
576 quality. For example, the cup in Figure 14 (b) is hard  
577 to be recognized due to the low data quality, where the  
578 cup-cup group helps recognize it.

579 We make two observations from the results. (1) The  
580 precision is consistently high with the increasing of the  
581 recall. (2) The recall converges to a high value but never  
582 reaches 1 with the precision decreasing. These obser-  
583 vations can be explained by the inter-restriction of the  
584 multiple MKL classifiers. Our method finds a labeling  
585 that tries to satisfy all the MKL detectors as much as  
586 possible, leading to more reliable labeling result.

587 To evaluate the performance our method on cluttered  
588 scenes, we scan six desktop scenes with an increasing  
589 degree of object clutter. The objects we recognized are  
590 highlighted with boxes in Figure 15. It is clear that our  
591 method achieves robust recognition on these cluttered  
592 scenes, especially the one in Figure 15 (c). As a com-  
593 parison, the method in [22] cannot recognize the mouse  
594 in (c), because the contour-based approach fails when

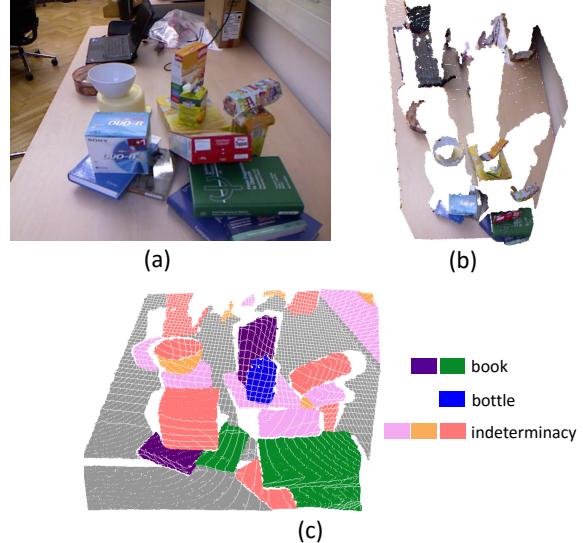


**Figure 14:** The contextual knowledge could benefit object recognition in two ways. (a): Resolving recognition ambiguity: The keyboard in blue box is recognized correctly due to the contextual information of the monitor-keyboard-mouse combo. (b): Enhancing recognition ability: The cup in blue box is in low scan quality but can be recognized based on the cup-cup combo.



**Figure 15:** Our recognition results on several scenes with increasing degree of object from (a) to (f). The monitors, keyboards and mouses are correctly recognized by our method and labeled with blue, orange and green boxes.

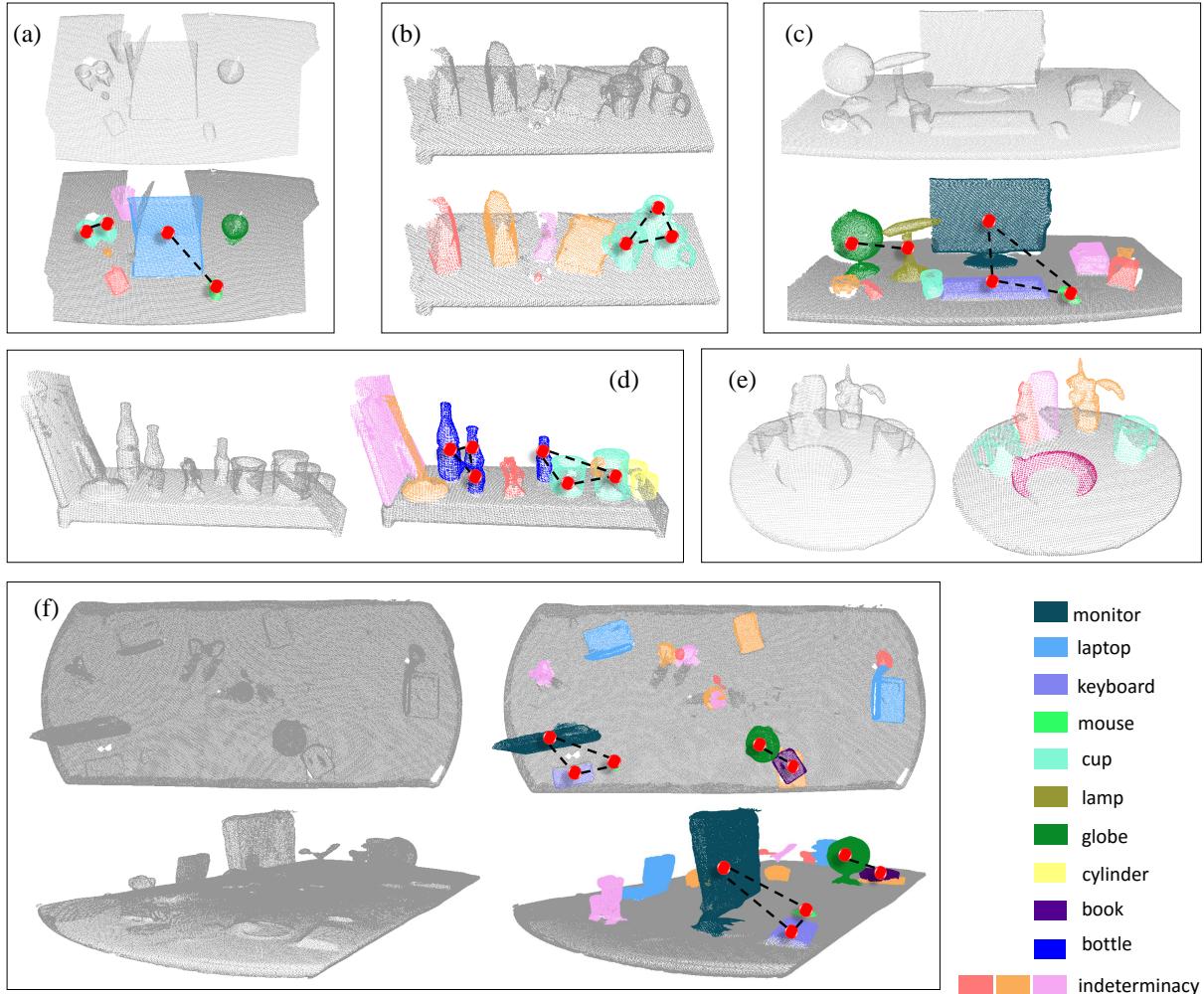
595 dealing with cluttered scenes due to the incorrect con-  
596 tour extraction. The contour of the red box area in (c) is  
597 shown on the top-right corner.



**Figure 16:** A failure case of our method. Our method cannot recognize most of the objects in a cluttered scene (c). This is due to the fact that the scene point cloud is only a single-view scan (b).

598 *Time Performance.* For a scene with 100K points, the  
599 segment detection takes 20 seconds. The training proce-  
600 dure of our object recognition is determined by the num-  
601 ber of individual object and object group categories. In  
602 our case, it takes about 1 hour to train a classifier us-  
603 ing SimpleMKL averagely. The training process takes  
604 about 32 hours in total for the 18 objects and the 10 ob-  
605 ject groups. The testing time is determined by the num-  
606 ber of segments and the degree of object clutter. The  
607 testing time for the scenes in Figure 18 (a) to (f) are 7.8,  
608 19.1, 39.5, 20.3, 1.7 and 12.9 minutes, respectively.

609 *Limitations.* Our method has the following limitations.  
610 First, our method does not provide a mechanism to deal  
611 with input data with severe missing parts. For example,  
612 if the input contains only a single-view scan, our method  
613 would not be able to produce meaningful segments for  
614 further analysis. A failure case of this is shown in Fig-  
615 ure 16. Second, our method can tolerate only moder-  
616 ate shape variation. It might fail when recognizing ob-  
617 jects with too special structure of segment graph, such  
618 as the case shown in Figure 17. Last, our method works  
619 the best for a scene containing a planar support. Al-  
620 though quite commonly seen in everyday indoor envi-  
621 ronments, the assumption does not generalize well for  
622 outdoor scenes.



**Figure 18:** A gallery of scene understanding results by our method.

## 623 7. Discussion and future work

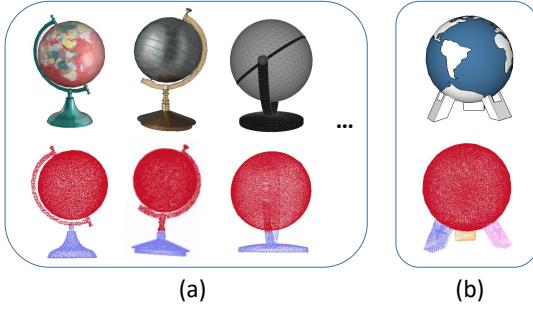
624 To achieve object analysis from clustered subscenes, we  
 625 have developed a unified framework for the discovery of  
 626 both individual objects and object groups, both of which  
 627 are based on the contextual information learned from a  
 628 database of 3D scene models. Our method makes the  
 629 contextual information applicable even without know-  
 630 ing the object segmentation of the input scene. The lat-  
 631 ter has so far been predominantly assumed by existing  
 632 methods, e.g., [22].

633 We see three venues for future work. First, our current  
 634 work focuses on subscene analysis. It would be inter-  
 635 esting to extend our method to deal with whole scene,

636 leading to multi-scale scene analysis in a unified frame-  
 637 work. Currently, the contextual information is based on  
 638 spatial proximity. As another future work, we would  
 639 like to expand our contextual features with multi-modal  
 640 object interaction, such as dynamic motion, to address  
 641 more complex mutual relations among objects. Finally,  
 642 it is natural to utilize our framework in robot-operated  
 643 autonomous scene scanning and understanding.

## 644 Acknowledgements

645 We thank all the reviewers for their comments and feed-  
 646 back. We would also like to acknowledge our research  
 647 grants: NSFC (61572507, 61202333, 61379103),



**Figure 17:** The object classifier for a globe is trained using the examples containing two components (a). The recognition may fail when testing an exceptional instance of globe with three legs (b).

973 Program (2014CB360503), Guangdong Science and Technology Program (2015A030312015, 649 650 2014B050502009, 2014TX01X033), Shenzhen Vi- 651 suCA Key Lab (CXB201104220029A).

## References

- [1] K. Xu, H. Huang, Y. Shi, H. Li, P. Long, J. Caichen, W. Sun, B. Chen, Autoscanning for coupled scene reconstruction and proactive object analysis, ACM Trans. on Graphics (Proc. of SIGGRAPH Asia) 34 (6) (2015) 177:1–177:14.
- [2] L. Nan, K. Xie, A. Sharf, A search-classify approach for cluttered indoor scene understanding, ACM Trans. on Graphics (Proc. of SIGGRAPH Asia) 31 (6) (2012) 137:1–137:10.
- [3] Y. M. Kim, N. J. Mitra, D.-M. Yan, L. Guibas, Acquiring 3d indoor environments with variability and repetition, ACM Trans. on Graphics (Proc. of SIGGRAPH Asia) 31 (6) (2012) 138:1–138:11.
- [4] T. Shao, W. Xu, K. Zhou, J. Wang, D. Li, B. Guo, An interactive approach to semantic modeling of indoor scenes with an RGBD camera, ACM Trans. on Graphics (Proc. of SIGGRAPH Asia) 31 (6) (2012) 136:1–136:11.
- [5] O. Mattausch, D. Panozzo, C. Mura, O. Sorkine-Hornung, R. Pajarola, Object detection and classification from large-scale cluttered indoor scans, Computer Graphics Forum (Proc. of Eurographics) 33 (2) 11–21.
- [6] Y. Li, A. Dai, L. Guibas, M. Nießner, Database-assisted object retrieval for real-time 3d reconstruction, Computer Graphics Forum (Proc. of Eurographics) 34 (2) (2015) 435–446.
- [7] R. A. Newcombe, A. J. Davison, S. Izadi, P. Kohli, O. Hilliges, J. Shotton, D. Molyneaux, S. Hodges, D. Kim, A. Fitzgibbon, KinectFusion: Real-time dense surface mapping and tracking, in: Proc. IEEE Int. Symp. on Mixed and Augmented Reality, 2011, pp. 127–136.
- [8] N. Silberman, P. Kohli, D. Hoiem, R. Fergus, Indoor segmentation and support inference from rgbd images, in: Proc. Euro. Conf. on Computer Vision, 2012, pp. 746–760.
- [9] M. Fisher, M. Savva, P. Hanrahan, Characterizing structural relationships in scenes using graph kernels, ACM Trans. on Graphics (Proc. of SIGGRAPH) 30 (4) (2011) 34:1–34:11.
- [10] K. Xu, K. Chen, H. Fu, W.-L. Sun, S.-M. Hu, Sketch2Scene: Sketch-based co-retrieval and co-placement of 3D models, ACM Trans. on Graphics (Proc. of SIGGRAPH) 32 (4) (2013) 123:1–123:10.
- [11] M. Gönen, E. Alpaydin, Multiple kernel learning algorithms, Journal of Machine Learning Research 12 (2011) 2211–2268.
- [12] A. Shamir, A survey on mesh segmentation techniques, Computer Graphics Forum 27 (6) (2008) 1539–1556.
- [13] E. Kalogerakis, A. Hertzmann, K. Singh, Learning 3d mesh segmentation and labeling, ACM Trans. Graph. 29 (2010) 102:1–102:12.
- [14] M. Johnson-Roberson, J. Bohg, M. Björkman, D. Kragic, Attention-based active 3d point cloud segmentation., in: Proc. IEEE Int. Conf. on Intelligent Robots & Systems, 2010, pp. 1165–1170.
- [15] R. Schnabel, R. Wahl, R. Klein, Efficient RANSAC for point-cloud shape detection, Computer Graphics Forum 26 (2) (2007) 214–226.
- [16] A. Berner, M. Bokeloh, M. Wand, A. Schilling, H.-P. Seidel, A graph-based approach to symmetry detection., in: Volume Graphics, Vol. 40, 2008, pp. 1–8.
- [17] A. Golovinskiy, T. Funkhouser, Min-cut based segmentation of point clouds, in: Proc. Int. Conf. on Computer Vision, IEEE, 2009, pp. 39–46.
- [18] L. A. Alexandre, 3d descriptors for object and category recognition: a comparative evaluation, in: Proc. IEEE Int. Conf. on Intelligent Robots & Systems, Vol. 1, pp. 1–6.
- [19] K. Lai, L. Bo, X. Ren, D. Fox, Rgb-d object recognition: Features, algorithms, and a large scale benchmark, in: Consumer Depth Cameras for Computer Vision, Springer, 2013, pp. 167–192.
- [20] K. Xu, V. G. Kim, Q. Huang, E. Kalogerakis, Data-driven shape analysis and processing, Computer Graphics Forum (2015) to appear.
- [21] S. Song, J. Xiao, Sliding shapes for 3d object detection in depth images, in: Proc. Euro. Conf. on Computer Vision, Springer, 2014, pp. 634–651.
- [22] K. Chen, Y.-K. Lai, Y.-X. Wu, R. Martin, S.-M. Hu, Automatic semantic modeling of indoor scenes from low-quality rgbd data using contextual information, ACM Trans. on Graphics (Proc. of SIGGRAPH Asia) 33 (6) (2014) 208:1–208:15.
- [23] J. S. Rudolph Triebel, Roland Siegwart, Unsupervised discovery of repetitive objects, in: Proc. IEEE Int. Conf. on Robotics & Automation, 2010, pp. 5041 – 5046.
- [24] Y. Zhang, W. Xu, Y. Tong, K. Zhou, Online structure analysis for real-time indoor scene reconstruction, ACM Trans. on Graphics 159:1–159:12.
- [25] J. Biswas, M. Veloso, Planar polygon extraction and merging from depth images, in: Proc. IEEE Int. Conf. on Intelligent Robots & Systems, IEEE, 2012, pp. 3859–3864.
- [26] M. Dou, L. Guan, J.-M. Frahm, H. Fuchs, Exploring high-level plane primitives for indoor 3d reconstruction with a hand-held rgbd camera, in: Computer Vision-ACCV 2012 Workshops, Springer, 2013, pp. 94–108.
- [27] A. Monszpart, N. Mellado, G. Brostow, N. Mitra, RAPter: Rebuilding man-made scenes with regular arrangements of planes 34 (2015) 103:1–103:12.
- [28] J. Papon, A. Abramov, M. Schoeler, F. Worgotter, Voxel cloud connectivity segmentation-supervoxels for point clouds, in: Proc. IEEE Conf. on Computer Vision & Pattern Recognition, IEEE, 2013, pp. 2027–2034.
- [29] S. Katz, A. Tal, Hierarchical mesh decomposition using fuzzy clustering and cuts, ACM Trans. on Graphics (Proc. of SIGGRAPH) 22 (3) (2003) 954–961.
- [30] A. Golovinskiy, V. G. Kim, T. A. Funkhouser, Shape-based

- 751 recognition of 3d point clouds in urban environments, in: Proc.  
 752 Int. Conf. on Computer Vision, 2009, pp. 2154–2161.
- 753 [31] Y. Cheng, Mean shift, mode seeking, and clustering, IEEE  
 754 Trans. Pattern Analysis & Machine Intelligence 17 (8) (1995)  
 755 790–799.
- 756 [32] N. J. Mitra, M. Wand, H. Zhang, D. Cohen-Or, V. Kim, Q.-  
 757 X. Huang, Structure-aware shape processing, in: ACM SIG-  
 758 GRAPH 2014 Courses, 2014.
- 759 [33] K. Xu, R. Ma, H. Zhang, C. Zhu, A. Shamir, D. Cohen-Or,  
 760 H. Huang, Organizing heterogeneous scene collection through  
 761 contextual focal points, ACM Trans. on Graphics (Proc. of SIG-  
 762 GRAPH) 33 (4) (2014) 35:1–35:12.
- 763 [34] C. Zhu, X. Liu, Q. Liu, Y. Ming, J. Yin, Distance based multiple  
 764 kernel elm: A fast multiple kernel learning approach, Mathematical  
 765 Problems in Engineering 2015.
- 766 [35] M. Kazhdan, H. Hoppe, Screened poisson surface reconstruc-  
 767 tion, ACM Trans. on Graphics 32 (3) (2013) 29:1–29:13.
- 768 [36] A. Karpathy, S. Miller, L. Fei-Fei, Object discovery in 3d scenes  
 769 via shape analysis, in: Proc. IEEE Int. Conf. on Robotics &  
 770 Automation, IEEE, 2013, pp. 2088–2095.
- 771 [37] A. Rakotomamonjy, F. Bach, S. Canu, Y. Grandvalet, Sim-  
 772 pleMKL, Journal of Machine Learning Research 9 (2008) 2491–  
 773 2521.
- 774 [38] J. Chen, D. Bautembach, S. Izadi, Scalable real-time volumet-  
 775 ric surface reconstruction, ACM Trans. on Graphics (Proc. of  
 776 SIGGRAPH) 32 (4) (2013) 113:1–113:16.
- 777 [39] D. Sparks, Euclidean cluster analysis, Applied Statistics (1973)  
 778 126–130.