

LeetCode Notes

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Part I.

LeetCode

LeetCode 27. Remove Element

Two Pointer Regular two pointer approach. The implementation is routine.

Code

LeetCode 53. Maximum Subarray

Dynamic Programming Let $f(i)$ denote the maximum subarray sum ending with `nums[i]`, then we have

$$f(i) = \begin{cases} \text{nums}[0] & \text{if } i = 0 \\ \max(f(i-1) + \text{nums}[i], \text{nums}[i]) & \text{otherwise} \end{cases} \quad (2.1)$$

Then the final answer is $\max_{i=0}^{n-1} f(i)$, where $n = \text{std::size}(\text{nums})$.

Code

LeetCode 55. Jump Game

Dynamic Programming 1 Let $f(i)$ denote the reachability of index i . Then it follows that

$$f(i) = \begin{cases} \text{true} & \text{if } i = 0 \\ \text{true} & \text{if there exists } k \in [1, i-1] \text{ such that } f(k) = \text{true} \text{ and } \text{nums}[k] + k \geq i \\ \text{false} & \text{otherwise.} \end{cases} \quad (3.1)$$

The final answer is $f(i)$. The overall runtime complexity is $O(n^2)$ and memory complexity is $O(n)$.

Code

Dynamic Programming 2 Let $f(i)$ denote the maximum distance that can be achieved from index i . Then we have

$$f(i) = \begin{cases} \text{nums}[0] & \text{if } i = 0 \\ \max(f(i-1), \text{nums}[i] + i) & \text{else if } f(i-1) \geq i \\ f(i-1) & \text{otherwise} \end{cases} \quad (3.2)$$

The final answer is $\max_{i=0}^{n-1} f(i) \geq n-1$. The runtime complexity is $O(n)$ and memory complexity is $O(n)$.

Code

LeetCode 66. Plus One

Simulation (Recursive) We use a stateful recursive lambda, $f_{[\text{carry}, \mathbf{D}]}(i)$, to recursively simulate the addition process, where $f(i)$ denote the process at index i , `carry` represents if a carry of one will be added in the current digit, and `D` is a mutable copy of `digits`. We start from $i = n-1$, where $n = \text{std::size}(\text{digits})$. The implementation of f is routine.

Code

LeetCode 88. Merge Sorted Array

Simulation (Recursive) We implement a function $f(i, n_1, n_2)$ to recursively fill `nums1` backward putting `nums1[i] = max(nums1[n1], nums2[n2])`. The implementation is routine. The resulting runtime complexity is $O(n+m)$ and memory complexity is $O(1)$.

Code

LeetCode 233. Number of Digit One

LeetCode 265. Paint House II

Dynamic Programming 1 Let $f(i, j)$ denote the minimum cost to paint all houses per the specification. Then we have

$$f(i, j) = \begin{cases} \text{costs}[0][j] & \text{if } i = 0 \\ \min_{k \in [0, k-1] \text{ and } k \neq j} \{ \text{costs}[i][j] + f(i-1, k) \} & \text{o.w.} \end{cases} \quad (7.1)$$

The time complexity is $O(nk^2)$.

Dynamic Programming 2 Let $f(i, j)$ denote the minimum cost to paint all houses per the specification. And $g(i) = \{\text{kth}(0, f([i][0, \dots, k-1]), \text{kth}(1, f([i][0, \dots, k-1]))\}$. Then it follows that

$$f(i, j) = \begin{cases} \text{costs}[0][j] & \text{if } i = 0, \\ f(i, g(i-1)[1].\text{index}) + \text{costs}[i][j] & \text{else if } g(i-1)[0].\text{index} = j, \\ f(i, g(i-1)[0].\text{index}) + \text{costs}[i][j] & \text{o.w.} \end{cases} \quad (7.2)$$

The time complexity is $O(nk)$.

LeetCode 276. Paint Fence

Dynamic Programming Let $f(i)$ denote the total numbers of way to paint fences $[0, \dots, i]$. Then we have

$$f(i) = \begin{cases} k & \text{if } i = 0 \\ k^2 & \text{else if } i = 1, \\ f(i-1) \times (k-1) + f(i-2) \times (k-1) & \text{o.w.} \end{cases} \quad (8.1)$$

where the two parts in the last transition function is to tackle with the two cases where the i th block has the same color as the $(i-1)$ th, in which case it must be difference from the $(i-2)$ th fence, and different color as the $(i-1)$ th fence.

LeetCode 300. Longest Increasing Subsequence

Patience Sorting There is a connection between the game of patience and and problem of LIS. The minimum number of piles formed in the game of patience is equal to the length of LIS. For more details, see [Section A.1](#). The time complexity is $O(n \log n)$.

Dynamic Programming Let $f(i)$ denote the length of the LIS ending at $\text{nums}[i]$. Then it follows that

$$f(i) = \begin{cases} \max_{0 \leq k \leq i-1 \text{ and } \text{nums}[k] < \text{nums}[i]} \{1 + f(k)\} & \text{if } i > 0 \\ 1 & \text{o.w.} \end{cases} \quad (9.1)$$

Then the final answer is $\max_{0 \leq i \leq n-1} f(i)$. The overall run time complexity is $O(n^2)$.

LeetCode 312. Burst Balloons

Dynamic Programming Let $f(i, j)$ denote the maximum coins after bursting `nums[i : j]`. Then we have that

$$f(i, j) = \begin{cases} \max_{i \leq k \leq j} \{ \text{nums}[k] \cdot \text{nums}[i-1] \cdot \text{nums}[j+1] + f(i, k-1) + f(k+1, j) \} & \text{if } i < j \\ \text{nums}[i] \cdot \text{nums}[i-1] \cdot \text{nums}[i+1] & \text{else if } i = j \\ 0 & \text{else if } i > j \end{cases} \quad (10.1)$$

The final answer is then $f(0, n-1)$, where $n = \text{std::size}(\text{nums})$. Note that `nums[-1]` and `nums[n]` is needs to be dealt with in the implementation if we don't pad `nums`. The overall running time is $O(n^2)$.

LeetCode 321. Create Maximum Number

Dynamic Programming with Greedy and Monotone Stack We can decompose this problem into three parts. The final solution of the problem is

$$\min_{(i,j) \in [0, \dots, n_1] \times [0, \dots, n_2] \text{ and } i+j=k} \text{merge}(g(\text{nums1}, i), g(\text{nums2}, j)). \quad (11.1)$$

There $g(A, k)$ returns the largest k element subsequence in A . And $\text{merge}(A_1, A_2)$ returns the largest sequentially merged array from A_1 and A_2 in term of lexicographical ordering. Note that $g(A, k)$ can be computed efficiently using a monotone stack, see [Section B.1.1](#). And merge can be implemented using a greedy idea: we with $i = 0$ and $j = 0$ and an accumulator `acc` of result. If $A_1[i : -1] \geq A_2[j : -1]$, we accumulate $A_1[i]$ into `acc` and increment i , otherwise we merge $A_2[j]$ into `acc` and increment j . The correctness of this merging algorithm can be proved using an exchange argument. The overall time complexity of this is $O(\max(n_1, n_2)^2 k)$.

LeetCode 322. Coin Change

Dynamic Programming Let $f(S)$ denote the minimum number of coins needed to reach value S . Then we have f

$$f(S) = \begin{cases} \min_{c \in \text{coins and } S-c \geq 0} \{1 + f(S-c)\} & \text{if } S > 0 \\ 0 & \text{else if } S = 0 \end{cases}, \quad (12.1)$$

where we let $\min(\emptyset) := +\infty$ to handle the infeasible cases. The time complexity is $O(nS)$, where $n = \text{std::size}(\text{coins})$.

LeetCode 338. Counting Bits

Dynamic Programming Let $f(i)$ be the number of 1's in i 's binary representation. Then we have that

$$f(i) = \begin{cases} 0 & \text{if } i = 0 \\ 1 & \text{else if } i = 1 \\ f(i/2) & \text{else if } i \text{ is even} \\ f(i-1) + 1 & \text{else if } i \text{ is odd} \end{cases}. \quad (13.1)$$

LeetCode 343. Integer Break

Dynamic Programming Let $f(i)$ denote the maximum product for number i . Then we have

$$f(i) = \begin{cases} 1 & \text{if } i = 1 \\ \max_{1 \leq k \leq i-1} (k \cdot f(i-k), k \cdot (i-k)) & \text{o.w.} \end{cases}. \quad (14.1)$$

The final answer is then $f(n)$. The overall runtime complexity is $O(n^2)$.

LeetCode 351. Android Unlock Patterns

Backtrack Let $f(i, k)$ denote the number of possible patterns with length k that starts from i . Then the final answer is $\sum_{i=1}^9 \sum_{k=m}^n f(i, k)$. We note that $f(i, k)$ can be computed using exhaustive search (backtrack). We will also create a list `blocks` to keep track of the jumping across cases for every key; for example, `blocks[1][{3, 9, 7}] = {2, 5, 4}` and `blocks[1][k] = ∅` for all other $k \in [1, \dots, 9] \setminus \{3, 9, 7\}$.

Dynamic Programming Using the similar idea as before, we note that f can actually be memoized. Let $f(S, k, l)$ denote the number of possible patterns of length l starting from k .

LeetCode 354. Russian Doll Envelopes

Patience Sorting Convert this problem into a LIS problem on the last coordinate. Note that LIS problem can be solved using the patience sorting algorithm in $O(n \log n)$ run time, see [Section A.1](#).

LeetCode 357. Count Numbers with Unique Digits

Dynamic Programming Let $f(i)$ denote the counts of numbers with unique digits such that $0 \leq x \leq 10^n$. Then we have that

$$f(i) = \begin{cases} 10 & \text{if } i = 1 \\ 9 \cdot 9 & \text{else if } i = 2 \\ f(i-1) \cdot (10-i+1) & \text{else if } i > 2 \end{cases} \quad (17.1)$$

Then the final answer is then $\sum_{i=1}^n f(i)$. We note that the special case of $n = 0$ is to be dealt with separately as a special case.

LeetCode 361. Bomb Enemy

Dynamic Programming Let $f(i, j, d)$ denote the number of enemies that can be killed in direction d if the bomb is dropped in `grid[i][j]`. Then we have

$$f(i, j, d) = \begin{cases} 0 & \text{if } \text{grid}[i][j] = \text{W} \text{ or not } \text{inbound}(i, j) \\ 1 + f(i + \text{dr}[d], j + \text{dc}[d], d) & \text{else if } \text{grid}[i][j] = \text{E} \\ f(i + \text{dr}[d], j + \text{dc}[d], d) & \text{else if } \text{grid}[i][j] = 0 \end{cases} \quad (18.1)$$

Then the final solution is $\max_{i,j} \text{ and } \text{grid}[i][j] = 0 \sum_d f(i, j, d)$.

LeetCode 368. Largest Divisible Subset

Dynamic Programming First we sort the `nums`. Let $f(i)$ denote the maximum divisible set size ending with `nums[i]`. Then it follows that

$$f(i) = \begin{cases} 1 & \text{if } i = 0 \\ \max_{0 \leq j \leq i-1 \text{ and } \text{nums}[i] \mid \text{nums}[j]} \{f(j) + 1\} & \text{o.w} \end{cases} \quad (19.1)$$

Then we can use backtrace to recursively build up the answer.

LeetCode 375. Guess Number Higher or Lower II

Dynamic Programming Let $f(i, j)$ denote the minimum number of amount one need a guarantee a win for number to be picked in range $[i, j]$. Then we have that

$$f(i, j) = \begin{cases} 0 & \text{if } i = j \text{ or } j > i \\ k + \min_{i \leq k \leq j} \{f(i, k-1) + f(k+1, j)\} & \text{else if } i < j \end{cases}. \quad (20.1)$$

The final answer is then $f(1, n)$. The overall run time complexity is $O(n^2)$.

LeetCode 392. Is Subsequence

Greedy with two pointer Just match **s** with **t** from the beginning.

LeetCode 376. Wiggle Subsequence

Dynamic Programming Let $f(i)$ denote the length of the longest wiggle subsequence ending with **nums** $[i]$ and the difference between last two elements is positive and $g(i)$ denote the length of the longest wiggle subsequence ending with **nums** $[i]$ and the difference between the last two elements is negative. Then we have

$$f(i) = \begin{cases} 1 & \text{if } i = 0 \\ \max_{0 \leq j < i, \text{nums}[i] < \text{nums}[j]} \{1 + g(j)\} & \text{o.w.} \end{cases}, \quad (22.1)$$

and

$$g(i) = \begin{cases} 1 & \text{if } i = 0 \\ \max_{0 \leq j < i, \text{nums}[i] > \text{nums}[j]} \{1 + f(j)\} & \text{o.w.} \end{cases}. \quad (22.2)$$

Then the final answer is $\max_{0 \leq i \leq n-1} \{\max(f(i), g(i))\}$. And the overall running time complexity is $O(n^2)$.

LeetCode 403. Frog Jump

Dynamic Programming Let $f(x, y)$ denote the reachability to x with step y . Then it follows that

$$f(x, y) = \begin{cases} \text{true} & \text{if } x = 1, y = 1 \\ f(x - y, y) \vee f(x - y, y - 1) \vee f(x - y, y + 1) & \text{o.w.} \end{cases}. \quad (23.1)$$

Since there is not limit on steps, we have that $\bigvee_{i=1}^{1001} f(\text{stones}[-1], i)$.

LeetCode 410. Split Array Largest Sum

Dynamic Programming Let $f(i, j)$ denote the largest sum splitting array **nums** $[0 : i]$ into j parts. Then we have

$$f(i, j) = \begin{cases} \text{RMQ}(0, i) & \text{if } j = 1 \\ \min_{j-1 \leq k \leq i} \{\text{RMQ}(k, i) + f(k-1, j-1)\} & \text{o.w.} \end{cases}. \quad (24.1)$$

The final answer is $f(n-1, m)$. The overall runtime complexity if $O(n^2m)$.

Binary Search Let $f(x)$ denote the minimum number of contiguous subarrays that can be splitted with sum less than or equal to x . Then we note that f is a decreasing function. The desired answer is then $\sup\{x : f(x) \leq m\}$. This can be queried using binary search on f on range $[\max_i \{\text{nums}[i]\}, \sum_i \text{nums}[i]]$. The runtime complexity is $O(n \log n)$.

LeetCode 413. Arithmetic Slices

Dynamic Programming Let $f(i)$ denote the number arithmetic slices ending with $A[i]$. Then we have

$$f(i) = \begin{cases} 0 & \text{if } i < 2 \\ 1 + f(i-1) & \text{else if } A[i] - A[i-1] = A[i-1] - A[i-2] \\ 0 & \text{else if } A[i] - A[i-1] \neq A[i-1] - A[i-2] \end{cases} \quad (25.1)$$

The final answer is $\sum_{i=0}^{n-1} f(i)$, where $n = \text{std::size}(A)$.

LeetCode 418. Sentence Screen Fitting

Memoization We design a function `fill(i)` which fills a row starting from `sentence[i]` and stop until this row cannot be filled. It returns the number of words filled and the word next to the last filled word. Note that the sentences can be filled multiple times in one row if the column size is sufficiently large. Then we fill the matrix row by row and accumulate the total number of words filled, which we denote as `acc_cnt`. The final result is then `acc_cnt/n`, where $n = \text{std::size}(\text{sentence})$. To speed things up, we note that `fill` is a pure function which does not depend on other states. Therefore, we can memoize it to save unnecessary computation.

LeetCode 446. Arithmetic Slices II

Dynamic Programming Let $f(i, d)$ denote the number of arithmetic slices ending with $A[i]$ with difference d . Then we have

$$f(i, d) = \begin{cases} \sum_{0 \leq j < i, A[i]-A[j]=d} f(j, d) + 1 & \text{if } i > 1 \\ 1 & \text{else if } i = 1 \text{ and } A[i] - d = A[i-1] \\ 0 & \text{else if } i = 1 \text{ and } A[i] - d \neq A[i-1] \end{cases} \quad (27.1)$$

We need to note that these sequences contains arithmetic sequences with length 2, which doesn't satisfy the requirement given in the problem. Hence we need to subtract them off. There are two ways to subtract them:

1. Let x denote the accumulated sum for all i and d . Then the final answer is $x - n(n-1)/2$, where $n = \text{std::size}(A)$.
2. Let x denote the final answer. Then $x = \sum_{i=0}^{n-1} \sum_{j=0}^{n-1} f(j, A[i] - A[j])$. By doing so, we are excluding out the two element sequence since we are starting from j instead of i . By doing so we are guaranteeing the first element any arithmetic slices therefore guaranteeing x counts all the arithmetic slices with at least three elements.

We also note that there some int max and int min issues to be dealt with separately. Also, to speed things up, we use a `value_index_map` to keep track of all the indices.

LeetCode 459. Repeated Substring Pattern

String Prefix Function To solve this, we note the following proposition:

Proposition 28.1. *Let s be a string. If s can be constructed by concatenating multiples of its proper substrings, then $n|(n_s - \pi(n_s - 1)) = 0$, where π is the string prefix function.*

Proof. Suppose $s = [t]_k$, where t is a proper substring of s and $k \geq 2$. Without loss of generality, we assume that t is the minimal proper substring that has the property. We let $n_t = \text{std::size}(t)$. Then it follows that $\pi(n_s - 1) = (k-1) \cdot n_t$. Then it follows that $n - \pi(n_s - 1) = n_t$. which is divisible by $n_s = kn_t$. On the other hand, suppose s cannot be written in the form of $[t]_k$. \square

With this in mind, it suffices to compute the prefix function, π , and check.

LeetCode 464. Can I Win

Dynamic Programming with BitSet Let $f(S, x)$ denote the possibility to guarantee a win for the first player with remaining available number set S and target x . Then we have that

$$f(S, x) = \begin{cases} \text{false} & \text{if } S = \emptyset \text{ or } \sum_{x \in S} S < x \\ (\max(S) \geq x) \text{ or } \bigvee_{x \in S} (\text{not } f(S \setminus \{x\} - x - i)) & \text{else} \end{cases} \quad (29.1)$$

The final answer is then $f([1, \dots, n], \text{desiredTotal})$. We note that we don't need to memoize both S and x since once we know S , x can be automatically calculated.

LeetCode 466. Count The Repetitions

Dynamic Programming with Doubling Let $f(i, k)$ denote the number of characters of the infinite stream of s_i 's starting from $s_1[i]$ needed to cover 2^k copies of s_2 . Then it follows that

$$f(i, k) = \begin{cases} \text{single_match_count}(i) & \text{if } k = 0 \\ f(i, k-1) + f((i + f(i, k-1)) \bmod \ell_1, k-1) & \text{o.w.} \end{cases}, \quad (30.1)$$

where $\text{single_match_count}(i)$ is the base case, which could be implemented as a simple accumulation. Then we just need to fill using double technique.

LeetCode 467. Unique Substrings in Wraparound String

Sliding Window Let $f(c)$ denote the length of the longest increasing contiguous subarray that ends with c in p . Then the final answer is $\sum_{c \in [a, \dots, z]} f(c)$. We also note the following:

- The contiguous subarray condition check needs to include the check to 'za' case.
- $f(c)$ can be precomputed using a sliding window.

The overall runtime is then $O(n)$, where $n = \text{std::size}(p)$.

LeetCode 471. Encode String with Shortest Length

Dynamic Programming with KMP Let $f(i, j)$ denote the shortest encoded string for $s[i : j]$. Then it follows that

$$f(i, j) = \begin{cases} \text{null_string} & \text{if } j - i + 1 \leq 4 \\ \text{std::to_string}((j - i + 1)/p) \oplus [\oplus f(i, i + p - 1) \oplus] & \text{else if } p := \text{compress}(s[i : j]) > 0 \\ \min_{i \leq k < j} \{f(i, k) \oplus f(k + 1, j)\} & \text{else if } \text{compress}(s[i : j]) = -1 \end{cases} \quad (32.1)$$

Note that the function $\text{compress}(i, j)$ returns the number of multiples of substrings that are used to encode $s[i : j]$. This can be solved efficiently using KMP algorithm like in [LeetCode 459. Repeated Substring Pattern](#). We will also use a more generalized form of the prefix function π_1 , where $\pi_1(i, j)$ denote equals $\pi_0(j)$ for $s[i : j]$, where π_0 is the original vanilla prefix function.

LeetCode 472. Concatenated Words

Fold over Trie We first build a Trie for [words](#). Then we implement a fold operation to check if a given word is a concatenated word. Let $f_s(n, i, k)$ denote the fold function representing if a given word s is a

concatenated word when we start checking from trie node n and index i of s . Then we have

$$f_s(n, i, k) = \begin{cases} n.\text{is_word} \text{ and } \text{cnt} \geq 1 & \text{if } i = \text{std::size}(s) \\ \text{false} & \text{else if } s[i] \notin n.\text{next} \\ f_s(n.\text{next}[s[i]], i+1, k) \text{ or } f(n, i+1, k+1) & \text{else if } s[i] \in n.\text{next} \text{ and } n.\text{next}[s[i]].\text{is_word} = \text{true} \\ f_s(n.\text{next}[s[i]], i+1, k) & \text{else if } s[i] \in n.\text{next} \text{ and } n.\text{next}[s[i]].\text{is_word} = \text{false} \end{cases} \quad (33.1)$$

The final answer is $\{s : s \in \text{words} \text{ and } f_s(\text{root}, 0, 0)\}$.

LeetCode 474. Ones and Zeros

Dynamic Programming Let $f(i, r_0, r_1)$ denote the maximum number of strings can be made with r_0 0's and r_1 1's for $\text{strs}[0 : i]$. Then we have that

$$f(i, r_0, r_1) = \begin{cases} 1 & \text{if } i = 0 \text{ and } \text{costs}[i] \leq (r_0, r_1) \\ 0 & \text{else if } i = 0 \text{ and } \text{costs}[i] > (r_0, r_1) \\ \max(f(i-1, r_0 - \text{costs}[i][0], r_1 - \text{costs}[i][1]), f(i-1, r_0, r_1)) & \text{else if } i > 0 \text{ and } \text{costs}[i] \leq (r_0, r_1) \\ f(i-1, r_0, r_1) & \text{else if } i > 0 \text{ and } \text{costs}[i] > (r_0, r_1) \end{cases} \quad (34.1)$$

Then the final solution is $f(\ell - 1, m, n)$, where $\ell = \text{std::size}(\text{strs})$.

LeetCode 486. Predict the Winner

Dynamic Programming Let $f(i, j)$ be the difference of score between player1 and player2 if they are to pick numbers between $[i, \dots, j]$ with player 1 pick first. Note that since both players are playing optimally, $f(i, j)$ also represents the difference player2 and player1 if they are to pick numbers between $[i, \dots, j]$ with player 2 pick first. Then we have that

$$f(i, j) = \begin{cases} \text{nums}[i] & \text{if } i = j \\ \max(\text{nums}[i], \text{nums}[j]) - \min(\text{nums}[i], \text{nums}[j]) & \text{else if } i + 1 = j \\ \max(\text{nums}[i] - f(i+1, j), \text{nums}[j] - f(i, j-1)) & \text{o.w.} \end{cases} \quad (35.1)$$

The final answer is then $f(0, n-1) \geq 0$, where $n = \text{std::size}(\text{nums})$.

LeetCode 514. Freedom Trail

Dynamic Programming Let $f(i, j)$ denote the minimum number to open the door given that is key is $\text{key}[j : -1]$ and the starting position of the ring is i . Then we have that

$$f(i, j) = \begin{cases} 0 & \text{if } \text{ring}[i] = \text{key}[j] \text{ and } j = n_{\text{key}} - 1 \\ f(i, j+1) & \text{else if } \text{ring}[i] = \text{key}[j] \text{ and } j < n_{\text{key}} - 1 \\ \min(\text{first_ll}(i, \text{key}[j]).\text{steps}, \text{first_rr}(i, \text{key}[j]).\text{steps}) & \text{else if } \text{ring}[i] \neq \text{key}[j] \text{ and } j = n_{\text{key}} - 1 \\ \min(G_{\text{ll}}, G_{\text{rr}}) & \text{else if } \text{ring}[i] \neq \text{key}[j] \text{ and } j < n_{\text{key}} - 1 \end{cases} \quad (36.1)$$

where

$$G_{\text{ll}}(i, j) = \text{first_ll}(i, \text{key}[j]).\text{steps} + f(\text{first_ll}(i, \text{key}[j]).\text{id}, \text{key}[j+1]), \quad (36.2)$$

$$G_{\text{rr}}(i, j) = \text{first_rr}(i, \text{key}[j]).\text{steps} + f(\text{first_rr}(i, \text{key}[j]).\text{id}, \text{key}[j+1]). \quad (36.3)$$

We note that `first_ll`(i, c) and `first_rr`(i, c) returns the first match on left (right) of the ring for character c .

LeetCode 516. Longest Palindromic Subsequence

Dynamic Programming Let $f(i, j)$ denote the longest palindrome for `s`[$i : j$]. Then we have

$$f(i, j) = \begin{cases} 1 & \text{if } i = j \\ 2 & \text{else if } i + 1 = j \text{ and } \text{s}[i] = \text{s}[j] \\ 1 & \text{else if } i + 1 = j \text{ and } \text{s}[i] \neq \text{s}[j] \\ 2 + f(i + 1, j - 1) & \text{else if } i + 1 < j \text{ and } \text{s}[i] = \text{s}[j] \\ \max(f(i + 1, j) + f(i, j - 1)) & \text{else if } i + 1 < j \text{ and } \text{s}[i] \neq \text{s}[j] \end{cases} \quad (37.1)$$

Then the final answer is $f(0, n - 1)$, where $n = \text{std::size}(s)$. The overall running time is $O(n^2)$.

LeetCode 517. Super Washing Machines

Greedy First, we need to check if the total number of machines is divisible by n . If not, then it is not possible to produce the desired outcome and therefore return -1 . Otherwise, we first compute the average number of clothes that are supposed to be in each machine, `avg`, keep track for each machine i ,

$$L_i = \max(0, (i + 1) \cdot \text{avg} + \text{RMQ}(0, i - 1)), \quad (38.1)$$

$$R_i = \max(0, (n - (i + 1)) \cdot \text{avg} + \text{RMQ}(i + 1, n - 1)), \quad (38.2)$$

$$T_i = R_i + L_i. \quad (38.3)$$

Note that L_i represents the total number of clothes needed to be transferred from `machines`[$i + 1 : -1$] to `machines`[$0 : i - 1$] if any to balance the clothes count and similarly R_i represents the total number of clothes needed to be transferred from `machines`[$0 : i - 1$] to `machines`[$i + 1, -1$] to balance the clothes. We claim that the final answer must be one of the T_i 's. This is because suppose otherwise there doesn't exist a washing machines whose total transfer T_i is not the answer, then there must be the cases where some machine A moved once machine B is fixed and then machine B moved once while A is fixed. This is a contradiction since A and B can be chosen at the same time. Hence, therefore the final answer is then $\max_i \{T_i\}$.

LeetCode 523. Continuous Subarray Sum

Prefix Sum Note that

$$\left(\sum_{p=i}^j \text{nums}[p] \right) \bmod k = \left(\sum_{p=0}^j \text{nums}[p] - \sum_{p=i-1}^j \text{nums}[p] \right) \bmod k \quad (39.1)$$

$$= \left[\left(\sum_{p=0}^j \text{nums}[p] \right) \bmod k \right] - \left[\sum_{p=i-1}^j \text{nums}[p] \bmod k \right]. \quad (39.2)$$

Therefore, it follows that

$$\sum_{p=i}^j \text{nums}[p] \mid k \iff \left[\left(\sum_{p=0}^j \text{nums}[p] \right) \bmod k \right] = \left[\sum_{p=i-1}^j \text{nums}[p] \bmod k \right]. \quad (39.3)$$

So we need to compute the prefix sum mod of k of `nums` and use a hashmap to check.

LeetCode 600. Non-negative Integers without Consecutive Ones

Dynamic Programming Let $f(k)$ denote the count of numbers without consecutive ones for k digits number that starts with 0. Then take $k = 6$ for example, there are only two portions are valid choices, namely $000000 \sim 011111$ and $010000 \sim 010111$. This is because any number that starts with $11\dots$ does not meet the condition. Note that the count of numbers that satisfy the condition in $000000 \sim 011111$ is essentially $f(5)$ because the first zero is fixed and similarly the count for $010000 \sim 010111$ is $f(4)$. Therefore, it follows that

$$f(k) = \begin{cases} 1 & \text{if } k = 0 \\ 2 & \text{else if } k = 1 \\ f(k-2) + f(k-1) & \text{o.w.} \end{cases} \quad (40.1)$$

Then let $g(i)$ denote the count of numbers that satisfy the condition for `nums[i : -1]`; we have that

$$g(i) = \begin{cases} 1 & \text{if } i = 0 \text{ and } \text{binary}[i] = 0 \\ 2 & \text{else if } i = 0 \text{ and } \text{binary}[i] = 1 \\ f(i) + g(i-1) & \text{else if } i > 0 \text{ and } \text{binary}[i] = 1 \text{ and } \text{binary}[i-1] = 0, \\ f(i) + f(i-1) & \text{else if } i > 0 \text{ and } \text{binary}[i] = 1 \text{ and } \text{binary}[i-1] = 1 \\ g(i-1) & \text{else if } i > 0 \text{ and } \text{binary}[i] = 0 \end{cases} \quad (40.2)$$

where `binary` is the binary representation of `num`. Then final answer is then $g(n-1)$, where $n = \text{std::size}(\text{binary})$.

LeetCode 624. Maximum Distance in Arrays

Prefix Max/Min First, we note that if we drop the requirement that the two elements has to be from distinct arrays then the maximum distance has to be the $\max(\text{flatten}(\text{arrays})) - \min(\text{flatten}(\text{arrays}))$. On the other hand, if we require the two elements to be from distinct arrays, then we have to exclude the some cases. One thing that is invariant is that the at least one of $\max(\text{flatten}(\text{arrays}))$ and $\min(\text{flatten}(\text{arrays}))$ will be involved in the resulting optimal distance, which one could prove using an exchange argument. So let $f(i)$ denote the maximum distance produced with one participating element in `array[i]`, then

$$f(i) = \begin{cases} \max(P_{\min}(i), P_{\max}(i), S_{\min}(i), S_{\max}(i)) & \text{if } 0 < i < n-1 \\ \max(S_{\min}(i), S_{\max}(i)) & \text{else if } i = 0 \\ \max(P_{\min}(i), P_{\max}(i)) & \text{else if } i = n-1 \end{cases}, \quad (41.1)$$

where as

$$P_{\min}(i) = |\max(\text{array}[i]) - \min(\text{flatten}(\text{array}[0 : i-1]))|, \quad (41.2)$$

$$P_{\max}(i) = |\min(\text{array}[i]) - \max(\text{flatten}(\text{array}[0 : i-1]))|, \quad (41.3)$$

$$S_{\max}(i) = |\max(\text{array}[i]) - \min(\text{flatten}(\text{array}[i+1 : n-1]))|, \quad (41.4)$$

$$S_{\min}(i) = |\min(\text{array}[i]) - \max(\text{flatten}(\text{array}[i+1 : n-1]))|, \quad (41.5)$$

which can be computed efficiently $O(n)$ where $n = \text{std::size}(\text{arrays})$ using prefix min and max arrays and the sorted structure of `arrays`. Code

LeetCode 629. K Inverse Pairs Array

Dynamic Programming Let $f(i, j)$ be the number of arrays from 1 to i that contains j inverse pairs. Then by noting that placing $(i+1)$ on x positions away from the right of $[1, \dots, i]$ creates x more inverse

pairs, we have that

$$f(i, j) = \begin{cases} 1 & \text{if } i = 1 \text{ and } j = 0 \\ 0 & \text{else if } i = 1 \text{ and } j > 0 \\ 1 & \text{else if } j = 0 \\ \sum_{m=0}^{\min(i-1, j)} f(i-1, j-m) & \text{o.w.} \end{cases}. \quad (42.1)$$

Such an algorithm has a running time complexity of $O(n^2k)$, which is unacceptable for the size of the input of the problem. So it is necessary to come up with an optimization scheme. Note that when $1 < i \leq j$, we have that

$$f(i, j) = \sum_{m=0}^{\min(i-1, j)} f(i-1, j-m) = \sum_{m=0}^{i-1} f(i-1, j-m), \quad (A)$$

$$f(i, j-1) = \sum_{m=0}^{\min(i-1, j-1)} f(i-1, j-1-m) = \sum_{m=1}^i f(i-1, j-m). \quad (B)$$

Subtracting (B) from (A) yields

$$f(i, j) - f(i, j-1) = \sum_{m=0}^{i-1} f(i-1, j-m) - \sum_{m=1}^i f(i-1, j-m) = f(i-1, j) - f(i-1, j-i), \quad (42.2)$$

which implies that

$$f(i, j) = f(i-1, j) + f(i, j-1) - f(i-1, j-i). \quad (42.3)$$

On the other hand, if $i > j > 0$, we have that

$$f(i, j) = \sum_{m=0}^{\min(i-1, j)} f(i-1, j-m) = \sum_{m=0}^j f(i-1, j-m), \quad (C)$$

$$f(i, j-1) = \sum_{m=0}^{\min(i-1, j-1)} f(i-1, j-1-m) = \sum_{m=1}^j f(i-1, j-m). \quad (D)$$

Subtracting (D) from (C) yields that

$$f(i, j) - f(i, j-1) = f(i-1, j), \quad (42.4)$$

which implies that

$$f(i, j) = f(i-1, j) + f(i, j-1). \quad (42.5)$$

Combining together, we have that

$$f(i, j) = \begin{cases} 0 & \text{if } i = 1 \text{ and } j > 0 \\ 1 & \text{else if } i = 1 \text{ and } j = 0 \\ 1 & \text{else if } j = 1 \\ f(i-1, j) + f(i, j-1) & \text{else if } i > j \\ f(i-1, j) + f(i, j-1) - f(i-1, j-i) & \text{else if } i \leq j \end{cases}. \quad (42.6)$$

Then the running time complexity is reduced to $O(nk)$.

LeetCode 639. Decode Ways II

Dynamic Programming Let $f(i)$ denote the number of ways to decode $\mathbf{s}[0 : i]$. Then

$$f(i) = \begin{cases} 9 & \text{if } i = 1 \text{ and } \mathbf{s}[i] = * \\ 1 & \text{else if } i = 1 \text{ and } \mathbf{s}[i] \in [1, \dots, 9] \\ 1 & \text{else if } i = 0 \\ 9 \cdot f(i-1) + 15 \cdot f(i-2) & \text{else if } \mathbf{s}[i] = * \text{ and } \mathbf{s}[i-1] = * \\ 9 \cdot f(i-1) + 9 \cdot f(i-2) & \text{else if } \mathbf{s}[i] = * \text{ and } \mathbf{s}[i-1] = 1 \\ 9 \cdot f(i-1) + 6 \cdot f(i-2) & \text{else if } \mathbf{s}[i] = * \text{ and } \mathbf{s}[i-1] = 2 \\ 9 \cdot f(i-1) & \text{else if } \mathbf{s}[i] = * \text{ and } \mathbf{s}[i-1] \in \{0\} \cup \{3, \dots, 9\} \\ 2 \cdot f(i-2) & \text{else if } \mathbf{s}[i] = 0 \text{ and } \mathbf{s}[i-1] = * \\ f(i-2) & \text{else if } \mathbf{s}[i] = 0 \text{ and } \mathbf{s}[i-1] \in \{1, 2\} \\ f(i-1) + 2 \cdot f(i-2) & \text{else if } \mathbf{s}[i] \in \{1, \dots, 6\} \text{ and } \mathbf{s}[i-1] \in \{*, 1, 2\} \\ f(i-1) & \text{else if } \mathbf{s}[i] \in \{1, \dots, 6\} \text{ and } \mathbf{s}[i-1] \in \{0\} \cup \{3, \dots, 9\} \\ f(i-1) + f(i-2) & \text{else if } \mathbf{s}[i] \in \{7, \dots, 9\} \text{ and } \mathbf{s}[i-1] \in \{*, 1\} \\ f(i-1) & \text{else if } \mathbf{s}[i] \in \{7, \dots, 9\} \text{ and } \mathbf{s}[i-1] \in \{0\} \cup \{2, \dots, 9\} \end{cases} . \quad (43.1)$$

The final answer is $f(n-1)$, where $n = \text{std::size}(\mathbf{s})$. The total running complexity is $O(n)$. Note that there are cases in which \mathbf{s} is not a valid input. We deal with these cases by exceptions.

LeetCode 646. Maximum Length of Pair Chain

Dynamic Programming First, we sort \mathbf{pairs} by lexicographical order. Let $f(i)$ denote the maximum length of the pair chained ending with $\mathbf{pairs}[i]$. Then we have

Patience Sorting

LeetCode 647. Palindromic Substrings

Dynamic Programming Let $f(i, j)$ denote if $\mathbf{s}[i : j]$ is palindrome or not. Then we have

$$f(i, j) = \begin{cases} \text{true} & \text{if } i = j \\ \text{true} & \text{else if } i + 1 = j \text{ and } \mathbf{s}[i] = \mathbf{s}[j] \\ \text{false} & \text{else if } i + 1 = j \text{ and } \mathbf{s}[i] \neq \mathbf{s}[j] \\ f(i+1, j-1) & \text{else if } \mathbf{s}[i] = \mathbf{s}[j] \\ \text{false} & \text{else if } \mathbf{s}[i] \neq \mathbf{s}[j] \end{cases} . \quad (45.1)$$

Then the final answer is $\sum_{(i,j) \in [0, \dots, n-1]^2} \mathbb{I}(f(i, j) = \text{true})$.

LeetCode 650. 2 Keys Keyboard

Dynamic Programming Let $f(i)$ denote the minimum number of operations to reach i copies of **A**. Then it follows that

$$f(i) = \begin{cases} 0 & \text{if } i = 1 \\ i & \text{else if } i \text{ is prime} \\ \min_{j \in [1, \dots, i] \text{ and } i|j} f(i/j) + j & \text{else if } i \text{ is not prime} \end{cases} , \quad (46.1)$$

where $f(i/j) + j$ comes from $f(i/j) + \underbrace{1}_{\text{copy}} + \underbrace{j-1}_{\text{paste}}$. The overall running time complexity is $O(N^2)$.

LeetCode 651. 4 Keys Keyboard

Dynamic Programming Let $f(i)$ denote the maximum number of characters with a max of i operations. Note that to achieve maximum characters the last operations must be a pressing **A** or pressing **Ctrl+V**. Then it follows that

$$f(i) = \begin{cases} 1 & \text{if } i = 1 \\ 2 & \text{else if } i = 2 \\ \max(f(i-1) + 1, \max_{2 \leq j \leq i-2} \{f(j) \cdot (i - (j+2) + 1)\}) & \text{o.w.} \end{cases} \quad (47.1)$$

The final answer is $f(N)$. The overall running time complexity is $O(N^2)$.

LeetCode 656. Coin Path

Dynamic Programming Let $f(i)$ denote the minimum path to reach n from **A**[i]. Then

$$f(i) = \begin{cases} \mathbf{A}[i] & \text{if } i = n - 1 \\ \min_{j \in \{i+1, \dots, i+B\}} \{\mathbf{A}[i] + f(j)\} & \text{o.w.} \end{cases} \quad (48.1)$$

The final answer is then constructed by reconstructing from f . The running time complexity is $O(nB)$.

LeetCode 664. Strange Printer

Dynamic Programming Let $f(i, j)$ denote the minimum operations to print **s**[$i : j$]. Note that there are two options for the first step of **s**[$i : j$] : 1. just print one letter; 2. print all occurrences of **s**[i] up to some $k \in [i+1, j]$. Then, it we have that

$$f(i, j) = \begin{cases} 1 & \text{if } i = j \\ 0 & \text{else if } i > j \\ 1 & \text{else if } i+1 = j \text{ and } \mathbf{s}[i] = \mathbf{s}[j] \\ 2 & \text{else if } i+1 = j \text{ and } \mathbf{s}[i] \neq \mathbf{s}[j] \\ \min(1 + f(i+1, j), \min_{k \in [i+1, \dots, j] \text{ and } \mathbf{s}[i] = \mathbf{s}[k]} \{f(i, k-1) + f(k+1, j)\}) & \text{o.w.} \end{cases} \quad (49.1)$$

LeetCode 723. Candy Crush

Simulation with Two Pointers Use two pointer method to mark consecutive entries in each row and each column. To do so, one can either maintain a separate matrix of boolean flags indicating whether the corresponding entry in **board** is to be deleted or negate the value in **board** directly as a flag. In our implementation, we choose the latter approach and the corresponding procedures are encapsulated in **mark_row()** and **mark_col()**. The crush procedure is implemented in **crush()**, which is routine. We will also implement a function **drop()** to simulate the gravity phenomena, which also uses a two pointer approach. Alternatively, one could also explicitly use a double ended queue to filter out the crushed candies column by column and reinsert the filtered result back into **board** starting from the bottom of each column. Code

LeetCode 746. Min Cost Climbing Stairs

Dynamic Programming Let $f(i)$ denote the minimum cost to climb to level i . Then we have

$$f(i) = \begin{cases} \min(f(i-1) + \text{cost}[i-1], f(i-2) + \text{cost}[i-2]) & \text{if } i > 1 \\ 0 & \text{else if } i \in \{0, 1\} \end{cases} \quad (51.1)$$

Then the desired answer is then $f(n)$, where $n = \text{std::size}(\text{cost})$.

Code

LeetCode 788. Rotated Digits

LeetCode 877. Stone Game

Dynamic Programming Let $f(i, j)$ denote the difference between the numbers of stones between Alex and Lee if they are to pick from $\text{piles}[i : j]$ with Alex picks first. Then note that because each player is playing optimally, $f(i, j)$ is also equal to the difference when Lee picks first. Then it follows that

$$f(i, j) = \begin{cases} \max(\text{piles}[i], \text{piles}[j]) - \min(\text{piles}[i], \text{piles}[j]) & \text{if } i + 1 = j \\ \max(\text{piles}[i] - f(i+1, j), \text{piles}[j] - f(i, j-1)) & \text{o.w.} \end{cases} \quad (53.1)$$

Then the final answer is $f(0, n-1) > 0$, where $n = \text{std::size}(\text{piles})$.

LeetCode 902. Number At Most N Given Digit Set

LeetCode 983. Minimum Cost For Tickets

Dynamic Programming Let $f(i)$ denote the minimum costs to cover $\text{days}[0 : i]$. Then we have

$$f(i) = \begin{cases} \max(\text{costs}[0], \text{costs}[1], \text{costs}[2]) & \text{if } i = 0 \\ \max(\text{costs}[i] + f(\text{next_lower}(\text{days}[0 : i-1], \text{days}[i] - \text{pass}[i])) & \text{else if } i \neq \emptyset, i > 0, \\ 0 & \text{else if } i = \emptyset \end{cases} \quad (55.1)$$

where $\text{next_lower}(A, x)$ return last element in array A that is strictly less than x ; we note that this procedure can be implemented in $O(\log n)$ times using binary search. Thus, the overall time complexity is $O(n \log n)$, where $n = \text{std::size}(\text{days})$.

LeetCode 1012. Numbers With Repeated Digits

LeetCode 1346. Check if N and Its Double Exist

HashSet Create a hashset arr_set to store non-zero unique elements in arr . Then we count the number of zeros in arr , if there are at least two zeros, we return true immediately; otherwise we loop through arr_set check if the condition is met.

Code

LeetCode 1351. Count Negative Numbers in a Sorted Matrix

Binary Search Let $[R, C] = \text{dimension}(\text{grid})$. We count row by row. If $\text{grid}[r][0] < 0$ for some $r \in [0, R-1]$, then we add all the items in the submatrix $\text{grid}[r : R-1][0 : C-1]$ to the final result; otherwise, we will use binary search to find the first negative entry c_N in each row and add to the final result $C - c_N$. The count process could be implemented as a function $f(r)$, where $f(i)$ means the number of negative entries

when counting from row i . Then

$$f(r) = \begin{cases} C - c_N + f(r+1) & \text{if } \min(\text{grid}[r]) < 0 \\ 0 & \text{else if } \min(\text{grid}[r]) > 0 \text{ or } r = R. \\ (R-r) \cdot C & \text{else if } \text{grid}[r][0] < 0 \end{cases} \quad (58.1)$$

And the desired answer is $f(0)$.

Code

LeetCode 1365. How Many Numbers Are Smaller Than the Current Number

Bucket Sort with Prefix Sum Create a bucket array, `bucket`, to store all the values in `nums` and then create range query module of `bucket` using prefix sum, which we name as `RSQ`. Let A denote the desired array, then we have

$$A[i] = \begin{cases} 0 & \text{if } \text{nums}[i] = 0 \\ \text{RSQ}(0, \text{nums}[i] - 1) & \text{otherwise} \end{cases}. \quad (59.1)$$

The overall runtime complexity is $O(n)$ and memory complexity is $O(n)$.

Code

LeetCode 1380. Lucky Numbers in a Matrix

Implementation Create two arrays, `row_min` and `col_max`, to store the minimum (maximum) of each row (column). Then we iterate through every entries `matrix` to check for lucky numbers.

Code

LeetCode 1385. Find the Distance Value Between Two Arrays

Binary Search We first let `sorted_arr2` be a sorted copy of `arr2`. Then for each $i \in [0, n_1 - 1]$, where $n_2 = \text{std::size}(\text{arr1})$, we use binary search to locate l, r such that $\text{sorted_arr2}[l : r] \subseteq [\text{arr1}[i] - d, \text{arr1}[i] + d]$ and add the element count of $\text{sorted_arr2}[l : r]$ to the final result.

Code

LeetCode 1389. Create Target Array in the Given Order

Simulation Just simply create a `std::vector<int>` and simulate the process using `insert`.

Code

LeetCode 1394. Find Lucky Integer in an Array

Implementation Create a hashmap `freq_map` to count the occurrences of each number in `arr`. Then filter out the keys in `freq_map` that satisfies the condition into a list, and return the maximum the list if the list is non-empty or -1 if otherwise.

Code

LeetCode 1397. Find All Good Strings

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Appendices

A. Sorting Algorithm

A.1. Patient Sorting

Consider the following game: deal cards c_1, c_2, \dots, c_n into piles according to two rules

- Can't place a higher valued card onto a lower valued card;
- Can form a new pile and put a card onto it.

And the goal is to form as few piles as possible.

Greedy Algorithm In the natural order, place each card on the leftmost pile that fits. Note that by construction, at any stage during the greedy algorithm, top cards of piles increase from left to right.

A.1.1. Connection with LIS

Lemma A.1 (Weak Duality). *In any legal game of the patience, the number of piles is larger than or equal to any increasing subsequence.*

Proof. Note that cards within a pile form a decreasing subsequence and any sequence can use at most one card from each pile. \square

Lemma A.2 (Strong Duality). *Min number of piles is equal to LIS. More over, the greedy algorithm finds both.*

Proof. Each card maintains a pointer to top card in previous pile. The we can follow pointers to obtain IS whose length is equal to the number of piles. The by the weak duality lemma above, the sequence if one member of the optimal solution set of the LIS problem. \square

Implementations This patient sorting algorithm could be implemented in $O(n \log n)$ running time by using an array of stack to represent the piles and binary search to bind the left most pile.

B. Elementary Data Structures

B.1. Monotone Stack

B.1.1. Find k -element subsequence that is lexicographically largest

B.1.2. Find [previous/next] [greater/smaller] element

C. String Algorithms

C.1. Prefix Function

Given a string s of size n , the prefix function $\pi(i) : [0, \dots, n-1]$ is defined as

$$\pi[i] = \max_{k=0, \dots, i} \{k : s[0 : k-1] = s[i - (k-1) : i]\}. \quad (\text{C.1})$$

In words, it represents the length of the longest prefix substring in $s[0 : i]$ that is also a suffix.