

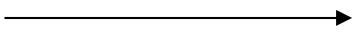

# Introduction to Wireless and Mobile Networking

## Lecture 2: Wireless PHY and Radio Propagation Model

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Review and More Overview

# What is special about "wireless"?

- Wireless channel
  - Electromagnetic
  - Channel variation 
  - Signal power attenuation 
  - Sharing wireless medium
- What will happen if we apply the same wired-line networking protocol in wireless environments?

Radio propagation  
model

# What is special about “mobile”?

- User mobility → where are you now?!
  - Mobility management
  - Handoff
- Tradeoffs
  - Precision of user location
    - Time to find your exact location
  - Signaling overhead
    - Cost of updating your location
  - Power consumption
    - Updating your location consumes battery power

# How do you categorize technologies?

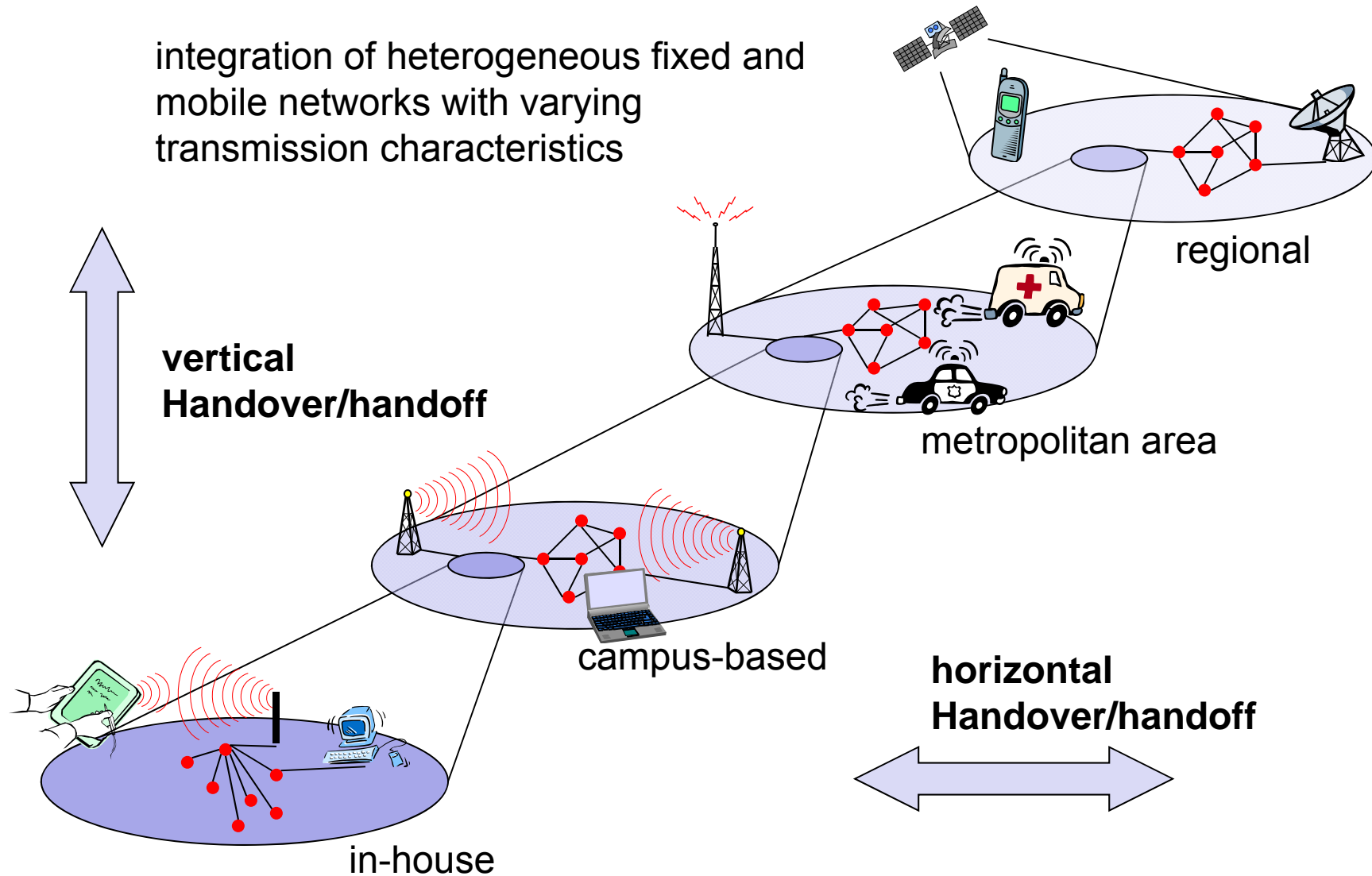
- Mobility - speed
  - Static, pedestrian, vehicular, high-speed rail
- Range
  - 1m, 10m, 100m, 1km, 10km, satellite
- Radio environment
  - Open space or Obstacles on transmission path
- Design goal
  - Low power v.s. high throughput

# Two campaigns of networks

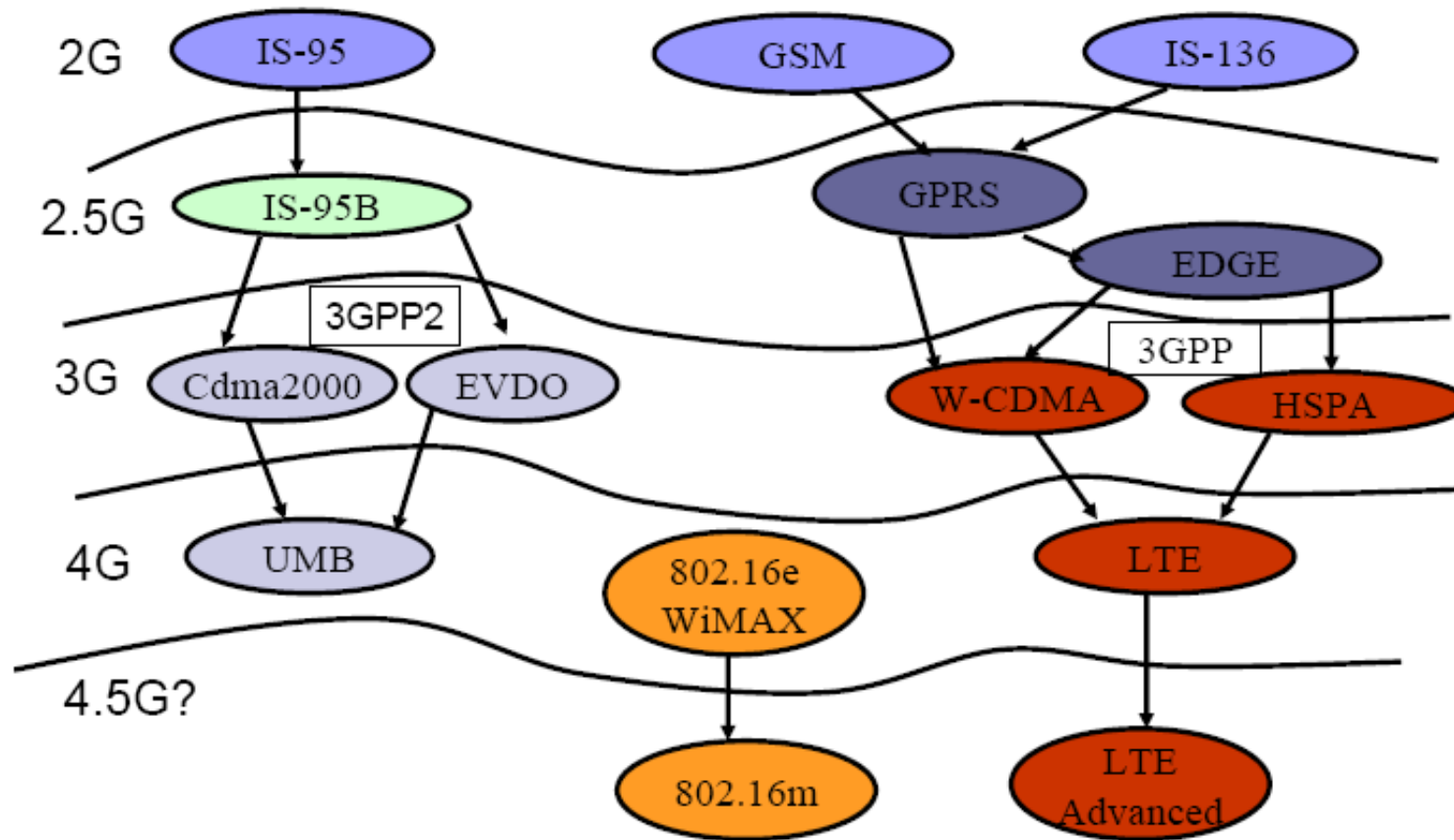
- Computer network (Internet)
  - TCP, IP, HTTP, IEEE 802.11
  - Standardization: IETF (Internet Engineering Task Force)
    - Internet drafts, RFC documents, Internet standards
- Telecommunications networks (telephony networks)
  - PSTN (your wireline telephony network)
  - SS7 (signaling network of PSTN)
  - Extend to GSM, 3G wireless telephony networks
  - Standardization: UMTS, 3GPP, 3GPP2
- Future trends
  - Confluence of these two types of networks
  - The boundary becomes more blurry

# Overlay Networks

integration of heterogeneous fixed and mobile networks with varying transmission characteristics



# Cellular Network Evolution





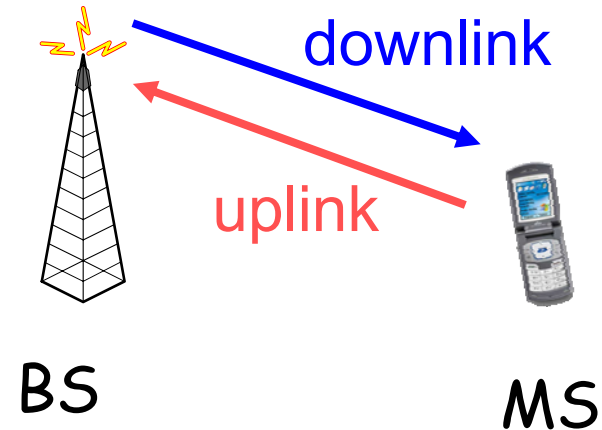
# Standards

- IETF
  - TCP, IP, Mobile IP, HTTP, SIP
- 3GPP
  - UMTS, HSDPA, HSUPA, LTE (Long Term Evolution)
- 3GPP2
  - Cdma2000, Ultra Mobile Broadband (UMB)
- IEEE 802 (PHY/MAC)
  - 802.11 WLAN (wireless local area network)
  - 802.15 WPAN (wireless personal area network)
  - 802.16 WMAN (wireless metropolitan area network)
  - 802.20 (mobile wireless broadband access)
  - 802.21 (handoff over heterogeneous networks)
- ITU

# Basics of communications, capacity, and channels

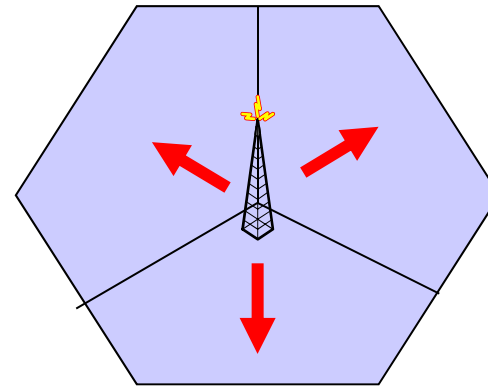
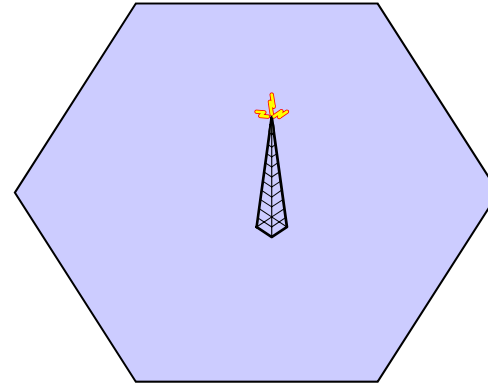
# Terminologies: BS & MS

- Base station (BS)
  - Access point (AP)
- Mobile station (MS)
  - SS (Subscriber station)
  - MT (mobile terminal)
  - MN (mobile node)
- Downlink
  - Forward link
  - BS → MS
- Uplink
  - Reverse link
  - MS → BS



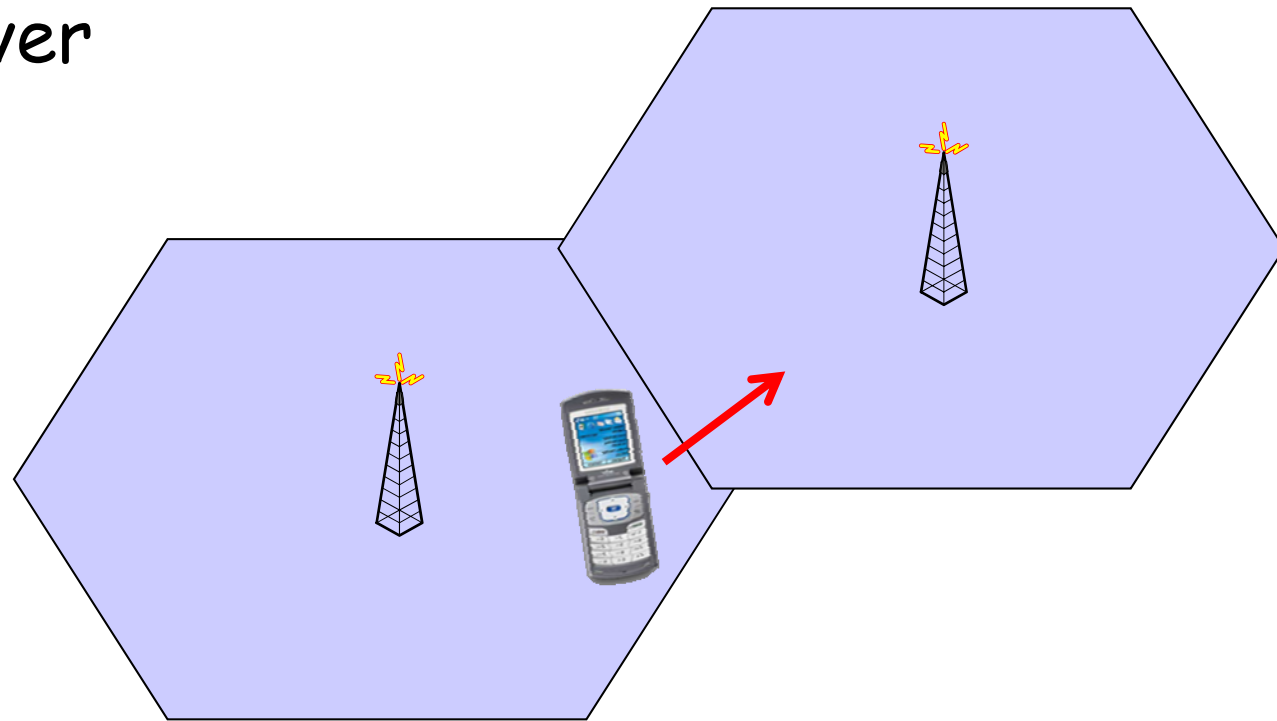
# Terminologies: cell and sector

- Cell
  - Coverage area of a BS
- Sector
  - Partial area of a cell that is served by a directional antenna

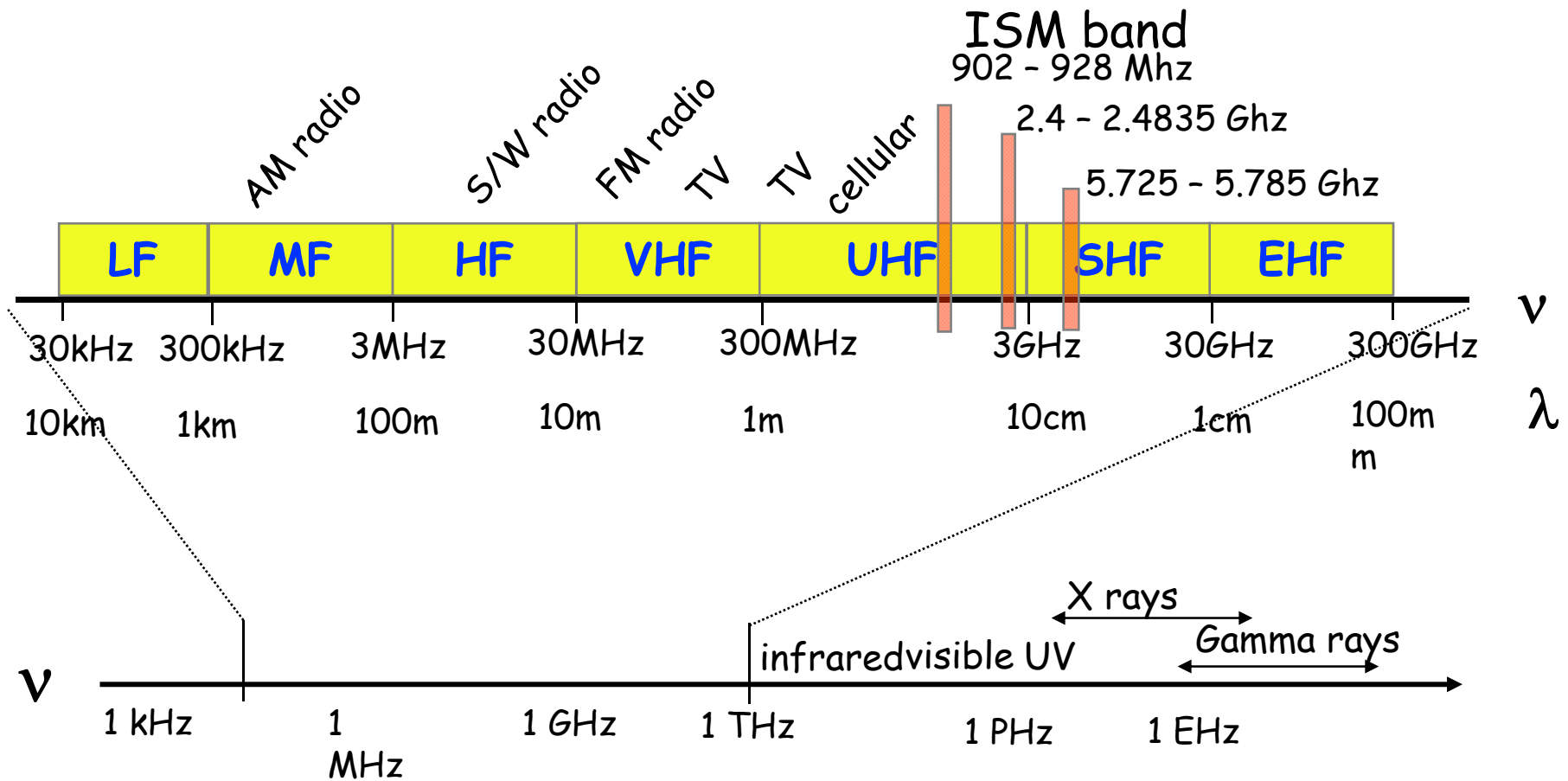


# Terminology: handoff

- Handoff
  - MS changes serving BS due to movement or radio channel variation
  - handover



# Radio Spectrum



# Wireless Spectrum Regulation

- Wireless spectrum is regulated by governments
  - Regulation has significant impact on technology advancement and business development
  - Who should use the spectrum? How should it be used?
  - Auction for licenses (e.g. 3G license)
- Organization
  - NCC (Taiwan)
  - FCC (USA)

# UNITED STATES FREQUENCY ALLOCATIONS THE RADIO SPECTRUM

## RADIO SERVICES COLOR LEGEND

AIRBORNE MOBILE	INTER SATELLITE	RADIOASTRONOMY
AIRBORNE MOBILE SATELLITE	LAND MOBILE	RADIODETERMINATION SATELLITE
AIRBORNE RADIOAGNATION	LAND MOBILE SATELLITE	RADIOAGNATION
AMATEUR	MARITIME MOBILE	RADIOLOCATION SATELLITE
AMATEUR SATELLITE	MARITIME MOBILE SATELLITE	RADIOAGNATION
BROADCASTING	MARITIME RADIOAGNATION	RADIOAGNATION SATELLITE
BROADCASTING SATELLITE	METEOROLOGICAL AID	SPACE OPERATION
EARTH EXPLORATION SATELLITE	METEOROLOGICAL SATELLITE	SPACE RESEARCH
FIXED	MOBILE	STANDARD FREQUENCY AND TIME SIGNAL
FIXED SATELLITE	MOBILE SATELLITE	STANDARD FREQUENCY AND TIME SIGNAL SATELLITE

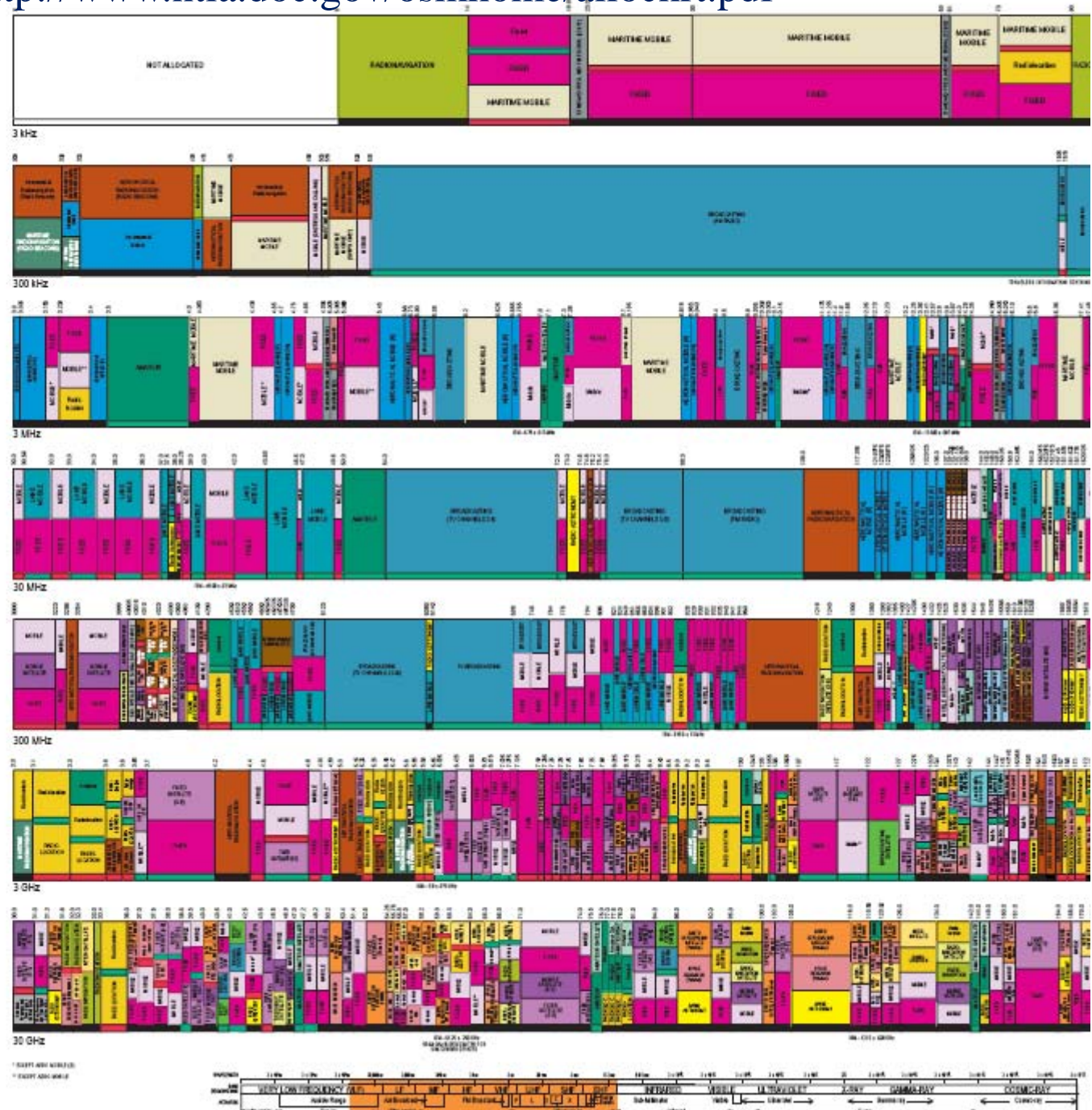
## ACTIVITY CODE

GOVERNMENT EXCLUSIVE	GOVERNMENT OR GOVERNMENT SHARED
NON-GOVERNMENT EXCLUSIVE	

## ALLOCATION USAGE DESIGNATION

SERVICE	EXAMPLE	DESCRIPTION
Primary	F1-D2	Coastal Station
Secondary	M1-B	1st Class with lower class letters

This chart is a graphic representation of the Table of Frequency Allocations used by the FCC and NTIA. It is not a legal document. It is intended to provide a visual summary of the Table of Frequency Allocations. It is not intended to be used as a legal document. It is intended to provide a visual summary of the Table of Frequency Allocations. It is not intended to be used as a legal document.





# Frequency and Wavelength

- $c = \lambda f$ 
  - $c$ : speed of light
  - $\lambda$ : wavelength
  - $f$ : frequency
- Example:
  - AM radio with frequency 1710 kHz
    - What's the wavelength? Ans: 175m
    - What's the period? Ans: 584 ns

# dB

- Decibels
  - $10 \log_{10} (x)$
  - Power in decibels
    - dB
    - $Y \text{ dB} = 10 \log_{10} (x \text{ Watt})$
  - Power ratio in decibels
    - dB
    - Power  $P_1, P_2$  in Watt
    - $10 \log_{10} (P_1/P_2)$
  - Example:
    - Input power 100W and output power 1W
    - What's the power ratio in decibel? Ans: 20dB

# dBm

- dBm
  - Reference power is 1 mW
  - $10 \log_{10} (\text{Watts}/10^{-3})$
  - Example:
    - 0 dB = 30 dBm = 1 Watt
- Summary
  - $P (\text{dBW}) = 10 \log (P/1 \text{ Watt})$
  - $P (\text{dBm}) = 10 \log (P/1 \text{ mWatt})$

# Gain and Attenuation in dB or dBm

- Gain/attenuation in dB
  - $10 \log_{10} (\text{output power}/\text{input power})$ 
    - $\text{Gain(dB)} = \text{Pout(dB)} - \text{Pin(dB)}$
  - Gain:  $\text{Pout} > \text{Pin}$
  - Attenuation  $\text{Pout} < \text{Pin}$
- Gain/attenuation in dBm
  - $X(\text{dBm}) + Y(\text{dB}) = ??(\text{dB}) = ??(\text{dBm})$
  - $X(\text{dBm}) - Y(\text{dB}) = ??(\text{dB}) = ??(\text{dBm})$
  - Example:
    - Input power is 2dBm, system gain is 5dB
    - What's the output power? Ans: 7dBm
  - Notice: is it dB or dBm?

# Wireless communication system

- Antenna gain
  - Transmitter antenna
  - Receiver antenna
- Wireless channel attenuation



- Questions: how do you represent the relationships between  $P_{tx}$  and  $P_{rx}$  ?
  - in dB
  - in Watt

# Signal-to-Noise ratio

- S/N
  - $\text{SNR} = \text{signal power(Watt)} / \text{noise power(Watt)}$
  - Signal-to-Noise power ratio
  - Relate to the performance of communications systems
    - Bit-error probability
    - Shannon capacity
- SNR in dB
  - $S/N(\text{dB}) = 10 \log_{10} (\text{S/N power ratio})$
  - $10 \log_{10} (\text{signal power(Watt)} / \text{noise power(Watt)})$

# Noise, Interference, SNR

- SNR

- $(\text{signal power})/(\text{noise power})$
- Noise: thermal noise

- SIR

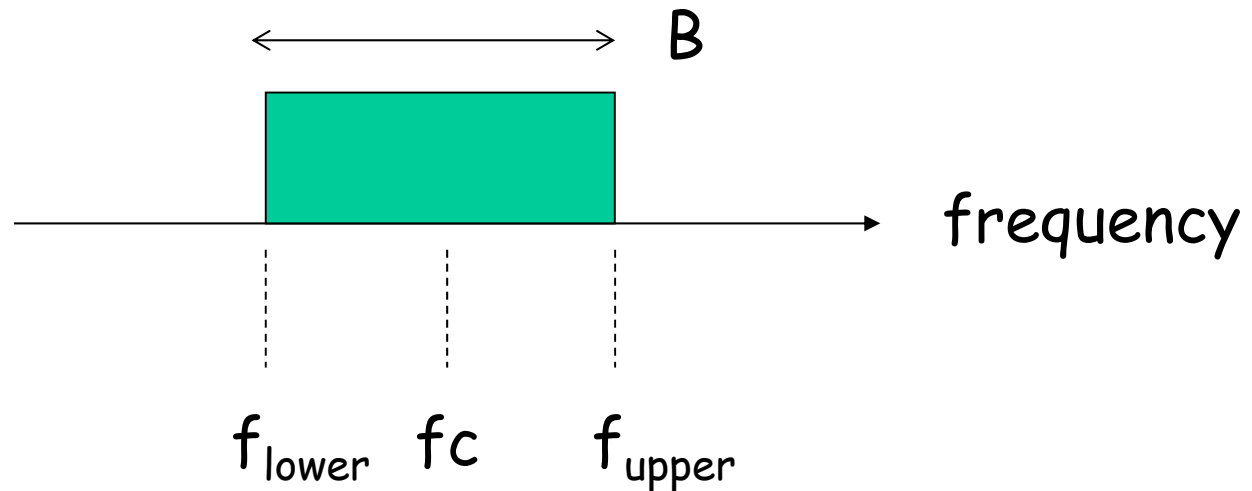
- Signal-to-Interference
  - Sometimes known as C/I (carrier-to-interference ratio)
- $(\text{signal power})/(\text{interference power})$
- Interference: signals from other simultaneous communications

- SINR

- Signal-to-Interference-Plus-Noise ratio
- $(\text{signal power})/(\text{interference power} + \text{noise power})$

# Bandwidth

- $B = f_{\text{upper}} - f_{\text{lower}}$
- Carrier frequency:  $f_c$
- Example:
  - 802.11 2.4GHz ISM band (channel 1)
    - $f_{\text{upper}} = 2434 \text{ MHz}$
    - $f_{\text{lower}} = 2412 \text{ MHz}$
    - $f_c = 2423 \text{ MHz}$
    - $B = 22 \text{ MHz}$





# Thermal Noise

- Thermal noise power
  - $N = kT_N B$
  - N: power in Watt
  - k: Boltzman's constant =  $1.38 \times 10^{-23}$
  - $T_N$ : temperature (degree Kelvin)
  - B: bandwidth of channel (Hz)

# Bit Energy to Noise Ratio

- $E_b/N_0$ 
  - Energy per bit over the noise power spectral density
  - Related to SNR power ratio
  - Independent of bandwidth

# Relate $E_b/N_0$ to SNR

- $SNR = S/N$  (Watt/Watt)
- $E_b = S t_b$ 
  - $E_b$ : energy per bit (J)
  - $S$ : signal power (carrier power) (W)
  - $t_b$ : duration of a bit (s)
- $E_b/N_0 = (S/N_0) * t_b = (S/N_0) * (1/f_b)$
- $N_0 = N/B$ 
  - $N$ : total noise power (W)
  - $B$ : bandwidth (Hz)
- $E_b/N_0 = (S/N)(B/f_b)$

## $S/N$ (or $E_b/N_0$ )

- To compare systems, generally they should have the same transmitted  $S/N$  (or  $E_b/N_0$ )
- The  $S/N$  (or  $E_b/N_0$ ) at the input to the receiver will determine the system performance

## Example

- Find the  $E_b/N_0$  for a system operating at 2Mbps in a bandwidth of 1MHz. The carrier power is 0.1pW. The system noise temperature is 120K.
- Ans:
  - $E_b/N_0 = (S/N) * (B/f_b)$
  - $(S/N) = (0.1 * 10^{-12}) / \{(1.38 * 10^{-23})(120)(1 * 10^6)\}$
  - $(B/f_b) = (1 * 10^6) / (2 * 10^6)$
  - $E_b/N_0 = 30.2$
  - $E_b/N_0(\text{dB}) = 14.8\text{dB}$

# Capture model

- $SNR_{received} \geq SNR_{threshold}$ 
  - Minimum SNR requirement, given a target bit-error-rate (or frame-error-rate)

# Shannon Capacity

- Theoretical (upper) bound of communication systems
- $C = B \cdot \log_2 (1 + S/N)$ 
  - C: capacity (bits/s)
  - B: bandwidth (Hz)
  - S/N: linear Signal-to-Noise ratio
- How to evaluate the performance of a communication scheme?
  - How close to Shannon bound?
  - Spectral efficiency
    - bit/s/Hz

# Concepts Related to Channel Capacity

- Data rate
  - rate at which data can be communicated (bps)
- Bandwidth
  - the bandwidth of the transmitted signal as constrained by the transmitter and the nature of the transmission medium (Hertz)
- Noise
  - average level of noise over the communications path
- Error rate - rate at which errors occur
  - Error
    - transmit 1 and receive 0
    - transmit 0 and receive 1



# Shannon Capacity Formula

- Equation:  $C = B \log_2(1 + \text{SNR})$
- Represents theoretical maximum that can be achieved (in AWGN channel)
- In practice, only much lower rates achieved
  - Formula assumes white noise (thermal noise)
  - Impulse noise is not accounted for
  - Attenuation distortion or delay distortion not accounted for
    - Additive
    - White
    - Gaussian
    - Noise

# Nyquist Bandwidth

- For binary signals (two voltage levels)
  - $C = 2B$
- With multilevel signaling
  - $C = 2B \log_2 M$ 
    - $M$  = number of discrete signal or voltage levels

## Example of Nyquist and Shannon Formulations

- Spectrum of a channel between 3 MHz and 4 MHz ;  $\text{SNR}_{\text{dB}} = 24 \text{ dB}$ 
  - What's the SNR value?
- Using Shannon's formula
  - What's the maximum capacity?

## Example of Nyquist and Shannon Formulations

- Spectrum of a channel between 3 MHz and 4 MHz ;  $\text{SNR}_{\text{dB}} = 24 \text{ dB}$

$$B = 4 \text{ MHz} - 3 \text{ MHz} = 1 \text{ MHz}$$

$$\text{SNR}_{\text{dB}} = 24 \text{ dB} = 10 \log_{10}(\text{SNR})$$

$$\text{SNR} = 251$$

- Using Shannon's formula

$$C = 10^6 \times \log_2(1 + 251) \approx 10^6 \times 8 = 8 \text{ Mbps}$$

# Example of Nyquist and Shannon Formulations

- How many signaling levels are required in modulation?

# Example of Nyquist and Shannon Formulations

- How many signaling levels are required?

$$C = 2B \log_2 M$$

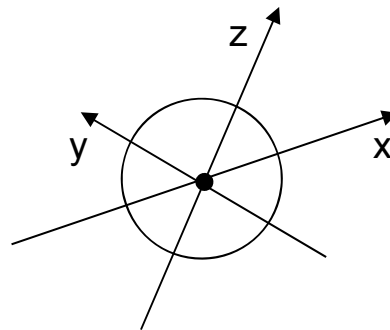
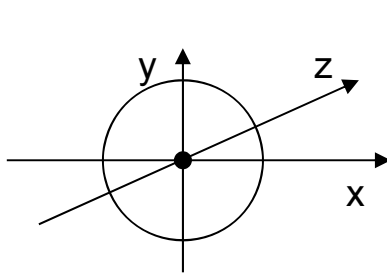
$$8 \times 10^6 = 2 \times (10^6) \times \log_2 M$$

$$4 = \log_2 M$$

$$M = 16$$

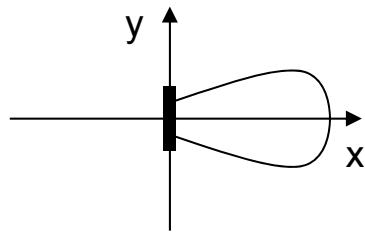
# Antennas: isotropic radiator

- Isotropic radiator: equal radiation in all directions
  - only a theoretical reference antenna
- Real antennas always have directive effects (vertically and/or horizontally)
- Radiation pattern: measurement of radiation around an antenna

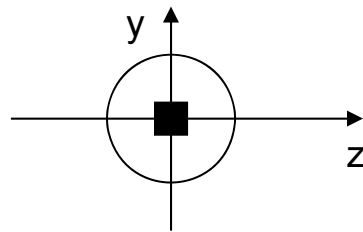


ideal  
isotropic  
radiator

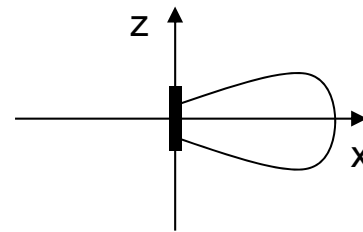
# Antennas: directed and sectorized



side view (xy-plane)

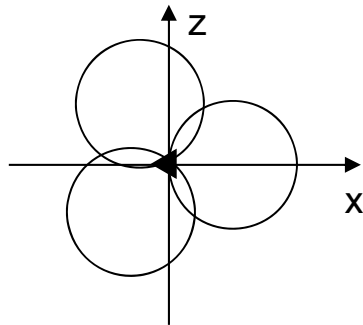


side view (yz-plane)

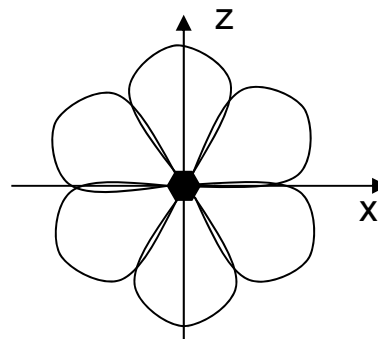


top view (xz-plane)

directed  
antenna



top view, 3 sector



top view, 6 sector

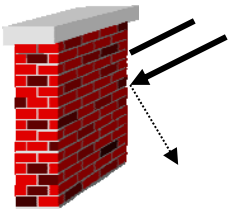
sectorized  
antenna



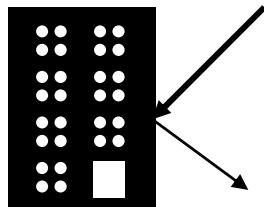
# Radio propagation model

# Signal propagation

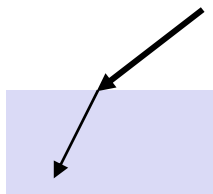
- Propagation in free space always like light (straight line)
- Receiving power proportional to  $1/d^2$  in free-space
- Receiving power additionally influenced by
  - fading (frequency dependent)
  - shadowing
  - reflection at large obstacles
  - refraction depending on the density of a medium
  - scattering at small obstacles
  - diffraction at edges



shadowing



reflection



refraction

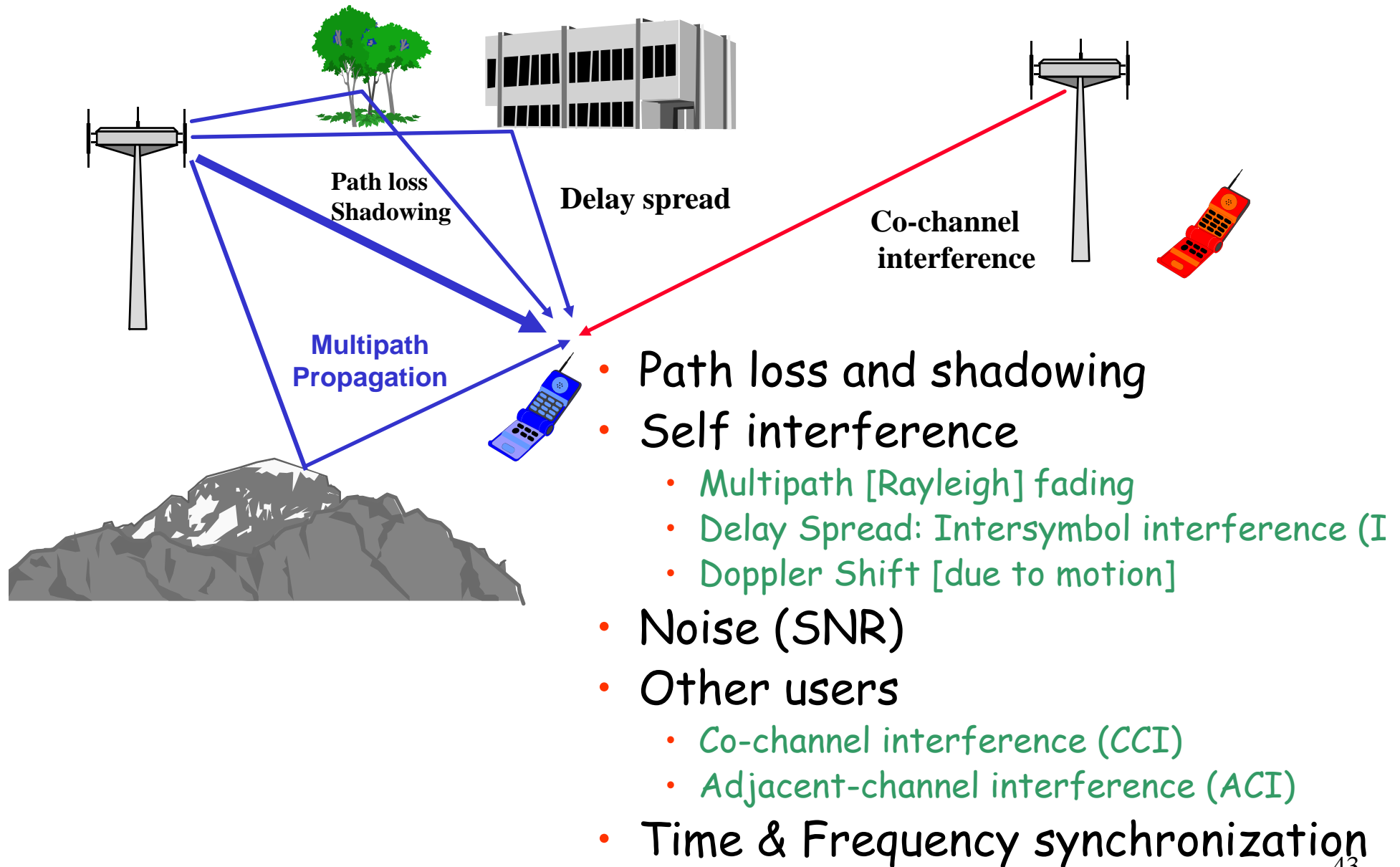


scattering



diffraction

# Wireless Channel

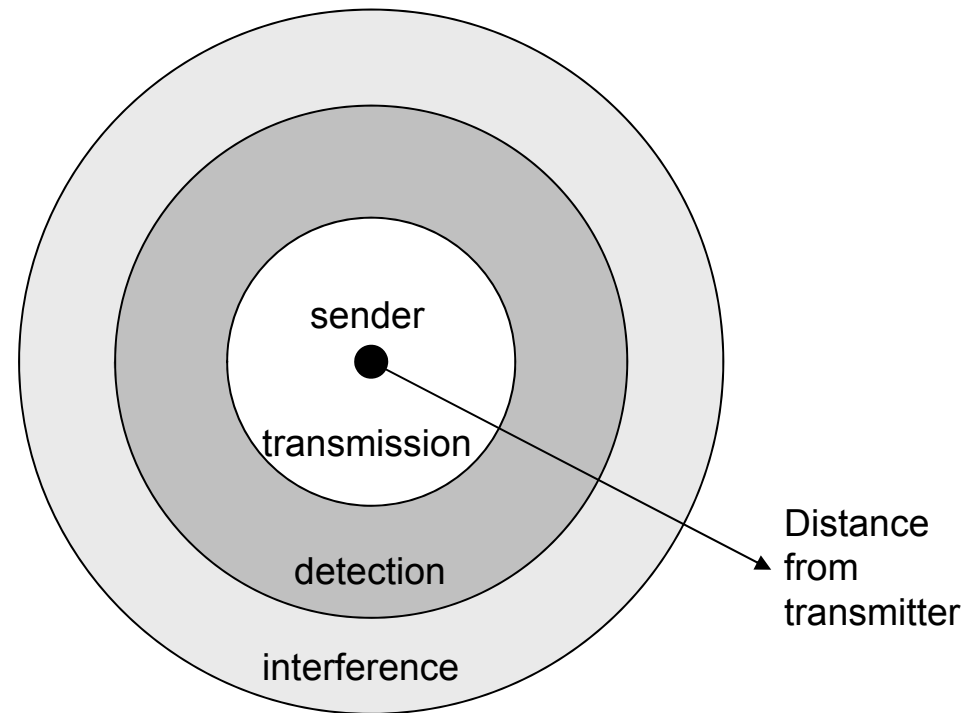


# The Effects of Multipath Propagation

- Multiple copies of a signal may arrive at different phases
  - If phases add destructively, the signal level relative to noise declines, making detection more difficult
- Intersymbol interference (ISI)
  - One or more delayed copies of a pulse may arrive at the same time as the primary pulse for a subsequent bit

# Signal Propagation Ranges

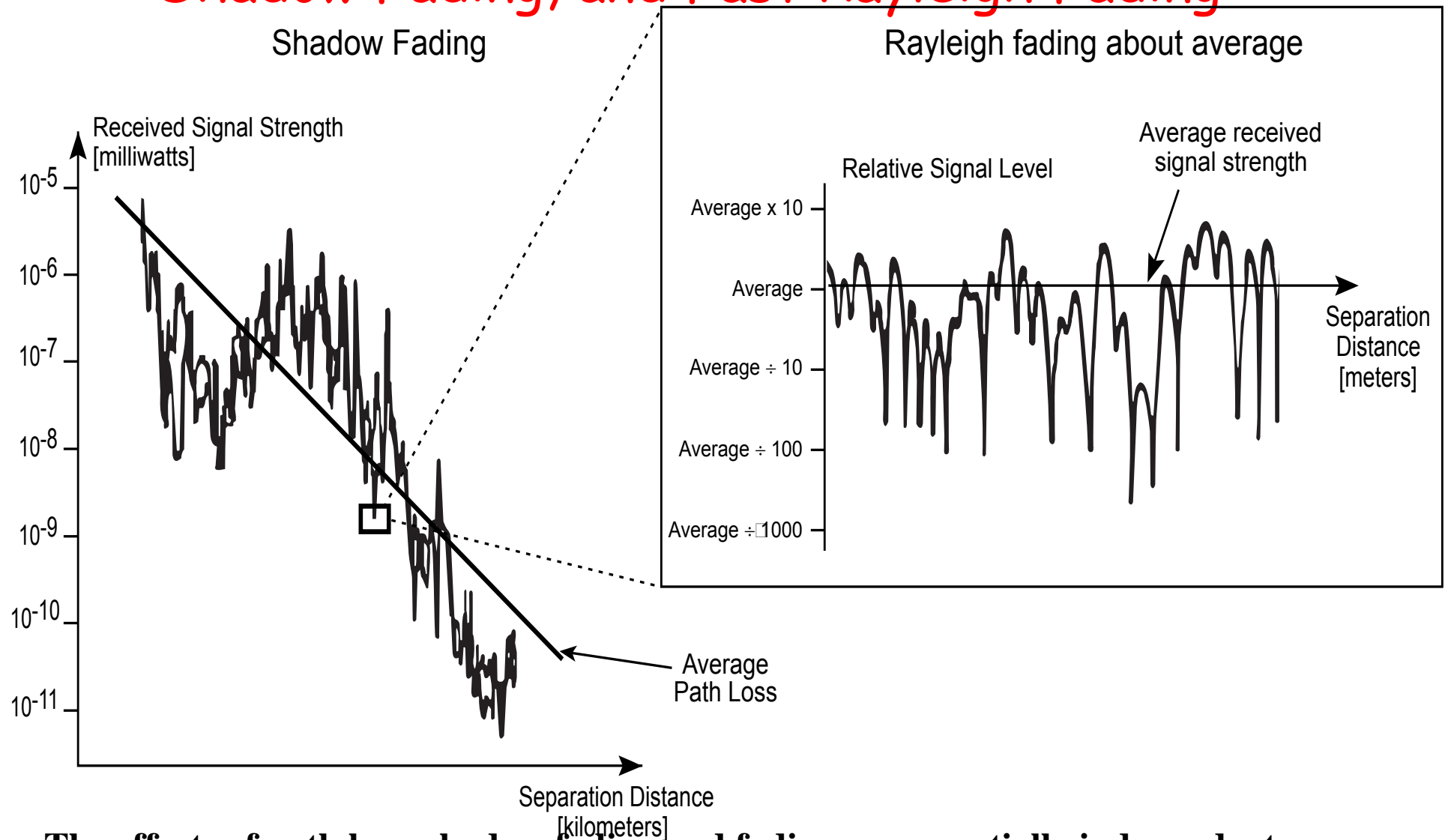
- **Transmission range**
  - communication possible
  - low error rate
- **Detection range**
  - detection of the signal possible, but communication may not be possible due to high error rate
- **Interference range**
  - signal may not be detected
  - signal adds to the background noise



# Radio Propagation Models

- Three components
  - Path-loss (long-term average)
    - Radio signal attenuation due to transmission over a certain distance
    - Depend on the distance
  - Shadowing (large time-scale variation)
    - Signal attenuation due to penetration of buildings and walls.
    - Log-normal distribution
  - Fading (small time-scale variation)
    - Due to multi-path transmission (reflection creates multiple radio paths)
    - Rayleigh distribution, Rician distribution

# Three-Part Propagation Model: Path Loss, Slow Shadow Fading, and Fast Rayleigh Fading



**The effects of path loss, shadow fading and fading are essentially independent and multiplicative**

# Radio Propagation Models

- Signal power at receiver: 3 components
  - Path-loss  $g(d)$
  - Log-normal shadowing  $10^{\frac{x}{10}}$
  - Rayleigh fading  $\alpha^2$

$$P_R = \alpha^2 10^{\frac{x}{10}} g(d) P_T G_T G_R$$



# Path-loss

- Path-loss

- Denoted as  $g(d)$

$$\overline{P}_R = g(d)P_T G_T G_R$$

- Represent average values (local mean power of area within several meters)

$$g(d) \propto d^{-n}$$

- In general received signal strength is proportional to  $d^{-n}$

- $n$ : path-loss exponent
- $k$ : constant
- $n=2 \sim 8$  in typical propagation scenarios
- $n=4$  is usually assumed in cellular system study

- Example: Free-space model

- $P_r = (P_t G_t G_r \lambda^2) / (16\pi^2 d^2) = (P_t G_t G_r) (\lambda / 4\pi d)^2$
- Proportional to  $d^{-2}$  (i.e.  $n=2$ )

# Some more path-loss models

- Smooth transition model
- Two-ray-ground model
- Okumura-Hata model
- More models in telecom standard evaluation
  - E.g. 3GPP, IMT-2000, 802.16, EU WINNER project
  - Common ground to evaluate proposed schemes
  - Reflect the radio operation conditions (frequency, terminal speed, urban/rural)

# Smooth transition model

- Improvement over simple distance-power relationship

- $d^{-n}$

$$g(d) = d^{-n_1} \left(1 + \frac{d}{b}\right)^{-n_2}$$

- Typically,  $n$  is smaller value in near-field and is a greater value in far-field

- Empirical measurement

$$g(d) = d^{-n_1} \quad 0 \leq d \leq b$$

- Two-stage transition model

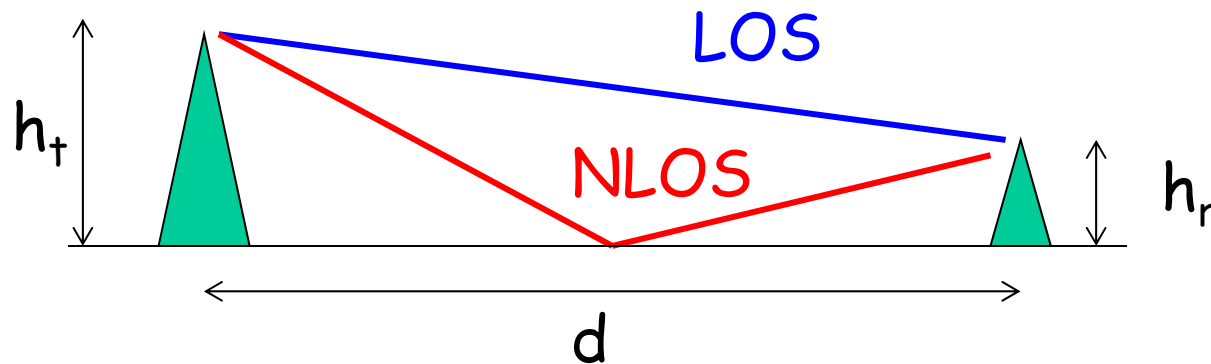
$$g(d) = d^{-n_1} (d / b)^{-n_2} \quad b \leq d$$

model	location	n1	n2	b(m)
Harley	Melbourne	1.5 to 2.5	3 to 5	150
Green	London	1.7 to 2.1	2 to 7	200-300
Pickholtz	Orlando	1.3	3.5	90

# Two-ray model

- 2 radio paths
  - LOS(line-of-sight)
  - NLOS(non-line-of-sight)
    - Reflection from the ground
- Proof?
  - Sum the power of these 2 EM waves

$$g(d) = \frac{(h_t h_r)^2}{d^4}$$



# Okumura-Hata model

- Model + measurement fit
- For macro-cellular network
  - Good fit for distance greater than 1km
  - 150-1500 MHz
- Practical use in cellular network planning
  - Extend by COST (European Cooperative for Scientific and Technical Research)
    - COST-231 model: suitable for urban microcells (1800-2000 MHz)

# COST-231 path-loss model

- Extend Hata model for PCS radio model in urban area

$$L(dB) = 46.3 + 33.9 \log f - 13.82 \log h_b - a(h_m) + [44.9 - 6.55 \log h_b] \log d + C_M$$

where  $a(h_m)$  = correction factor for mobile antenna heights given in Hata model

$f$  is in MHz,  $h_b$  and  $h_m$  is in m,  $d$  is in km

- Large cities

$$C_M = 0 \text{ dB}$$

- Small and medium size cities

$$C_M = 3 \text{ dB}$$

# Shadowing

- Shadowing is also known as shadow fading
- Received signal strength fluctuation around the mean value
  - Due to radio signal blocking by buildings (outdoor), walls (indoor), and other obstacles.
- Large time-scale variation
  - Signal fluctuation is much slower than multipath fading

# Log-normal distribution

- If logarithm of a variable  $x$  follows normal distribution, then  $x$  follows log-normal distribution
- Log-normal distribution for shadowing model
- P.d.f

$$f(x) = \frac{1}{\sqrt{2\pi}\sigma x} \exp\left(-\frac{(\ln x - \mu)^2}{2\sigma^2}\right)$$



# Log-normal shadowing

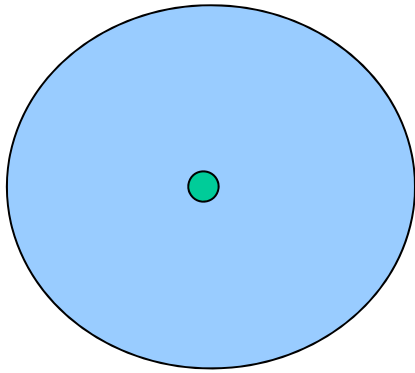
- Path loss component indicates the “expected” signal attenuation at distance  $d$ 
  - The actual signal attenuation at  $d$  depends on the environment. This is modeled with shadowing effect.
- Statistical model for shadowing
  - Received mean power of the radio signal fluctuates about the area-mean power with a log-normal distribution
  - Log-normal distribution (in Watt)
    - Normal distribution if measured in dB
- $x$  is a zero-mean Gaussian variable with standard deviation  $\sigma$  dB. Typically,  $\sigma = 6 \sim 10$  dB

$$P_R = \alpha^2 10^{\frac{x}{10}} g(d) P_T G_T G_R$$

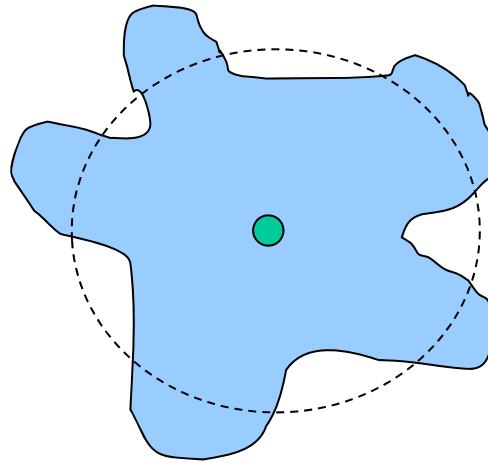
$$P_R(dB) = \bar{P}_R(dB) + S$$

$$S \sim N(0, \sigma^2), \quad \sigma = 4 \sim 10 dB$$

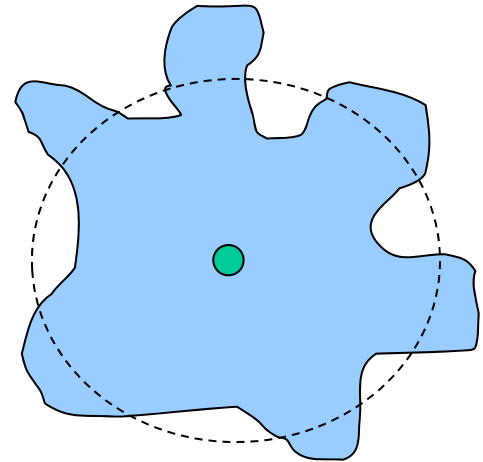
# Transmission range



Ideal case



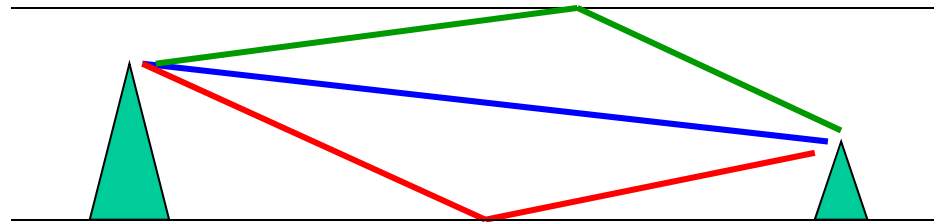
With shadowing



It might vary  
with time

# Multi-path fading

- Multiple radio propagation paths
  - Might include LOS path or not
  - Multiple copies of received signals
    - Different time delay
    - Different phase
    - Different amplitude
- More severe in urban area or indoor
- Characterized by
  - Rayleigh or Rician distribution
  - Delay spread profile

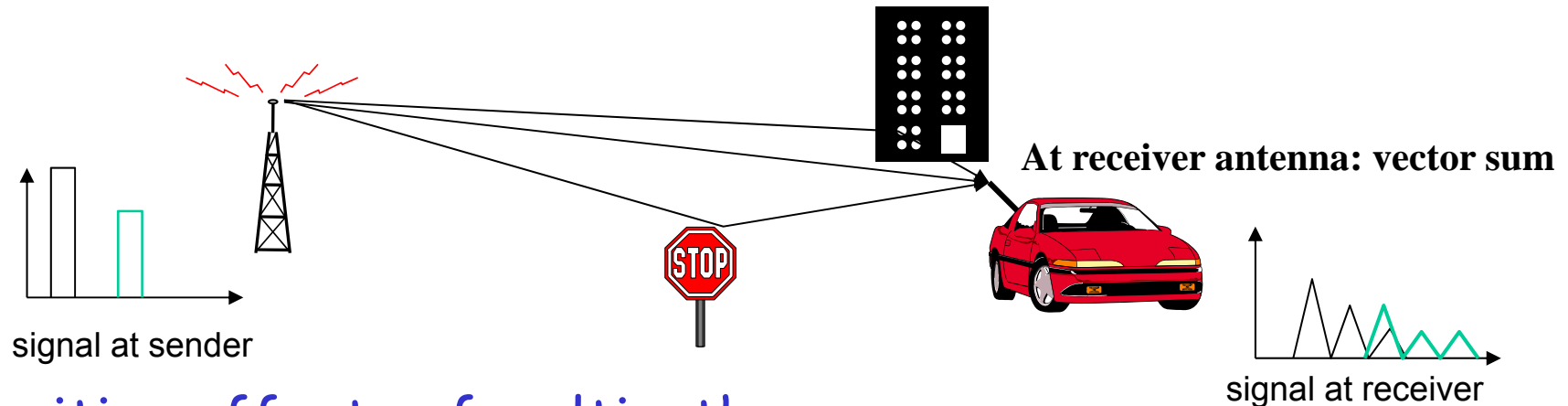


# Effects of multi-path signals

- Multiple copies of a signal may arrive at different phases
  - If phases add destructively, the signal level relative to noise declines, making detection more difficult
- Intersymbol interference (ISI)
  - One or more delayed copies of a pulse may arrive at the same time as the primary pulse for a subsequent bit

# Multipath Propagation

- Signals can take many different paths between sender and receiver due to reflection, scattering, diffraction



- Positive effects of multipath:
  - Enables communication even when transmitter and receiver are not in LOS conditions - allows radio waves effectively to go through obstacles by getting around them, thereby increasing the radio coverage area
  - By proper processing of the multipath signals, with smart or adaptive antennas, you can substantially increase the usable received power
    - With multiple antennas you capture energy that would otherwise be absorbed by the atmosphere and you can compensate for fades --- since it is highly unlikely that a signal will experience severe fading at more than one antenna

# Negative effects of small-scale fading

- Time dispersion or delay spread: signal is dispersed over time due signals coming over different paths of different lengths. This causes interference with “neighboring” symbols, this is referred to as **Inter Symbol Interference (ISI)**
- The signal reaches a receiver directly and phase shifted (due to reflections) as a distorted signal depending on the phases of the different paths; this is referred to as **Rayleigh fading**, due to the distribution of the fades. Rayleigh fading creates fast fluctuations of the received signal.
- Random frequency modulation due to **Doppler frequency shifts** on the different paths. Doppler shift is caused by the relative velocity of the receiver to the transmitter, leads to a frequency variation of the received signal.

# Delay spread and coherent bandwidth

- Reminder

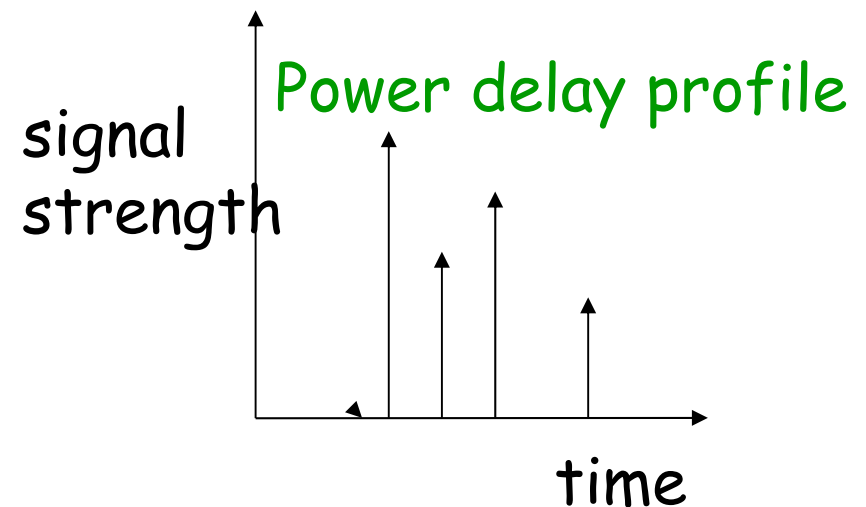
- duality property of signals in time-domain and frequency domain

- Time domain

- multi-path delay spread

- Frequency domain

- coherent bandwidth  $B_c$
- Highly correlated signals among these frequency components



# Power Delay Profile

- In order to compare different multi-path channels, the time dispersive power profile is treated as an (non-normalized) pdf from which the following are computed

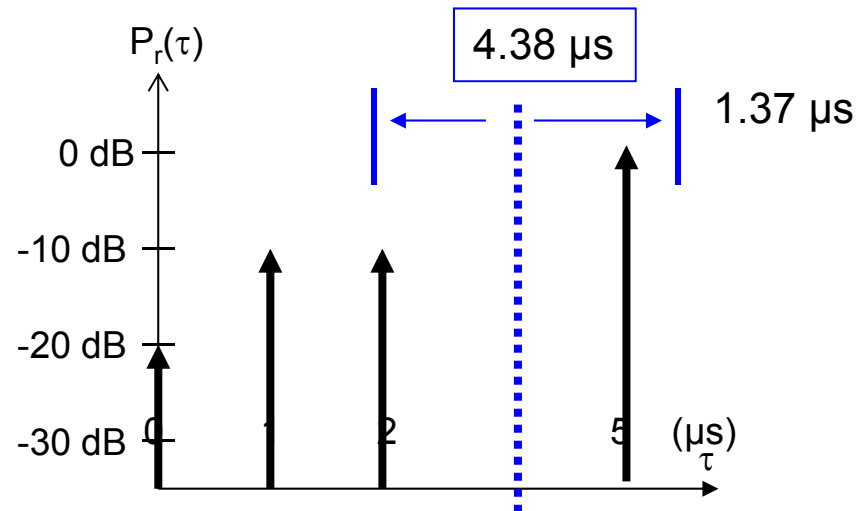
$$\text{Mean delay : } \bar{\tau} = \frac{\sum_k \alpha_k^2 \tau_k}{\sum_k \alpha_k^2}, \quad \text{Mean square delay : } \overline{\tau^2} = \frac{\sum_k \alpha_k^2 \tau_k^2}{\sum_k \alpha_k^2}$$

$$\text{The RMS Delay Spread : } \sigma_\tau = \sqrt{\overline{\tau^2} - (\bar{\tau})^2} \quad (2.25)$$

- Typical values of *rms delay spread* are on the order of microseconds in outdoor mobile radio channels [GSM specifies a maximum delay less than 20μs] and on the order of nanoseconds in indoor radio channels



# Example (Power delay profile)



Avg delay

$$\bar{\tau} = \frac{(1)(5) + (0.1)(1) + (0.1)(2) + (0.01)(0)}{[0.01 + 0.1 + 0.1 + 1]} = 4.38 \mu s$$

$$\bar{\tau}^2 = \frac{(1)(5)^2 + (0.1)(1)^2 + (0.1)(2)^2 + (0.01)(0)^2}{[0.01 + 0.1 + 0.1 + 1]} = 21.07 \mu s^2$$

$$\sigma_{\tau} = \sqrt{21.07 - (4.38)^2} = 1.37 \mu s \quad \longrightarrow \text{Delay spread}$$

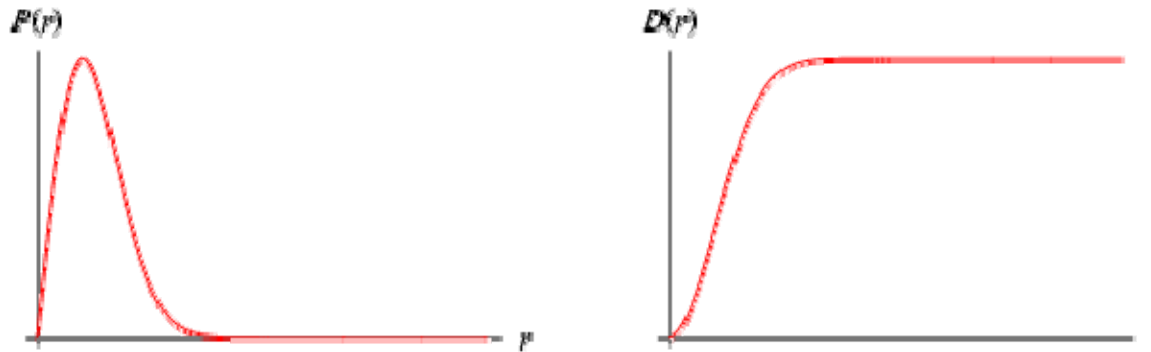
# Rayleigh fading

- “Amplitude” follows Rayleigh distribution
- How to derive it?

$$P_R = \alpha^2 10^{\frac{x}{10}} g(d) P_T G_T G_R$$

- Add several scaled and delayed versions of a sinusoid function

$$p_R(\alpha) = \frac{\alpha}{\sigma^2} e^{-\alpha^2 / 2\sigma^2}$$



# Rician Fading

- Some types of scattering environments have a **LOS (line-of-sight)** component
  - In addition to the NLOS scattered components
  - LOS dominant path may significantly decrease the depth of fading

$$p_r(x) = \frac{x}{\sigma^2} e^{-\frac{(x^2+s^2)}{2\sigma^2}} I_0\left(\frac{xs}{\sigma^2}\right) \quad x \geq 0$$

$$\text{where } s^2 = m_I^2(t) + m_Q^2(t)$$

and the zero order Bessel function of the first kind  $I_0(x)$  is defined by

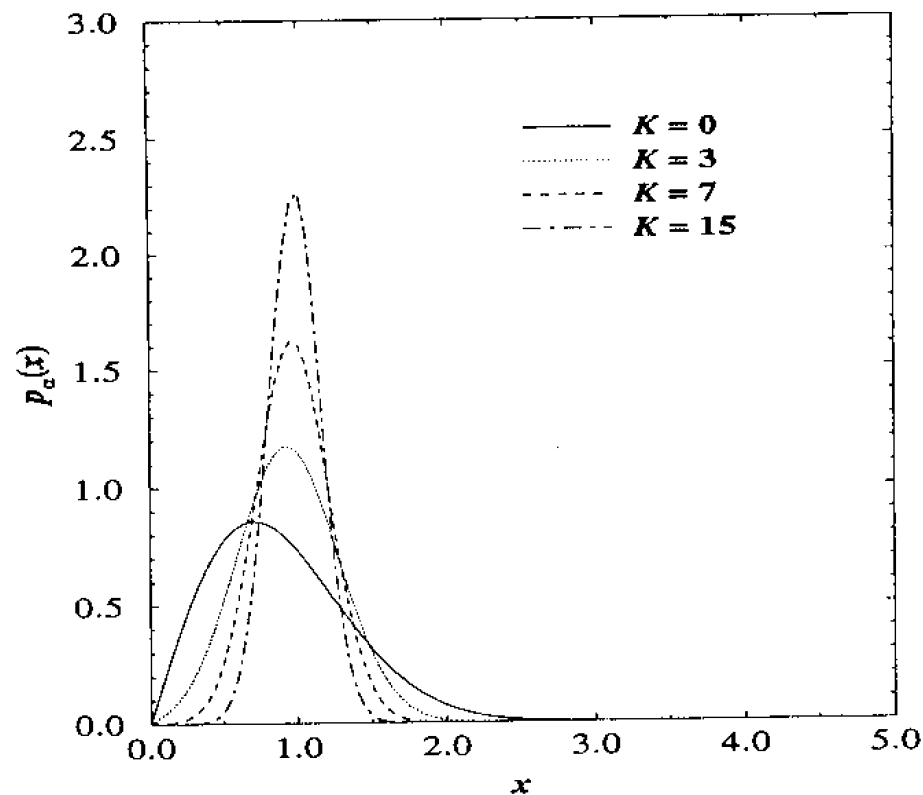
$$I_0(x) = \frac{1}{2\pi} \int_0^{2\pi} e^{-x \cos \theta} d\theta$$

- The **Rician factor, K**, is defined as the ratio of the specular (LoS) power to the scattered power

$$K = \frac{\text{power in the dominant (specular) path}}{\text{power in the scattered paths}} = \frac{s^2}{2\sigma^2}$$

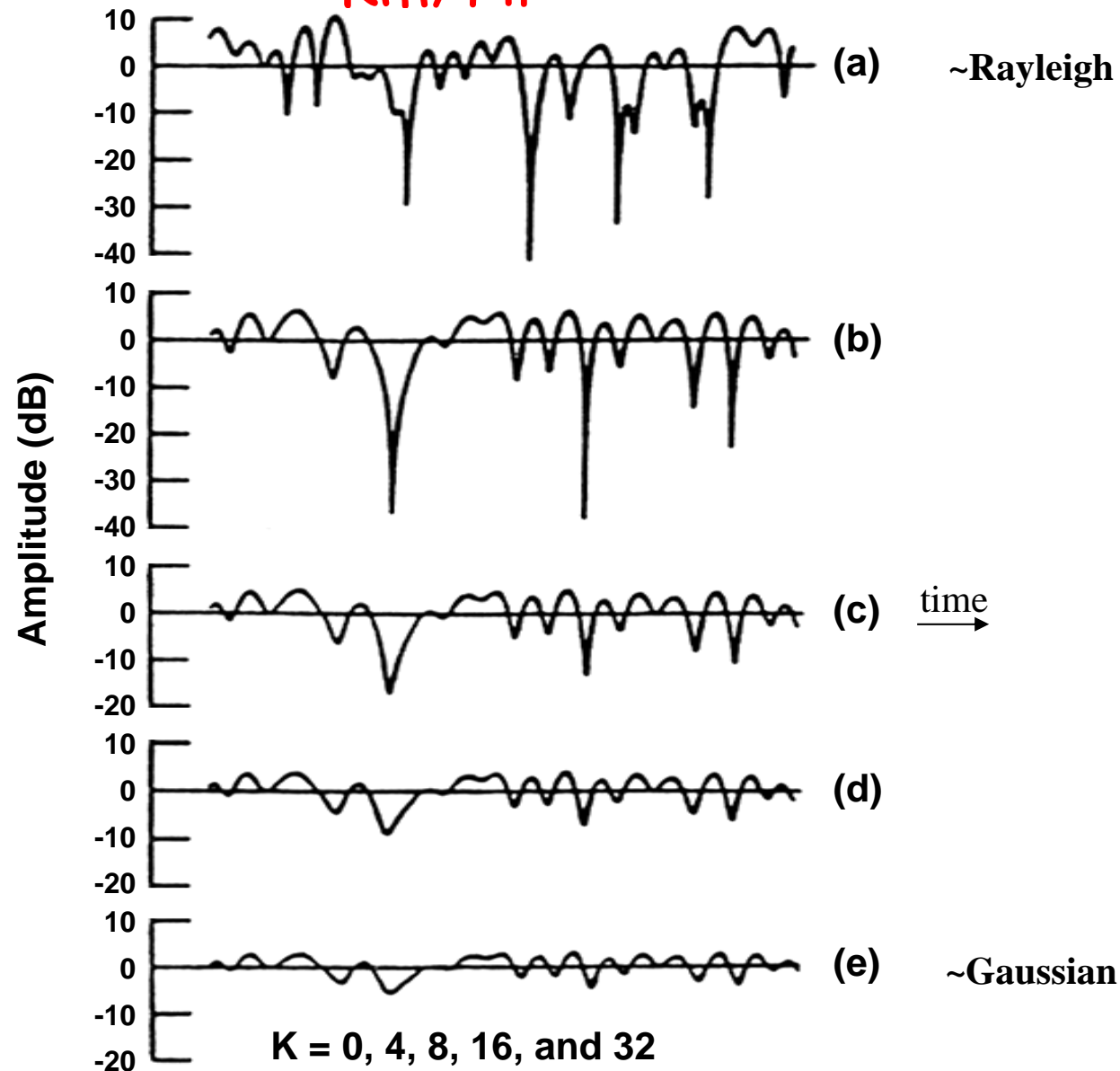
# Rician Fading

- When  $K=0$ , the channel exhibits Rayleigh fading and for  $K \rightarrow \infty$  there is no fading and the channel is Gaussian.
- Most channels can be characterized as either Rayleigh, Rician, or Gaussian --- with Rician being the most general case --- the Rician pdf is shown below.



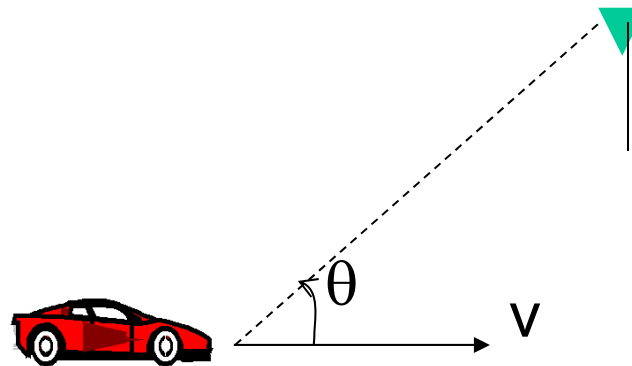
The Rice pdf for several values of  $K$

# Rician Fading Profiles for a Mobile at 90 Km/Hr



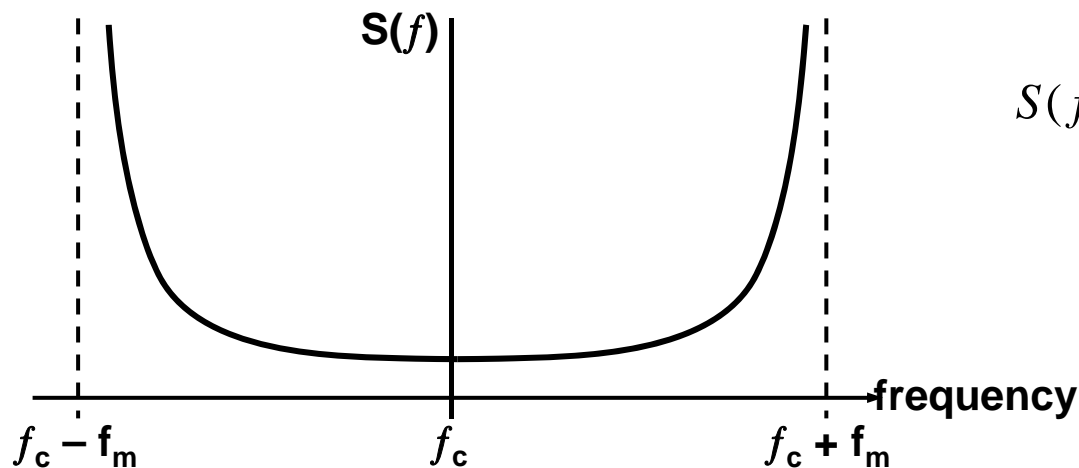
# Doppler Shift

- The motion of the mobile introduces a *Doppler (or frequency) shift* into the incident plane wave and is given by
  - $f_D = f_m \cos\theta_n$  Hz
  - where  $f_m = v/\lambda$  is the maximum Doppler shift that occurs when  $\theta = 0$ . Waves arriving from the direction of motion will experience a positive shift, while those arriving from the opposite direction will experience a negative shift.



# Doppler Shift Spectrum

- For isotropic 2-dimensional scattering and isotropic scattering
- The power spectrum of the received signal is limited in range to  $f_m$  about the carrier frequency)



$$S(f) = \frac{A}{4\pi f_m} \frac{1}{\sqrt{1 - \left(\frac{f - f_c}{f_m}\right)^2}} \quad |f - f_c| \leq f_m$$

# Effect of Doppler Shift

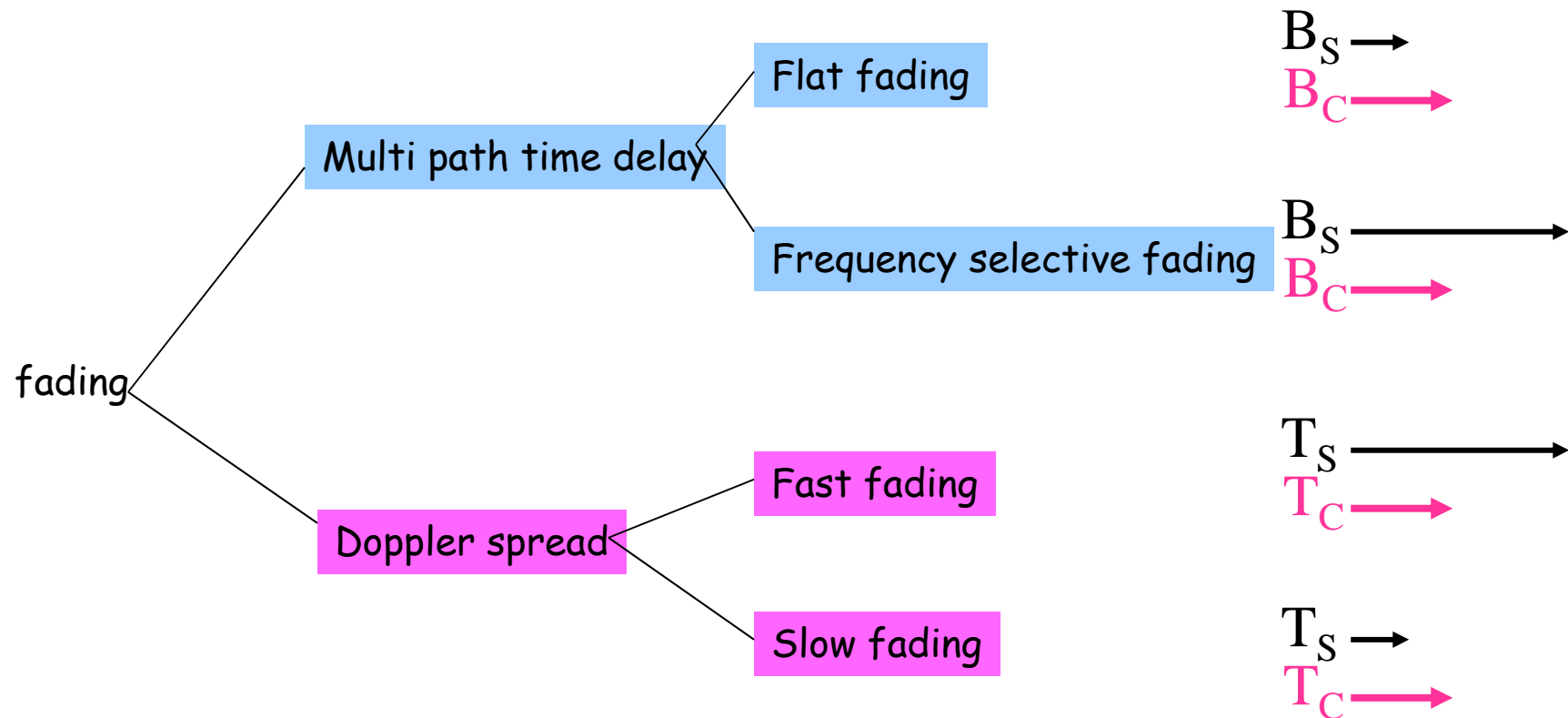
- Time-frequency duality
  - The Doppler effect produces frequency dispersion (an increase in the bandwidth occupancy)
  - This is equivalent to time-selective fading in the received signal
- Coherence Time
  - Doppler frequency shift (frequency domain) could be represented as coherence time (time domain)  $T_c$
  - Represent the time duration that channel is stable
  - If symbol time is smaller than  $T_c$ , it is called slow fading. Otherwise it is fast fading.



# Types of fading

- Summary: Fading (based on multipath time delay spread)
  - Signal is correlated or not (time)
  - Channel frequency response depends on frequency or not (frequency)
  - 1. Flat Fading
    - BW of signal  $<$  BW of channel
    - Delay spread  $<$  Symbol period
  - 2. Frequency Selective (non-flat) Fading
    - BW of signal  $>$  BW of channel
    - Delay spread  $>$  symbol period
- Summary: Fading (based on Doppler spread)
  - Channel varies faster or slower than signal symbol (time)
  - High or low frequency dispersion (frequency)
  - 1. Slow Fading
    - Low Doppler spread
    - Coherence time  $>$  Symbol period
    - Channel variations slower than baseband signal variations
  - 2. Fast Fading
    - High Doppler spread
    - Coherence time  $<$  symbol period (time selective fading)
    - Channel variations faster than baseband signal variations

# Small scale fading



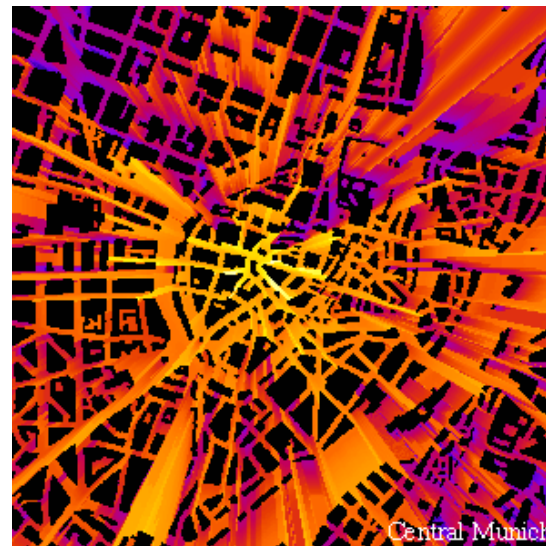
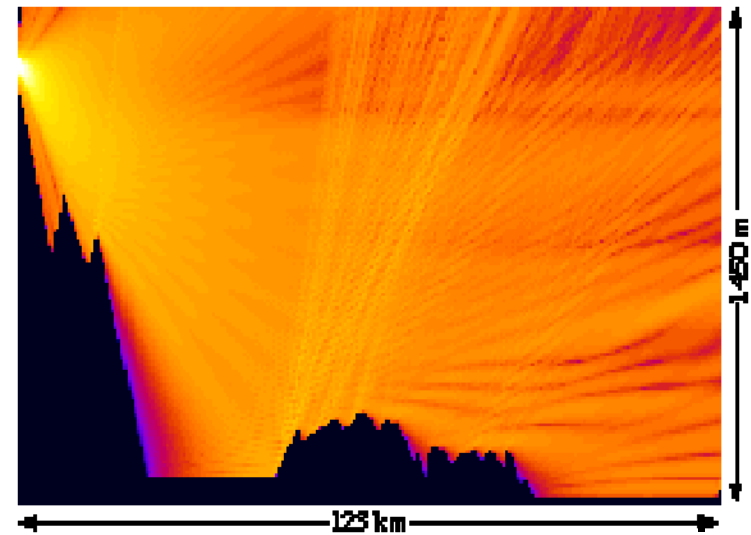
# Summary of radio propagation and mitigations

- Shadowing
  - Problem: received signal strength
  - Mitigation:
    - increase transmit power
    - Reduce cell size
- Fast fading
  - Problem: error rate (BER, FER, PER)
  - Mitigation:
    - Interleaving
    - Error correction coding
    - Frequency hopping
    - Diversity techniques
- Delay spread
  - Problem: ISI and error rates
  - Mitigation:
    - Equalization
    - Spread spectrum
    - OFDM
    - Directional antenna

# How to create propagation models?

- General ray-tracing method (simulation)
  - 3D building database with topography
  - Multiple ray-tracing with propagation effects (reflection, diffraction, LOS path, scattering, etc)
  - Might consider building material (steel, concrete, brick, etc)
- Empirical method
  - On-site measurement
  - Curve-fitting
  - Could be combined with ray-tracing method

# Real world example



## Review question?

- In which case do you expect better propagation condition?
  - Indoor or outdoor
  - With LOS or NLOS
  - Fixed or mobile user

# What's your propagation environment?

- Surroundings
  - Indoor, outdoor, street, open-area
- LOS or NLOS
  - Line-of-sight or not?
- Design choices?
  - Coding, modulation
  - Re-transmission (ARQ-Automatic Repeat-reQuest)
  - QoS requirement (at different layers)
    - Data rate requirement
    - BER (bit-error-rate)
    - FER (frame-error-rate)
      - Depend on BER and frame size