

1.

(a)

Node A is accessed first. 66 is larger than 40, the only key stored in node A. Hence, we access Node C next.

We find 66 larger than 48,62 and smaller than 74. Hence, we access Node J next.

We find 66 larger than 62,64 first. Then we find 66 is stored in node J. This is a leaf node. We access the pointer of 66 to find the record we want.

(b)

Node A is accessed first.  $18 < 40$ . Hence, we access Node B next.

We find 18 larger than 10 first. Then we find 18 is stored in node B. Hence, we access node F next.

We find 18 is stored in node F. This is a leaf node. We access the pointer of 18 to find the record we want.

(c)

Node A is accessed first. Since  $15 < 40$  and  $35 < 40$ , we search node B next.

We find  $10 < 15 < 18$  and  $32 < 35$ . Hence, we search node E, F, G next.

When we search node E, we find  $14 < 15 < 16 < 35$ . This is a leaf node. We access the pointer of 16 to find the record we want.

When we search node F, we find  $15 < 18 < 20 < 22 < 24 < 26 < 28 < 30 < 35$ . This is a leaf node. We access the pointers of all values stored in node F to find the records we want.

When we search node G, we find  $15 < 32 < 34 < 35 < 36$ . This is a leaf node. We access the pointers of 32,34 to find the records we want.

2.

(a)

Insert 15 into node E between value 14 and 16.

(b)

Split node F into F and F'. Node F has value 18,20,22,24. Node F' has value 26,27,28,30.

Insert 26 into node B between value 18 and 32.

(c)

Split node I into I and I'. Node I has value 48,49,50,52. Node I' has value 54,56,58,60.

Split node C into C and C'. Node C has value 48,54,62,74. Node C' has value 82,100,200,300.

Insert 82 into node A after 40.

3.

(a)

Delete 54 from node I.

(b)

Delete 20 from node F.

(c)

Delete 6 from node D. Merge node D and E into node D'. Node D' has

value 2,4,8,10,12,14,16. Let Node D' be the child of node B.  
Delete 10 from node B. Insert 40 into node B after 32. Let node H be the child of node B after 40.  
Delete 40 from node A. Insert 48 into node A.  
Delete 48 from node C. Move all values in node C to the left. Update the corresponding children pointers.