## Homework3

2023-03-25

### Read the lifetime data:

```
shock.absorber <- read.table("ShockAbsorber.txt", header = T)</pre>
shock.absorber$Failure <- ifelse(shock.absorber$Status == "Failure", 1, 0)</pre>
head(shock.absorber)
    Distance
                  Mode
                         Status Failure
## 1
        6700
                 Mode1 Failure
## 2
         6950 Censored Censored
## 3
         7820 Censored Censored
## 4
         8790 Censored Censored
## 5
         9120
                 Mode2 Failure
## 6
         9660 Censored Censored
```

### Using the location and scale parameters

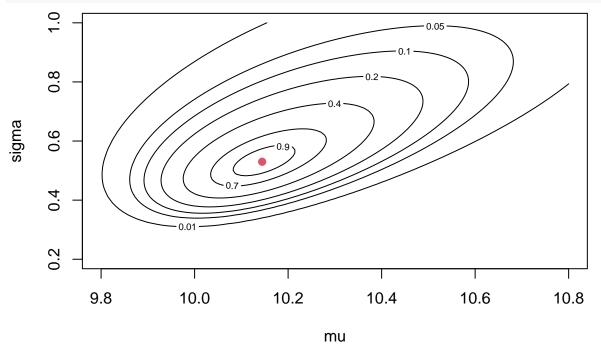
```
neg.log.likelihood.lnorm <- function(pars, data){
   mu <- pars[1]
   sigma <- pars[2]
   n <- length(data[,1])
   time <- data[,1]
   ind.F <- data[,4]

if (sigma > 0){
    lj <- ind.F * dlnorm(time, mu, sigma, log = TRUE) +
        (1-ind.F) * log(1-plnorm(time, mu, sigma))
    return(-sum(lj))
} else {
   return(10^10)
}</pre>
```

## **Initial Guess and Estimation**

```
## [1] 10.1445504 0.5298805
par.hat.lnorm$value
## [1] 124.6086
```

# Check contour plot



### Observed information

```
hessian.lnorm <- par.hat.lnorm$hessian
cov.lnorm <- solve(hessian.lnorm)
corr.lnorm <- cov2cor(cov.lnorm)
rho.lnorm <- corr.lnorm[1,2]
cov.lnorm</pre>
```

```
## [,1] [,2]
## [1,] 0.020756975 0.009718164
## [2,] 0.009718164 0.012674546
```

#### Confidence Intervals for the Parameters

```
est <- round(c(par.hat.lnorm$par[1], par.hat.lnorm$par[2]), 4)</pre>
se \leftarrow round(c(cov.lnorm[1,1]^0.5, cov.lnorm[2,2]^0.5), 4)
CIs <- data.frame(matrix(NA, 2, 6))
colnames(CIs) <- c("parameter", "est", "se", "trans", "lower", "upper")</pre>
# Normal-Approximate CI for mu
log.tr.CIs <- function(est, se.est, alpha = 0.05, parameter = "theta"){</pre>
  w <- exp(qnorm(1-alpha/2)*se.est/est)
  lower <- round(est/w, 4)</pre>
  upper <- round(est*w, 4)</pre>
  res <- data.frame(parameter = parameter,</pre>
                     est = est,
                     se = se.est,
                     trans = "log-trans",
                     lower = lower,
                     upper = upper)
  return(res)
}
no.tr.CIs <- function(est, se.est, alpha = 0.05, parameter = "theta"){
  lower <- est - qnorm(1-alpha/2)*se.est</pre>
  upper <- est + qnorm(1-alpha/2)*se.est
  res <- data.frame(parameter = parameter,
                     est = est,
                     se = se.est,
                     trans = "no-trans",
                     lower = lower,
                     upper = upper)
  return(res)
}
CIs[1, ]<- no.tr.CIs(est[1], se[1], parameter = "mu")</pre>
CIs[2, ] <- log.tr.CIs(est[2], se[2], parameter = "sigma")</pre>
```

# Homewor(a)

```
## parameter est se trans lower upper
## 1 mu 10.1446 0.1441 no-trans 9.862169 10.42703
## 2 sigma 0.5299 0.1126 log-trans 0.349400 0.80370
```

# Homewor(b)

```
xlab = "mu", ylab = "sigma")
points(par.hat.lnorm$par[1], par.hat.lnorm$par[2], col = 2, pch = 19)

8.0

8.0

9.0

0.1

0.9

0.9
```

10.2

mu

10.6

10.8

10.4

0.2

9.8

10.0