

# A Structure Tensor Based Voronoi Decomposition Technique For Optic Cup Segmentation

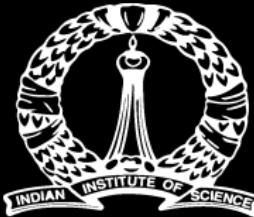
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# Overview

- ▷ The number of people with **glaucoma** worldwide is expected to rise from 64 million to 76 million by 2020 and 111 million by 2040.<sup>1</sup>
- ▷ Increase in intraocular pressure causes the retinal vessels to bend — defines the optic cup boundary.
- ▷ Ophthalmologists use **Vertical Cup - Disk ratio (CDR)** to assess the severity of glaucoma.

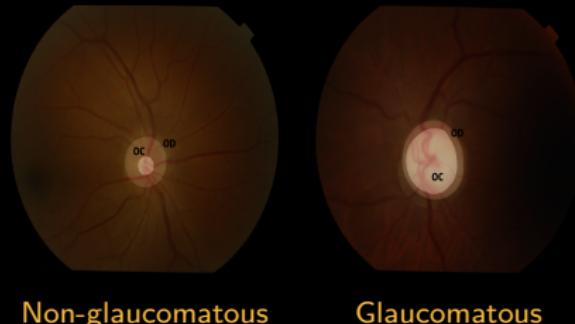


Figure 1. Examples of Non-glucomatous and Glaucomatous conditions.

<sup>1</sup>Tham, Y. C. et al. *Ophthalmology*. 2014.

# Outline

- ▷ Optic disc extraction based on expert annotation.
- ▷ Landmark point (LP) detection using multi-scale Harris corner method.
- ▷ A new Voronoi decomposition technique for removing irrelevant points.

# Objective

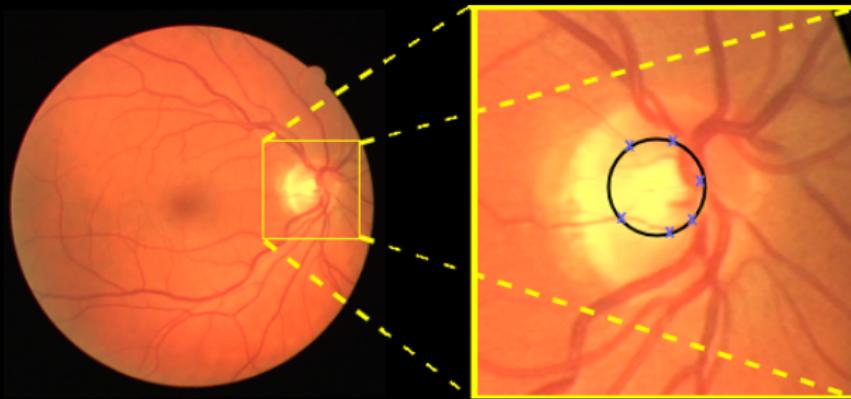


Figure 2. Objective of the proposed method.

# Harris Corner Detection<sup>2</sup>

- ▷ Consider an image  $\mathbf{I}(x, y)$ , whose horizontal and vertical derivatives are  $\partial_x I$  and  $\partial_y I$ , respectively:

$$\begin{aligned}\partial_x I &= \mathbf{I}(x, y) * g_{\sigma_d}^{(1)}(x, y), \\ \partial_y I &= \mathbf{I}(x, y) * g_{\sigma_d}^{(2)}(x, y),\end{aligned}\tag{1}$$

where  $*$  denotes the convolution operation, and  $g_{\sigma_d}^{(1)}$  and  $g_{\sigma_d}^{(2)}$  are the horizontal and vertical derivative-of-Gaussian (DoG) operators;  $\sigma_d$  is the standard deviation.

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<sup>2</sup>Harris, C. and Stephens, M. *Proceedings of Alvey Vision Conference*. 1988.

# Harris Corner Detection

- ▷ The structure tensor  $\mathbf{S}$  at each point is obtained as the outer product of the gradient vector with itself:

$$\mathbf{S} = \begin{bmatrix} v * (\partial_x I)^2 & v * (\partial_x I \partial_y I) \\ v * (\partial_y I \partial_x I) & v * (\partial_y I)^2 \end{bmatrix}, \quad (2)$$

where  $v$  is a Gaussian filter with standard deviation  $\sigma_a = 0.7 \sigma_d$ .

- ▷ The detection of landmark points  $LP(x, y)$  is performed on the green channel of the fundus image.

# Multi-Scale Harris Corner Detection

- ▷ The likelihood of a point being detected as a landmark point is determined using:

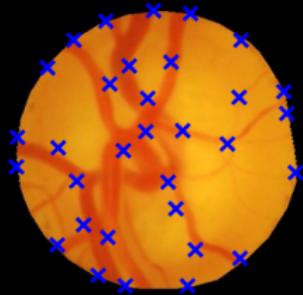
$$R_p(x, y) = \det(\mathbf{S}) - k \operatorname{trace}^2(\mathbf{S}), \quad (3)$$

where  $k$  is the trade-off factor and is typically set to 0.04.

- ▷ In a multiscale framework, the set of landmark points is determined using (1)-(3) for  $\sigma_d^i = \alpha^{i-1} \beta$ , where  $i = 1$  to 5;  $\alpha$  is the step size, and  $\beta$  is the scale factor.

# Problem Addressed

How to decide the relevant *Landmark points*?



# Voronoi Decomposition<sup>3</sup>

We partition the optic disc into convex regions based on the Euclidean distance between the landmark points such that each region contains exactly one landmark point.

- ▷ Consider a set  $S$  of co-planar points  $P_n$  with  $n \geq 3$ ,  
 $S = \{P_1, P_2, \dots, P_n\}$ .
- ▷ Let  $D(P_i, x)$  denote the Euclidean distance between  $P_i$  and a point  $x$ .
- ▷ The perpendicular bisector of the line joining the points  $P_1$  and  $P_2$  is given by:  
$$B(P_1, P_2) = \{x | D(P_1, x) = D(P_2, x)\},$$

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<sup>3</sup>Barber, C. B. et al. *ACM Transactions on Mathematical Software (TOMS)*. 1996.

# Voronoi Decomposition

- ▷ Let  $H(P_1, P_2)$  denote the half-plane containing the set of all points that are closer to  $P_1$  than to  $P_2$ :

$$H(P_1, P_2) = \{x | D(P_1, x) < D(P_2, x)\}.$$

- ▷ The Voronoi cell containing  $P_1$  is the intersection of several such half-planes and is specified as:

$$VC(P_1, S) = \bigcap_{P_i \in S, i \neq 1} H(P_1, P_i),$$

- ▷ The Voronoi decomposition is the union of the closure of the Voronoi cells:

$$V(S) = \bigcup_{P_i, P_j \in S, i \neq j} \overline{VC(P_1, S)} \cap \overline{VC(P_2, S)}.$$

where the overbar denotes set closure.

# Voronoi Decomposition

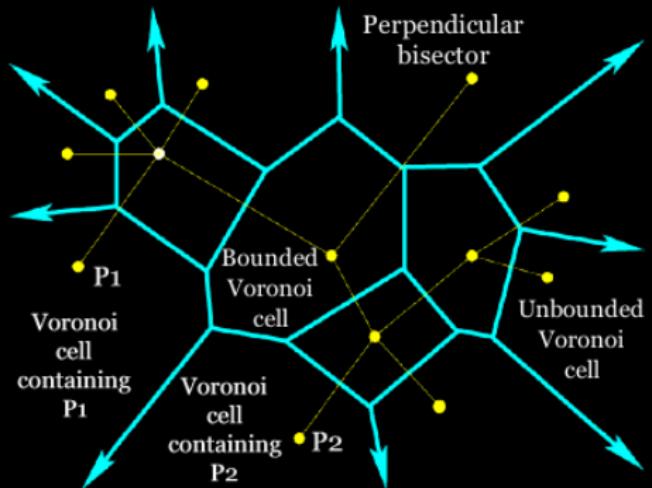
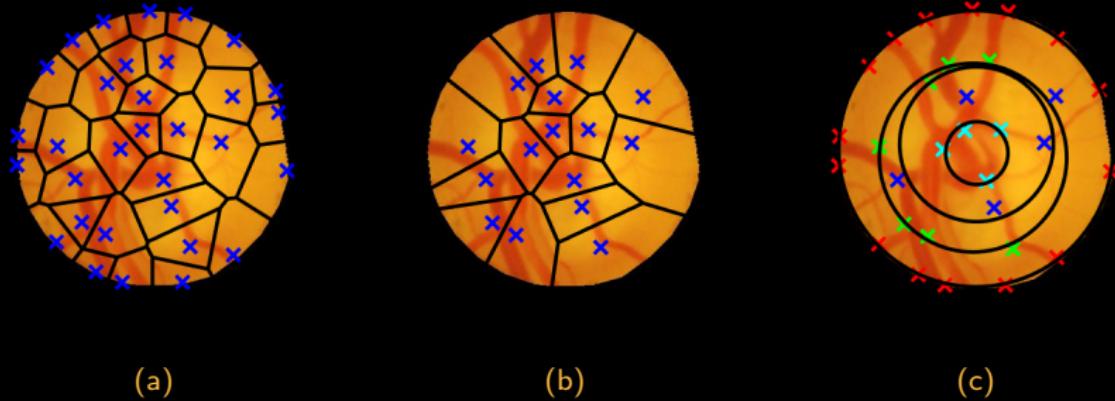


Figure 3. Voronoi partitioning of the space.

# Voronoi Partitioning of the Optic Disc



**Figure 4.** Voronoi partitioning using (a) the initial landmark points; (b) after removing the landmark points on the OD boundary; and (c) different levels of landmark points; **red:** 1<sup>st</sup>, **green:** 2<sup>nd</sup>, **blue:** 3<sup>rd</sup>, **cyan:** 4<sup>th</sup>, and corresponding circle fits.

## Selection of Relevant $L_p(x, y)$

- ▷ Selection of points that constitute the relevant kinks from the identified ones is based on the intensity and the area of the pallor.
- ▷ We consider the brightest pixel group  $\mathbf{B}_p$  within the OD obtained from a 4-level Otsu thresholding<sup>4</sup>.
- ▷ If  $\mathbf{B}_p$  constitutes to more than 50% of the OD area, then we consider 2<sup>nd</sup> level points as the relevant kinks, else the 4<sup>th</sup> level points are considered as the relevant ones.
- ▷ Finally, a circle is fit to the relevant landmark points using Pratt's technique<sup>5</sup> resulting in an accurate OC segmentation.

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<sup>4</sup>Otsu, N. *IEEE Transactions on Systems, Man, and Cybernetics*. 1979.

<sup>5</sup>Pratt, V. *ACM SIGGRAPH Computer Graphics*. 1987.

# Results

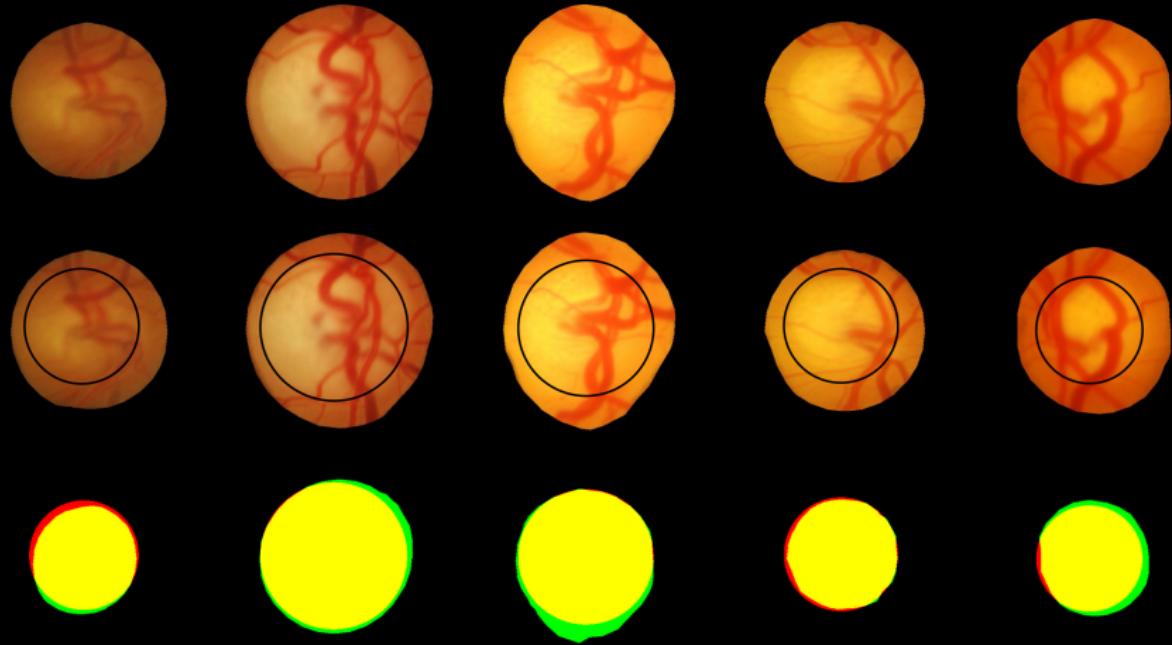


Figure 5. Row 1: Segmented OD region, Row 2: OC segmentation using the proposed technique, Row 3: Comparison of the algorithm output (shown in red), the expert annotations (shown in green) & the region shown in yellow indicates overlap.

# Results

Table 1. Performance of the proposed OC segmentation algorithm.

Database (# of images)	$S_e$	$S_p$	$Acc$	$J_i$	$D_c$
Drishti-GS (101)	0.87	0.95	0.93	0.7	0.82
MESSIDOR (90)	0.83	0.99	0.99	0.69	0.80
Average (191)	0.85	0.97	0.96	0.67	0.81

<sup>1</sup>  $S_e$  - sensitivity;  $S_p$  - specificity;  $Acc$  - accuracy;  $J_i$  - Jaccard index and  $D_c$  - Dice coefficient.

$$^2 S_e = \frac{TP}{TP+FN}; S_p = \frac{TN}{TN+FP}; Acc = \frac{TP+TN}{TP+TN+FP+FN}$$

$$^3 D_c = \frac{2TP}{2TP+FP+FN}; J_i = \frac{D_i}{2-D_i}$$

# Results

Table 2. Performance comparison with the state-of-the-art techniques.

Algorithm	Dataset used (# of Images)	$J_i$	$D_c$
Joshi et al. <sup>6</sup>	Drishti-GS (101)	0.63	0.77
Chakravarthy et al. <sup>7</sup>	Drishti-GS (101)	0.67	0.80
Zilly et al. (ML) <sup>8</sup>	Drishti-GS (10)	0.77	0.87
Sevastopolsky (ML) <sup>9</sup>	Drishti-GS (50)	0.74	0.85
BCF (ML) <sup>10</sup>	Drishti-GS (10)	0.71	0.83
<b>Proposed method</b>	Drishti-GS (101) MESSIDOR (90)	0.70 0.69	0.82 0.80

<sup>6</sup> Joshi, G. D. et al. *IEEE Transactions on Biomedical Engineering*. 2012.

<sup>7</sup> Chakravarty, A. and Sivaswamy, J. *MICCAI*. 2014.

<sup>8</sup> Zilly, J. G. et al. *Computerized Medical Imaging and Graphics*. 2017.

<sup>9</sup> Sevastopolsky, A. *Pattern Recognition and Image Analysis*. 2017.

<sup>10</sup> Zilly, J. G. et al. *Proceedings of International Workshop on Machine Learning in Medical Imaging*. 2015.

# Conclusions

- ▷ A novel technique for automatic segmentation of the OC region in retinal fundus images is proposed.
- ▷ A method for removing the redundant landmark points is proposed.
- ▷ The proposed technique relies on structural properties – namely, the landmark points found in retinal vasculature to determine the contour of the OC.

## Acknowledgements

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# Thank you