

Bits & Bytes

Computer Systems Organization



01000111
01100101
01100101
01101011

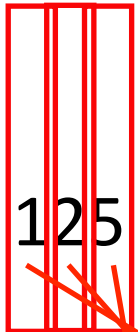
And if you can read
that you are too.

Why Don't Computers Use Decimal Numbers?

Decimal representation (base 10): Natural representation used by humans

Decimal representation
(base 10)

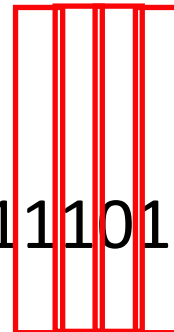
1 0 0 0 1



$$= 5 \times 10^0 + 2 \times 10^1 + 1 \times 10^2$$

Binary representation
(base 2)

8 4 2 1



$$= 1 \times 2^0 + 0 \times 2^1 + 1 \times 2^2 + 1 \times 2^3 + 1 \times 2^4 + 1 \times 2^5 + 1 \times 2^6 + 1 \times 2^7$$

Why Don't Computers Use Base 10?

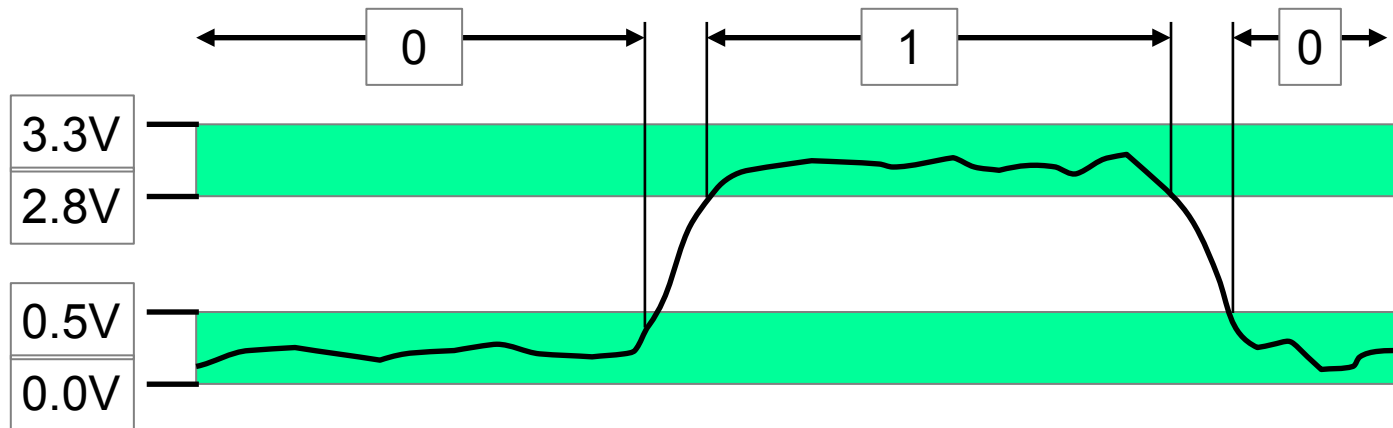
Question: why don't computers use decimal numbers?

Implementing electronically

- Hard to represent the signal: need high precision to encode 10 signal levels on single wire

Solution

- Use a binary (0/1) representation of numbers/data



How to Calculate Binary Representations?

Binary representation of 75

Subtraction method (or division by 2 method with the last remainder most significant)

- What is the biggest multiple of two that is less or equal than 75?
- $75 - 64 = 11$
- What is the biggest multiple of two that is less or equal than 11?
- $11 - 8 = 3$
- $3 - 2 = 1$
- $1 - 1 = 0$

Keep the multiples of 2 in mind

256	128	64	32	16	8	4	2	1
0	0	1	0	0	1	0	1	1

How to Calculate Binary Representations?

Binary representation of 339

Subtraction method

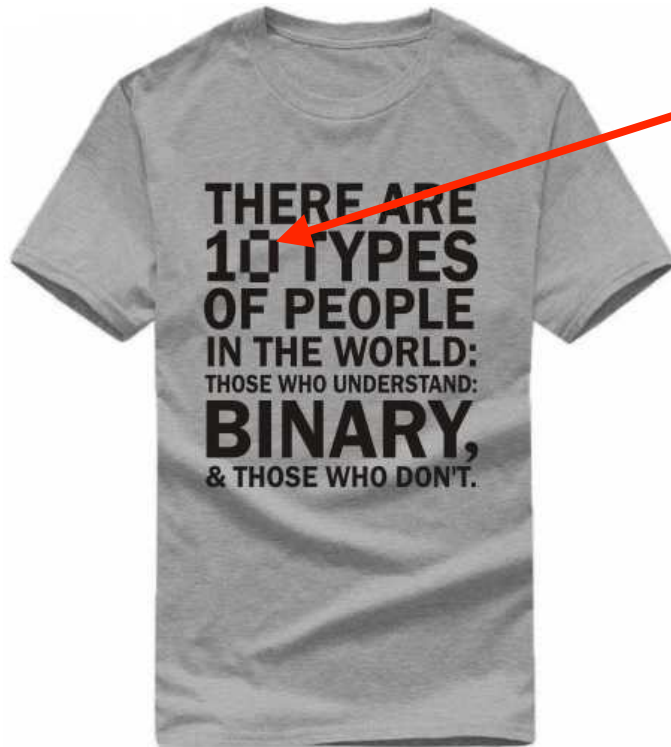
- $339 - 256 = 83$
- $83 - 64 = 19$
- $19 - 16 = 3$
- $3 - 2 = 1$
- $1 - 1 = 0$

Multiples of 2

512	256	128	64	32	16	8	4	2	1
	1	0	1	0	1	0	0	1	1

Small Binary Numbers

Useful to keep in mind



Decimal	Binary
0	0000
1	0001
2	0010
3	0011
4	0100
5	0101
6	0110
7	0111
8	1000
9	1001
10	1010
11	1011
12	1100
13	1101
14	1110
15	1111

Hexadecimal Numbering System (Base 16)

- Binary (base 2): 0 1
- Decimal (base 10): 0 1 2 3 4 5 6 7 8 9
- Hexadecimal (base 16): 0 1 2 3 4 5 6 7 8 9 A B C D E F
10 11 12 13 14 15

E7

$E \times 16^1$ $7 \times 16^0 = 7$

$$14 \times 16^1 = 224$$

$$E7 = 224 + 7 = 231$$

You can write this hexadecimal number
in C as 0xE7 Or 0xe7

Hex	Decimal
0	0
1	1
2	2
3	3
4	4
5	5
6	6
7	7
8	8
9	9
A	10
B	11
C	12
D	13
E	14
F	15

Hexadecimal <=> Binary

- Hexadecimal -> Binary
 - Expand each hexadecimal digit to its binary equivalent

1 7 3 A 4 C

Hex	Decimal	Binary
0	0	0000
1	1	0001
2	2	0010
3	3	0011
4	4	0100
5	5	0101
6	6	0110
7	7	0111
8	8	1000
9	9	1001
A	10	1010
B	11	1011
C	12	1100
D	13	1101
E	14	1110
F	15	1111

- Binary -> Hexadecimal
 - Split it into groups of 4 bits each, then convert each group to the hexadecimal equivalent

Try to memorize
this table

Practice

- Calculate the binary representation of

5 3 A 1 F E

Hex	Decimal	Binary
0	0	0000
1	1	0001
2	2	0010
3	3	0011
4	4	0100
5	5	0101
6	6	0110
7	7	0111
8	8	1000
9	9	1001
A	10	1010
B	11	1011
C	12	1100
D	13	1101
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Decimal \longleftrightarrow hexadecimal

Decimal to Hexadecimal (division by 16 with the last remainder as most significant):

$$314,156 = 19,634 \times 16 + 12 \quad (C)$$

$$19,634 = 1,227 \times 16 + 2 \quad (2)$$

$$1,227 = 76 \times 16 + 11 \quad (B)$$

$$76 = 4 \times 16 + 12 \quad (C)$$

$$4 = 0 \times 16 + 4 \quad (4)$$

0x4CB2C

Hexadecimal to Decimal:

0x7AF

$$\begin{aligned} 7 \times 16^{\text{pow}2} + 10 \times 16^{\text{pow}1} + 15 \times 16^{\text{pow}0} &= 7 \times 256 + 10 \times 16 \\ + 15 &= 1,792 + 160 + 15 = 1,967 \end{aligned}$$

Bits, Bytes and Words

Bit = 0 or 1

Byte = 8 bits

- Binary 00000000_2 to 11111111_2
- Decimal: 0_{10} to 255_{10}
- Hexadecimal 00_{16} to FF_{16}

Word = multiple bytes

- E.g., 4 bytes (32 bits) or 8 bytes (64 bits)
- Size of pointer data usually determines the number of bytes in a word
- W-bit word size
 - => The virtual addresses can range from 0 to $2^w - 1$ bytes
- Older machines are 32 bits (4 bytes)
 - Limits addresses to 4GB
 - Becoming too small for memory-intensive applications
- Today systems are 64 bits (8 bytes)
 - Can address 1.84×10^{19} bytes

Data Representations

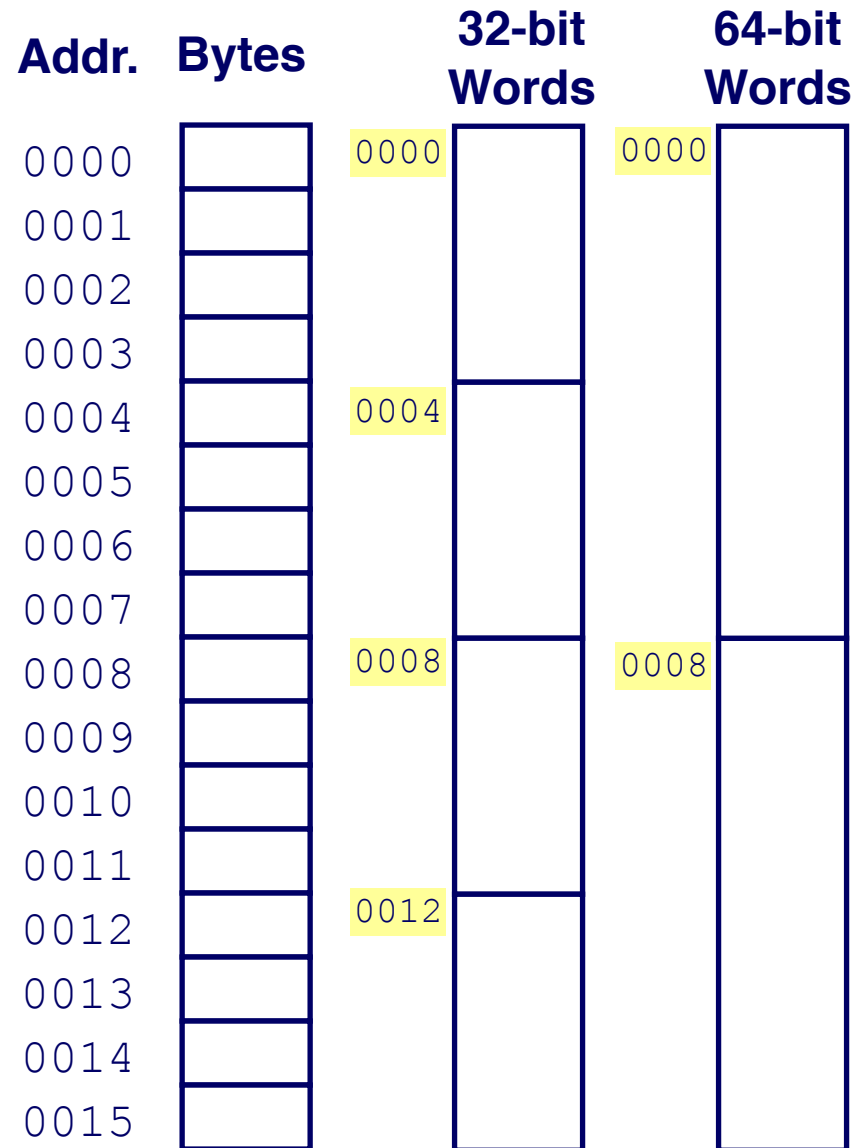
Sizes of C objects (in Bytes)

C Data Types	32-bit machine	64-bit
char	1	1
short	2	2
int	4	4
long int	4	8
int32_t	4	4
int64_t	8	8
float	4	4
double	8	8
Pointer	4	8

Word-Oriented Memory Organization

Memory is a sequence of bytes

- The byte is the smallest addressable unit in memory
- Each byte has an address
- Addresses of successive words differ by 4 (32-bit) or 8 (64-bit)

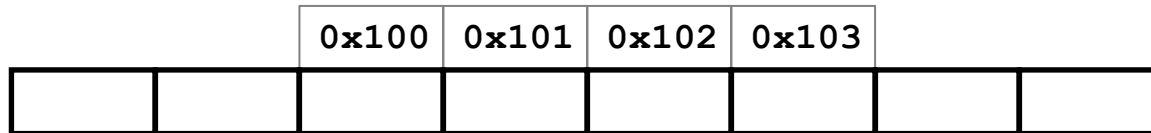
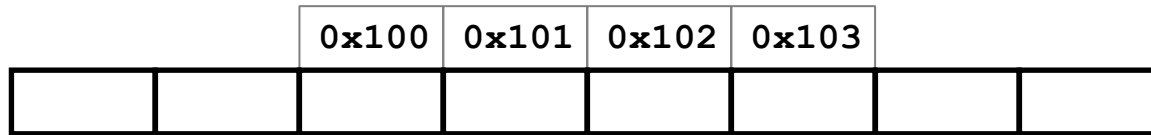


Byte Ordering

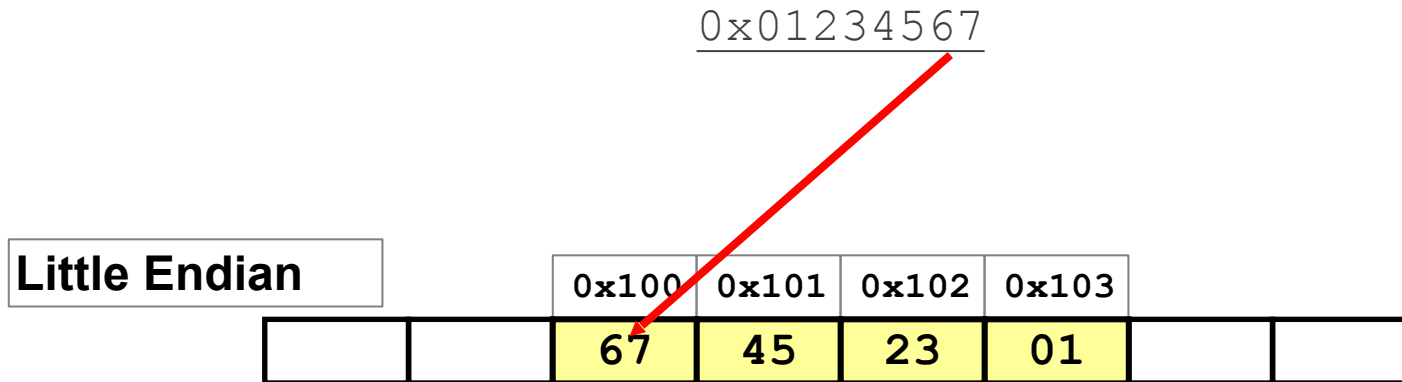
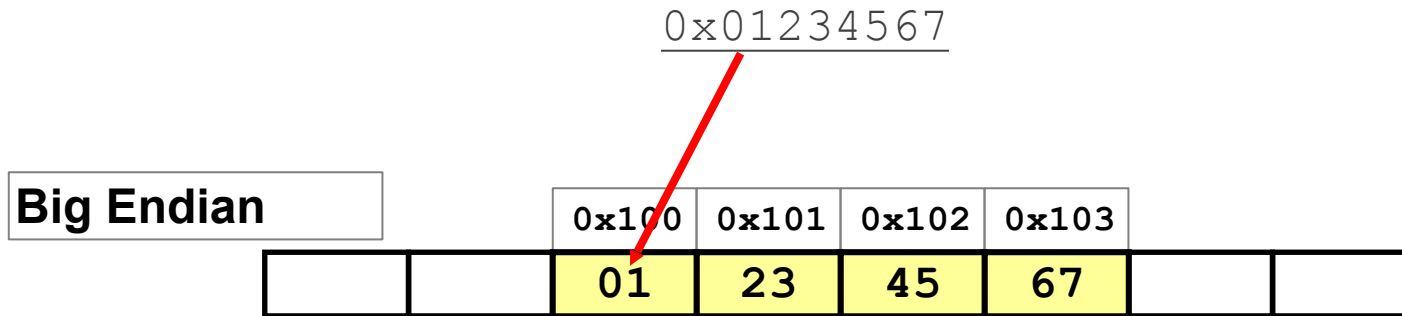
Example

- Variable `x` has 4-byte representation `0x01234567`
- Address given by `&x` is `0x100`

How should `x` be stored in memory?



Byte Ordering



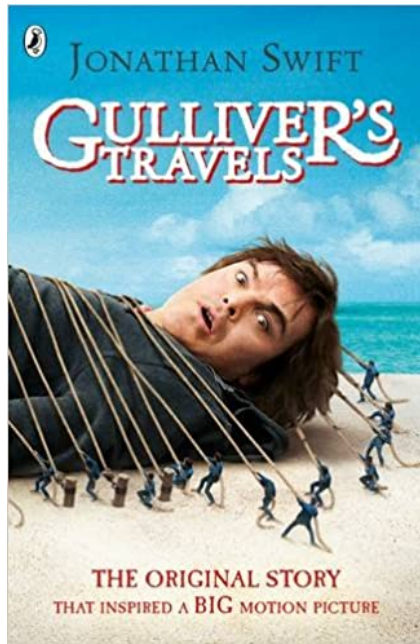
Byte Ordering Example

Big Endian

- Most significant byte has lowest address
- Sun's, Mac's (PowerPC)

Little Endian

- Least significant byte has lowest address
- PC's (x86), Mac's (x86), Alphas, ARM with iOS and Android



BIG ENDIAN



LITTLE ENDIAN

Examining Data Representations

Code to Print Byte Representation of Data

- Casting pointer to `unsigned char *` creates byte array

```
typedef unsigned char * pointer;

void show_bytes(pointer start, int len)
{
    int i;
    for (i = 0; i < len; i++)
        printf("%p \t %.2x\n", start+i, start[i]);
    printf("\n");
}
```

Printf directives:

%p: Print pointer

%x: Print Hexadecimal

show_bytes Execution Example

```
int a = 15213;
printf("%d is", a);
printf("%x in hexadecimal \n", a);
show_bytes((pointer) &a, sizeof(int));
```

```
15213 is 0x00003b6d in hexadecimal
```

Result (Linux, Intel X86):

```
int a = 15213;
0x11ffffcb8    6d
0x11ffffcb9    3b
0x11ffffcba    00
0x11ffffcbb    00
```

Result (Solaris, Sun SPARC):

```
int a = 15213;
0x11ffffcb8    00
0x11ffffcb9    00
0x11ffffcba    3b
0x11ffffcbb    6d
```

Representing Strings in C

- Represented by array of characters
- Strings end with a null character
 - Final character = 0
- Each character encoded in ASCII format
 - ASCII = American Standard Code for Information Interchange
 - Standard 7-bit encoding of character set
 - Other encodings exist, but uncommon

```
char S[6] = "15213";
```

ASCII TABLE



01000111
01100101
01100101
01101011

And if you can read
that you are too.

Practice

Write a function that takes a character as input and returns whether it is a digit:

isdigit('4') ==> 1

isdigit('9') ==> 1

isdigit('a') ==> 0

isdigit('?') ==> 0

Try to write isdigit()!

```
int isdigit(char c)
{
    if ((c >= '0') && (c <= '9'))
        return 1;
    else
        return 0;
}
```

Machine-Level Code Representation

- A program as a sequence of instructions
- Each instruction is a simple operation
 - Arithmetic operation
 - Read or write memory
 - Conditional branch
- Instructions encoded as bytes

```
int sum(int x, int y)
{
    return x+y;
}
```

- Different instruction encodings for different machines
 - Most code not binary compatible

Programs are Byte Sequences Too!

PC sum

55
89
E5
8B
45
0C
03
45
08
89
EC
5D
C3

Practice

Write a C function that finds the length of a string

```
int strlen(char * text)
{
    int index= 0;

    while(text[index] != '\0')
    {
        index++;
    }

    return index;
}
```