

# **Machine-Level Programming: Basics & Arithmetic**

# Notes

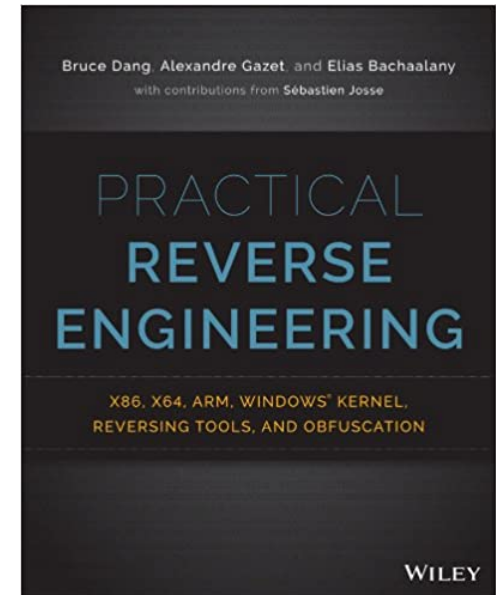
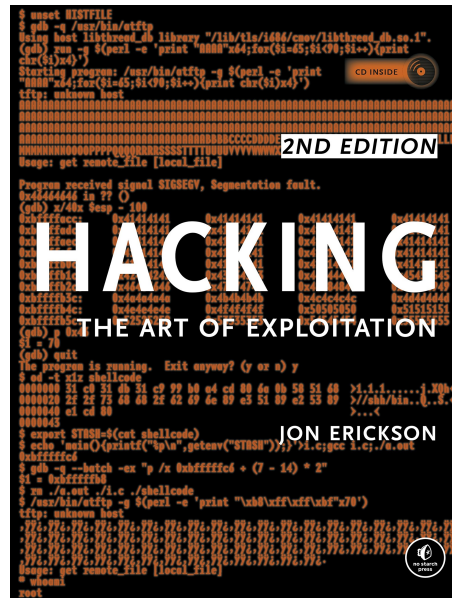
- Lectures will become more and more challenging
- Low level textbook details are “good to know” but not required
- In the next lecture we will have some practice problems

# **Why Learn Assembly?**

# Assembly is Important for Security

- System attacks
- Reverse engineering

Offensive Security  
Certified Expert



# Today: Machine Programming I: Basics

- History of Intel processors and architectures
- C, assembly, machine code
- Assembly Basics: Registers, operands, move
- Arithmetic & logical operations

# Intel x86 Processors

- Dominate laptop/desktop/server market

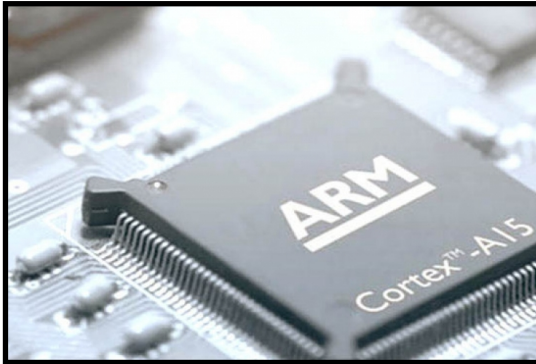
- Evolutionary design

- Backwards compatible up until 8086, introduced in 1978
- Added more features as time goes on



# Other Processors

- Which CPU company dominates mobile/smartphones?



- Sold 160 billion chips!



# Types of Instruction Sets: CISC and RISC

## ■ Intel CPUs: Complex instruction set computer (CISC)

- Complex, specialized instructions
- Too many of these complex instructions
  - But, only small subset encountered with Linux programs

## ■ ARM CPUs: Reduced instruction set computer (RISC)

- Small number of basic instructions
- These instructions are composed to create complex functionalities
- It is hard for CISC to match performance of RISC
- But, Intel has done just that!
  - In terms of speed. Less so for low power.

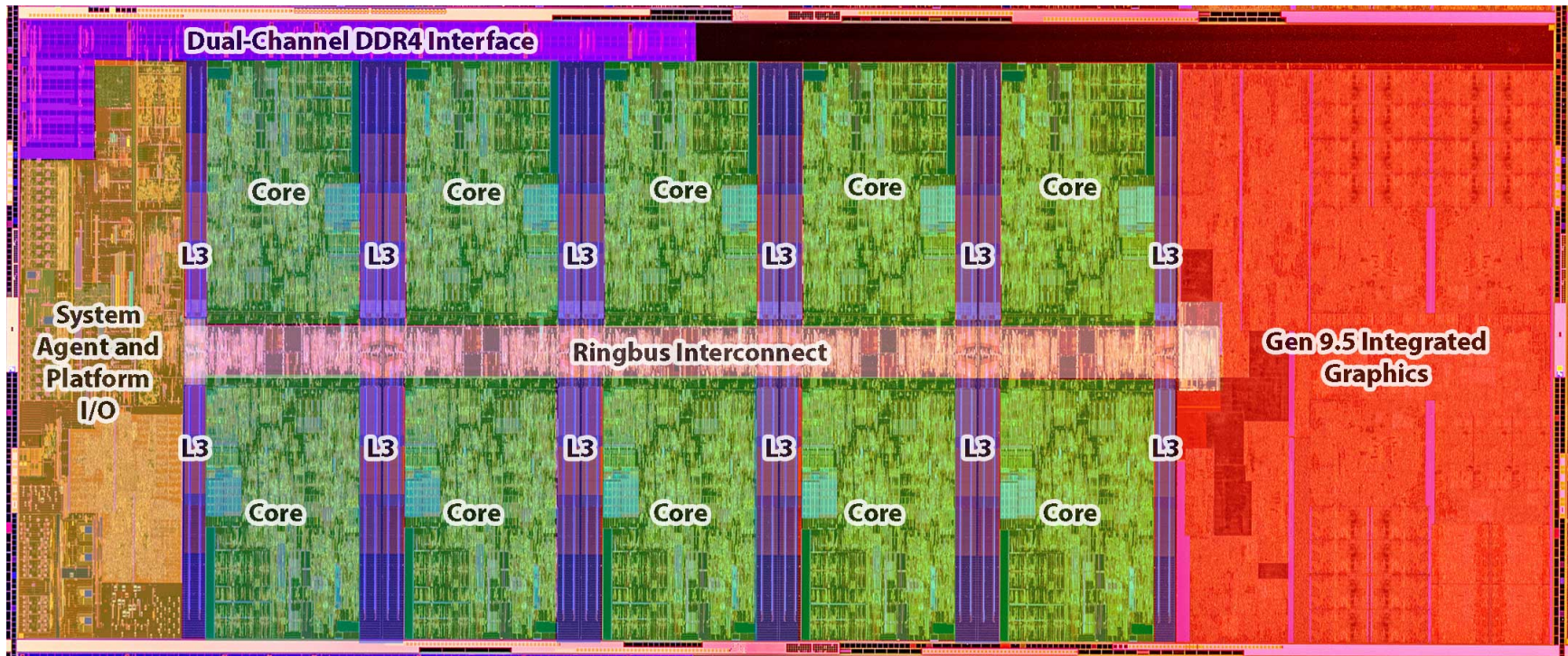


# Intel x86 Evolution: Milestones

<i>Name</i>	<i>Date</i>	<i>Transistors</i>	<i>MHz</i>
■ <b>8086</b>	<b>1978</b>	<b>29K</b>	<b>5-10</b>
<ul style="list-style-type: none"><li>■ First 16-bit Intel processor. Basis for IBM PC &amp; DOS</li><li>■ 1MB address space</li></ul>			
■ <b>386</b>	<b>1985</b>	<b>275K</b>	<b>16-33</b>
<ul style="list-style-type: none"><li>■ First 32 bit Intel processor , referred to as IA32</li></ul>			
■ <b>Pentium 4E</b>	<b>2004</b>	<b>125M</b>	<b>2800-3800</b>
<ul style="list-style-type: none"><li>■ First 64-bit Intel x86 processor, referred to as x86-64</li></ul>			
■ <b>Core i9 10'th</b>	<b>2020</b>		<b>3600</b>
<ul style="list-style-type: none"><li>■ 10 cores</li></ul>			

# Intel x86 Processors, cont.

- Core i9 10'th generation



## ■ Desktop Model

- 10 cores
- 3.6-5.3 GHz
- Integrated graphics
- 125 W

# x86 Clones: Advanced Micro Devices (AMD)

## ■ Historically

- AMD has followed just behind Intel
- A little bit slower, a lot cheaper

## ■ Then

- Recruited top circuit designers from Digital Equipment Corp. and other downward trending companies
- Built Opteron: tough competitor to Pentium 4
- Developed x86-64, their own extension to 64 bits

## ■ Recent Years

- Intel got its act together
  - Leads the world in semiconductor technology
- AMD has fallen behind
  - Relies on external semiconductor manufacturer

# Our Coverage

## ■ x86-64

- The standard now

## ■ We will only cover x86-64

# Today: Machine Programming I: Basics

- History of Intel processors and architectures
- C, assembly, machine code
- Assembly Basics: Registers, operands, move
- Arithmetic & logical operations

# Definitions

## ■ **Architecture (ISA: Instruction Set Architecture)**

- Abstract CPU design that one needs to understand to write assembly
- Examples: instruction set specification, registers

## ■ **Microarchitecture: Implementation of the architecture**

- Examples: cache sizes and core frequency

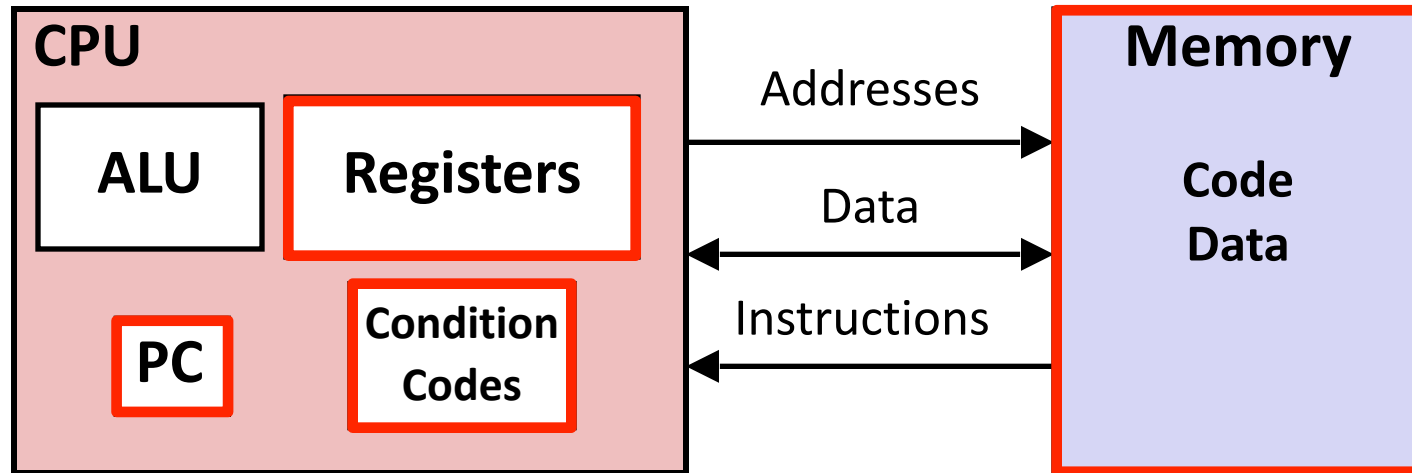
## ■ **Code Forms:**

- **Machine Code:** The byte-level programs that a processor executes
- **Assembly Code:** A text representation of machine code

## ■ **Example ISAs:**

- Intel: x86, IA32, Itanium, x86-64
- ARM: Used in almost all mobile phones

# Assembly/Machine Code View



## Programmer-Visible State

### ■ PC: Program counter

- Address of next instruction
- Called “RIP” (x86-64)

### ■ Register file

- Heavily used program data

### ■ Condition codes

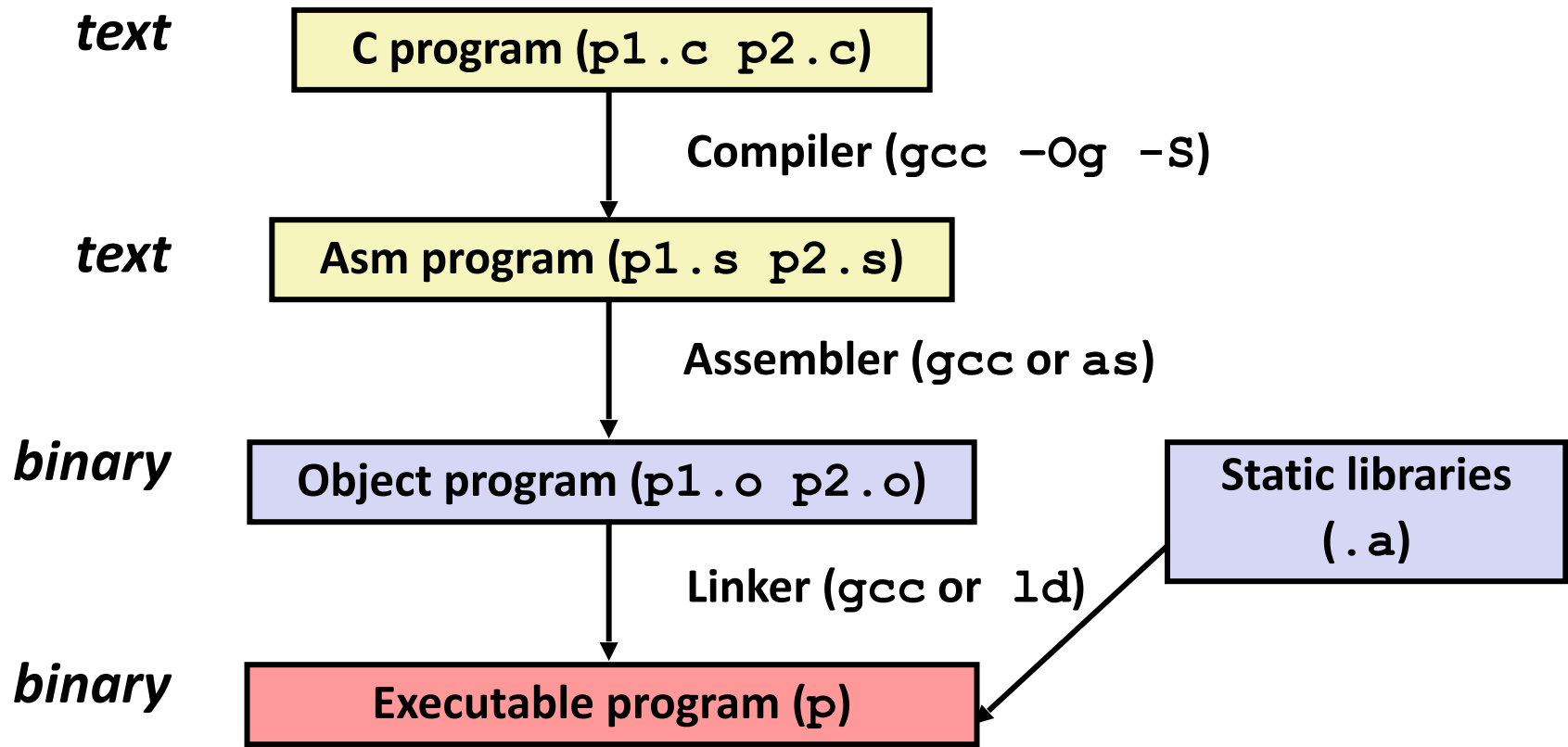
- Store status information about most recent arithmetic or logical operation
- Used for conditional branching

### ■ Memory

- Byte addressable array
- Code and user data
- Stack to support procedures

# Turning C into Object Code

- Use basic optimizations (**-Og**) [New to recent versions of GCC]
  - Compile with command: **gcc -Og p1.c p2.c -o p**





# Compiling Into Assembly

C Code (sum.c)

Generated x86-64 Assembly

```
long plus(long x, long y);

void sumstore(long x, long y,
              long *dest)
{
    long t = plus(x, y);
    *dest = t;
}
```

```
sumstore:
    pushq    %rbx
    movq     %rdx, %rbx
    call     plus
    movq     %rax, (%rbx)
    popq     %rbx
    ret
```

Obtain with command

```
gcc -Og -S sum.c
```

Produces file sum.s

**Warning:** Will get very different results on your machine  
(Andrew Linux, Mac OS-X, ...) due to different versions of  
gcc and different compiler settings

# Assembly Characteristics: Data Types

## ■ “Integer” data of 1, 2, 4, or 8 bytes

- Data values
- Addresses (untyped pointers)

## ■ Floating point data of 4 or 8 bytes

## ■ Code: Byte sequences encoding series of instructions

## ■ No aggregate types such as arrays or structures

- Just contiguously allocated bytes in memory

# Assembly Characteristics: Operations

- **Perform arithmetic function on register or memory data**
- **Transfer data between memory and register**
  - Load data from memory into register
  - Store register data into memory
- **Transfer control**
  - Unconditional jumps to/from procedures
  - Conditional branches

# Object Code

## Code for `sumstore`

0x0400595:

0x53

0x48

0x89

0xd3

0xe8

0xf2

0xff

0xff

0xff

0x48

0x89

0x03

0x5b

0xc3

- Total of 14 bytes

- Starts at address  
0x0400595

## ■ Assembler

- Translates `.s` into `.o`
- Binary encoding of each instruction
- Nearly-complete image of executable code
- Missing linkages between code in different files

## ■ Linker

- Resolves references between files
- Combines with static run-time libraries
  - E.g., code for `malloc`, `printf`
- Some libraries are *dynamically linked*
  - Linking occurs when program begins execution

# Machine Instruction Example

```
*dest = t;
```

## ■ C Code

- Store value `t` where designated by `dest`

```
movq %rax, (%rbx)
```

## ■ Assembly

- Move 8-byte value to memory
  - Quad words in x86-64 parlance
- Operands:
  - `t:` Register `%rax`
  - `dest:` Register `%rbx`
  - `*dest:` Memory `M[%rbx]`

```
0x40059e: 48 89 03
```

## ■ Object Code

- 3-byte instruction
- Stored at address `0x40059e`

# Disassembling Object Code

## Disassembled

```
0000000000400595 <sumstore>:
 400595:  53                      push    %rbx
 400596:  48 89 d3                mov     %rdx,%rbx
 400599:  e8 f2 ff ff ff         callq   400590 <plus>
 40059e:  48 89 03                mov     %rax, (%rbx)
 4005a1:  5b                      pop     %rbx
 4005a2:  c3                      retq
```

## ■ Disassembler

`objdump -d sum`

- Useful tool for examining object code
- Analyzes bit pattern of series of instructions
- Produces approximate rendition of assembly code
- Can be run on either a `.out` (complete executable) or `.o` file

**Demo**

# Alternate Disassembly

## Object

0x0400595:

0x53

0x48

0x89

0xd3

0xe8

0xf2

0xff

0xff

0xff

0x48

0x89

0x03

0x5b

0xc3

## Disassembled

Dump of assembler code for function sumstore:

0x0000000000400595 <+0>: push %rbx

0x0000000000400596 <+1>: mov %rdx,%rbx

0x0000000000400599 <+4>: callq 0x400590 <plus>

0x000000000040059e <+9>: mov %rax, (%rbx)

0x00000000004005a1 <+12>: pop %rbx

0x00000000004005a2 <+13>: retq

## ■ Within gdb Debugger

`gdb sum`

`disassemble sumstore`

- Disassemble procedure



# What Can be Disassembled?

```
% objdump -d WINWORD.EXE
```

```
WINWORD.EXE:      file format pei-i386
```

```
No symbols in "WINWORD.EXE".
```

```
Disassembly of section .text:
```

```
30001000 <.text>:
```

```
30001000:
```

```
30001001:
```

```
30001003:
```

```
30001005:
```

```
3000100a:
```

**Reverse engineering forbidden by  
Microsoft End User License Agreement**

- Anything that can be interpreted as executable code
- Disassembler examines bytes and reconstructs assembly source

# Today: Machine Programming I: Basics

- History of Intel processors and architectures
- C, assembly, machine code
- **Assembly Basics: Registers, operands, move**
- Arithmetic operations

# x86-64 Integer Registers

<b>%rax</b>	<b>%eax</b>
<b>%rbx</b>	<b>%ebx</b>
<b>%rcx</b>	<b>%ecx</b>
<b>%rdx</b>	<b>%edx</b>
<b>%rsi</b>	<b>%esi</b>
<b>%rdi</b>	<b>%edi</b>
<b>%rsp</b>	<b>%esp</b>
<b>%rbp</b>	<b>%ebp</b>

<b>%r8</b>	<b>%r8d</b>
<b>%r9</b>	<b>%r9d</b>
<b>%r10</b>	<b>%r10d</b>
<b>%r11</b>	<b>%r11d</b>
<b>%r12</b>	<b>%r12d</b>
<b>%r13</b>	<b>%r13d</b>
<b>%r14</b>	<b>%r14d</b>
<b>%r15</b>	<b>%r15d</b>

- Can reference low-order 4 bytes (also low-order 1 & 2 bytes)

# Some History: IA32 Registers

general purpose	<b>%eax</b>	<b>%ax</b>	<b>%ah</b>	<b>%al</b>	<i>accumulate</i>
	<b>%ecx</b>	<b>%cx</b>	<b>%ch</b>	<b>%cl</b>	<i>counter</i>
	<b>%edx</b>	<b>%dx</b>	<b>%dh</b>	<b>%dl</b>	<i>data</i>
	<b>%ebx</b>	<b>%bx</b>	<b>%bh</b>	<b>%bl</b>	<i>base</i>
	<b>%esi</b>	<b>%si</b>			<i>source index</i>
	<b>%edi</b>	<b>%di</b>			<i>destination index</i>
	<b>%esp</b>	<b>%sp</b>			<i>stack pointer</i>
	<b>%ebp</b>	<b>%bp</b>			<i>base pointer</i>
<div>16-bit virtual registers (backwards compatibility)</div>					

# Moving Data

## ■ Moving Data

`movq Source, Dest`

## ■ Operand Types

- **Immediate:** Constant integer data
  - Example: `$0x400`
- **Register:** One of 16 integer registers
  - Example: `%rax`
- **Memory:**
  - Example: `(%rax)`

`%rax`

`%rcx`

`%rdx`

`%rbx`

`%rsi`

`%rdi`

`%rsp`

`%rbp`

`%rN`

# movq Operand Combinations

	Source	Dest	Src, Dest	C Analog
movq	Imm	Reg	movq \$0x4, %rax	temp = 0x4;
		Mem	movq \$-147, (%rax)	*p = -147;
	Reg	Reg	movq %rax, %rdx	temp2 = temp1;
		Mem	movq %rax, (%rdx)	*p = temp;
	Mem	Reg	movq (%rax), %rdx	temp = *p;

*Cannot do memory-memory transfer with a single instruction*

# Practice

## ■ Write the corresponding assembly code

```
long t1 = t0;           //t0 is stored in %rax
long t2 = *xp;          //xp is stored in %rdx
```

```
movq    %rax, %rbx
movq    (%rdx), %rcx
```

# Practice

## ■ Which ones are correct?

```
movq    %rax, $0x010
movq    %rax, (%rbx)
movq    (%rdx), (%rcx)
```

## ■ Answers

```
movq    %rax, $0x010
--> Incorrect: immediate can't be a destination
```

```
movq    %rax, (%rbx)
--> Correct
```

```
movq    (%rdx), (%rcx)
--> Incorrect: can't move from a memory address
to a memory address
```



# Simple Memory Addressing Modes

■ **Normal**                      (R)                      Mem[Reg[R]]

- Register R specifies memory address
- Aha! Pointer dereferencing in C

```
movq (%rcx), %rax
```

■ **Displacement**              D(R)               $\rightarrow (D+R) \rightarrow \text{Mem}[\text{Reg}[R]+D]$

- Register R specifies start of memory region
- Constant displacement D specifies offset

```
movq 2(%rcx), %rdx
```

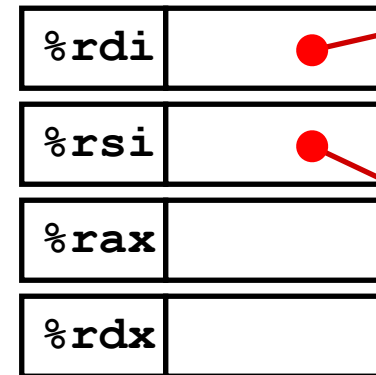
# Example of Simple Addressing Modes

```
void swap
    (long *xp, long *yp)
{
    long t0 = *xp;
    long t1 = *yp;
    *xp = t1;
    *yp = t0;
}
```

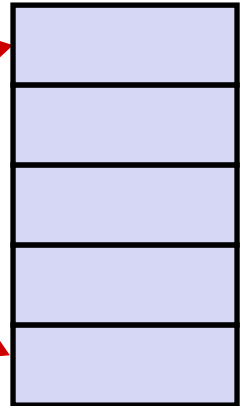
# Understanding Swap()

```
void swap
(long *xp, long *yp)
{
    long t0 = *xp;
    long t1 = *yp;
    *xp = t1;
    *yp = t0;
}
```

## Registers



## Memory



## Register Value

Register	Value
%rdi	xp
%rsi	yp
%rax	t0
%rdx	t1

swap:

```
movq    (%rdi), %rax    # t0 = *xp
movq    (%rsi), %rdx    # t1 = *yp
movq    %rdx, (%rdi)    # *xp = t1
movq    %rax, (%rsi)    # *yp = t0
ret
```

# Understanding Swap()

## Registers

%rdi	0x120
%rsi	0x100
%rax	
%rdx	

## Memory

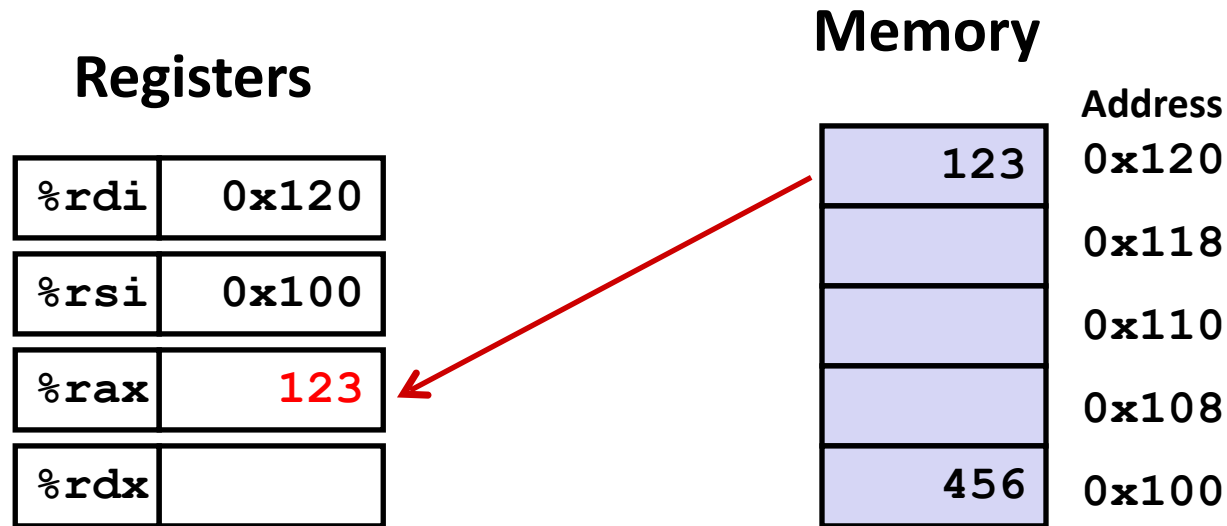
Address
0x120
0x118
0x110
0x108
0x100

123
456

swap:

```
    movq    (%rdi), %rax    # t0 = *xp
    movq    (%rsi), %rdx    # t1 = *yp
    movq    %rdx, (%rdi)    # *xp = t1
    movq    %rax, (%rsi)    # *yp = t0
    ret
```

# Understanding Swap()



swap:

```
movq    (%rdi), %rax    # t0 = *xp
movq    (%rsi), %rdx    # t1 = *yp
movq    %rdx, (%rdi)    # *xp = t1
movq    %rax, (%rsi)    # *yp = t0
ret
```

# Understanding Swap()

## Registers

%rdi	0x120
%rsi	0x100
%rax	123
%rdx	456

## Memory

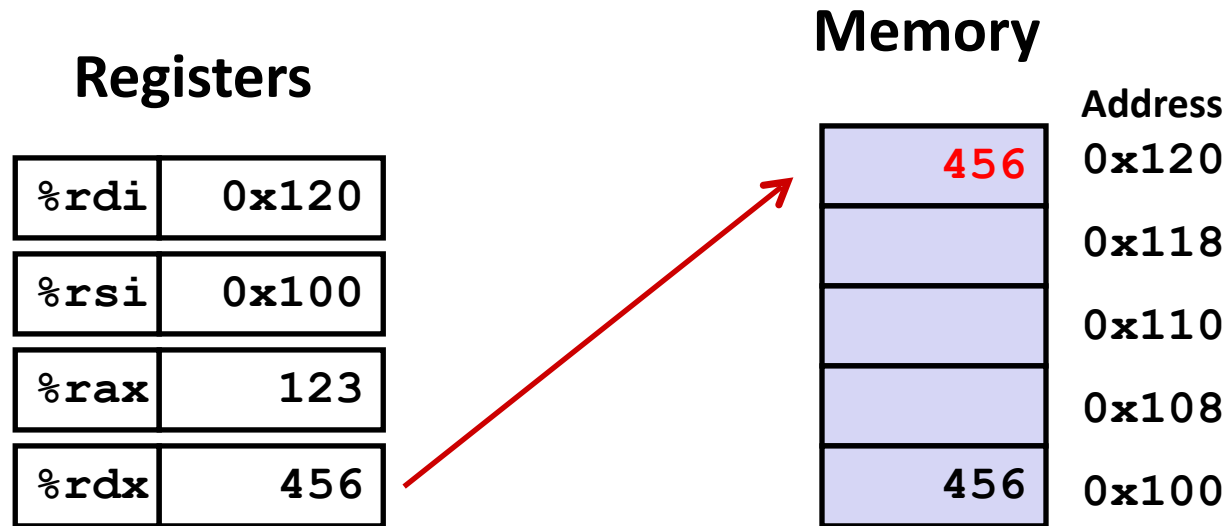
Address
0x120
123
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0x108
456
0x100



swap:

```
movq    (%rdi), %rax    # t0 = *xp
movq    (%rsi), %rdx    # t1 = *yp
movq    %rdx, (%rdi)    # *xp = t1
movq    %rax, (%rsi)    # *yp = t0
ret
```

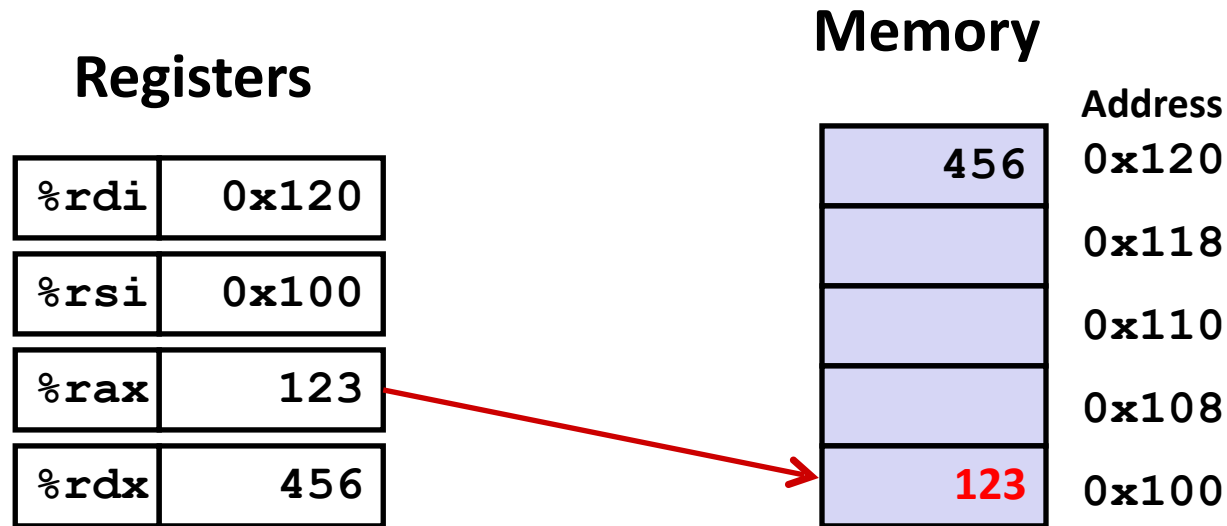
# Understanding Swap()



**swap:**

```
movq    (%rdi), %rax    # t0 = *xp
movq    (%rsi), %rdx    # t1 = *yp
movq    %rdx, (%rdi)    # *xp = t1
movq    %rax, (%rsi)    # *yp = t0
ret
```

# Understanding Swap()



swap:

```
movq    (%rdi), %rax    # t0 = *xp
movq    (%rsi), %rdx    # t1 = *yp
movq    %rdx, (%rdi)    # *xp = t1
movq    %rax, (%rsi)    # *yp = t0
ret
```



# Complete Memory Addressing Modes

## ■ Most General Form

$D(Rb, Ri, S)$   $(D + Rb + Ri * S)$

- D: Constant “displacement” 1, 2, or 4 bytes
- Rb: Base register: Any of 16 integer registers
- Ri: Index register: Any, except for `%rsp`
- S: Scale: 1, 2, 4, or 8 (*why these numbers?*)

## ■ Special Cases

$(Rb, Ri)$	$(Rb + Ri)$
$D(Rb, Ri)$	$(D + Rb + Ri)$
$(Rb, Ri, S)$	$(Rb + Ri * S)$

# Complete Memory Addressing Modes

## ■ Most General Form

**$D(Rb, Ri, S)$                        $Mem[Reg[Rb] + S * Reg[Ri] + D]$**

- D: Constant “displacement” 1, 2, or 4 bytes
- Rb: Base register: Any of 16 integer registers
- Ri: Index register: Any, except for `%rsp`
- S: Scale: 1, 2, 4, or 8 (*why these numbers?*)

## ■ Special Cases

**$(Rb, Ri)$                        $Mem[Reg[Rb] + Reg[Ri]]$**

**$D(Rb, Ri)$                        $Mem[Reg[Rb] + Reg[Ri] + D]$**

**$(Rb, Ri, S)$                        $Mem[Reg[Rb] + S * Reg[Ri]]$**

# Address Computation Examples

<code>%rdx</code>	<code>0xf000</code>
<code>%rcx</code>	<code>0x0100</code>

Expression	Address Computation	Address
<code>0x8(%rdx)</code>	<code>0xf000 + 0x8</code>	<code>0xf008</code>
<code>(%rdx,%rcx)</code>	<code>0xf000 + 0x100</code>	<code>0xf100</code>
<code>(%rdx,%rcx,4)</code>	<code>0xf000 + 4*0x100</code>	<code>0xf400</code>
<code>0x80(,%rdx,2)</code>	<code>2*0xf000 + 0x80</code>	<code>0x1e080</code>

# Today: Machine Programming I: Basics

- History of Intel processors and architectures
- C, assembly, machine code
- Assembly Basics: Registers, operands, move
- **Arithmetic operations**

# Some Arithmetic Operations

## ■ Two Operand Instructions:

<i>Format</i>	<i>Computation</i>		
addq	<i>Src, Dest</i>	Dest = Dest + Src	+=
subq	<i>Src, Dest</i>	Dest = Dest – Src	-=
imulq	<i>Src, Dest</i>	Dest = Dest * Src	...
salq	<i>Src, Dest</i>	Dest = Dest << Src	<i>Also called shlq</i>
sarq	<i>Src, Dest</i>	Dest = Dest >> Src	<i>Arithmetic</i>
shrq	<i>Src, Dest</i>	Dest = Dest >> Src	<i>Logical</i>
xorq	<i>Src, Dest</i>	Dest = Dest ^ Src	
andq	<i>Src, Dest</i>	Dest = Dest & Src	
orq	<i>Src, Dest</i>	Dest = Dest   Src	

## ■ Watch out for argument order!

# Some Arithmetic Operations

## ■ One Operand Instructions

<code>incq</code>	<i>Dest</i>	$Dest = Dest + 1$
-------------------	-------------	-------------------

<code>decq</code>	<i>Dest</i>	$Dest = Dest - 1$
-------------------	-------------	-------------------

<code>negq</code>	<i>Dest</i>	$Dest = - Dest$
-------------------	-------------	-----------------

<code>notq</code>	<i>Dest</i>	$Dest = \sim Dest$
-------------------	-------------	--------------------

# Address Computation Instruction

■ What do you expect the generated assembly to be?

```
long m12(long x)
{
    return x*12;
}
```

Converted to ASM by compiler:

```
leaq (%rdi,%rdi,2), %rax
salq $2, %rax
```

# Address Computation Instruction

## ■ **leaq** *Src, Dst*

- *Src* is address mode expression
- Set *Dst* to address denoted by expression

## ■ **Use**

- Computing addresses without a memory reference
  - E.g., translation of `p = &x[i];`

## ■ **leaq** **7(%rdx,%rdx,4), %rax**

- Set register `%rax` to  $5\%rdx + 7$



# Address Computation Instruction

## ■ Used also to do arithmetic operations

- Computing arithmetic expressions of the form  $x + k*y$ 
  - $k = 1, 2, 4, \text{ or } 8$

```
long m12(long x)
{
    return x*12;
}
```

## Converted to ASM by compiler:

```
leaq (%rdi,%rdi,2), %rax # t <- x+x*2
salq $2, %rax           # return t<<2
```

# Arithmetic Expression Example

```
long arith
(long x, long y, long z)
{
    long t1 = x+y;
    long t2 = z+t1;
    long t3 = x+4;
    long t4 = y * 48;
    long t5 = t3 + t4;
    long rval = t2 * t5;
    return rval;
}
```

```
arith:
    leaq    (%rdi,%rsi), %rax
    addq    %rdx, %rax
    leaq    (%rsi,%rsi,2), %rdx
    salq    $4, %rdx
    leaq    4(%rdi,%rdx), %rcx
    imulq   %rcx, %rax
    ret
```

## Interesting Instructions

- **leaq**: address computation
- **salq**: shift
- **imulq**: multiplication
  - But, only used once

# Understanding Arithmetic Expression Example

```
long arith
(long x, long y, long z)
{
    long t1 = x+y;
    long t2 = z+t1;
    long t3 = x+4;
    long t4 = y * 48;
    long t5 = t3 + t4;
    long rval = t2 * t5;
    return rval;
}
```

```
arith:
    leaq    (%rdi,%rsi), %rax    # t1
    addq    %rdx, %rax          # t2
    leaq    (%rsi,%rsi,2), %rdx
    salq    $4, %rdx           # t4
    leaq    4(%rdi,%rdx), %rcx   # t5
    imulq    %rcx, %rax         # rval
    ret
```

Register	Use(s)
%rdi	Argument <b>x</b>
%rsi	Argument <b>y</b>
%rdx	Argument <b>z</b>
%rax	t1, t2, rval
%rdx	t4
%rcx	t5

# Practice

## ■ Calculate the address

<code>%rdx</code>	<code>0xff00</code>
<code>%rcx</code>	<code>0x0110</code>

Expression	Address Computation	Address
<code>0x10(%rdx)</code>	<code>0xff00 + 0x10</code>	<code>0xff10</code>
<code>(%rdx,%rcx)</code>	<code>0xff00 + 0x0110</code>	<code>0x10010</code>
<code>(%rdx,%rcx,4)</code>	<code>0xff00 + 4*0x0110</code>	<code>0x10340</code>
<code>0x80(,%rdx,2)</code>	<code>2*0xff00 + 0x80</code>	<code>0x1fe80</code>

# Practice

- Represent 7.125 in the normalized encoding of floating points
- Assume 1 bit for sign, 8 bits for exponent and 8 bits for the fractional part



# Practice

$$v = (-1)^s M 2^E$$
$$E = \text{Exp} - \text{Bias}$$

$$\blacksquare 7.125_{10} = 111.001_2$$



$$\blacksquare 111.001 = 1.\underline{11001} \times 2^2$$

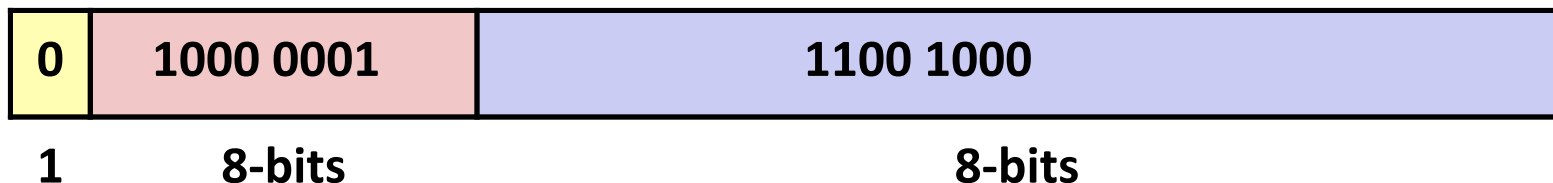
$$\blacksquare M = 1.\underline{11001} \implies \text{frac} = \underline{11001}$$

$$\blacksquare E = 2$$

$$\blacksquare \text{Exp} = E + \text{Bias}$$

$$\blacksquare \text{Bias} = 2^{k-1} - 1 = 2^{8-1} - 1 = 2^7 - 1 = 127$$

$$\blacksquare \implies \text{Exp} = 2 + 127 = 129_{10} = 10000001_2$$



# Xor properties

■  $A \oplus B = ?$

# Practice

■ What does the following function do?

```
void s(int& a, int& b)
{
    a = a ^ b;
    b = a ^ b;
    a = a ^ b;
}
```

■ It's a function to swap two variables in place without having to use a temporary variable



# Practice

■ Write the C analog for the following assembly instructions

## Assembly

```
movq $0x10,%rbx
movq %rbx, (%rax)
movq $7, (%rcx)
movq (%rax), %rdx
```

## C Analog

```
b = 0x10;
*a = b;
*c = 7;
d = *a;
```