The following methods are defined for STL vectors, STL lists, and STL deques:

vector(p,q) or list(p,q) or deque(p,q): **Construct** the container **by iterating** the range [p,q) and **copying** each of these elements into the new container.

```
Example:
   vector<int> x;
   ...
   vector<int> y( x.begin(), x.end() );
```

This way, y is assigned a new vector containing copies of the elements in x. Of course, x must have the same base type as y.

Note that the method operates on the range [p,q), i.e., from p to q-1. However, since x.end() returns an imaginary element that lies just after the end of the container, then y(x.begin(), x.end()) would copy all elements of x.

The following methods are defined for STL vectors, STL lists, and STL deques:

```
vector(p,q) or list(p,q) or deque(p,q): Construct the container by iterating the range [p,q) and copying each of these elements into the new container.
```

assign(p,q): **Delete** the contents, and **assigns its new contents by iterating** the range [p,q) and **copying** each of these elements into the container.

```
Example:
  vector<int> x;
  ...
  y.assign( x.begin(), x.end() );
```

This way, the content of y will be deleted, and then y will be assigned a new vector containing copies of the elements in x. Of course, x must have the same base type as y.

• The following methods are defined for STL vectors, STL lists, and STL deques:

```
vector(p,q) or list(p,q) or deque(p,q): Construct the container by iterating the range [p,q) and copying each of these elements into the new container.
```

assign(p,q): **Delete** the contents, and assigns its new contents by iterating the range [p,q) and copying each of these elements into the container.

insert(p,e): Insert a copy of e just prior to the position given by iterator p and shift the subsequent elements one position to the right. (except for STL lists, where no shifting occurs, since it is implemented as a doubly-linked list)

erase(p): Remove and destroy the element at the position given by p and shift the subsequent elements one position to the left. (except for STL lists)

erase(p,q): Iterate the range [p,q), removing and destroying all these elements and shifting subsequent elements to the left to fill the gap. (except for STL lists)

clear(): **Delete** all elements of the container.

The following methods are defined for STL vectors, STL lists, and STL deques:

sort(p,q): **Sort** the elements in the range [p,q) in **ascending order**. It is assumed that ("<") is defined for the base type. (sort is not supported by STL lists)

• The following methods are defined for STL vectors, STL lists, and STL deques:

```
sort(p,q): Sort the elements in the range [p,q) in ascending order. It is assumed
          that ("<") is defined for the base type. (sort is not supported by STL lists)
random_shuffle(p,q): Rearrange the elements in the range [p,q) in random order.
                      (random shuffle is not supported by STL lists)
reverse(p,q): Reverse the elements in the range [p,q).
find(p,q,e): Return an iterator to the first element in the range [p,q) that is equal
            to e; if e is not found, q is returned.
min_element(p,q): Return an iterator to the minimum element in the range [p,q).
\max_{e} element(p,q): Return an iterator to the maximum element in the range [p,q).
for_each(p,q,f): Apply the function f to the elements in the range [p,q).
```

#### Write the output of each line here

#### **EXAMPLE**

```
int a[] = \{17, 12, 33, 15, 62, 45\};
vector<int> v(a, a + 6);
                                              // v: 17 12 33 15 62 45
cout << v.size();</pre>
                                              // outputs: 6
                                              // v: 17 12 33 15 62
v.pop_back();
cout << v.size();</pre>
                                              // outputs: 5
v.push_back(19);
                                              // v: 17 12 33 15 62 19
cout << v.front() << " " << v.back();
                                              // outputs: 17 19
sort(v.begin(), v.begin() + 4);
                                              // v: (12 15 17 33) 62 19
v.erase(v.end() – 4, v.end() – 2);
                                              // v: 12 15 62 19
                                              // outputs: 4
cout << v.size();
char x[] = {'b', 'r', 'a', 'v', 'o'};
vector<char> w(x, x + 5);
                                              // w: bravo
// #include <algorithm> to use random_shuffle
random_shuffle(w.begin(), w.end());
                                        // w: o v r a b
                                              // w:sovrab
w.insert(w.begin(), 's');
for (vector<char>::iterator p = w.begin(); p != w.end(); ++p)
   cout << *p << " ":
                                              // outputs: s o v r a b
return EXIT SUCCESS;
```

# 63 SEQUENCES

## SEQUENCES

- A sequence is an ADT that:
  - > Supports all the functions of the **List ADT**
  - > Provides functions for accessing elements by their index (as in the Vector ADT)

More specifically, the Sequence ADT consists of the operations of the List ADT, plus the following two functions:

- $\triangleright$  atIndex( i ): Return the **position/iterator** of the element at **index** i
- $\rightarrow$  indexOf( p ): Return the index of the element at position/iterator p

A sequence can be implemented using either a linked list, or an array.

## SEQUENCES – LIST IMPLEMENTATION



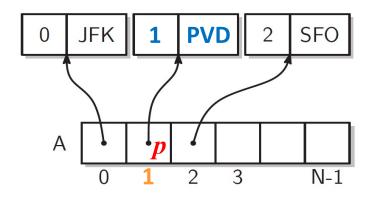
```
// get index from position
int indexOf(const Iterator& p) const {
    Iterator q = begin();
    int j = 0;
    while (q != p) // until finding p
        {++q; ++j;} // advance and count hops
    return j;
}
```

```
// get position from index
Iterator atIndex(int i) const {
    Iterator p = begin();
    for (int j = 0; j < i; j++)
        ++p; // advance
    return p;
}</pre>
```

- **Disadvantage:** atIndex(i) and indexOf(p) run in O(n); they may perform n iterations!
- Advantage: insert( p, e) and erase( p ) run in O(1); no need to shift elements!

## SEQUENCES - ARRAY IMPLEMENTATION

- Recall that a sequence is an ADT that supports "indexOf(p)" and "atIndex(i)"
- If implemented as an array, we must have an array of positions, each of which points to a pair consisting of an element, and the index of that element.

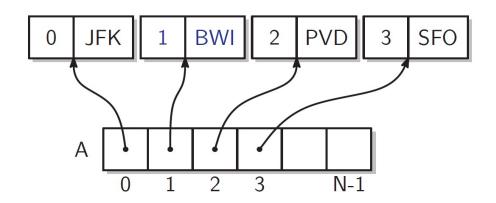


A[1] is a position, p, pointing to a pair consisting of:

- An element, which is PVD
- The index of that element, which is 1

To insert an element at index 1, we must:

- $\triangleright$  **Shift** all the positions whose index is  $\ge 1$
- ightharpoonup Update the indices of all the positions whose index is  $\geq 1$

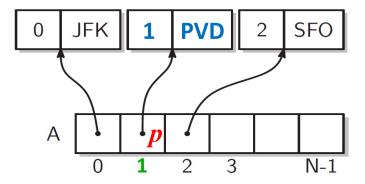


### LIST VS. ARRAY IMPLEMENTATION

## List:



- Disadvantage: atIndex( i ) and indexOf( p ) run in O(n); they may perform n iterations!
- Advantage: insert(p, e) and erase(p) run in O(1); no need to shift elements!



#### **Array:**

- **Disadvantage:** insert(p, e) and erase(p) run in O(n); we must shift elements!
- Advantage: atIndex(i) and indexOf(p) run in O(1), because:
  - $\triangleright$  Given an index *i*, the position at *i* is stored in A[*i*].
  - Given a position p, the index of p is stored in the object that p points to.



- "Bubble Sort" is a sorting algorithm that performs a series of passes over a sequence.
- In each pass, it compares each element to the one after it, and swaps them if needed!

#### 1<sup>st</sup> pass:

```
initial array:
                5, 7, 2, 6, 9, 3
Swap? No!
               5, 7, 2, 6, 9, 3
                5, 7, 2, 6, 9, 3
Swap? Yes
                5, 2, 7, 6, 9, 3
Swap? Yes
                5, 2, 6, 7, 9, 3
Swap? No!
                5, 2, 6, 7, 9, 3
Swap? Yes
After 1<sup>st</sup> pass: 5, 2, 6, 7, 3, 9
```

### 2<sup>nd</sup> pass:

initial array: 5, 2, 6, 7, 3, 9

Swap? Yes 5, 2, 6, 7, 3, 9

Swap? No! 2, 5, 6, 7, 3, 9

Swap? No! 2, 5, 6, 7, 3, 9

Swap? Yes 2, 5, 6, 7, 3, 9

Swap? No! 2, 5, 6, 3, 7, 9

After 2<sup>nd</sup> pass: 2, 5, 6, 3, 7, 9

#### 3<sup>rd</sup> pass:

2, 5, 6, 3, 7, 9

initial array:

Swap? No! 2,5,6,3,7,9

Swap? Yes 2,5,6,3,7,9

Swap? No! 2,5,6,3,7,9

Swap? No! 2,5,3,6,7,9

Swap? No! 2,5,3,6,7,9

After 3<sup>rd</sup> pass: 2,5,3,6,7,9

#### 1<sup>th</sup> pass:

initial array: 5, 7, 2, 6, 9, 3

Swap? No! 2, 5, 3, 6, 7, 9

Swap? Yes 2, 5, 3, 6, 7, 9

Swap? No! 2, 3, 5, 6, 7, 9

Swap? No! 2, 3, 5, 6, 7, 9

After 4<sup>th</sup> pass: 2, 3, 5, 6, 7, 9

- "Bubble Sort" has the following properties:
  - ➤ In 1<sup>st</sup> pass, once the **largest element** is reached, it keeps on being swapped until it gets to the **last position**
  - ➤ In 2<sup>nd</sup> pass, once the **second largest element** is reached, it keeps on being swapped until it gets to the **second-to-last position**
  - At the end of the  $i^{th}$  pass, the last i elements (i.e., those at indices n-i to n-1) are sorted.
- The last property implies that
  - $\triangleright$  It suffices to **stop after** n **passes**.
  - $\rightarrow$  The *i*<sup>th</sup> pass can be limited to the first n-i+1 elements.

## 1st pass:

```
initial array:
               5, 7, 9, 6, 2, 3
Swap? No!
Swap? No!
Swap? Yes
               5, 7, 9, 6, 2, 3
Swap? Yes
Swap? Yes
               5, 7, 6, 2, 9, 3
After 1<sup>st</sup> pass: 5, 7, 6, 7, 3, 9
```

- In the example we saw earlier, we can see how:
  - At the end of the  $i^{th}$  pass, the last i elements are sorted, implying that the  $i^{th}$  pass can be limited to the first n-i+1 elements.

#### 1<sup>st</sup> pass:

initial array: 5, 7, 2, 6, 9, 3 Swap? No! 5, 7, 2, 6, 9, 3 5, 7, 2, 6, 9, 3 Swap? Yes 5, 2, 7, 6, 9, 3 Swap? Yes 5, 2, 6, 7, 9, 3 Swap? No! 5, 2, 6, 7, 9, 3 Swap? Yes After 1<sup>st</sup> pass: 5, 2, 6, 7, 3, 9

#### 2<sup>nd</sup> pass:

initial array: 5, 2, 6, 7, 3, 9

Swap? Yes 5, 2 6, 7, 3, 9

Swap? No! 2, 5, 6, 7, 3, 9

Swap? No! 2, 5, 6, 7, 3, 9

Swap? Yes 2, 5, 6, 7, 3, 9

Swap? No! 2, 5, 6, 3, 7, 9

After 2<sup>nd</sup> pass: 2, 5, 6, 3, 7, 9

#### 3<sup>rd</sup> pass:

initial array: 2, 5, 6, 3, 7, 9

Swap? No! 2, 5, 6, 3, 7, 9

Swap? No! 2, 5, 6, 3, 7, 9

Swap? Yes 2, 5, 6, 3, 7, 9

Swap? No! 2, 5, 3, 6, 7, 9

Swap? No! 2, 5, 3, 6, 7, 9

After 3<sup>rd</sup> pass: 2, 5, 3, 6, 7, 9

#### 4<sup>th</sup> pass:

initial array: 5, 7, 2, 6, 9, 3

Swap? No! 2, 5, 3, 6, 7, 9

Swap? Yes 2, 5, 3, 6, 7, 9

Swap? No! 2, 3, 5, 6, 7, 9

Swap? No! 2, 3, 5, 6, 7, 9

After 4<sup>th</sup> pass: 2, 3, 5, 6, 7, 9

What is the complexity of Bubble Sort?

The number of comparisons is  $\approx n + (n-1) + (n-2) + ... + 2 + 1 = \frac{n(n+1)}{2}$  which is  $O(n^2)$ 

#### 1<sup>st</sup> pass:

initial array: 5, 7, 2, 6, 9, 3

Swap? No! 5, 7, 2, 6, 9, 3

Swap? <u>Yes</u> 5, 7, 2, 6, 9, 3

Swap? <u>Yes</u> 5, 2, 7, 6, 9, 3

Swap? No! 5, 2, 6, 7, 9 3

Swap? <u>Yes</u> 5, 2, 6, 7, 9, 3

After 1<sup>st</sup> pass: 5, 2, 6, 7, 3, 9

#### 2<sup>nd</sup> pass:

initial array: 5, 2, 6, 7, 3, 9

Swap? <u>Yes</u> [5, 2] 6, 7, 3, 9

Swap? No! 2,5,6,7,3,9

Swap? No! 2, 5, 6, 7, 3, 9

Swap? <u>Yes</u> 2, 5, 6, 7, 3, 9

Swap? No! 2, 5, 6, 3, **7, 9** 

After 2<sup>nd</sup> pass: 2, 5, 6, 3, 7, 9

#### 3<sup>rd</sup> pass:

initial array: 2, 5, 6, 3, 7, 9

Swap? No! 2, 5, 6, 3, 7, 9

Swap? No! 2,5,6,3,7,9

Swap? <u>Yes</u> 2, 5, 6, 3, 7, 9

Swap? No! 2, 5, 3, 6, 7, 9

Swap? No! 2, 5, 3, 6, 7, 9

After 3<sup>rd</sup> pass: 2, 5, 3, <u>6, 7, 9</u>

#### 4<sup>th</sup> pass:

initial array: 5, 7, 2, 6, 9, 3

Swap? No! [2, 5] 3, 6, 7, 9

Swap? <u>Yes</u> 2,5,3,6,7,9

Swap? No! 2, 3, 5, 6, 7, 9

Swap? No! 2, 3, 5, 6, 7, 9

Swap? No! 2, 3, 5, 6, 7, 9

After 4<sup>th</sup> pass: 2, 3, 5, 6, 7, 9

What is the complexity of Bubble Sort?

```
The number of comparisons is \approx n + (n-1) + (n-2) + ... + 2 + 1 = \frac{n(n+1)}{2} which is O(n^2)
```

- Clearly, Bubble Sort requires accessing elements at different indices. The above analysis assumes that an element at index i can be accessed in O(1) time.
- Now, suppose we are sorting a sequence. Then:
  - If we use an array-based implementation, where atIndex(i) runs in O(1), the total runtime of BubbleSort is indeed  $O(n^2)$
  - $\triangleright$  On the other hand, if we use a **list-based implementation**, where atIndex(i) runs in O(n) time, the total runtime becomes O(n<sup>3</sup>)
- Thus, choosing the appropriate implementation of the ADT matters!