Synchronization (I)
Operating Systems
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Background
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Outline

- Background
- Critical section
- Synchronization hardware
- Semaphores

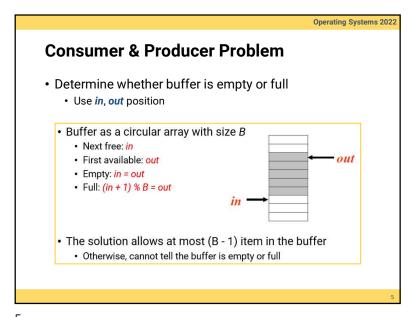
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Background

- Concurrent access to shared data may result in data inconsistency
- Maintaining data consistency requires mechanism to ensure the **orderly execution** of cooperating processes



Concurrent Operations on Counter

• The statement "counter++" may be implemented in machine language as

move ax, counter add ax, 1 move counter, ax

• The statement "counter-" may be implemented as

move bx, counter sub bx, 1

move counter, bx

```
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   Consumer & Producer Problem (cont.)
   • Determine whether buffer is empty or full
        · Use count value
/* Producer */
                                      /* Consumer */
while (true) {
                                       while (true) {
    // produce an item in next produced.
                                          while (counter == 0);
   while (counter == BUFFER_SIZE);
                                              // do nothing
                                          next_consumed = buffer[out];
        // do nothing.
    buffer[in] = next_produced;
                                          out = (out + 1) % BUFFER_SIZE;
    in = (in + 1) % BUFFER_SIZE;
                                          counter--;
    counter++;
                                          // consume the item in next consumed.
```

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```
Instruction Interleaving
```

 Assume counter is initially 5. One interleaving of statement is

```
producer: move ax, counter

producer: add ax, 1

context switch

consumer: move bx, counter

consumer: sub bx, 1

context switch

producer: move counter, ax

context switch

consumer: move counter, ax

context switch

consumer: move counter, bx

\Rightarrow counter = 6
```

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Operating Systems 2022 Another Example · An example in the kernel P_0 P_1 pid_t child = fork (); pid_t child = fork (); request request next available pid = 2615 return return 2615 2615 child = 2615 child = 2615

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Critical Section

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Race Condition

- The situation where several processes access and manipulate shared data concurrently.
- The final value of the shared data depends upon which process finishes last
- To prevent race condition, concurrent processes must be **synchronized**
 - On a single-processor machine, we could disable interrupt or use non-preemptive CPU scheduling
 - But how about on multi-processor machines and preemptive scheduling?
- We need a mechanism to solve the synchronization issue, commonly described as critical section problem

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The Critical-Section Problem

- Purpose
 - · A protocol for processes to cooperate
- Problem description
 - N processes are competing to use some shared data
 - Each process has a code segment, called critical section, in which the shared data is accessed
 - Ensure that when one process is executing in its critical section, no other process is allowed to execute in its critical section
 - → mutually exclusive!

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The Critical-Section Problem (cont.)

• General code section structure

• Only one process can be in a critical section

do {

entry section

critical section

modified shared data

exit section

remainder section

} while (1);

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CS Solutions and Synchronization Tools

- Software solution
- · Synchronization hardware
- Semaphore
- Monitor

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Critical-Section Requirements

- Mutual exclusion
 - If a process P is executing in its critical section (CS), no other processes can be executing in their CS
- Progress
 - If no process is executing in its CS and there exist some processes that wish to enter their CS, there processes cannot be postponed indefinitely
- Bounded Waiting
 - A bound must exist on the number of times that other processes are allowed to enter their CS after a process has made a request to enter its CS
- How to design entry and exit section to satisfy the above requirement?

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```
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 Algorithm for Two Processes
 • Only 2 processes P_0 and P_1
  · Shared variables
      • int turn; // initially turn = 0
      • turn == i → P<sub>i</sub> can enter its critical section
     /* Process 0 */
                                          /* Process 1 */
         while (turn != 0); — entry section
                                              while (turn != 1);
           critical section
                                                critical section
         turn = 1:
                              exit section — turn = 0;
           remainder section
                                                remainder section
     } while (1);
                                          } while (1);
                                                bounded-wait? Y
mutual exclusion? Y
                           progress? N
```

```
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Peterson's Solution for Two Processes
· Shared variables
    • int turn; // initially turn = 0
    • turn == i \rightarrow P_i can enter its critical section
    • boolean flag[2]; // initially flag[0] = flag[1] = false
    • flag[i] == true → P<sub>i</sub> is ready to enter its critical section
      /* Process i */
          flag[i] = true;
          turn = i;
                                        - entry section
          while (flag[i] \&\& turn == i);
            critical section
         flag[i] = false;
                                           exit section
            remainder section
      } while (1);
```

```
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Proof of Peterson's Solution
• Progress (e.g., P<sub>0</sub> withes to enter its CS)
    • (1) If P_1 is not ready \rightarrow flag[1] = false \rightarrow P_0 can enter
    • (2) If both are ready → flag[0] == flag[1] == true
         \rightarrow If turn == 0 then P_0 enters, otherwise P_1 enters
    · Either cases, some waiting process can enter CS
       /* Process 0 */
                                               /* Process 1 */
           flag[0] = true;
                                                   flag[1] = true;
           turn = 1;
                                              (2) turn = 0;
                                              while (flag[0] && turn == 0),
          → while (flag[1] && turn == 1)
              critical section
                                                     critical section
           flag[0] = false;
                                              (1) flag[1] = false;
              remainder section
                                                    remainder section
       } while (1);
                                              } while (1);
```

```
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Proof of Peterson's Solution

    Mutual exclusion

    If P<sub>0</sub> in CS → flag[1] == false || turn == 0

    If P₁ in CS → flag[0] == false || turn == 1

     • Assume both processes in CS → flag[0] == flag[1] == true
         \rightarrow turn == 0 for P_0 to enter, turn == 1 for P_1 to enter
         \rightarrow turn will be either 0 or 1, so P_0, P_1 cannot in CS at the same time
       /* Process 0 */
                                                 /* Process 1 */
       do {
                                                 do {
             flaq[0] = true;
                                                      flag[1] = true;
            turn = 1:
                                                     turn = 0:
            while (flag[1] && turn == 1)
                                                     while (flag[0] \&\& turn == 0)
                                                     flag[1] = false;
            flag[0] = false;
              remainder section
                                                        remainder section
       } while (1);
                                                 } while (1);
```

```
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Proof of Peterson's Solution
• Bounded waiting (e.g., Po withes to enter its CS)

    (1) Once P₁ exits CS → flag[1] == false → P₀ can enter

     • (2) If P₁ exits CS and reset flag[1] = true
         \rightarrow turn == 0 (overwrite P_0 setting) \rightarrow P_0 can enter
     • P<sub>0</sub> won't wait infinitely
       /* Process 0 */
                                               /* Process 1 */
            flag[0] = true;
                                               (2) flag[1] = true;
            turn = 1;
                                              → turn = 0;
          → while (flag[1] && turn == 1)
                                                   while (flag[0] && turn == 0);
              critical section
                                                    critical section
            flag[0] = false;
                                                  flag[1] = false;
              remainder section
                                                     remainder section
       } while (1);
                                               } while (1);
```

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Peterson's Solution and Modern Architecture

- Peterson's solution is not guaranteed to work on modern architectures
 - To improve performance, processors and/or compilers may reorder operations that have no dependencies
- For **single-threaded process** this is **OK** as the result will always be the same
- For multi-threaded process the reordering may produce inconsistent or unexpected results

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Peterson's Solution and Modern Architecture (cont.)

- Example (cont.):
 - Because the variables *flag* and *x* are independent of each other, the instructions:

```
x = 100;
flag = true;
```

for Thread2 may be reordered

• If this occurs, the output may be 0!

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Peterson's Solution and Modern Architecture (cont.)

- Example:
 - · Two threads share the data:

```
bool flag = true;
int x = 0;
```

Thread1 performs

```
while (!flag);
print x;
```

· Thread2 performs

```
x = 100;
flag = true;
```

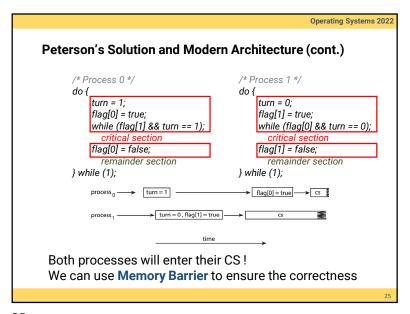
• Expected output will be 100

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```
Peterson's Solution and Modern Architecture (cont.)
      /* Process 0 */
                                           /* Process 1 */
      do {
                                              flag[1] = true;
           flag[0] = true;
           turn = 1:
                                               turn = 0:
          while (flag[1] && turn == 1);
                                               while (flag[0] && turn == 0);
            critical section
                                                 critical section
          flag[0] = false;
                                              flag[1] = false;
            remainder section
                                                 remainder section
      } while (1);
                                           } while (1);
 The variables flag[] and turn are independent, so they
 might be reordered
```



Memory Barrier (cont.)

 When a memory barrier instruction is performed, the system ensures that all loads and stores are completed before any subsequent loads or stores operations are performed

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Modification:

For Thread 1, we are guaranteed that the value of *flag* is loaded before the value of *x*

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Memory Barrier

- When a memory barrier instruction is performed, the system ensures that all loads and stores are completed before any subsequent loads or stores operations are performed
- Recall previous example:

```
/* Thread 1 */ /* Thread 2 */ while (! flag); load x = 100; store print x flag = true;
```

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Memory Barrier (cont.)

- When a memory barrier instruction is performed, the system ensures that all loads and stores are completed before any subsequent load or store operations are performed
- Modification:

For Thread 2, we are guaranteed that the assignment to x occurs before the assignment to flag

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```
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Producer & Consumer Problem
 /* Producer process 0 */
                                    /* Consumer process 0 */
 while (true) {
                                    while (true) {
      entry section
                                        entry section
                                        while (counter == 0):
     nextItem = getItem();
     while (counter == BUFFER_SIZE);
                                        item = buffer[out];
                                        out = (out + 1) % BUFFER SIZE:
     bufferlinl = nextItem:
     in = (in + 1) % BUFFER_SIZE;
                                        counter--:
     counter++;
                                        computing();
     computing();
                                        exit section
      exit section
 Incorrect. Deadlock if consumer enters the CS first
```

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```
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Producer & Consumer Problem (cont.)
 /* Producer process 0 */
                                   /* Consumer process 0 */
 while (true) {
                                   while (true) {
     nextItem = getItem();
                                       while (counter == 0);
     while (counter == BUFFER_SIZE);
                                       item = buffer[out];
                                       out = (out + 1) % BUFFER_SIZE;
     buffer[in] = nextItem;
     in = (in + 1) % BUFFER_SIZE;
                                       entry section
     entry section
                                       counter--;
     counter++;
                                       exit section
      exit section
                                       computing();
     computing();
Correct and maximize concurrent performance
```

```
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Producer & Consumer Problem (cont.)
 /* Producer process 0 */
                                    /* Consumer process 0 */
 while (true) {
                                    while (true) {
     nextItem = getItem();
                                        while (counter == 0);
     while (counter == BUFFER_SIZE);
                                        item = buffer[out];
                                        out = (out + 1) % BUFFER_SIZE;
     buffer[in] = nextItem:
     in = (in + 1) % BUFFER_SIZE;
                                        entry section
      entry section
                                        counter--;
     counter++;
                                        computing();
     computing();
                                         exit section
      exit section
 Correct but poor performance
```

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```
Bakery Algorithm (n processes)
```

- Before entering its CS, each process receives a number (#)
- Holder of the smallest # enters CS
- The numbering scheme always generates # in non-decreasing order; i.e., 1, 2, 3, 3, 4, 5, 5, 5 ...
- If processes P_i and P_j receive the same #, if i < j, then P_i is served first
- Notation:

```
• (a, b) < (c, d) if
```

a < c or

• a == c && b < d

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```
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    Bakery Algorithm (n processes) (cont.)
           // Process i:
           do {
               choosing[i] = true;
get ticket
               num[i] = max (num[0], num[1], ...num[n-1]) + 1;
               choosing[i] = false;
               for (j = 0; j < n; j++) {
                   while (choosing[i]);
FCFS
                   while ((num[i]!= 0) && ((num[i], i) < (num[i], i)));
              critical section
release ticket
               num[i] = 0:
               remainder section
    Bounded waiting because processes enter CS on a first
    come, first served basis
```

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Pthread Lock/Mutex Routines

- To use mutex, it must be declared as of type pthread_mutex_t and initialized with pthread_mutex_init()
- A mutex is destroyed with pthread_mutex_destroy()
- A critical section can then be protected using pthread_mutex_lock() and pthread_mutex_unlock()

```
#include "pthread.h"
pthread_mutex mutex;
pthread_mutex_init(&mutex, NULL);
pthread_mutex_lock(&mutex);
critical section
pthread_mutex_unlock(&mutex);
pthread_mutex_destroy(&mutex);
```

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Bakery Algorithm (n processes) (cont.)

- Why cannot compare when num is being modified?
- Without locking
 - · Let 5 be the current maximum number
 - If P_1 and P_4 take number together, but P_4 finishes before P_1
 - $P_1 = 0$, $P_4 = 6 \rightarrow P_4$ will enter the CS
 - After P₁ takes the number
 - $P_1 = P_4 = 6 \rightarrow P_1$ will enter the CS as well!
- With locking
 - P_4 will have to wait until P_1 finish taking the number
 - Both $P_1 \& P_4$ will have the new number "6" before comparison

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Condition Variables

- Condition variables (CV) represent some condition that a thread can
 - · Wait on, until the condition occurs; or
 - · Notify other waiting threads that the condition has occurred
- Three operations on condition variables
 - wait() block until another thread calls signal() or broadcast() on the CV

pthread_cond_wait(&theCV, &someLock)

- signal() wake up one thread waiting on the CV pthread_cond_signal(&theCV)
- broadcast() wake up all threads waiting on the CV pthread_cond_broadcast(&theCV)

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```
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 Condition Variables (cont.)

    Example

     • A thread is designed to take action when x == 0
     · Another thread is responsible for decrementing the counter
      pthread_cont_t cond;
      pthread_cond_init(cond, NULL);
      pthread_mutex_t mutex;
      pthread_mutex_init(mutex, NULL);
action() {
                                       counter() {
    pthread_mutex_lock(&mutex);
                                           pthread_mutex_lock(&mutex);
    if (x != 0)
        pthread_cond_wait(cond, mutex);
                                           if (x == 0)
    pthread_mutex_unlock(&mutex);
                                               pthread_cond_signal(cond);
                                           pthread_mutex_unlock(&mutex);
    take_action();
```

```
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    Using Condition Variables
action() {
                                           counter() {
                                               pthread_mutex_lock(&mutex);
   pthread_mutex_lock(&mutex);
   if (x != 0)
       pthread_cond_wait(cond, mutex);
                                               if (x == 0)
   pthread_mutex_unlock(&mutex);
                                                   pthread_cond_signal(cond);
   take_action();
                                               pthread_mutex_unlock(&mutex);
 Lock mutex
                                                Lock mutex
 Wait()

    Put the thread into sleep and releases

    the lock
```

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```
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    Using Condition Variables
                                           counter() {
action() {
                                               pthread_mutex_lock(&mutex);
   pthread_mutex_lock(&mutex);
   if (x != 0)
       pthread_cond_wait(cond, mutex);
                                               if (x == 0)
   pthread_mutex_unlock(&mutex);
                                                   pthread_cond_signal(cond);
   take_action();
                                               pthread_mutex_unlock(&mutex);
 Lock mutex
                                                Lock mutex
  Wait()
                                                Signal()
  • Put the thread into sleep and releases
    the lock
  · Waked up, but the thread is locked
```

```
Operating Systems 2022
  Using Condition Variables
  pthread_mutex_lock(&mutex);
                                            pthread_mutex_lock(&mutex);
  if (x != 0)
     pthread_cond_wait(cond, mutex);
                                            if (x == 0)
  pthread_mutex_unlock(&mutex);
                                                pthread_cond_signal(cond);
  take_action();
                                            pthread_mutex_unlock(&mutex);
Lock mutex
                                             Lock mutex
Wait()
                                             Signal()
· Put the thread into sleep and releases
                                             Release the lock

    Waked up, but the thread is locked

· Re-acquire lock and resume execution
```

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```
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     ThreadPool Implementation

    Task structure

    ThreadPool structure

      typedef struct {
                                                        pthread_mutex_t lock;
          void (*function)(void *)
                                                        pthread cond t notify;
          void *argument;
        threadpool_task_t;
                                                        threadpool task t queue
                                                        int queue size:
                                                        int tail;
                                                        int shutdown:
                                                        int started;
 · Allocate thread and task queue
pool->threads = (pthread_t *) malloc(sizeof(pthread_t) * thread_count);
pool->queue = (threadpool task t *) malloc(sizeof(threadpool task t) * queue size);
```

```
Operating Systems 2022
   Using Condition Variables
   pthread_mutex_lock(&mutex);
                                             pthread_mutex_lock(&mutex);
   if (x != 0)
       pthread_cond_wait(cond, mutex);
                                              if (x == 0)
pthread_mutex_unlock(&mutex);
                                                 pthread_cond_signal(cond);
   take_action();
                                             pthread_mutex_unlock(&mutex);
 Lock mutex
                                              Lock mutex
  Wait()
                                              Signal()
  · Put the thread into sleep and releases
                                              Release the lock

    Waked up, but the thread is locked

  • Re-acquire lock and resume execution
  Release the lock
```

```
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 ThreadPool Implementation (cont.)
static void *threadpool thread(void *threadpool)
    threadpool t *pool = (threadpool t *)threadpool;
    threadpool task t task;
    for(;;) {
        pthread_mutex_lock(&(pool->lock));
        while((pool->count == 0) && (!pool->shutdown)) {
            pthread_cond_wait(&(pool->notify), &(pool->lock));
```

```
ThreadPool Implementation (cont.)

/* Grab our task */

task.function = pool->queue[pool->head].function;
task.argument = pool->queue[pool->head].argument;

pool->head += 1;
pool->head = (pool->head == pool->queue_size) ? 0 : pool->head;
pool->count -= 1;

/* Unlock */
pthread_mutex_unlock(&(pool->lock));

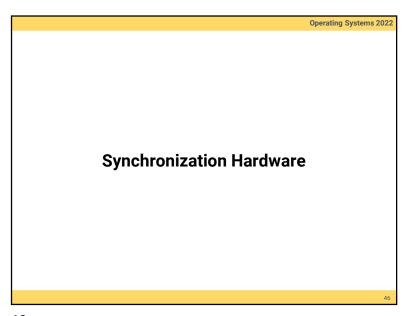
/* Get to work */
[*(task.function))(task.argument);
}
```

Hardware Support

• The CS problem occurs because the modification of a shared variable may be **interrupted**

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- If disable interrupts when in CS
 - · Not feasible in multiprocessor machine
 - · Clock interrupts cannot fire in any machine
- HW support solution: atomic instructions
 - · atomic: as one uninterruptible unit
 - Example: TestAndSet(var) and Swap(a, b)



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```
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 Atomic TestAndSet()
bool TestAndSet (bool &lock) {
                                    execute atomically:
   bool value = lock;
   lock = true;
                                    return the value of "lock" and
   return value;
                                    set "lock" to true
shared data: bool lock; // initially lock = false
do {
                                         while (TestAndSet (lock));
   while (TestAndSet (lock));
   critical section
                                          critical section
   lock = false;
                                         lock = false;
   remainder section
                                          remainder section
} while (1);
                                      } while (1);
                                               bounded-wait? N
mutual exclusion? Y
                          progress? Y
```

```
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  Atomic Swap()
Enter CS if lock == false
shared data: bool lock; // initially lock = false
do {
    key0 = true;
                                           key1 = true;
   while (key0 == true)
                                          while (key1 == true)
       Swap(lock, key0);
                                              Swap(lock, key1);
    critical section
                                           critical section
   lock = false:
                                          lock = false:
    remainder section
                                           remainder section
} while (1);
                                       } while (1);
                                                bounded-wait? N
mutual exclusion? Y
                           progress? Y
```

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Atomic Variables

 Atomic variable is another tool that provides atomic (uniterruptible) updates on basic data types such as integers and Booleans

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- Usually built with atomic instructions such as CompareAndSwap
- Example:
 - Let sequence be an atomic variable
 - Let increment() be an operation for incrementing the atomic variable sequence
 - The command *increment(&sequence)* ensures *sequence* is incremented without interruption

```
Operating Systems 2022
 Atomic CompareAndSwap()
bool CompareAndSwap (int &value, int expected, int new_value) {
   int temp = value;
   if (value == expected)
       value = new_value;
   return temp:
shared data: int lock; // initially lock = 0
do {
   while (CompareAndSwap (lock, 0, 1) != 0);
   critical section
   lock = 0:
   remainder section
} while (1);
                                              bounded-wait? N
mutual exclusion? Y
                          progress? Y
```

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```
Atomic Variables (cont.)

• The increment() function can be implemented as follows

5
bool increment (atomic_int &v) {
    int temp;
    do {
        temp = v;
    }
    while (temp != (CompareAndSwap (v, temp, temp+1));
}

bool CompareAndSwap (int &value, int expected, int new_value) {
    int temp = value;
    if (value == expected)
        value = new_value;
    return temp;
}
```

```
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    Atomic Variables (cont.)
    • The increment() function can be implemented as
      follows
       bool increment (atomic_int &v) {
           int temp;
           do {
               temp = v;
v is modified }
           while (temp != (CompareAndSwap (v, temp, temp+1));
                                            3 5
       bool CompareAndSwap (int &value, int expected, int new_value) {
           int temp = value;
                                    5
           if (value == expected)
               value = new_value;
           return temp;
```

```
Semaphores

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```

```
Atomic Variables (cont.)

• The increment() function can be implemented as follows

bool increment (atomic_int &v) {
    int temp;
    do {
        temp = v;
    v is modified }

    while (temp!= (CompareAndSwap (v, temp, temp+1));
    }
    3     3     4

bool CompareAndSwap (int &value, int expected, int new_value) {
    int temp = value;
    if (value == expected)
        value = new_value;
    return temp;
}
```

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POSIX Semaphore

• Semaphore is part of POSIX standard BUT it is not belonged to pthread
• It can be used with or without thread

• POSIX Semaphore routines

#include < semaphore.h>
sem_t sem;
sem_init(&sem);
sem_wait(&sem);
critical section

sem_signal(&sem);
sem_destroy(&sem);

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```
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Semaphores with Non-busy Waiting
· Semaphore is a data structure with queue
    • May use any queuing strategy (FIFO, FILO, etc)
      typedef struct {
        int value; // init to 0
                                        E.g.,:
                                          Value = -3
        struct process *L; // PCB queue
     } semaphore;
wait() and signal()

    Use system calls: block() and wakeup()

    Must be executed atomically

void wait (semaphore S) {
                                   void signal (semaphore S) {
    S.value-; // subtract first
                                       S.value++;
                                       if (S. value <= 0) {
    if (S.value < 0) {
                                           remove this process from S.L;
        add this process to S.L;
        sleep();
                                           wakeup(P);
   }}
                                       }}
```

```
    n-Process CS Problem Revisit
    Shared data:
        semaphore mutex; // initially mutex = 1
    Process P<sub>i</sub>:
        do {
            wait(mutex); // pthread_mutex_lock(&mutex) critical section signal(mutex); remainder section } while (1);
        progress? Y
        bounded-wait? depends on the implementation of wait()
```

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```
How to Ensure Atomic Wait & Signal Ops?
```

- Hardware support
 - TestAndSet
 - Swap
- · Software solution
 - · Peterson's solution
 - Bakery algorithm

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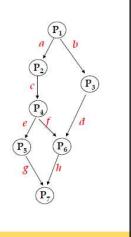
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```
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Semaphore with Critical Section
void wait (semaphore S) {
                                   void signal (semaphore S) {
    entry section
                                       entry section
   S.value--;
                                       S.value++;
    if (S.value < 0) {
                                       if (S.value <= 0) {
                                          remove this process from S.L;
        add this process to S.L;
        exit section
                                           exit section
                                           wakeup(P);
        sleep();
                                       } else {
   } else {
                                           exit section
        exit section
```

A More Complicated Example

- Initially, all semaphores are 0
- Begin
 - P1: S1; signal(a); signal(b);
 - P2: wait(a); S2; signal(c);
 - P3: wait(b); S3; signal(d);
 - P4: wait(c); S4; signal(e); signal(f);
 - P5: wait(e); S5; signal(g);
 - P6: wait(f); wait(d); S6; signal(h);
 - P7: wait(g); wait(h); S7;
- End

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```
Cooperation Synchronization

• P1 executes S1; P2 executes S2
• S2 will be executed only after ...

• Implementation
Shared variable:
semaphore sync; // initially sync = 0

P1:
P2:
S1; wait (sync);
signal (sync); S2;
```

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```
Deadlocks and Starvation
```

- Deadlock
 - Two processes are waiting indefinitely for each other to release resources

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- Starvation
 - · Some processes (threads) wait infinitely

```
P_0 P_1 wait(S); wait(Q); wait(Q); P_1 P_2 P_3 P_4 P
```