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# **Data Abstractions**

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# **Data Structure Concepts**

- Example: give an array, find the minimal element
  - How about doing this step 100 times
  - Sorting?
  - But if we need to insert a new element or update an old element?
- Static v.s. dynamic structures

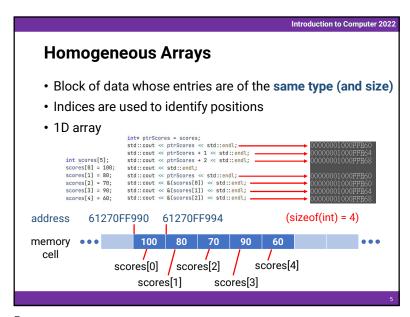
**Outline** 

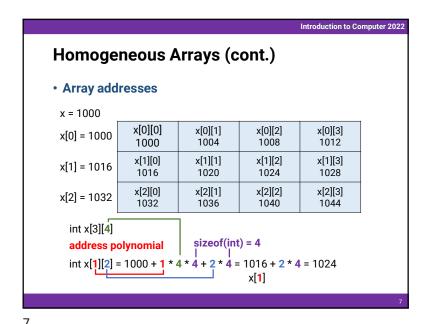
- Arrays
- Lists
- Stacks
- Queues
- Trees

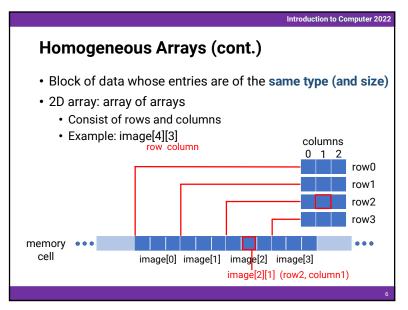
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**Outline** 

- Arrays
- Lists
- Stacks
- Queues
- Trees







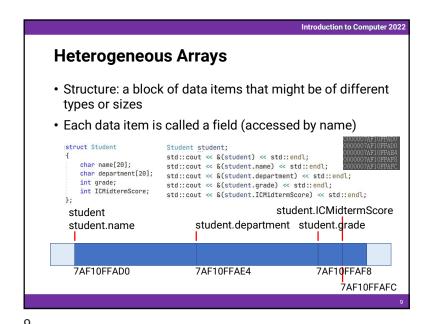
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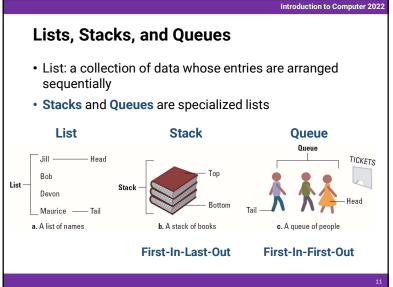
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Homogeneous Arrays (cont.)

    Parameter passing

    · Does it work?
    void UpdateArray2D(int **ptrX)
                                 void UpdateArray2D(int ptrX[3][4])
        ptrX[2][3] = 5;
                                     ptrX[2][3] = 5;
                                 void UpdateArray2D(int ptrX[][4])
    int main()
       int x[3][4];
                                     ptrX[2][3] = 5;
       UpdateArray2D(x);
     gbs E0167 類型 "int (*)[4]" 的引數與類型 "int **" 的參數不相容
     Why? no enough information for address polynomial
     Need the number of elements per row
```

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Outline

Arrays
Lists
Stacks
Queues
Trees

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Operations of a List

• Empty()

· Return true if the list is empty

• Size()

• Return the number of elements in the list

GetElement(index)

• Return the element with the given index

EraseElement(index)

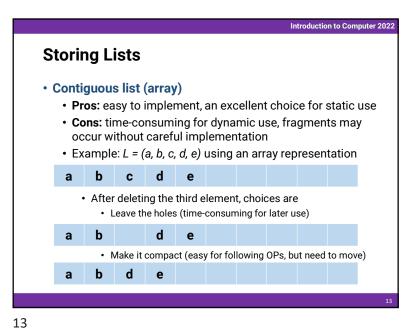
• Remove the element at the index

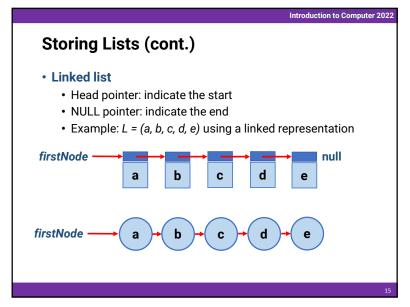
Insert(index, data)

• Insert a new element with the given data at the given index

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Storing Lists (cont.)

• Linked list

• Head pointer: indicate the start (firstNode)

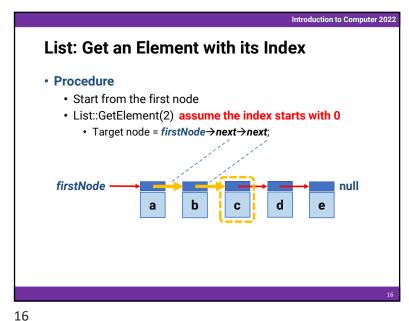
• NULL pointer: indicate the end

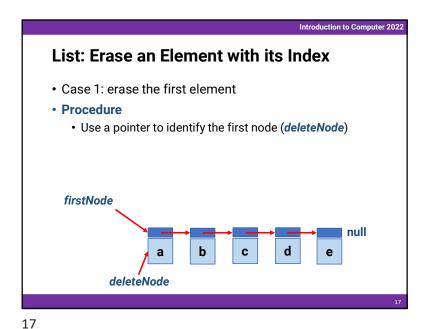
• Example: L = (a, b, c, d, e) using a linked representation

null

c a e b d

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List: Erase an Element with its Index

Case 1: erase the first element

Procedure

Use a pointer to identify the first node (deleteNode)

Change firstNode pointer to the second node

Delete the deleteNode

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List: Erase an Element with its Index

Case 1: erase the first element

Procedure

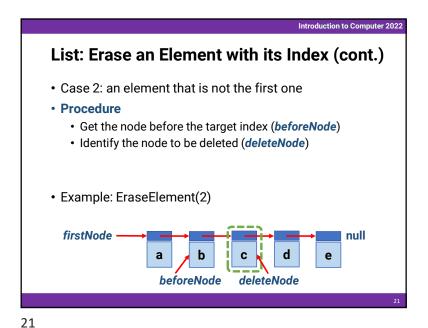
Use a pointer to identify the first node (deleteNode)
Change firstNode pointer to the second node

firstNode

deleteNode

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List: Erase an Element with its Index (cont.)

• Case 2: an element that is not the first one

• Procedure

• Get the node before the target index (beforeNode)

• Identify the node to be deleted (deleteNode)

• Change pointer in beforeNode

• Delete the deleteNode

• Example: EraseElement(2)

firstNode

beforeNode

List: Erase an Element with its Index (cont.)

• Case 2: an element that is not the first one

• Procedure

• Get the node before the target index (beforeNode)

• Identify the node to be deleted (deleteNode)

• Change pointer in beforeNode

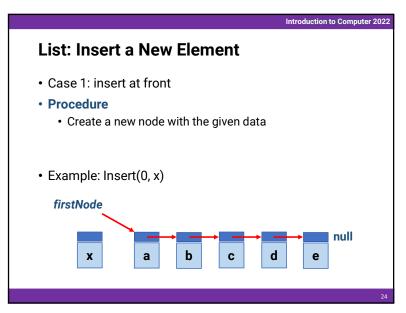
• Example: EraseElement(2)

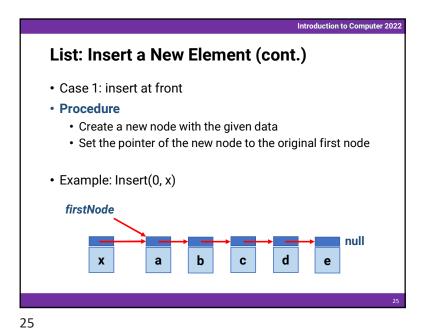
firstNode

beforeNode

beforeNode

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List: Insert a New Element (cont.)

Case 2: insert in the middle

Procedure

Find the node before the target (beforeNode)

Example: Insert(3, x) assume the index starts with 0

firstNode

List: Insert a New Element (cont.)

• Case 1: insert at front

• Procedure

• Create a new node with the given data
• Set the pointer of the new node to the original first node
• Update the firstNode pointer

• Example: Insert(0, x)

firstNode

u d e

List: Insert a New Element (cont.)

Case 2: insert in the middle

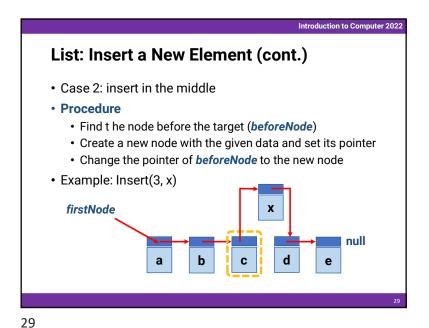
Procedure

Find the node before the target (beforeNode)

Create a new node with the given data and set its pointer

Example: Insert(3, x)

firstNode



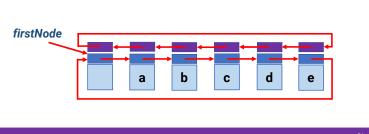
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Doubly linked circular list with header
Efficient for inserting at the end
C++ Standard Template Library (STL) adopts this implementation (std::list)

Variations (cont.)

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 $\bullet \ \underline{\text{https://en.cppreference.com/w/cpp/container/list}}\\$ 



Variations

• List with a dummy header node

firstNode

• Circular list

firstNode

a
b
c
d
e

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Outline

• Arrays

• Lists

• Stacks

• Queues

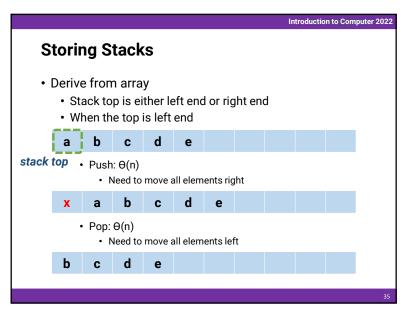
• Trees

# **Stacks and Queues**

- · Special cases of linked list
  - · Stack: record the stack point
  - · Queue: record head and tail
- Both can be implemented either using contiguous memory (array) or linked list
  - Contiguous (array) implementation is more common

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Stacks

Stack: a list in which entries are removed and inserted only at the head

Last-in-first-out (LIFO)

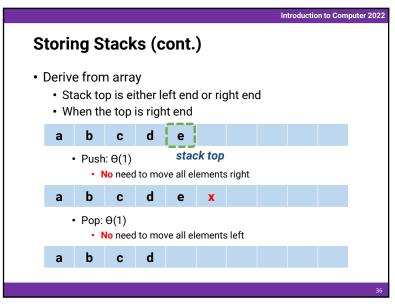
Operations

Top: get the head of the list (stack)

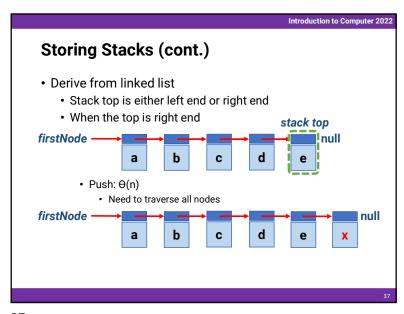
Pop: to remove the entry at the top

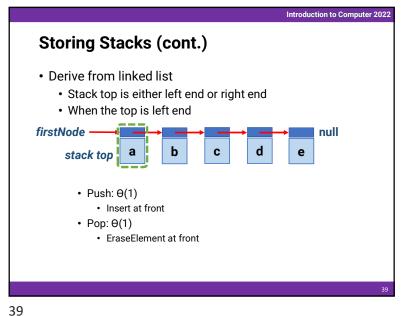
Push: to insert an entry at the top

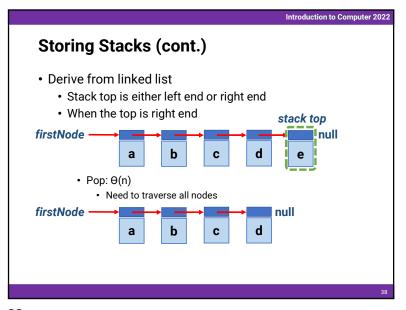
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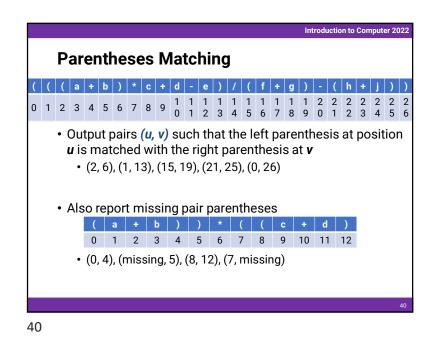


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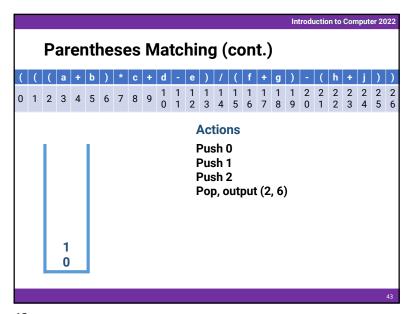


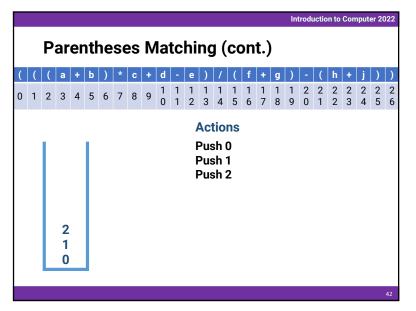
**Parentheses Matching (cont.)** 

- Scan expression from left to right
- When a left parenthesis is encountered, push its position to the stack

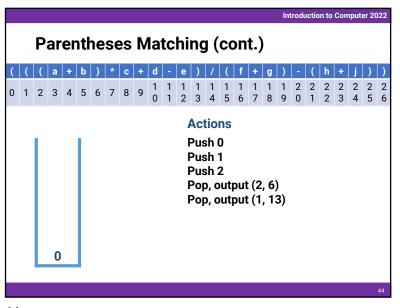
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 When a right parenthesis is encountered, pop matching position from the stack



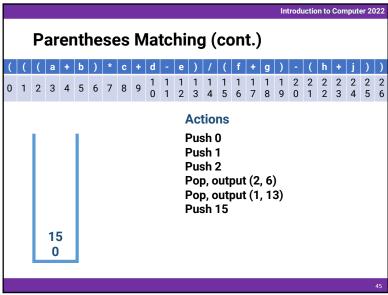


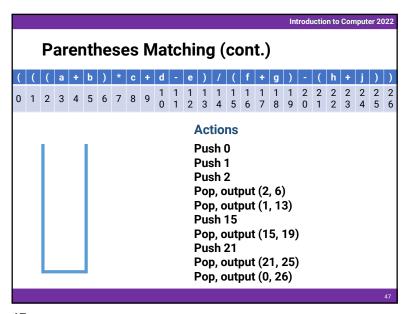
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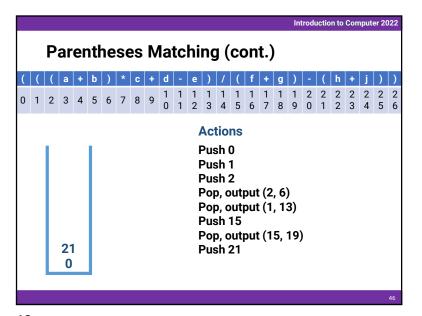


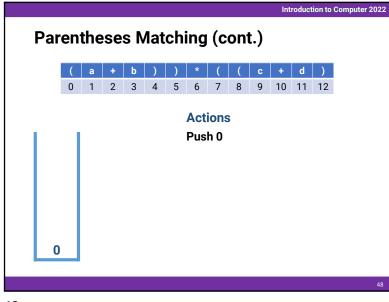
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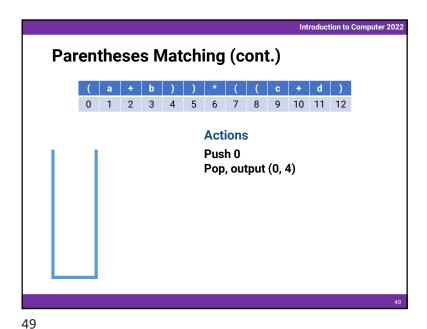
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Parentheses Matching (cont.)

( a + b ) ) \* ( ( c + d ) ) 0 1 2 3 4 5 6 7 8 9 10 11 12

Actions
Push 0
Pop, output (0, 4)
Pop, error for stack is empty!

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Parentheses Matching (cont.)

( a + b ) ) \* ( ( c + d ) ) 0 1 2 3 4 5 6 7 8 9 10 11 12

Actions
Push 0
Pop, output (0, 4)
Pop, error for stack is empty!
Push 7
Push 8

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Parentheses Matching (cont.)

( a + b ) ) \* ( ( c + d ) ) 
0 1 2 3 4 5 6 7 8 9 10 11 12

Actions

Push 0

Pop, output (0, 4)

Pop, error for stack is empty!

Push 7

Push 8

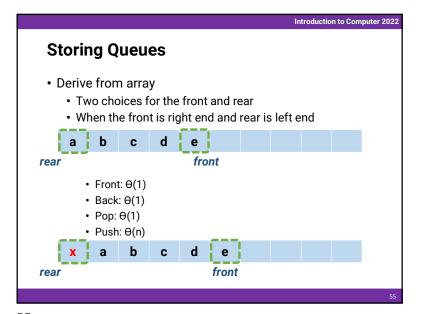
Pop, output (8, 12)

error for the left parenthesis at 7 is not matched any right parenthesis

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Outline

Arrays
Lists
Stacks
Queues
Trees



Queues

• Queue: a list in which entries are removed at the head and are inserted at the tail

• First-in-first-out (FIFO)

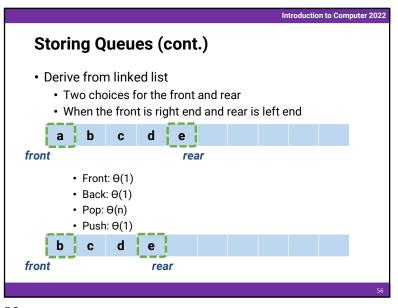
• Operations

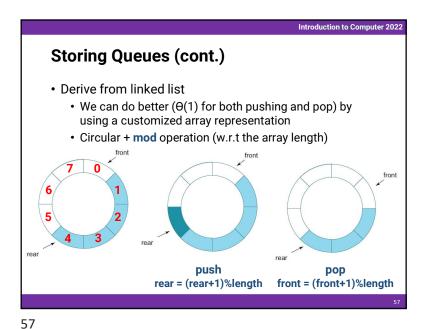
• Front: get the value of the front element

• Back: get the value of the back element

• Pop: remove the front element

• Push: add an element at the back of the queue





Storing Queues (cont.)

• Derive from linked list

• Handle empty and full queue (both front == rear)

• Use a size variable

• When pushing, ++size

• When popping, -size

• Queue is empty iff (size == 0)

• Queue is full iff (size == length)

Outline

 Arrays
 Lists
 Stacks
 Queues
 Trees

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Tree

Lists are useful for serially ordered data
Trees are useful for hierarchically ordered data

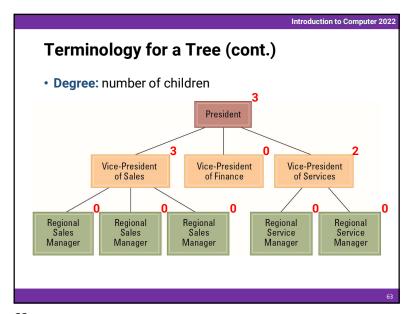
#### **Terminology for a Tree**

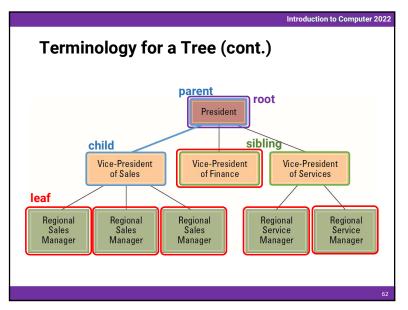
- Node: an entry in a tree
- Parent: the node immediately above a specified node

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- Child: a node immediately below a specified node
- Ancestor: parent, parent of the parent, etc.
- Descendent: child, child of a child, etc.
- Siblings: nodes sharing a common parent
- Root node: the node at the top
- Leaf node: the node at the bottom (thus has no children)

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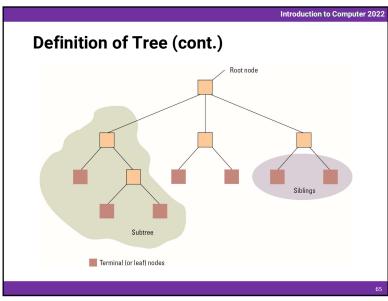
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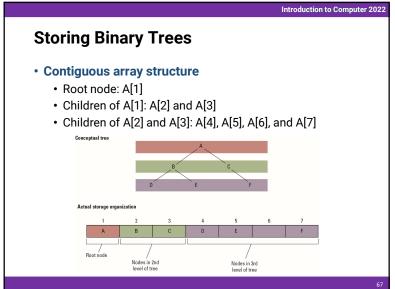
### **Definition of Tree**

- Recursive definition
- A tree t is a finite non-empty set of elements
- One of these elements is called the root
- The remaining elements, if any, are partitioned into trees, which are called the subtrees of *t*

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Binary Trees

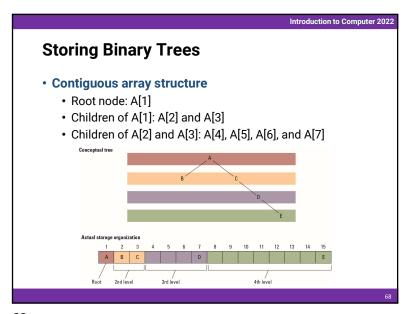
• Finite non-empty collection of elements

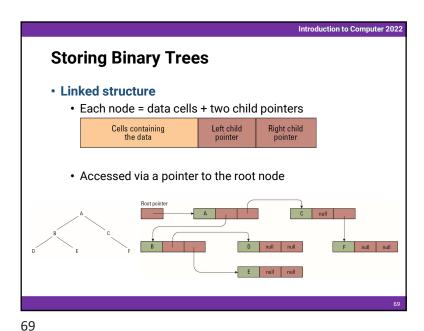
• A binary tree has a root element

• The remaining elements (if any) are partitioned into at most two binary trees

• Called the left and right subtrees

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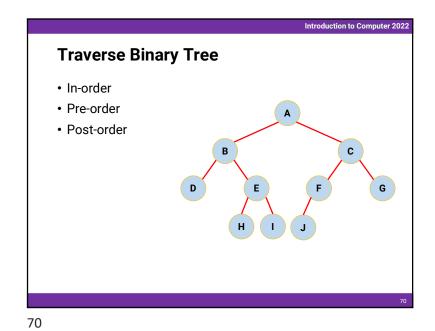


Traverse Binary Tree

• In-order

• Visit the left branch
• Visit the root node
• Visit the right branch

D  $\rightarrow$  B  $\rightarrow$  H  $\rightarrow$  E  $\rightarrow$  I  $\rightarrow$  A  $\rightarrow$  J  $\rightarrow$  F  $\rightarrow$  C  $\rightarrow$  G



Traverse Binary Tree (cont.)

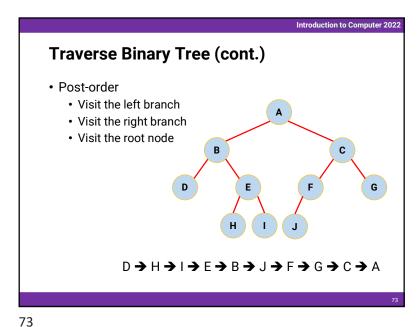
• Pre-order

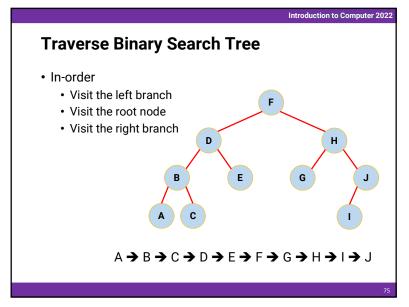
• Visit the root node

• Visit the left branch

• Visit the right branch

•  $A \Rightarrow B \Rightarrow D \Rightarrow E \Rightarrow H \Rightarrow I \Rightarrow C \Rightarrow F \Rightarrow J \Rightarrow G$ 





Binary Search Tree (BST)

• A binary tree

• Each node has a (key, value) pair

• For every node x, all keys in the left subtree of x are smaller than that in x

• For every node x, all keys in the right subtree of x are greater than that in x

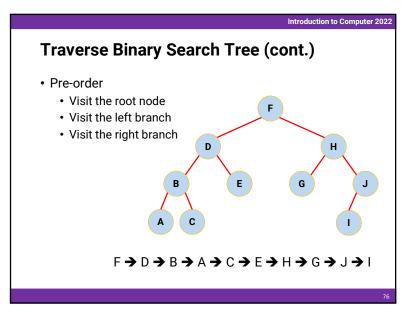
• Operations

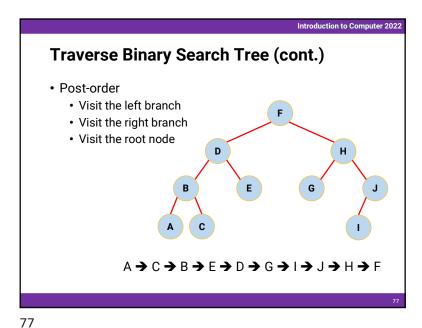
• Traversal

• Search

• Insertion

• Deletion





Search Binary Search Tree

• Similar to binary search (but may not be half-half)
• Example: find J

G

H

J

L

Deletion in Binary Search Tree

• Erase a leaf element whose key is 7

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40

6

15

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6

15

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2

8

12

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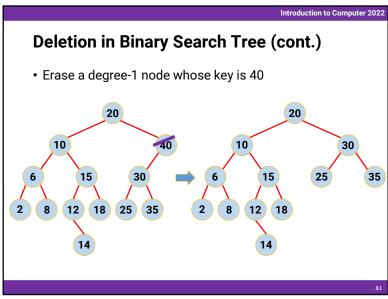
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Deletion in Binary Search Tree (cont.)

• Swap its with its successor

• The minimum node of the right subtree (keep going left)

• Or the parent if it is a left child

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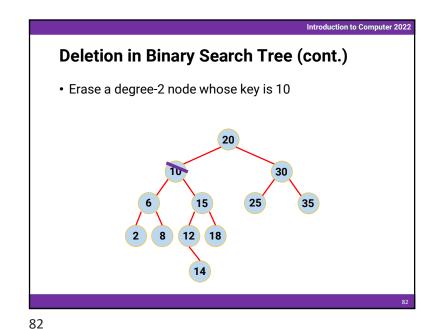
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8 10

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Deletion in Binary Search Tree (cont.)

• Since Its successor has a degree of 1 or 0, we can simply cut and reconnect the rest of the tree

