Camera

Introduction to Computer Graphics
Yu-Ting Wu

(Some of this slides are borrowed from Prof. Yung-Yu Chuang)

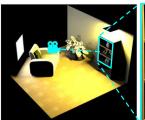
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How a Real-world Camera Works

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Recap.

- In computer graphics, we generate an image from a virtual 3D world
 - We are going to introduce the virtual camera and its projection used to render the scene

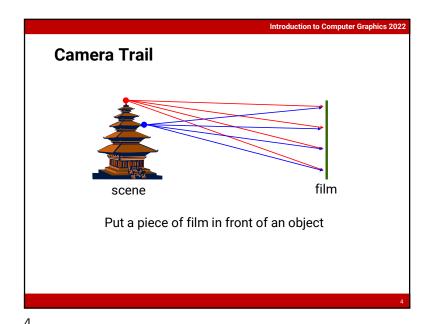




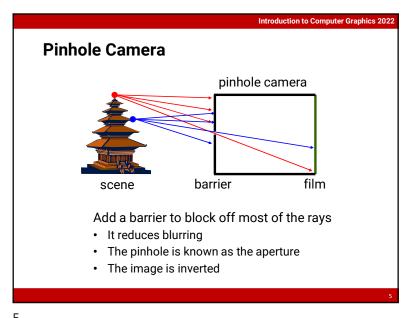
3D virtual world

rendered image

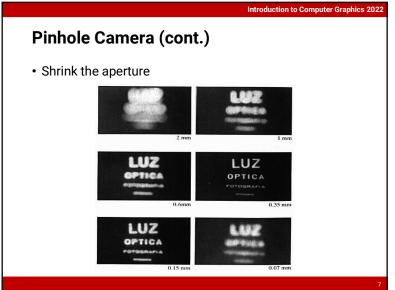
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Pinhole Camera (cont.)

• Shrink the aperture

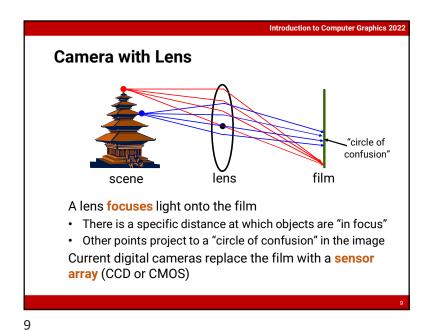
Why not make the aperture as small as possible?

• Less light gets through

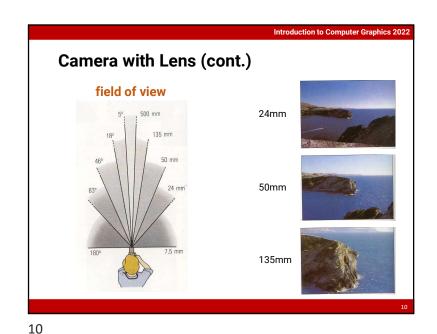
• Diffraction effect

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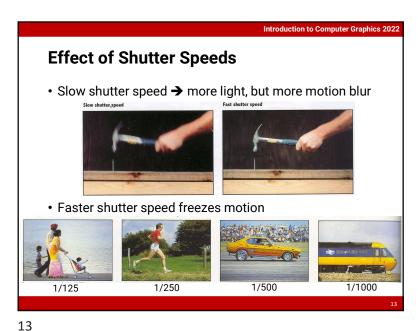


Introduction to Computer Graphics 2022 Exposure • Exposure = aperture + shutter speed • Aperture of diameter **D** restricts the range of rays (aperture may be on either side of the lens) • Shutter speed is the amount of time that light is allowed to pass through the aperture aperture optical axis



Introduction to Computer Graphics 2022 Exposure • Aperture (in f stop) • Shutter speed (in fraction of a second) Blade (closing) Blade (open) Focal plane (closed) Focal plane (open)

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Depth of Field

• Changing the aperture size affects depth of field
• A smaller aperture increases the range in which the object is approximately in focus

diaphragm

object with texture

Depth of Field (cont.)

• Changing the aperture size affects depth of field.

• A smaller aperture increases the range in which the object is approximately in focus

diaphragm

point in focus

object with texture

Effect of Depth of Field

LESS DEPTH OF FIELD

MORE DEPTH OF FIELD

Wider aperture

f/2

More Depth of Field

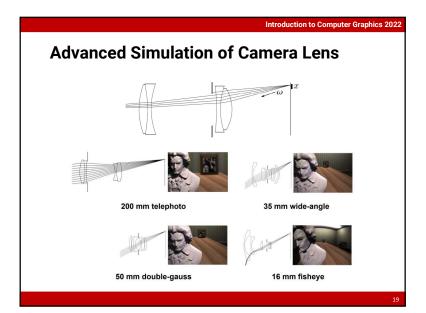
Smaller aperture

f/16

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Computer Graphics Camera

- To mimic the real-world functionality of a real-world camera
- In offline (high-quality) graphics, we can simulate all the imaging processes of a camera using ray tracing



Introduction to Computer Graphics 2022 **Advanced Simulation of Camera Lens**

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Computer Graphics Camera

- To mimic the real-world functionality of a real-world camera
- In offline (high-quality) graphics, we can simulate all the imaging processes of a camera using ray tracing
- In interactive or real-time graphics, we usually use a pinhole camera for its simplicity
 - Every object will always be in-focus
 - Depth of field and motion blur are simulated by other rendering techniques

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Computer Graphics Camera (cont.) The second of the secon

Camera (View) Transform

- The camera can be at an arbitrary position and have an arbitrary viewing direction in the world space
- This makes the projection difficult in terms of mathematics



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Introduction to Computer Graphics 2022 Camera Properties • The film is in front of the camera (to avoid up-side-down) Basic properties Camera position Viewing direction Camera local frame Field of view Aspect ratio viewing volume (view frustum) Advanced properties Right · Shutter speed Perspective projection (P) Lens system

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Camera (View) Transform (cont.) • To keep the math of projection simpler, we additionally define a camera (view, eye) space • In the camera space, the camera is at the origin (0, 0, 0) and looking at the negative Z-axis | Normalized Device Coordinates (NDC) | Ine of sight - Z | Inear plane |

...

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Camera (View) Transform (cont.)

OpenGL itself is not familiar with the concept of a camera
Instead, we simulate one by moving all objects in the scene in the reverse direction

Position: (0 0, 0 0, 0 0)
Rotation: (0 0, 0 0, 0 0)

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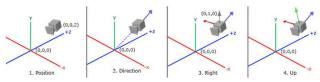
Camera (View) Transform (cont.) • Camera's local frame • Formed by the view direction (D), right (R), and up (U) vectors of the camera • The three axes of the local frame should be orthogonal

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Camera (View) Transform (cont.)

• To do this, we need to define the camera's local frame



- For each object, we transform its world coordinate to the camera coordinate by
 - Moving it with the inverse translation of the camera's position
 - Rotate the object to match the camera's local frame

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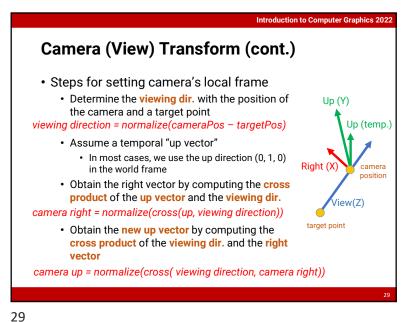
Camera (View) Transform (cont.)

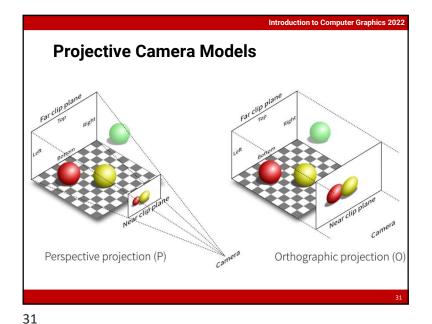
- · Set camera's local frame
 - However, it is usually difficult for a user to specify an orthogonal basis
 - OpenGL will do it for you (with the **Gram-Schmidt process**)

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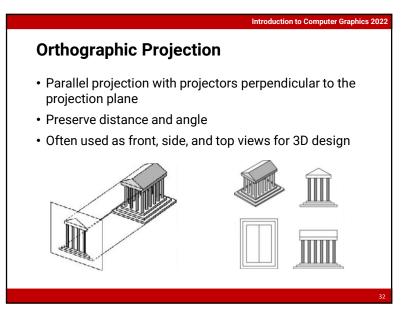
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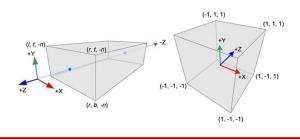
Introduction to Computer Graphics 2022 Camera (View) Transform (cont.) (P_x, P_y, P_z) is the • Camera (view) transformation camera's position right vector up vector viewing vector rotation matrix translation matrix

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Orthographic Projection (cont.)

- Need to define the viewing volume with its six planes: left, right, top, bottom, near, and far
 - The viewing volume (frustum) is cube-like
- Map the xyz-coordinate to the range [-1, 1]



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Orthographic Projection (cont.)

- Let the *I*, *r*, *t*, *b*, *n*, *f* be the boundaries of the left, right, top, bottom, near, and far planes
- An orthographic projection matrix can be written as

$$\begin{bmatrix} \frac{2}{r-l} & 0 & 0 & -\frac{r+l}{r-l} \\ 0 & \frac{2}{t-b} & 0 & -\frac{t+b}{t-b} \\ 0 & 0 & \frac{-2}{f-n} & -\frac{f+n}{f-n} \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

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Orthographic Projection (cont.)

• Let the *I*, *r*, *t*, *b*, *n*, *f* be the boundaries of the left, right, top, bottom, near, and far planes

$$l \le x \le r$$
 \longrightarrow $0 \le x - l \le r - l$

$$\longrightarrow -1 \le 2(\frac{x-l}{r-l}) - 1 \le 1 \implies -1 \le \frac{22}{r-l} - \frac{r+l}{r-l} \le 1$$

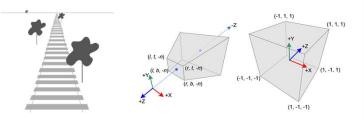
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Perspective Projection

- In our real lives, the objects that are farther away appear much smaller
- This effect is called perspective
- A perspective projection tries to mimic the vision of human eyes



Perspective Projection (cont.)

- Four components for the perspective projection matrix
 - · The aspect ratio of the screen
 - · The ratio between the width and the height
 - · The vertical field of view
 - The vertical angle of the camera through which we are looking at the world
 - The location of the near Z plane
 - · Used to clip objects that are too close to the camera
 - The location of the far Z plane
 - · Used to clip objects that are too distant from the camera

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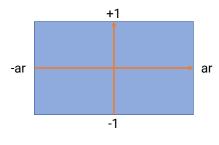
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Perspective Projection (cont.)

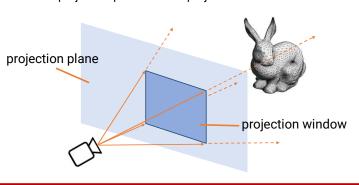
- Derivation of the perspective projection matrix
 - Determine the height of the projection window as 2
 - The width of the projection window becomes 2 times the aspect ratio (ar)



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Perspective Projection (cont.)

- Derivation of the perspective projection matrix
 - The projection plane and the projection window



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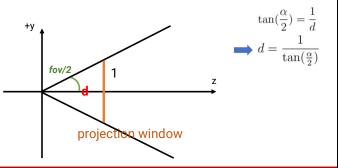
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Perspective Projection (cont.)

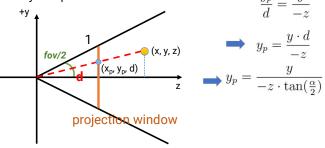
- Derivation of the perspective projection matrix
 - We can determine the distance from the camera to the projection window based on the field of view (fov)



Perspective Projection (cont.)

- Derivation of the perspective projection matrix
 - Assume we want to find the projected coordinate (x_p, y_p) of a 3D point (x, y, z)

• The y component can be derived as ...



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Perspective Projection (cont.)

- Derivation of the perspective projection matrix
 - Fill-in the matrix, based on the following conditions

$$x_p = \frac{x}{ar \cdot (-z) \cdot \tan(\frac{\alpha}{2})} \qquad y_p = \frac{z}{-z \cdot t}$$

$$\begin{bmatrix} x_p \\ y_p \\ z_p \\ w \end{bmatrix} = \begin{bmatrix} & & & & \mathbf{f(x)} & & & \\ & & & \mathbf{f(y)} & & & \\ & & & & \mathbf{f(z)} & & & \\ & & & & \mathbf{f(w)} & & & \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

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Perspective Projection (cont.)

- Derivation of the perspective projection matrix
 - Do the same derivation for the x component
 - Note in the x-direction we have to multiply the aspect ratio ar
 - · After that, we can obtain the following equations

$$x_p = \frac{x}{ar \cdot (-z) \cdot \tan(\frac{\alpha}{2})}$$

$$y_p = \frac{y}{-z \cdot \tan(\frac{\alpha}{2})}$$

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Perspective Projection (cont.)

- Derivation of the perspective projection matrix
 - Fill-in the matrix, based on the following conditions

$$x_p = \frac{x}{ar \cdot (-z) \cdot \tan(\frac{\alpha}{2})} \qquad y_p = \frac{x}{ar \cdot (-z)} \cdot \tan(\frac{\alpha}{2})$$

$$y_p = \frac{y}{-z \cdot \tan(\frac{\alpha}{2})}$$

$$\begin{bmatrix} x_p \\ y_p \\ z_p \\ w \end{bmatrix} = \begin{bmatrix} \frac{1}{ar \cdot \tan(\frac{\alpha}{2})} & 0 & 0 & 0 \\ 0 & \frac{1}{\tan(\frac{\alpha}{2})} & 0 & 0 \\ & & \mathbf{f(z)} & & \\ 0 & 0 & -1 & 0 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

Perspective Projection (cont.)

- Derivation of the perspective projection matrix
 - · Fill-in the matrix, based on the following conditions
 - Assume the Z function has a shape f(z) = A(-z) + B
 - · After perspective division, it becomes

$$f(z) = A - \frac{B}{z}$$

$$\begin{bmatrix} x_p \\ y_p \\ z_p \\ w \end{bmatrix} = \begin{bmatrix} \frac{1}{ar \cdot \tan(\frac{\alpha}{2})} & 0 & 0 & 0 \\ 0 & \frac{1}{\tan(\frac{\alpha}{2})} & 0 & 0 \\ 0 & 0 & A & B \\ 0 & 0 & -1 & 0 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

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Perspective Projection (cont.)

- Derivation of the perspective projection matrix
 - Fill-in the matrix, based on the following conditions

$$\begin{bmatrix} x_p \\ y_p \\ z_p \\ 1 \end{bmatrix} = \begin{bmatrix} \frac{1}{ar \cdot \tan(\frac{\alpha}{2})} & 0 & 0 & 0 \\ 0 & \frac{1}{\tan(\frac{\alpha}{2})} & 0 & 0 \\ 0 & 0 & \frac{-nearZ - farZ}{nearZ - farZ} & \frac{2 \cdot farZ \cdot nearZ}{nearZ - farZ} \\ 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

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Perspective Projection (cont.)

- Derivation of the perspective projection matrix
 - Fill-in the matrix, based on the following conditions

$$f(-nearZ) = -1 \implies A - \frac{B}{-nearZ} = -1 \implies A = -1 - \frac{B}{nearZ}$$

$$f(-farZ) = 1$$
 \longrightarrow $A - \frac{B}{-farZ} = 1$ \longrightarrow $A = 1 - \frac{B}{farZ}$

$$2 = \frac{B}{farZ} - \frac{B}{nearZ}$$

 $\Rightarrow \frac{B \cdot nearZ - B \cdot farZ}{farZ \cdot farZ} = 2$ $\Rightarrow B(nearZ - farZ) = 2 \cdot farZ \cdot farZ$ $\Rightarrow B(nearZ - farZ) = 2 \cdot farZ \cdot farZ$ $A = \frac{-nearZ - farZ}{nearZ - farZ}$

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Camera Models Comparison





