



# **GPU Graphics Pipeline** (Part I)

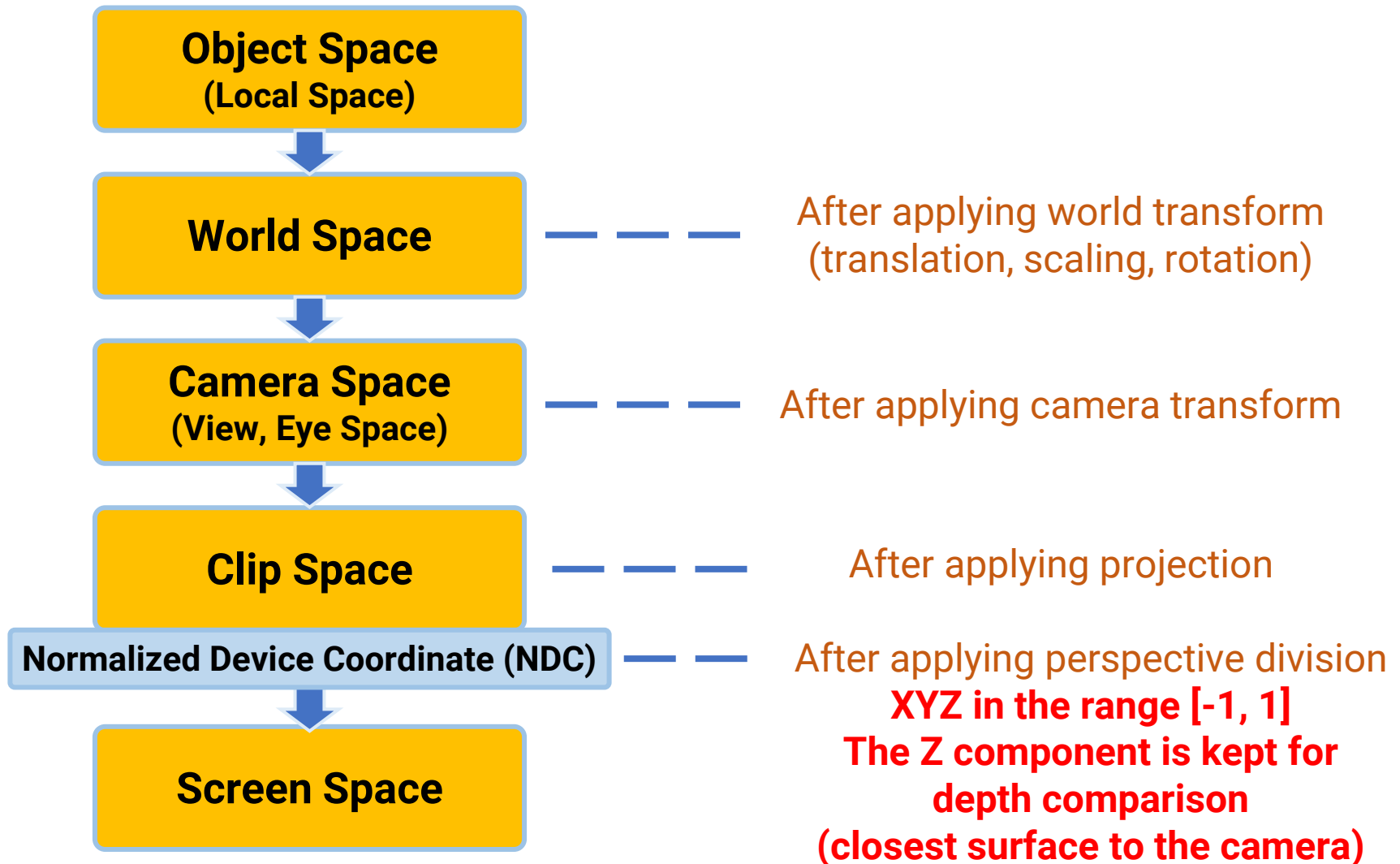
**Computer Graphics**

**Yu-Ting Wu**

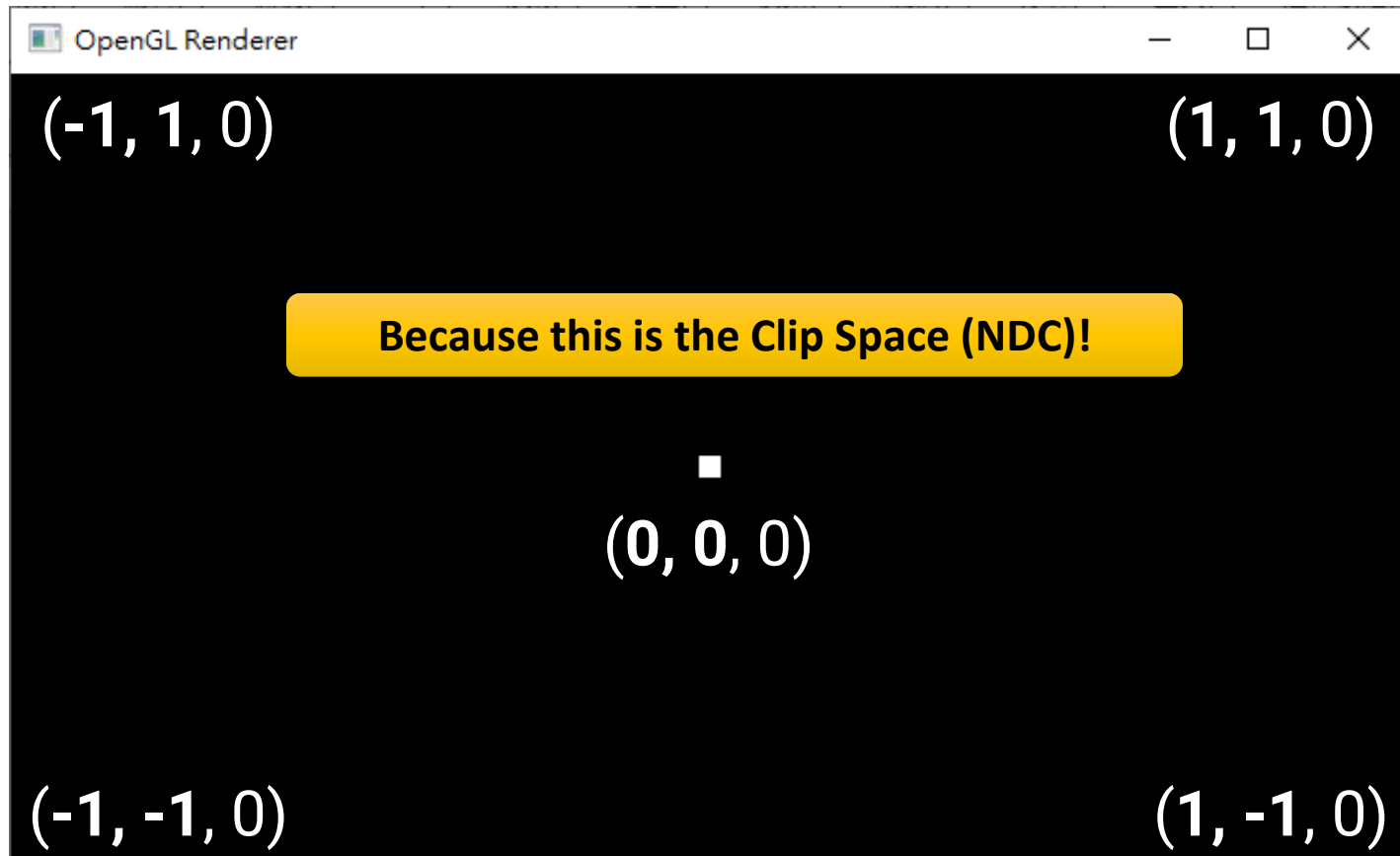
# Outline

- [GPU graphics pipeline](#) (Part I)
  - [OpenGL graphics pipeline 1.x](#)
- 
- OpenGL graphics pipeline 2.0 (Part II)
  - OpenGL and shader implementation

# Recap: Transformations



# Recap: NDC

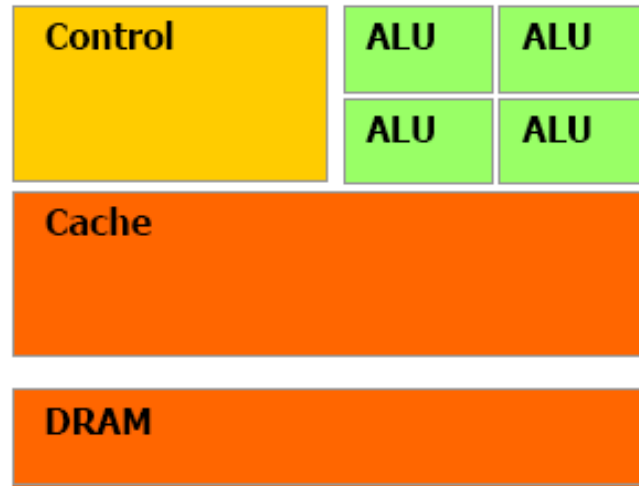


What about the z coordinate? You can find the point will only be visible if its z value is within  $[-1, 1]$

# Outline

- **GPU graphics pipeline**
- OpenGL graphics pipeline 1.x
- OpenGL graphics pipeline 2.0
- OpenGL and shader implementation

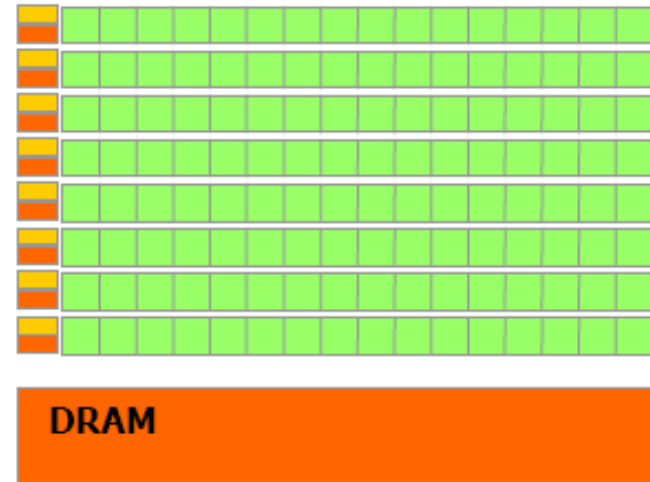
# CPU v.s. GPU



**CPU**

Good at

- Serial processing
- Control (branching)
- Larger cache

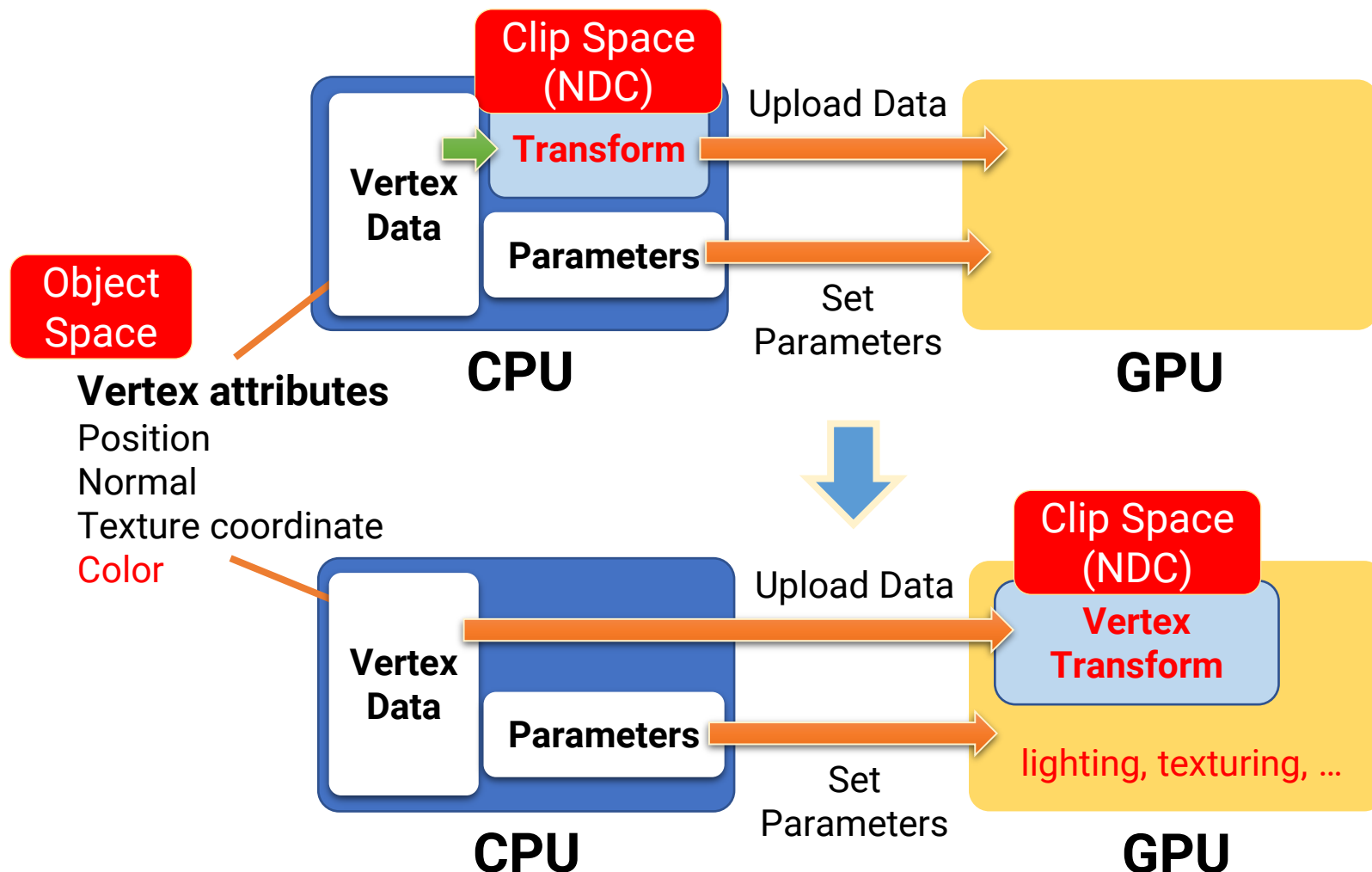


**GPU**

Good at

- Parallel processing
- SIMD
- Higher throughput

# CPU v.s. GPU (cont.)



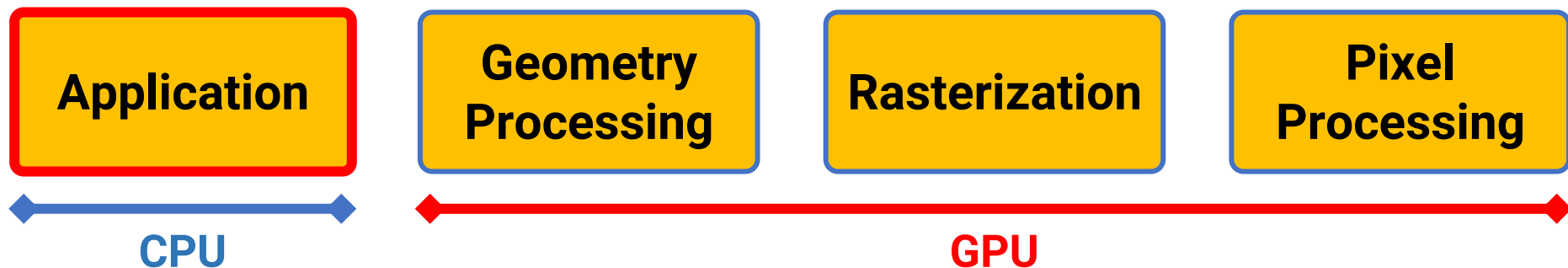
# Pipeline





# GPU Graphics Pipeline Overview

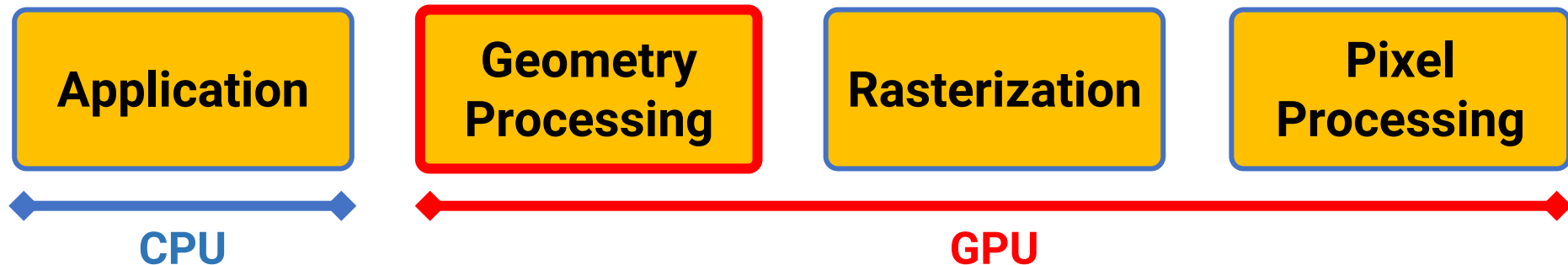
- Responsible for the fixed routines of bringing triangles to pixels
- Can be roughly categorized into 3 stages



- Physical simulation
- Animation
- Collision detection
- Global acceleration
- etc.

# GPU Graphics Pipeline Overview (cont.)

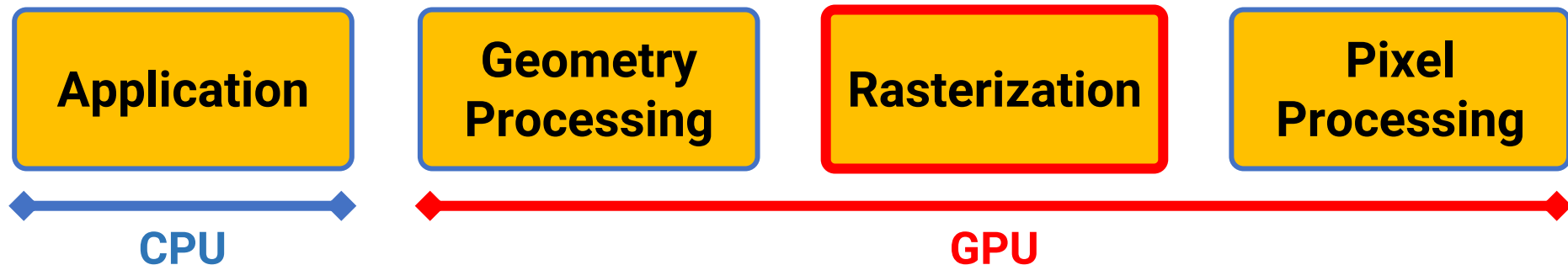
- Responsible for the fixed routines of bringing triangles to pixels
- Can be roughly categorized into 3 stages



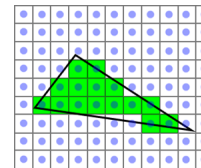
- Vertex transform and projection
- Vertex lighting and shading (rarely used now)
- Geometry assembly
- Clipping
- Culling

# GPU Graphics Pipeline Overview (cont.)

- Responsible for the fixed routines of bringing triangles to pixels
- Can be roughly categorized into 3 stages



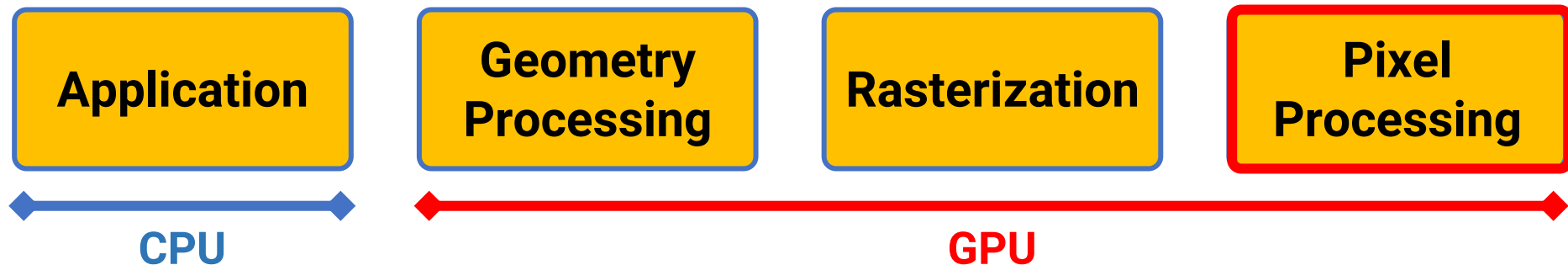
- Fragments (pixels) generation
  - Attribute interpolation



**from continuous  
to discrete**

# GPU Graphics Pipeline Overview (cont.)

- Responsible for the fixed routines of bringing triangles to pixels
- Can be roughly categorized into 3 stages



- Pixel shading / Texturing
- Depth testing
- Alpha blending

# GPU Graphics Pipeline Overview (cont.)

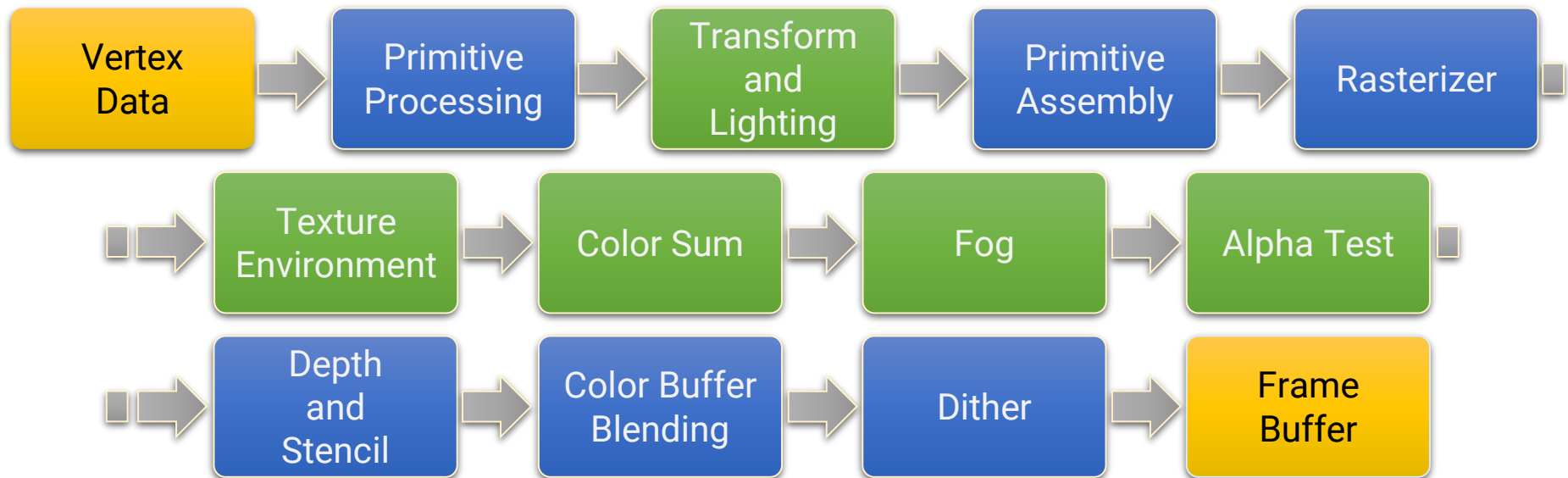
- In this topic, we will first introduce the GPU rendering pipeline revealed in **OpenGL 1.x**
- After that, we will show why (and how) some stages become **programmable** in **OpenGL 2.0**

# Outline

- GPU graphics pipeline
- **OpenGL graphics pipeline 1.x**
- OpenGL graphics pipeline 2.0
- OpenGL and shader implementation

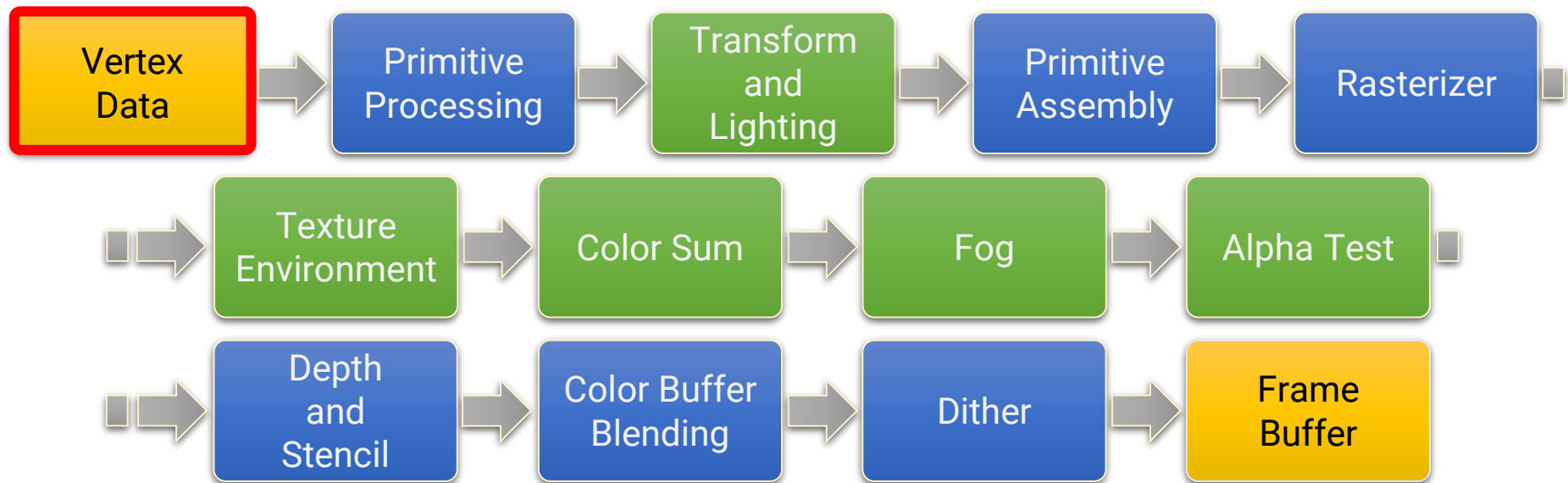
# OpenGL (1.x) Fixed Function Pipeline

- Used when OpenGL was first introduced
- All the functions performed by OpenGL are **fixed** and **could not** be modified except through the manipulation of the **rendering states**



- The stages shown in **green** have been replaced by **shaders**

# OpenGL (1.x) Fixed Function Pipeline

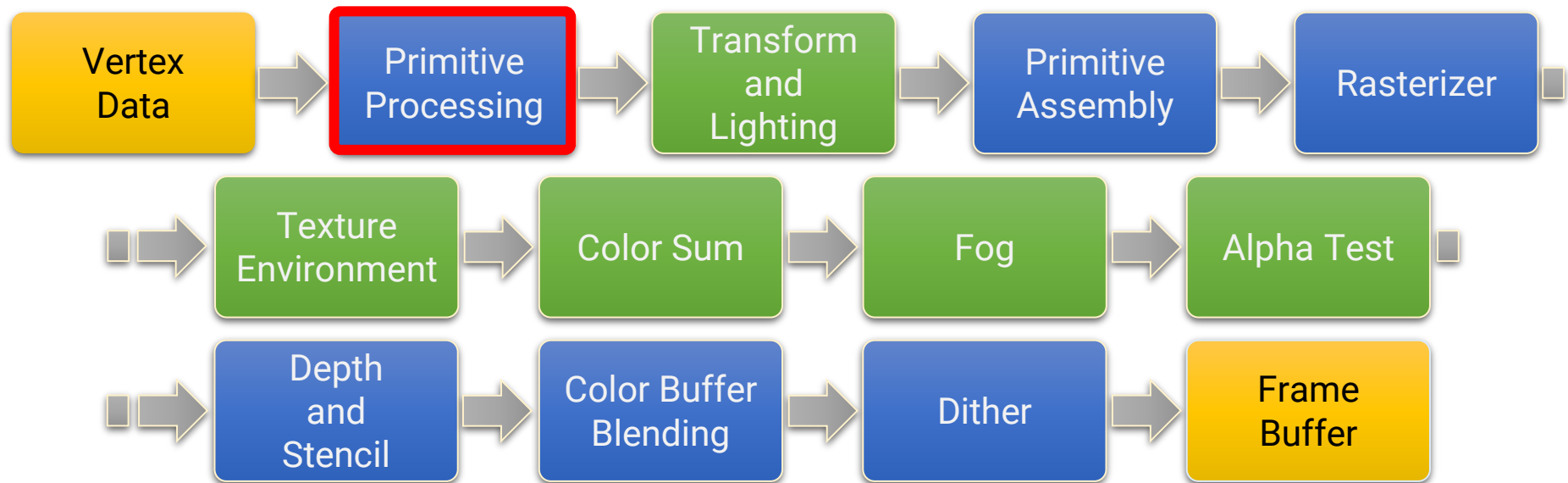




# Vertex Data

- Send the vertex data to the GPU
- **Vertex attributes** include vertex position, vertex normal, texture coordinate, vertex color, fog coordinate, etc.
- The vertex data processed by the GPU is referred to as the **vertex stream**

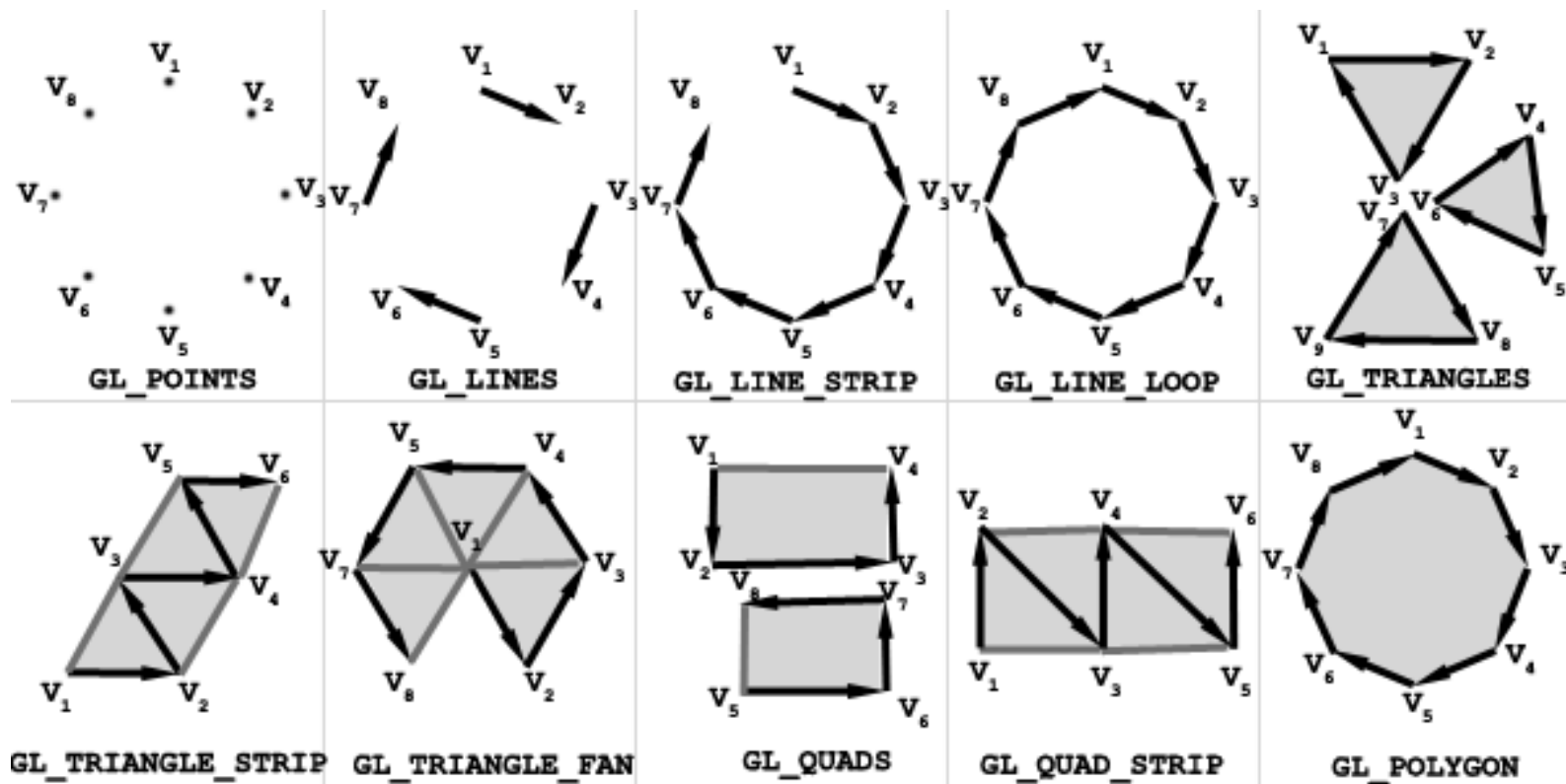
# OpenGL (1.x) Fixed Function Pipeline



# Primitive Processing

- Vertex stream is processed **per primitive**
- OpenGL supports several types of primitives, including points, lines, triangles, ~~quads~~, and ~~polygons~~ (**deprecated** after OpenGL 3.1)

# Primitive Processing (cont.)



primitive types in OpenGL 1.1

# Primitive Processing (cont.)

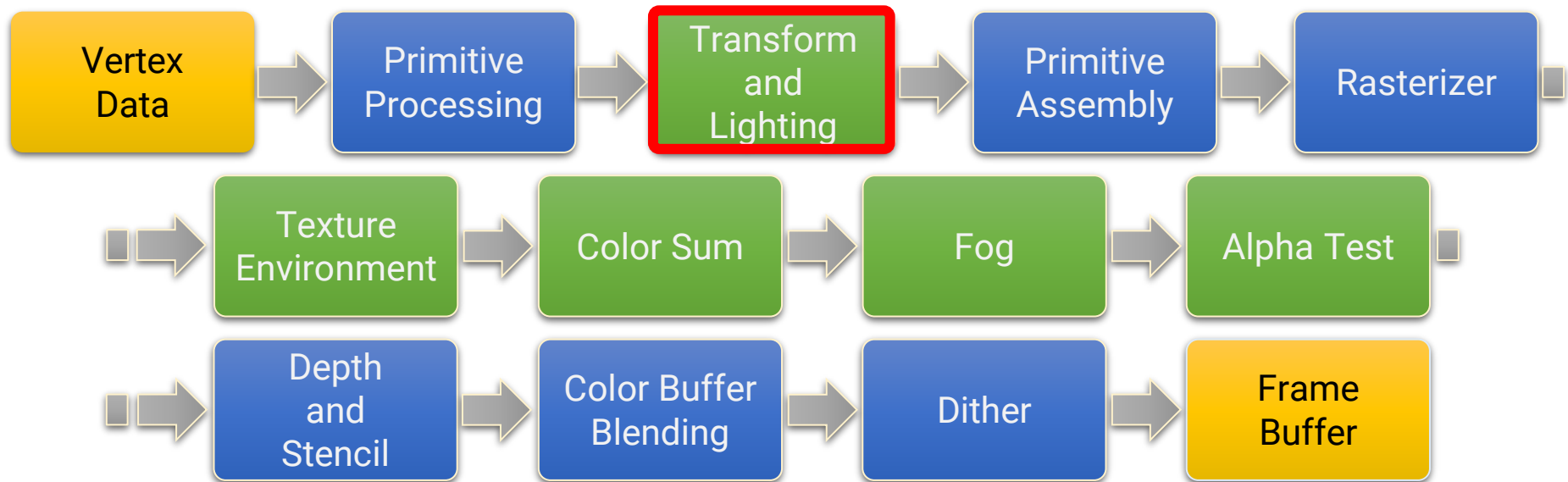
```
glBegin(GL_POINTS); //starts drawing of points
    glVertex3f(1.0f,1.0f,0.0f); //upper-right corner
    glVertex3f(-1.0f,-1.0f,0.0f); //lower-left corner
glEnd(); //end drawing of points
```

```
glBegin(GL_TRIANGLES); //start drawing triangles
    glVertex3f(-1.0f,-0.25f,0.0f); //triangle one first vertex
    glVertex3f(-0.5f,-0.25f,0.0f); //triangle one second vertex
    glVertex3f(-0.75f,0.25f,0.0f); //triangle one third vertex
    //drawing a new triangle
    glVertex3f(0.5f,-0.25f,0.0f); //triangle two first vertex
    glVertex3f(1.0f,-0.25f,0.0f); //triangle two second vertex
    glVertex3f(0.75f,0.25f,0.0f); //triangle two third vertex
glEnd(); //end drawing of triangles
```

```
glBegin(GL_POLYGON); //begin drawing of polygon
    glVertex3f(-0.5f,0.5f,0.0f); //first vertex
    glVertex3f(0.5f,0.5f,0.0f); //second vertex
    glVertex3f(1.0f,0.0f,0.0f); //third vertex
    glVertex3f(0.5f,-0.5f,0.0f); //fourth vertex
    glVertex3f(-0.5f,-0.5f,0.0f); //fifth vertex
    glVertex3f(-1.0f,0.0f,0.0f); //sixth vertex
glEnd(); //end drawing of polygon
```

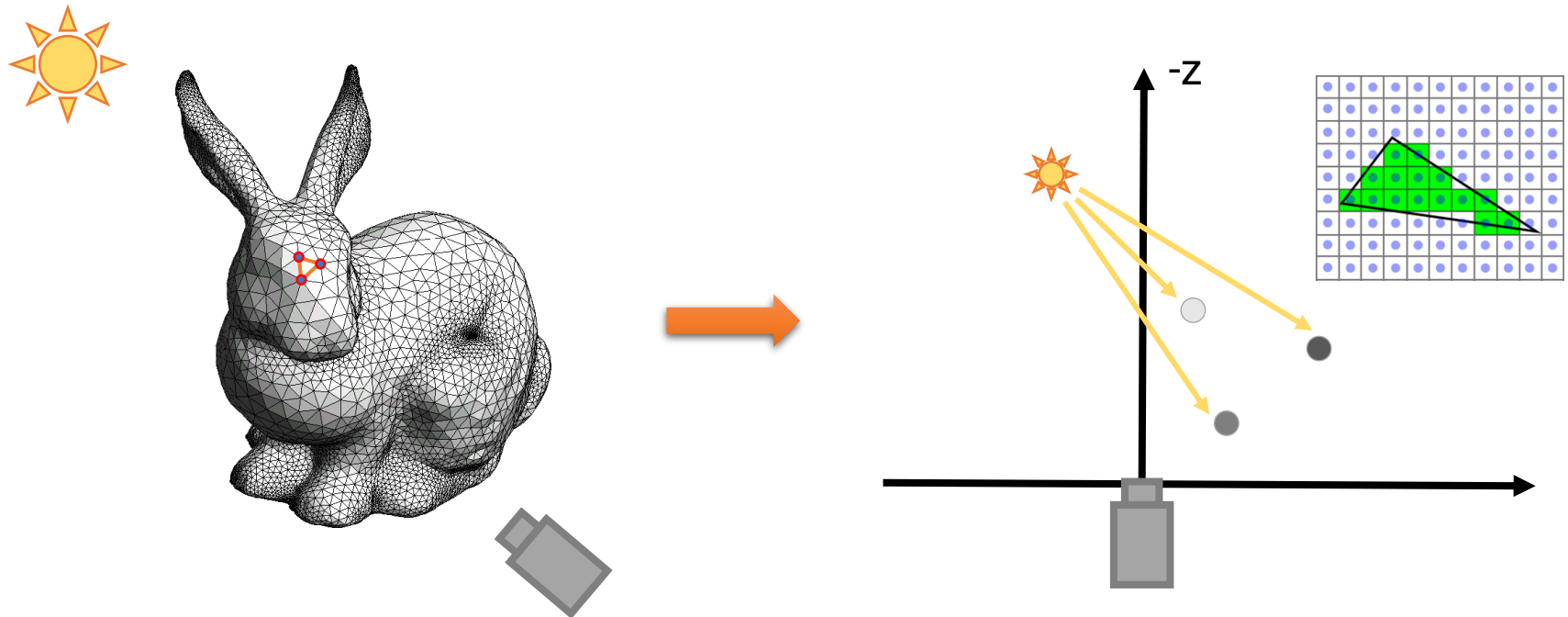
primitive drawing in  
OpenGL 1.1  
**(deprecated, DO NOT USE!)**

# OpenGL (1.x) Fixed Function Pipeline



# Transform and Lighting

- Vertex is transformed to **camera space** by the current **ModelView** matrix
- Lighting is computed at each vertex (Gouraud shading)



# Transform and Lighting (cont.)

- **Transform in OpenGL 1.x (deprecated, DO NOT USE!)**

```

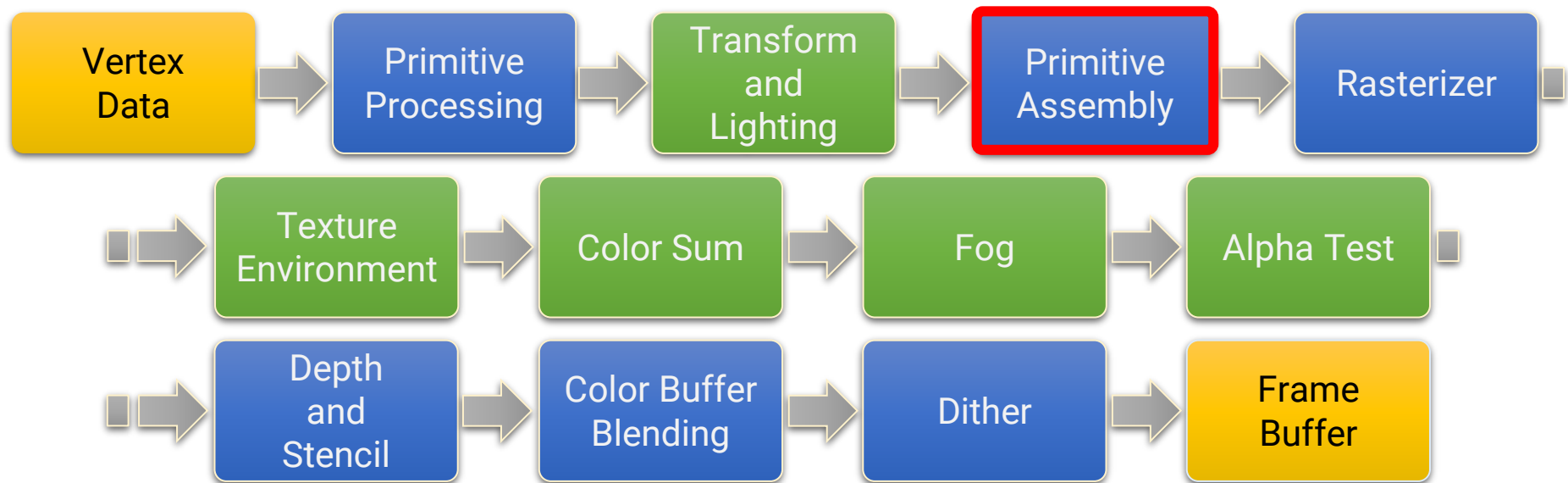
void display(void)
{
    glClear (GL_COLOR_BUFFER_BIT);
    glColor3f (1.0, 1.0, 1.0);
    glLoadIdentity ();          /* clear the matrix */
    /* viewing transformation */
    V gluLookAt (0.0, 0.0, 5.0, 0.0, 0.0, 0.0, 1.0, 0.0);
    M glScalef (1.0, 2.0, 1.0);      /* modeling transformation */
    glutWireCube (1.0);
    glFlush ();
}

void reshape (int w, int h)
{
    glViewport (0, 0, (GLsizei) w, (GLsizei) h);
    glMatrixMode (GL_PROJECTION);
    glLoadIdentity ();
    P glFrustum (-1.0, 1.0, -1.0, 1.0, 1.5, 20.0);
    glMatrixMode (GL_MODELVIEW);
}

```

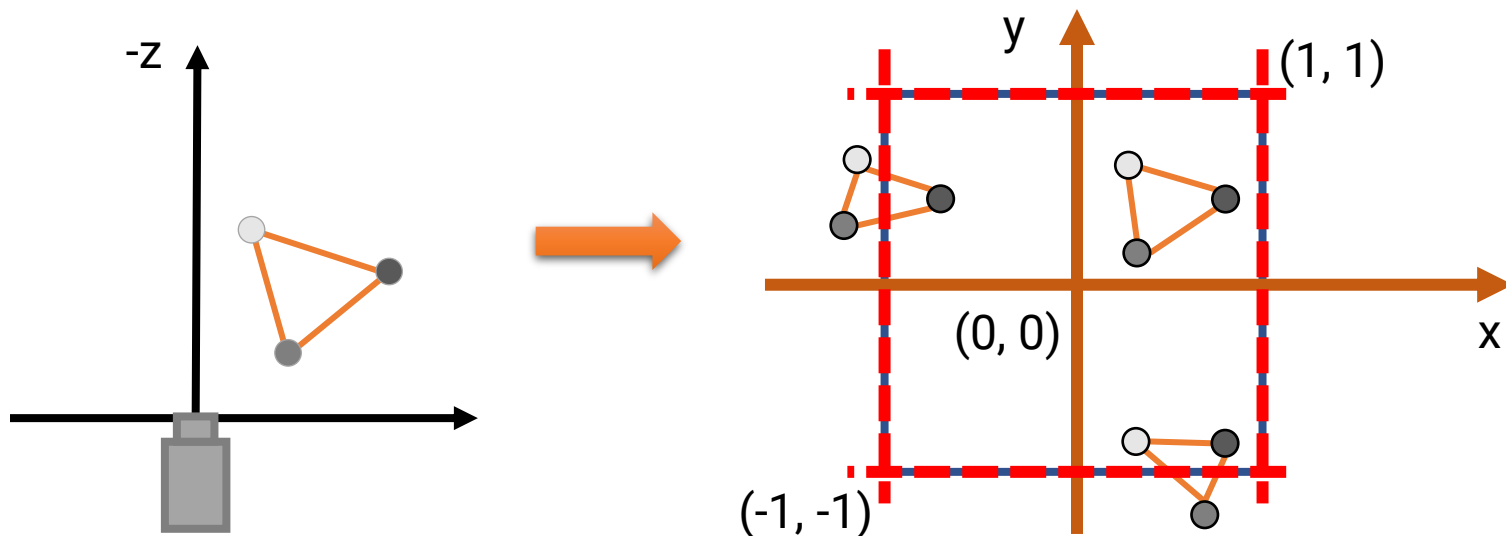


# OpenGL (1.x) Fixed Function Pipeline



# Primitive Assembly

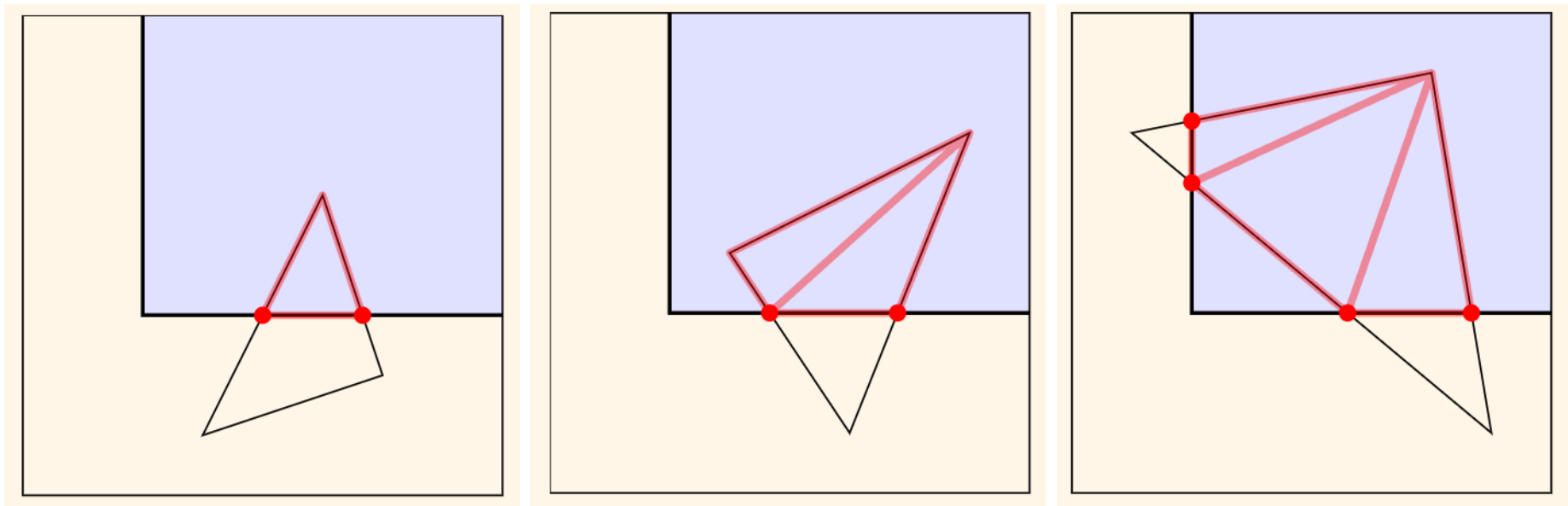
- Convert primitives from the basic primitive types (e.g., triangle strip) into triangles
- Triangles are transformed to NDC and got **clipped** to fit within the viewport boundaries



# Primitive Assembly (cont.)

- **Clipping**

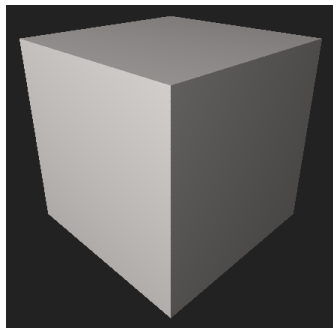
- In OpenGL, clipping is performed by adding new vertices and triangulation



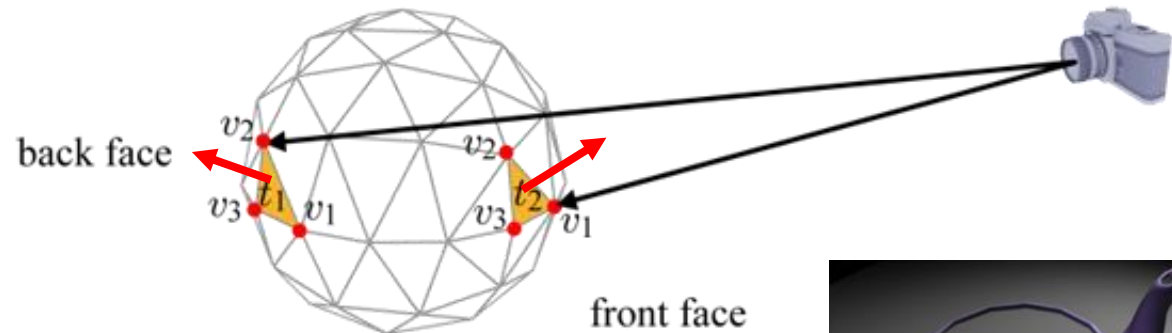
# Primitive Assembly (cont.)

- **Back-face culling**

- If a triangle is facing away from the camera, it will never be seen
- We can cull these back-facing triangles for saving unnecessary computation



we can only see three faces from six!

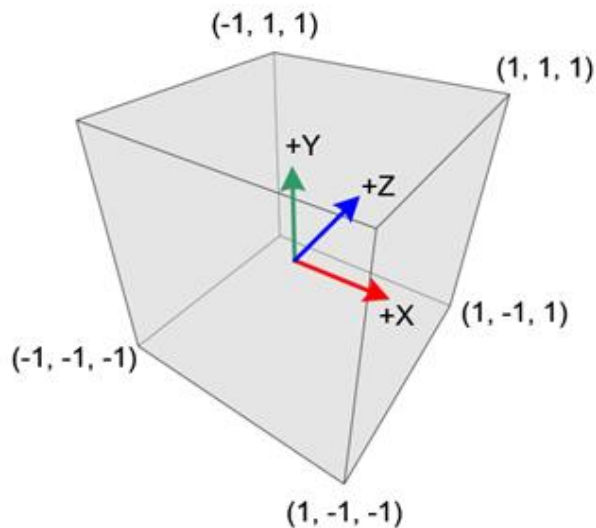


How about this case?

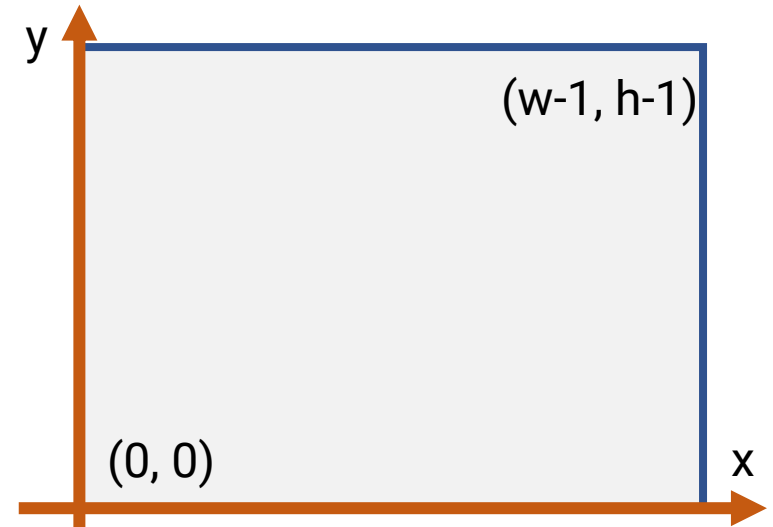


# Primitive Assembly (cont.)

- Screen mapping (OpenGL will handle this!)



OpenGL NDC

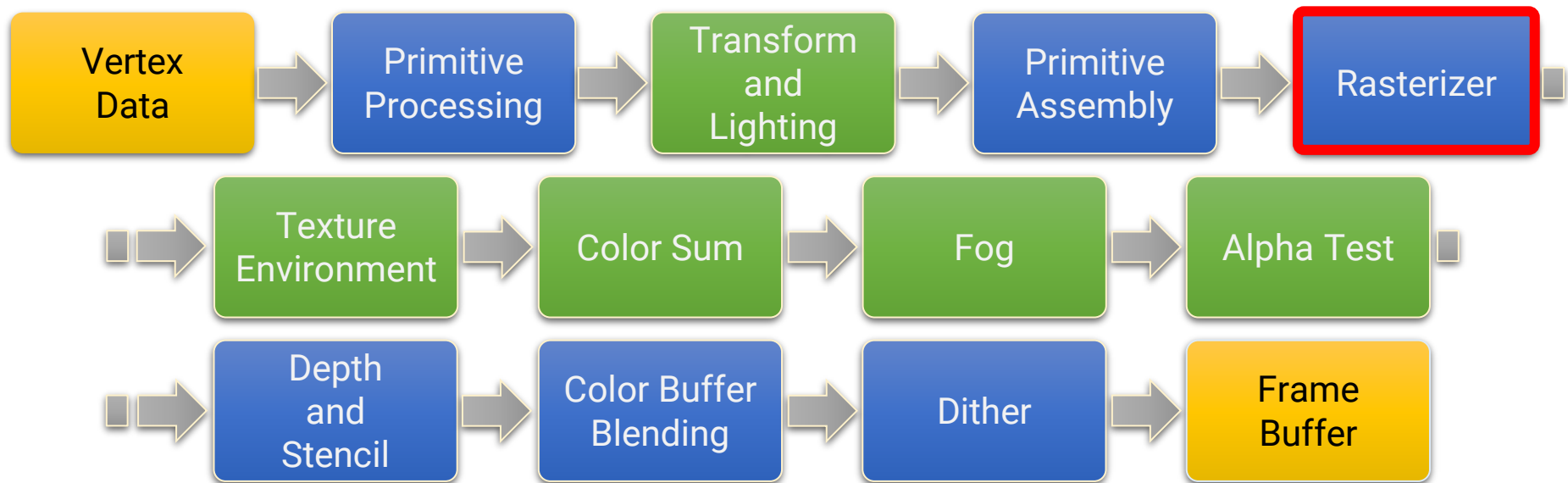


OpenGL Screen Space

$$\begin{aligned}
 x_s &= w(x_{ndc} + 1)/2 \\
 y_s &= h(y_{ndc} + 1)/2 \\
 z_s &= (z_{ndc} + 1)/2 \\
 w_s &= w_{ndc}
 \end{aligned}$$

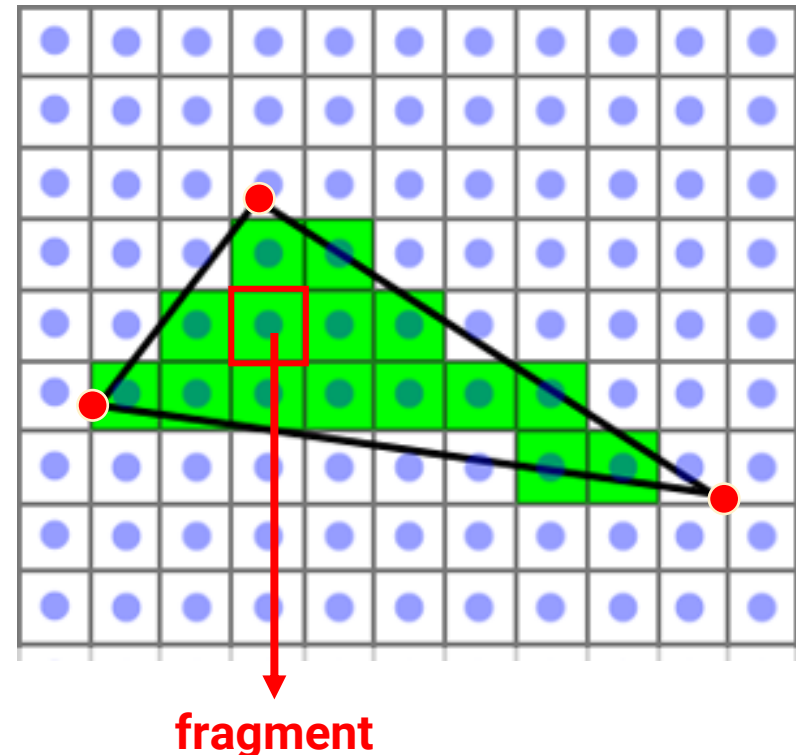
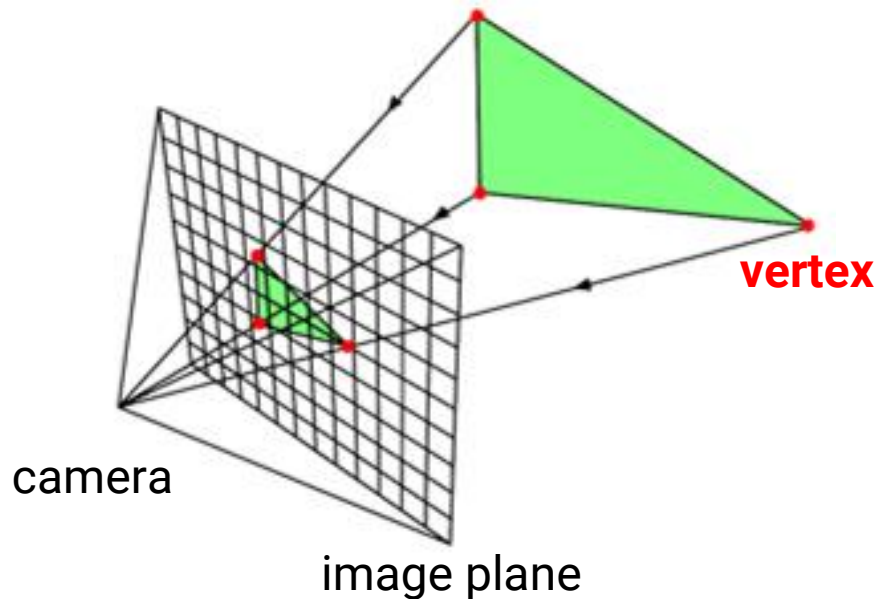
+ screen location

# OpenGL (1.x) Fixed Function Pipeline



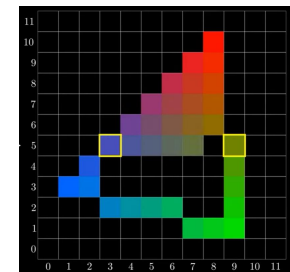
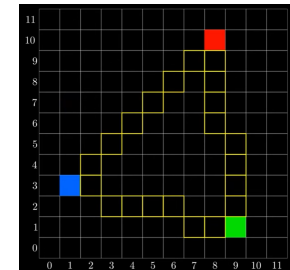
# Rasterization

- Convert **triangles** (**continuous**) into **fragments** (**discrete**)
  - For each pixel that is inside the triangle in the screen space, generate a **fragment**



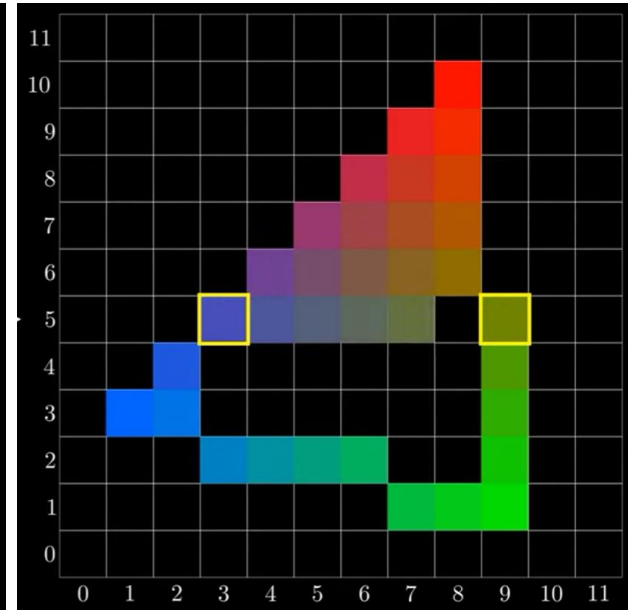
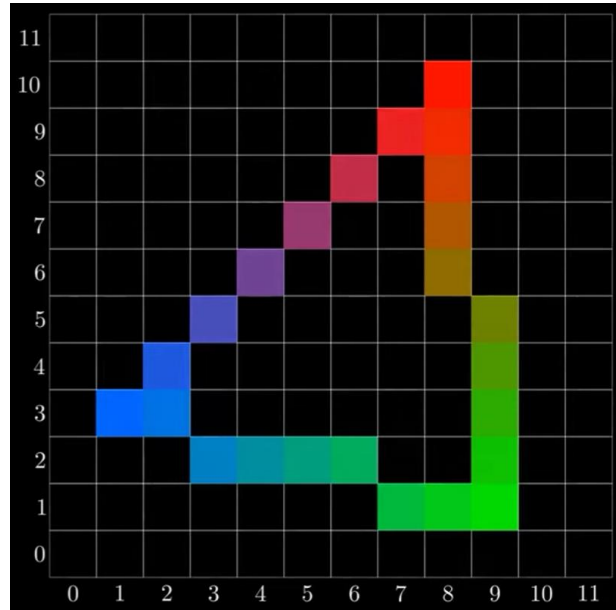
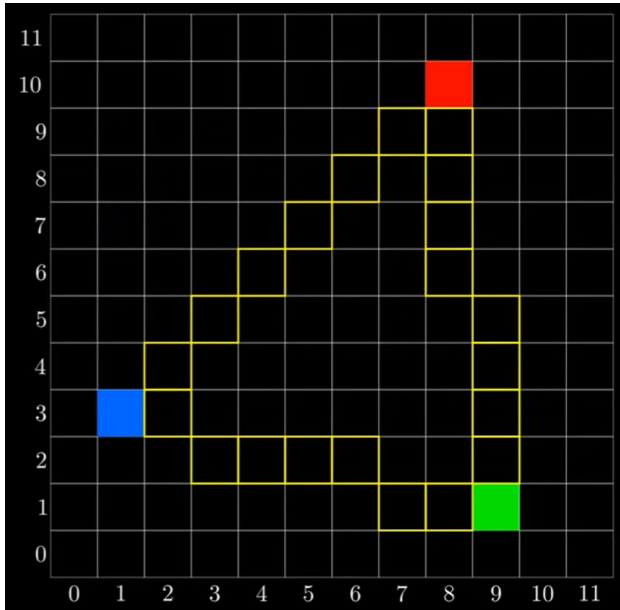
# Rasterization (cont.)

- Convert **triangles (continuous)** into **fragments (discrete)**
  - For each pixel that is inside the triangle in the screen space, generate a **fragment**
- Obtain **per-fragment data** using **interpolation**: vertex attributes are **interpolated** across the face, such as
  - (Lighting) color      **used for per-vertex lighting**
  - Texture coordinate
  - Position      **used for per-fragment lighting**
  - Normal      **(after OpenGL 2.0)**
  - Anything you want to interpolate





# Scanline Rasterization



Find edge pixels

- DDA [\[link\]](#)
- Bresenham [\[link\]](#)

Attributes interpolation  
of edge pixels using  
vertices

Attributes interpolation  
of inner pixels using  
edge points

# Digital Differential Analyzer (DDA)

- Draw a line segment passing through  $(x_1, y_1) = (1, 1)$  and  $(x_2, y_2) = (7, 5)$

$$y = mx + b$$

$$\text{slope } m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{\Delta y}{\Delta x}$$

$$\Delta y = m \Delta x = m \quad (\text{if } \Delta x = 1)$$

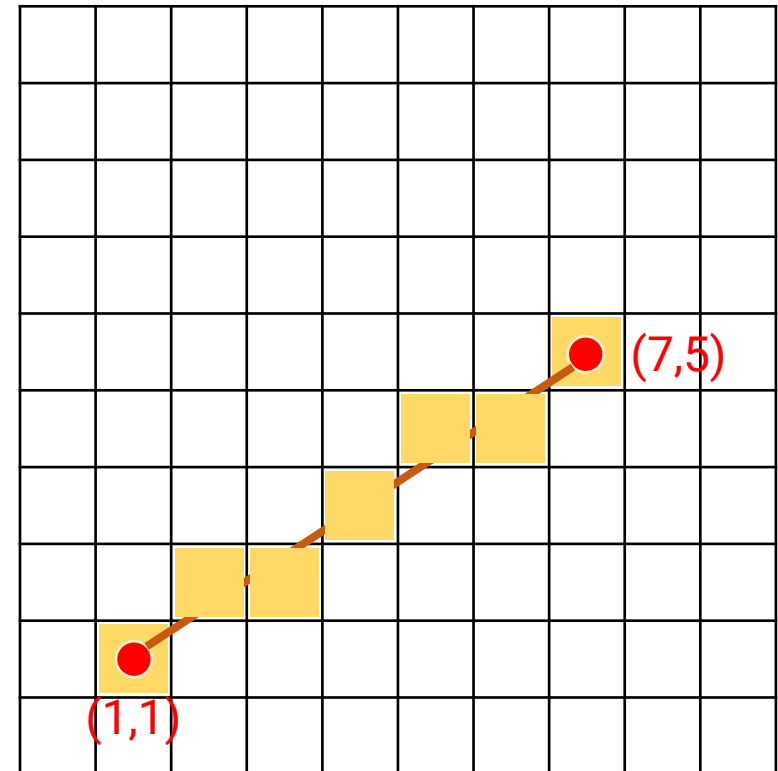
$$x_a = 2 \rightarrow y_a = y_1 + m = 1.667 \rightarrow (2, 1.667) \quad (2, 2)$$

$$x_b = 3 \rightarrow y_b = y_a + m = 2.333 \rightarrow (3, 2.333) \quad (3, 2)$$

$$x_c = 4 \rightarrow y_c = y_b + m = 3.000 \rightarrow (4, 3.000) \quad (4, 3)$$

$$x_d = 5 \rightarrow y_d = y_c + m = 3.667 \rightarrow (5, 3.667) \quad (5, 4)$$

$$x_e = 6 \rightarrow y_e = y_d + m = 4.333 \rightarrow (6, 4.333) \quad (6, 4)$$



floating-point addition / comparison

# Bresenham Algorithm

- Draw a line segment passing through  $(x_1, y_1) = (1, 1)$  and  $(x_2, y_2) = (7, 5)$

$$y = mx + b$$

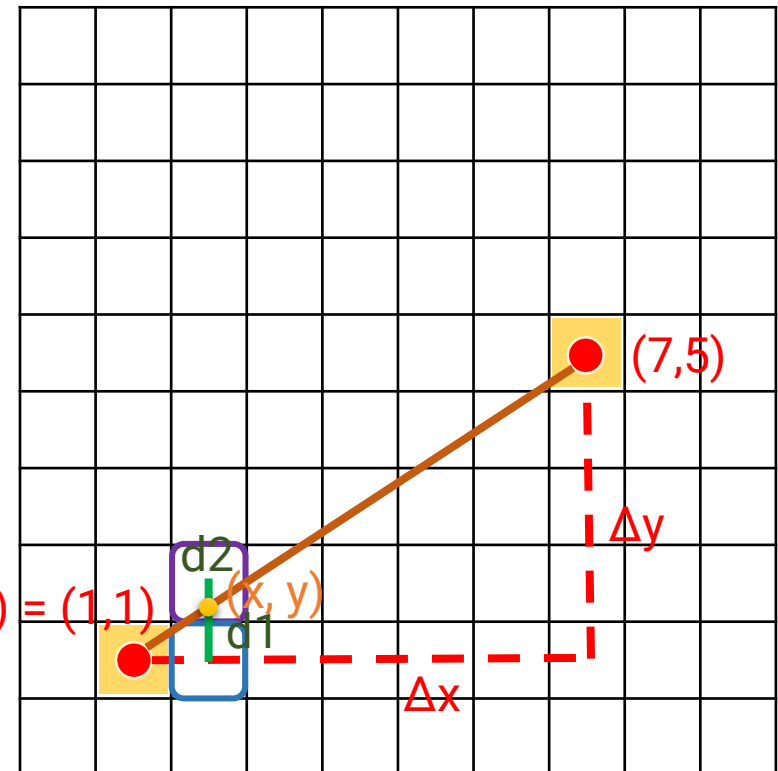
$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{\Delta y}{\Delta x}$$

$$d1 = y - y_i = (m(x_i + 1) + b) - y_i$$

$$d2 = (y_i + 1) - y = y_i + 1 - (m(x_i + 1) + b)$$

$$d1 - d2 = 2m(x_i + 1) - 2y_i + 2b - 1$$

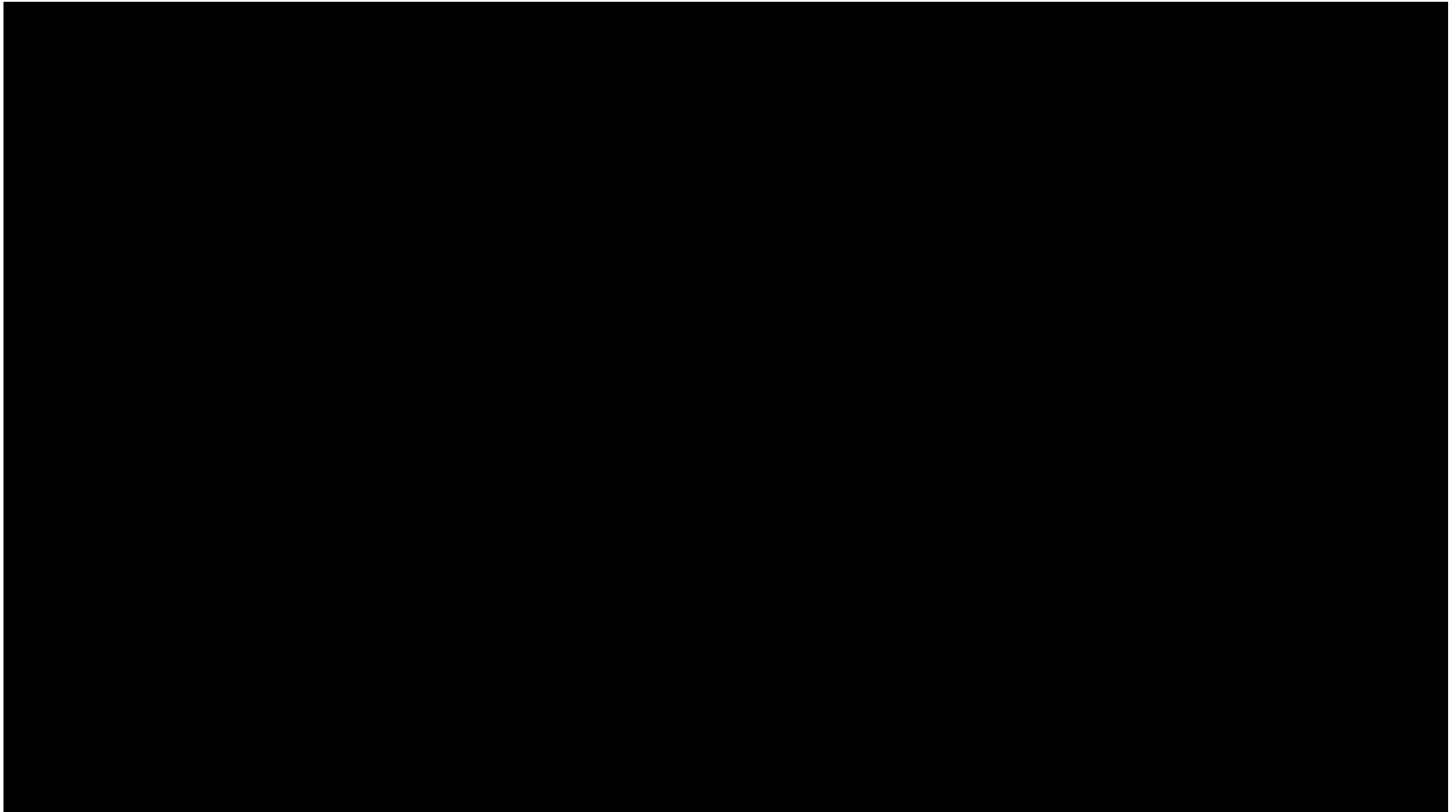
$$\Delta x(d1 - d2) = 2\Delta yx_i - 2\Delta xy_i + c$$



integer multiplication / comparison

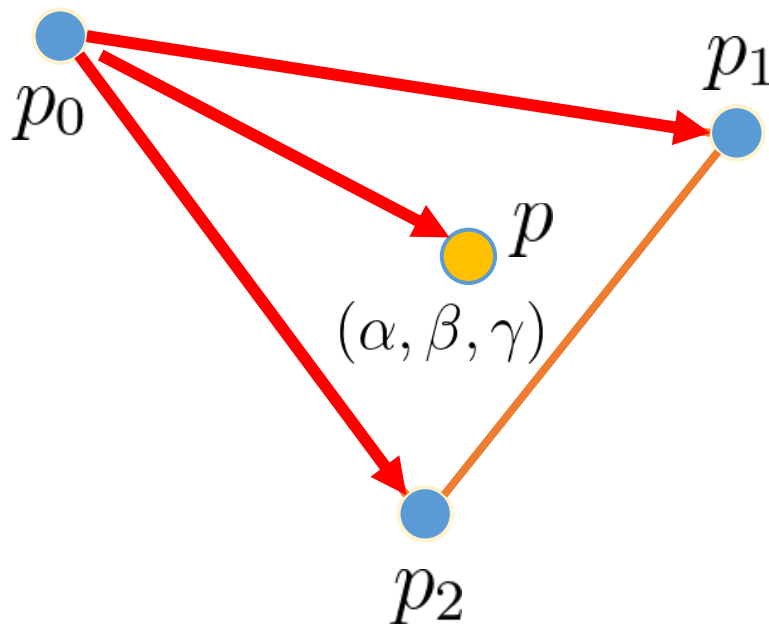
# Scanline Rasterization (cont.)

- <https://www.youtube.com/watch?v=t7Ztio8cwqM>



# Barycentric Coordinates

- Barycentric coordinates inside a triangle



$$\begin{aligned} p &= p_0 + \beta(p_1 - p_0) + \gamma(p_2 - p_0) \\ &= (1 - \beta - \gamma)p_0 + \beta p_1 + \gamma p_2 \\ &= \alpha p_0 + \beta p_1 + \gamma p_2 \\ \alpha + \beta + \gamma &= 1 \end{aligned}$$

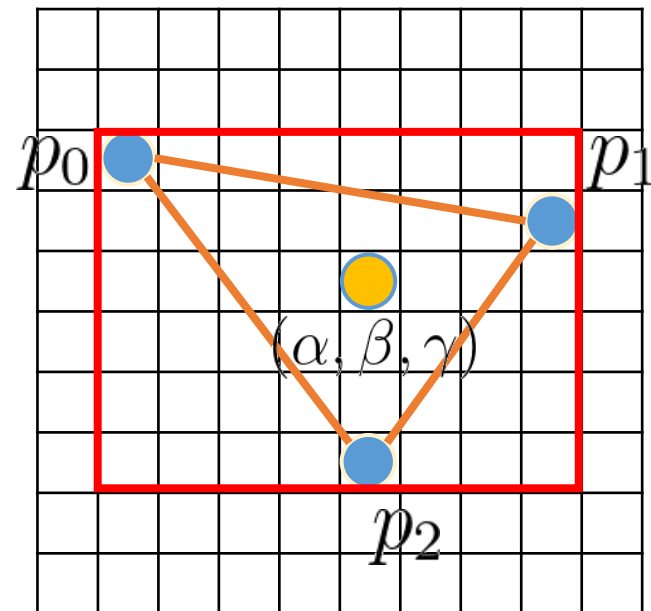
The values  $\alpha, \beta, \gamma \in [0, 1]$  **if and only if**  
 **$p$  is inside the triangle**

# Barycentric Coordinates (cont.)

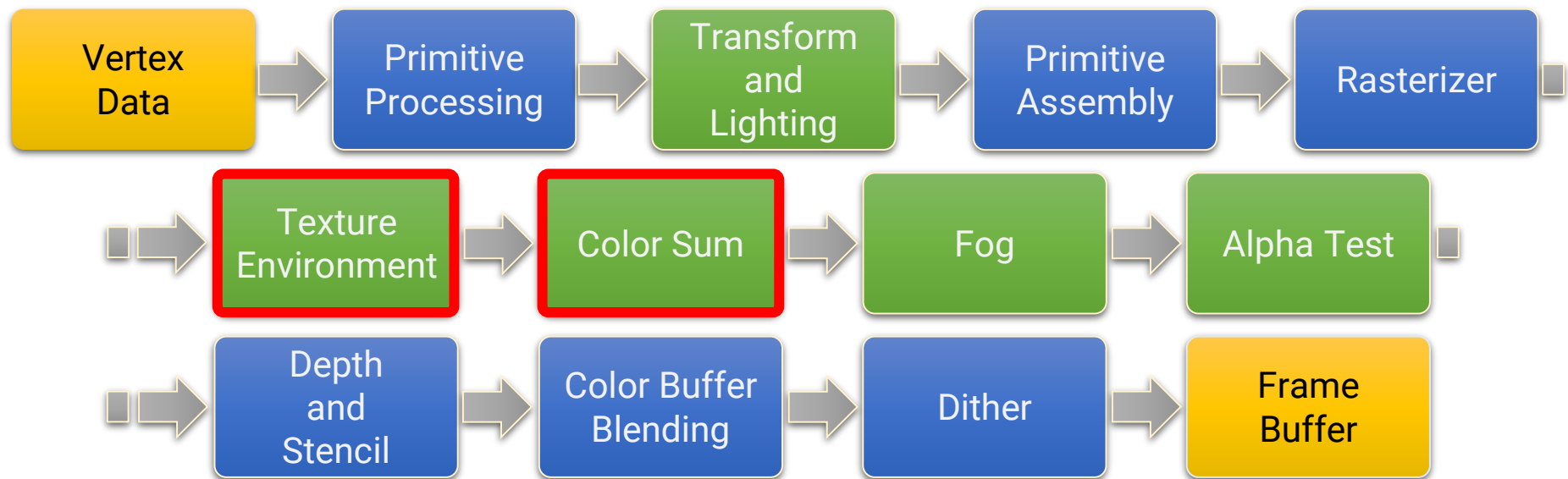
- Compute the 2D bounding box of the 2D triangle
- For each pixel inside the bounding box, compute its barycentric coordinates [\[link\]](#)
- If the coordinates are all  $\geq 0$  and  $\leq 1$ , the pixel is covered by the triangle

The barycentric coordinates  $\alpha, \beta, \gamma$  can be used to interpolate vertex attributes directly

$$\begin{aligned} p &= p_0 + \beta(p_1 - p_0) + \gamma(p_2 - p_0) \\ &= \alpha p_0 + \beta p_1 + \gamma p_2 \end{aligned}$$

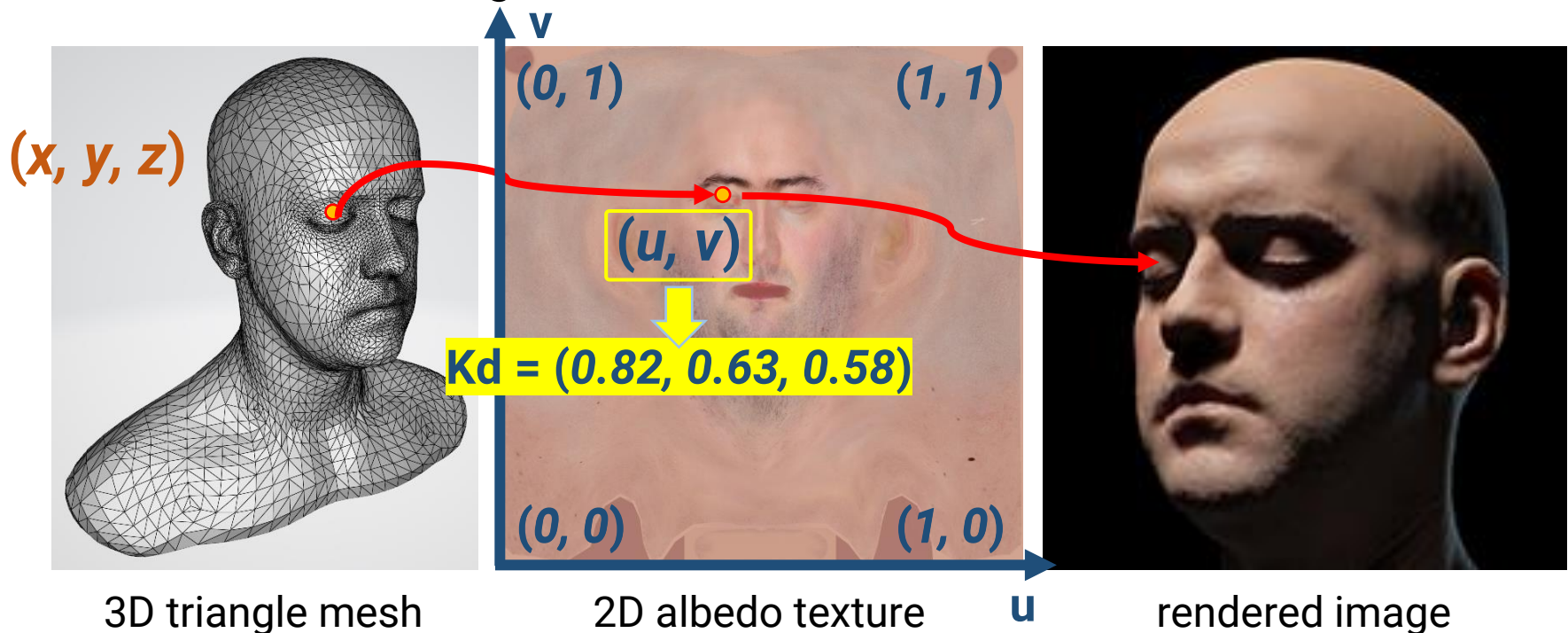


# OpenGL (1.x) Fixed Function Pipeline



# Recap: Texturing

- Textures are used to describe complex materials
- A (vertex) texture coordinate is used to look up the texture
  - The way to map a point on the 3D surface to a pixel (texel) on a 2D image texture





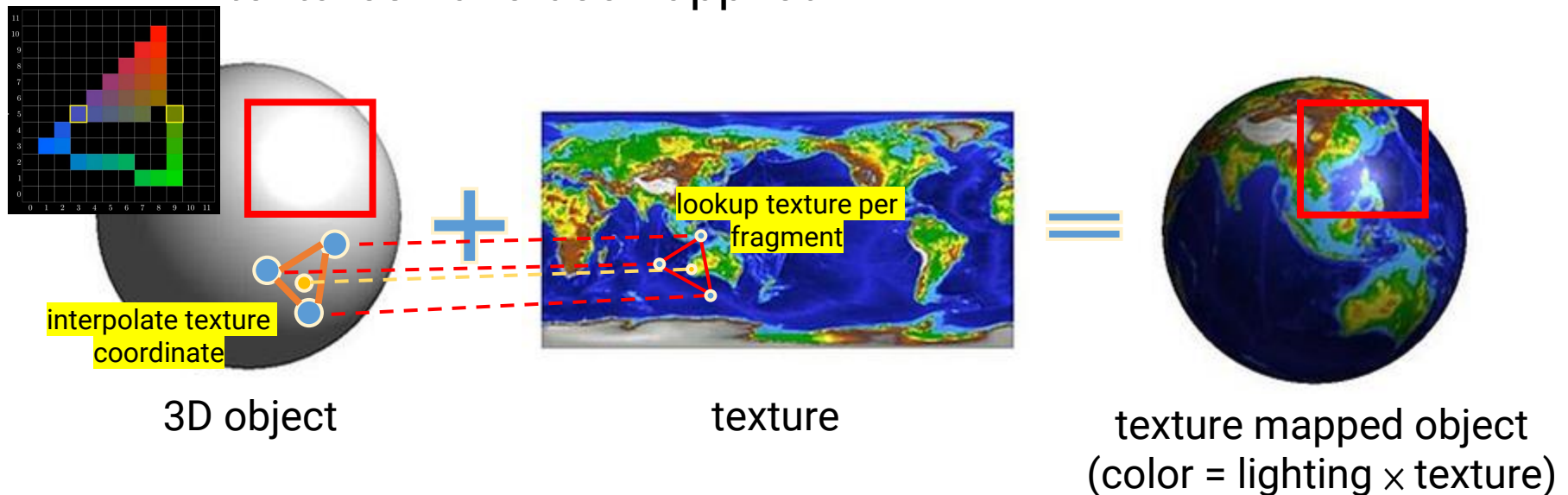
# Texture Environment and Color Sum

- **Texture Environment**

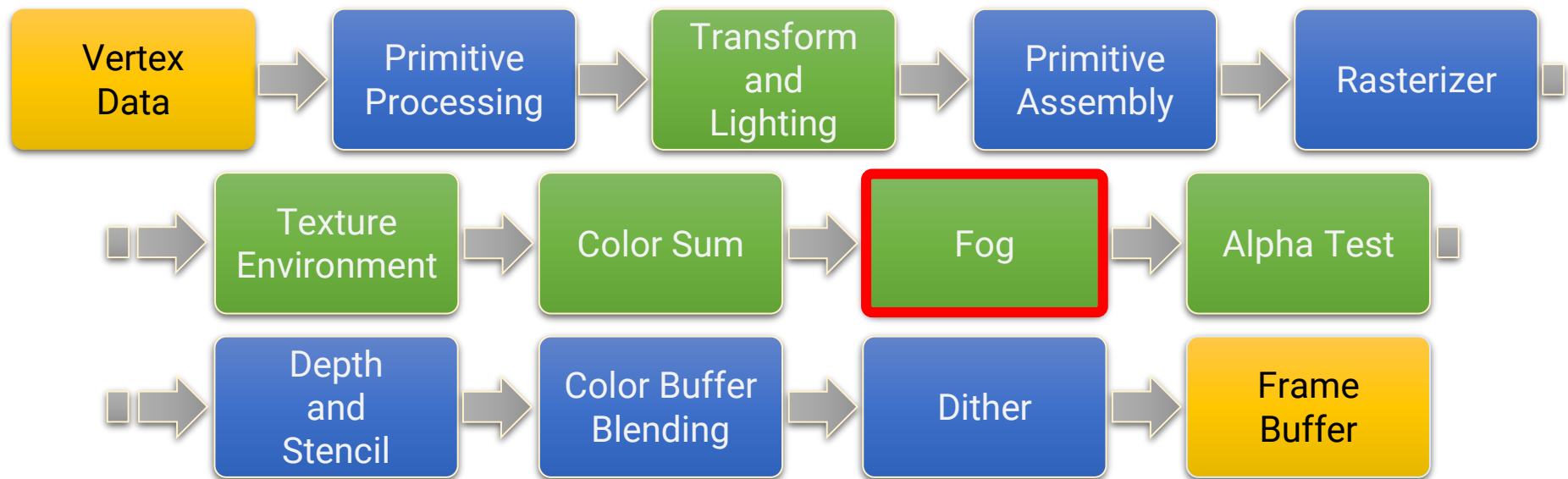
- Apply the textures to the fragments

- **Color Sum**

- Used to add-in a secondary color to the geometry after the textures have been applied



# OpenGL (1.x) Fixed Function Pipeline



# Fog

- Simulate the effect of geometry fadeout as dimmed by fog
- Blend the **fragment color** with the **fog color** according to **object distance**



# Fog in Games

Copyright © Silent Hill 2, 2001, Konami Inc.

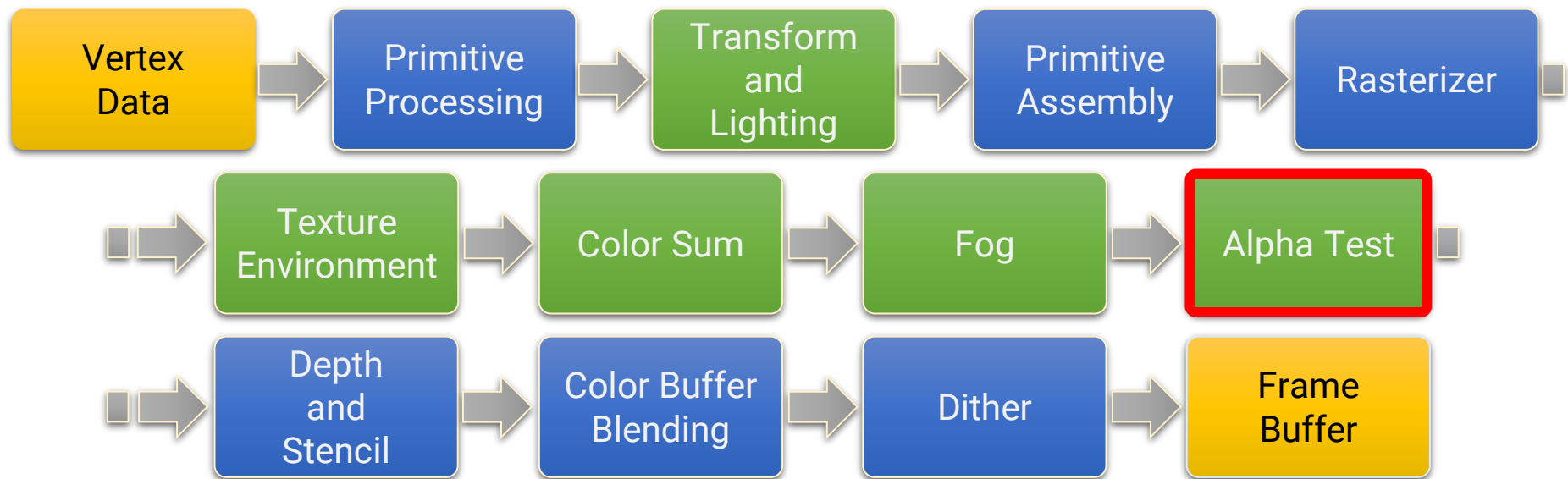




# Fog in Games (cont.)

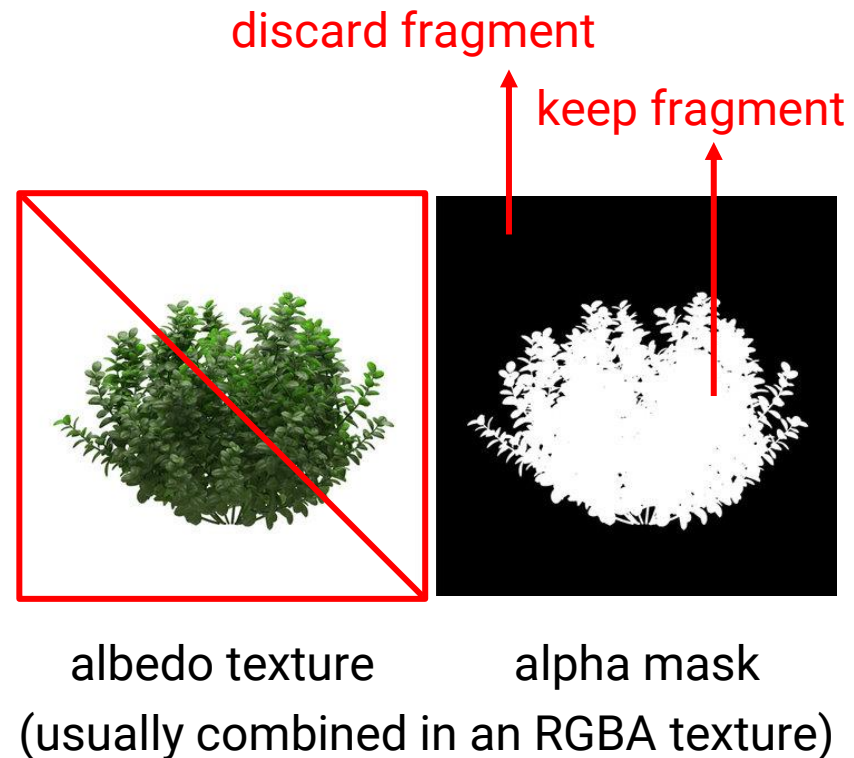
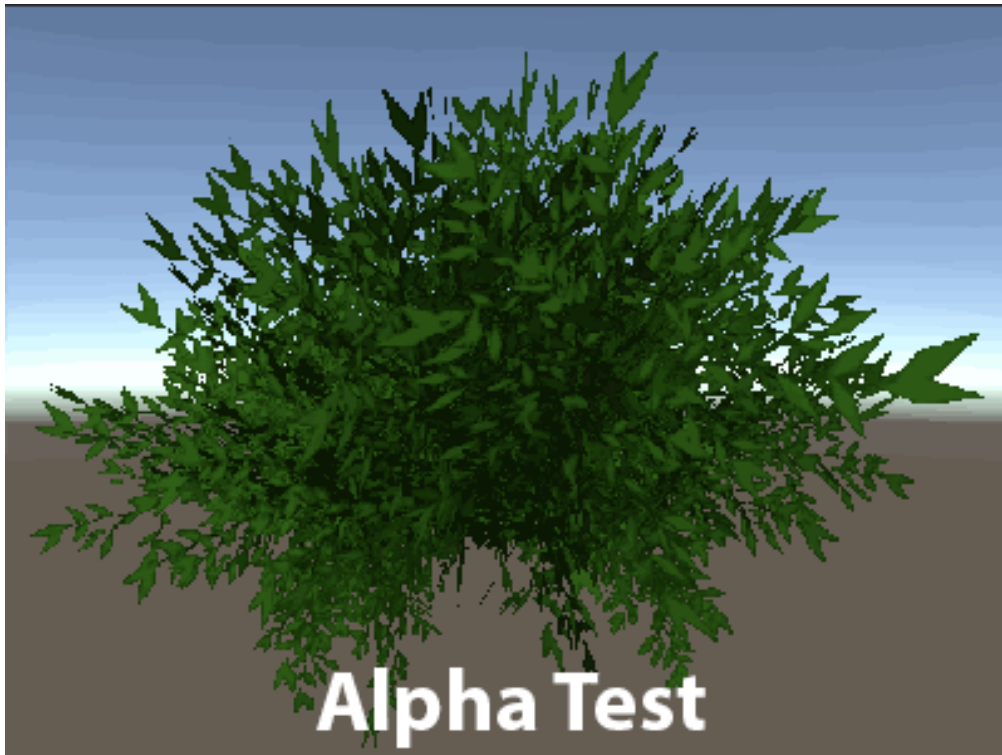


# OpenGL (1.x) Fixed Function Pipeline



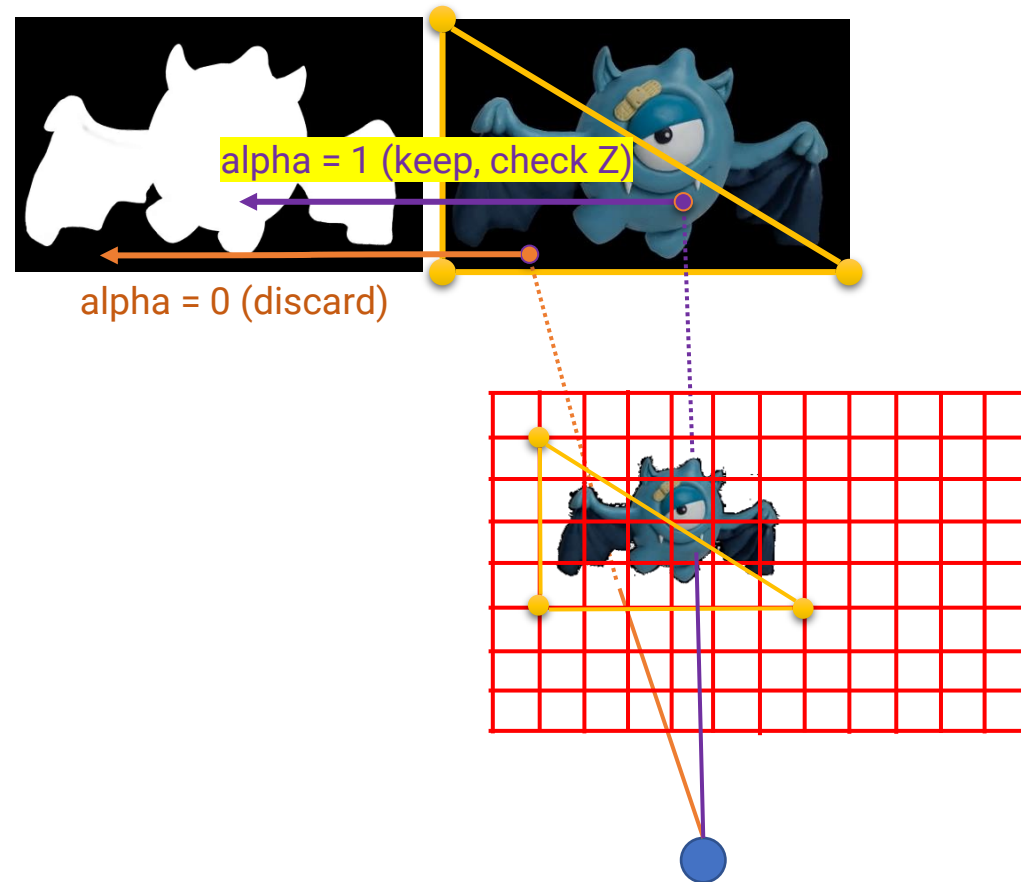
# Alpha Test

- Discard fragments if their alpha values are below a certain threshold



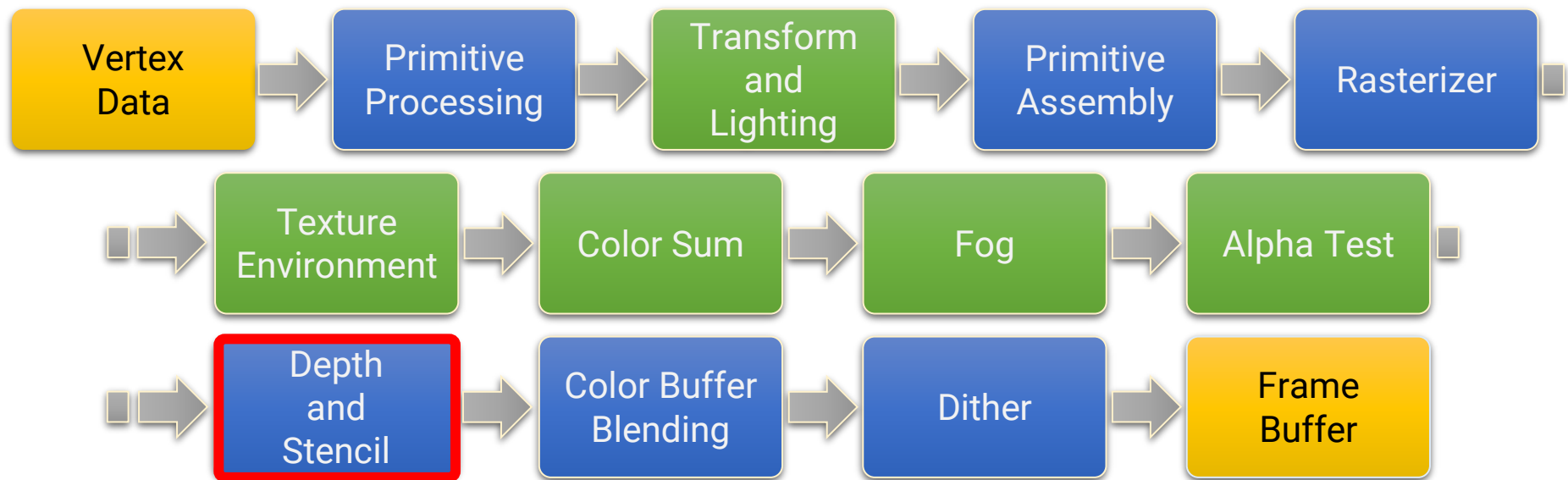
# Alpha Test (cont.)

- Discard fragments if their alpha values are below a certain threshold



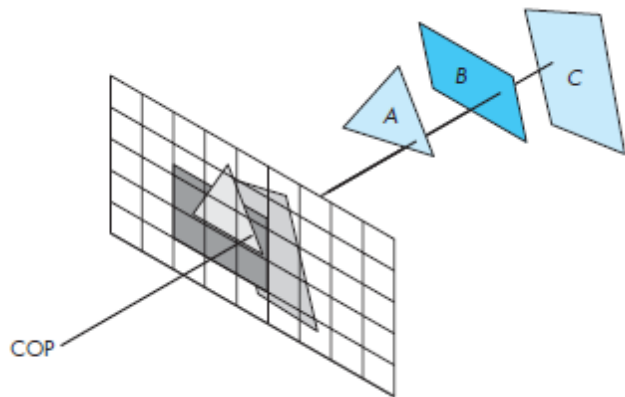


# OpenGL (1.x) Fixed Function Pipeline



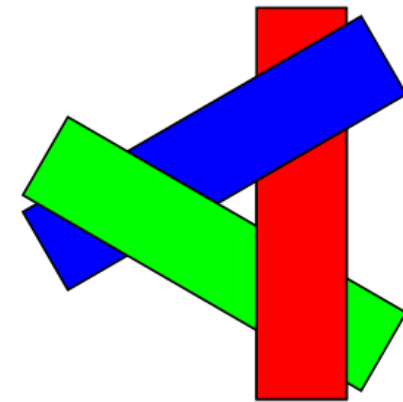
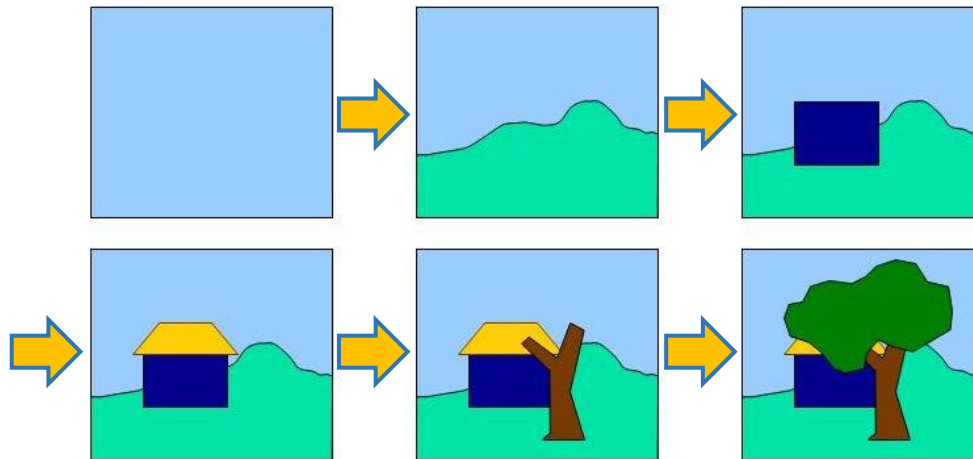
# Depth Test

- Used for **hidden surface removal**
  - Only show the **closest** surfaces to the camera at each pixel



# Depth Test (cont.)

- Used for **hidden surface removal**
  - Only show the **closest** surfaces to the camera at each pixel
- Earlier approach: painter's algorithm

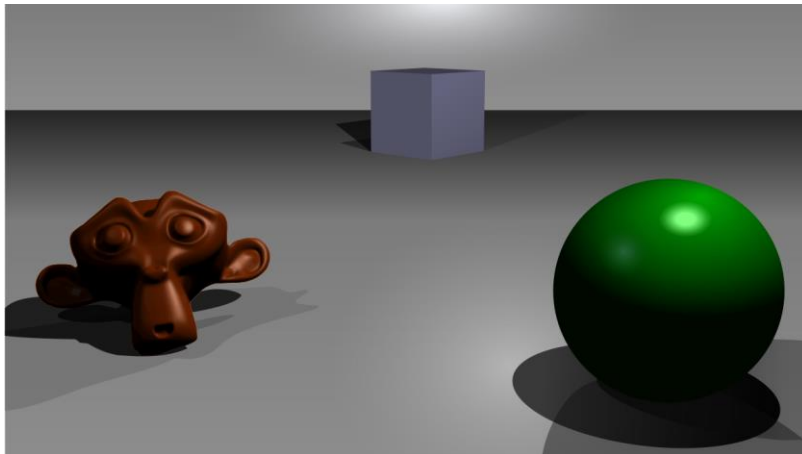


How about this?  
(cyclical overlapping)

# Depth Test (cont.)

- **Z-buffer**

- An additional buffer used to maintain the z value of the closest surface to a pixel
- Discard fragments if they have larger depth values than the ones stored in their corresponding positions in the Z buffer



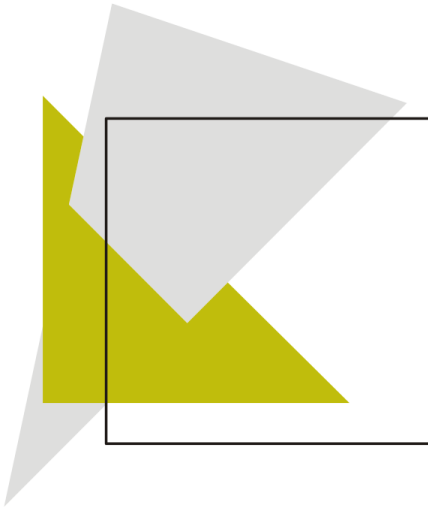
color frame buffer



Z (depth) buffer

# Z-Buffer

- Z-buffer update



∞	∞	∞	∞	∞	∞	∞	∞
∞	∞	∞	∞	∞	∞	∞	∞
∞	∞	∞	∞	∞	∞	∞	∞
∞	∞	∞	∞	∞	∞	∞	∞
∞	∞	∞	∞	∞	∞	∞	∞
∞	∞	∞	∞	∞	∞	∞	∞
∞	∞	∞	∞	∞	∞	∞	∞
∞	∞	∞	∞	∞	∞	∞	∞

+

5	5	5	5	5	5	5
5	5	5	5	5	5	
5	5	5	5	5		
5	5	5	5			
5	5	5				
5	5					
5						

=

5	5	5	5	5	5	5	∞
5	5	5	5	5	5	∞	∞
5	5	5	5	5	∞	∞	∞
5	5	5	5	∞	∞	∞	∞
5	5	5	∞	∞	∞	∞	∞
5	5	∞	∞	∞	∞	∞	∞
5	∞	∞	∞	∞	∞	∞	∞
∞	∞	∞	∞	∞	∞	∞	∞

5	5	5	5	5	5	5	∞
5	5	5	5	5	5	∞	∞
5	5	5	5	5	∞	∞	∞
5	5	5	5	∞	∞	∞	∞
5	5	5	∞	∞	∞	∞	∞
5	5	∞	∞	∞	∞	∞	∞
5	∞	∞	∞	∞	∞	∞	∞
∞	∞	∞	∞	∞	∞	∞	∞

+

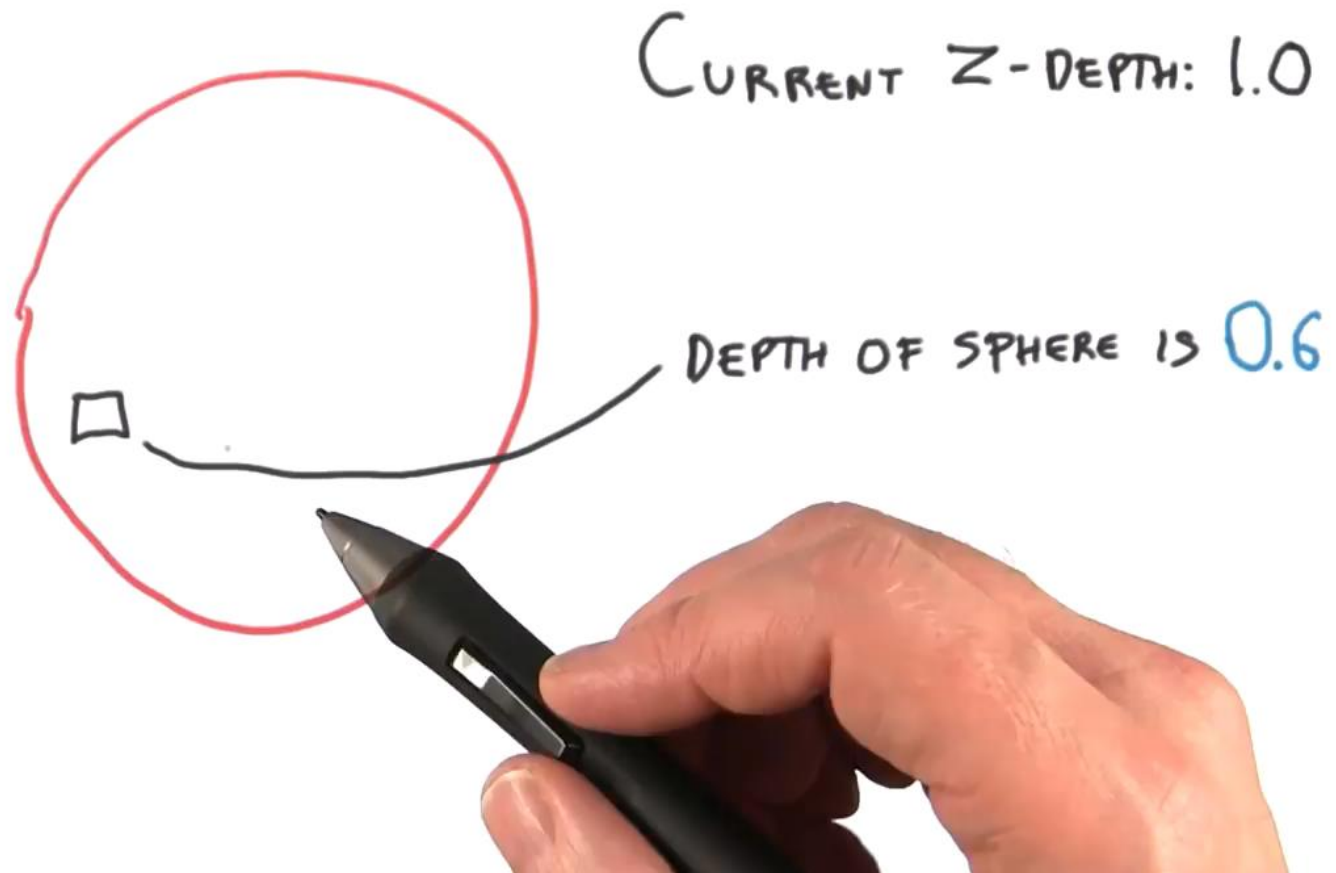
7						
6	7					
5	6	7				
4	5	6	7			
3	4	5	6	7		
2	3	4	5	6	7	

=

5	5	5	5	5	5	5	∞
5	5	5	5	5	5	∞	∞
5	5	5	5	5	∞	∞	∞
5	5	5	5	∞	∞	∞	∞
4	5	5	7	∞	∞	∞	∞
3	4	5	6	7	∞	∞	∞
2	3	4	5	6	7	∞	∞
∞	∞	∞	∞	∞	∞	∞	∞

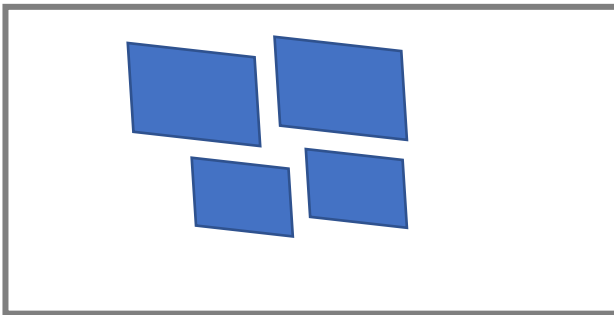
## Z-Buffer (cont.)

- [https://www.youtube.com/watch?v=yhwg\\_05HBwQ](https://www.youtube.com/watch?v=yhwg_05HBwQ)



# Stencil Test

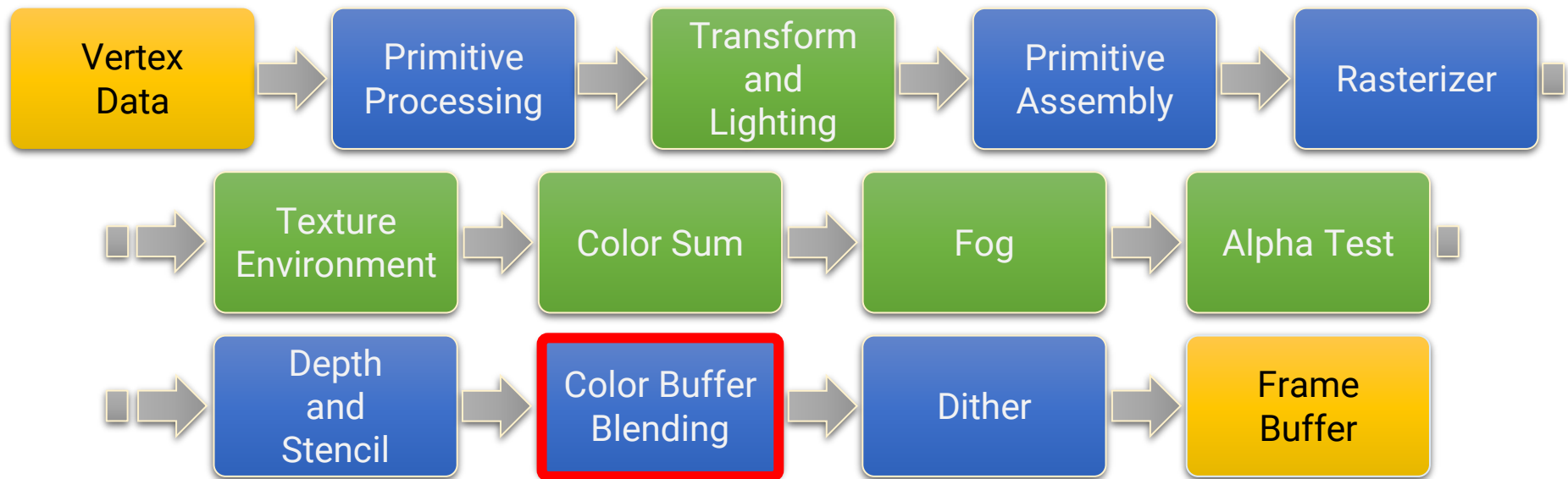
- Used to discard fragments that fail a stencil comparison, based on the content of the stencil buffer



stencil buffer



# OpenGL (1.x) Fixed Function Pipeline





# Color Buffer Blending

- Blend the color of fragments with the previous results in the frame buffer based on the **alpha values** of the current fragments, as well as the **blend function** and the **blend equations**



# Color Buffer Blending (cont.)

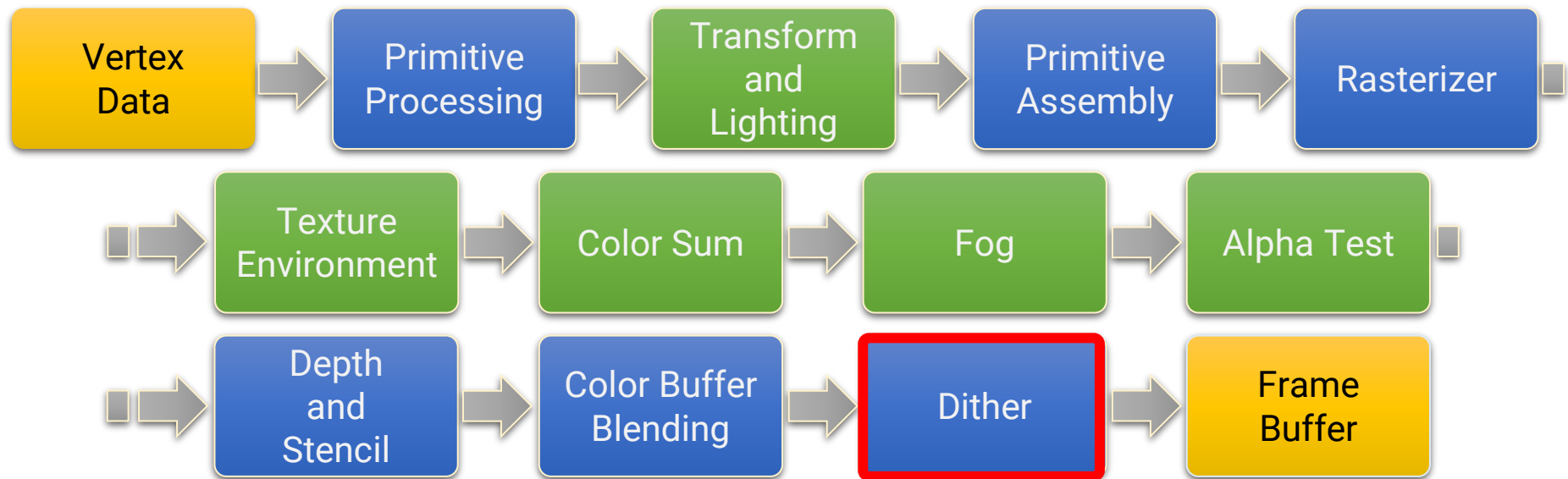
- Blend the color of fragments with the previous results in the frame buffer based on the **alpha values** of the current fragments, as well as the **blend function** and the **blend equations**

$$\bar{C}_{result} = \bar{C}_{source} * \boxed{F_{source}} + \bar{C}_{destination} * \boxed{F_{destination}}$$

GL\_SRC\_ALPHA                      GL\_ONE\_MINUS\_SRC\_ALPHA

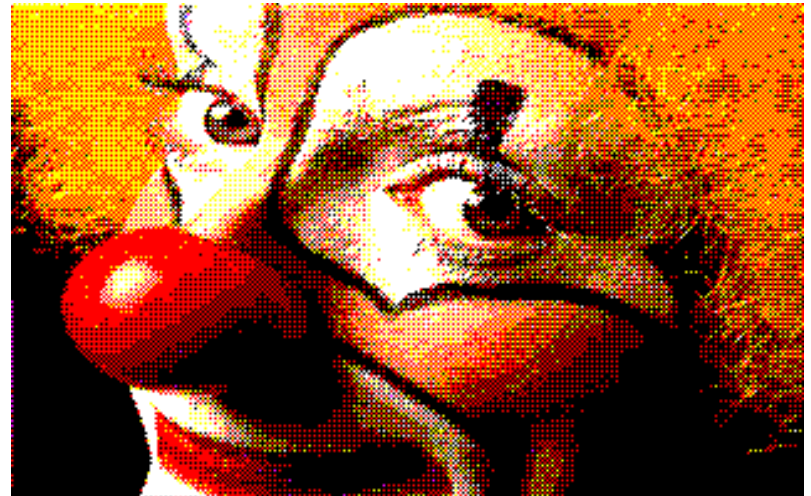
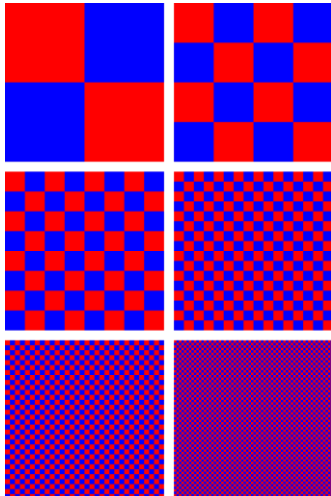


# OpenGL (1.x) Fixed Function Pipeline



# Dither

- If a color palette is used, OpenGL will try to simulate a larger color palette by mixing colors in close proximity
- Areas of a single color are replaced by a pattern of dots of several different colors, in such a way that optical mixing in the eye produces a color close to the desired one

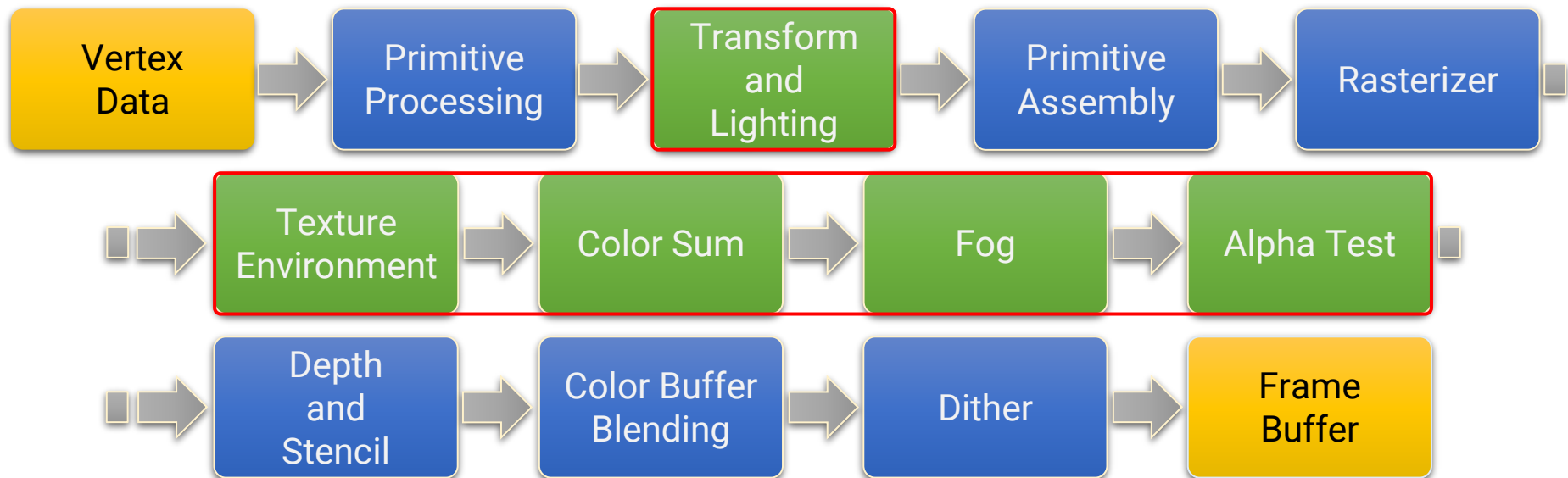


# Summary of Fixed Function Pipeline

- An 3D object will come to the screen with a series of “fixed” steps
  - Fixed transformation (MVP matrix)
    - How about user interface on the screen?
  - **Fixed (Phong) lighting model on vertices**
  - **Fixed modulation of lighting color and texture color**
    - $\text{Color} = \text{Lighting} \times \text{Texture}$
- **We would like more flexibility!**
- In Part II, we will introduce how to add **flexibility** by using **shaders**

# Spoiler: OpenGL 1.x to OpenGL 2.0

- All the functions performed by OpenGL are **fixed** and **could not** be modified except through the manipulation of the **rendering states**
- The stages shown in **green** have been replaced by **shaders**



# Spoiler: OpenGL 1.x to OpenGL 2.0 (cont.)

- Released in 2004
- Provide the ability to **programmatically** define the vertex transformation and lighting and the fragment operations (with small GPU programs called **shaders**)

