

Employment Contracts for Earnings and Hours

Kevin Hunt*

University of Wisconsin-Madison

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Abstract

Legal regulations of hours have become increasingly common, yet less is known about how workers' earnings and hours are set in employment contracts. In this paper, I document that workers commonly report changes in their hours, but the association of changes in earnings with changes in hours differs depending on whether their explicit contract pays them by the hour or not. To understand these patterns, I develop and estimate a frictional labor market model with implicit contracts motivated by risk-sharing and constrained by limited commitment. Although the model has no explicit hourly and non-hourly contracts, implicit contracts generate a larger association between earnings and hours for low-income workers and when turnover is higher as in the data. I find that hours variability plays a quantitatively important role to increase workers' output, which yields caution to policymakers when restricting hours variability. This is especially true for high income and long tenure workers who benefit the most from risk-sharing in implicit contracts.

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1 Introduction

Government policies in the United States increasingly regulate how workers' hours are set and adjusted at their jobs. Recently, the federal minimum salary threshold that exempts white-collar workers from overtime payments increased from \$683 to \$1,128 per week. Local governments, including New York City and San Francisco, have passed predictive scheduling laws that penalize firms for changing work schedules on short notice. Additionally, the states of Maine, Nevada, and Illinois now mandate that all workers receive paid time off from their employers. In order to effectively evaluate these policies, it is crucial to understand how workers' hours are determined in tandem with earnings.

While the textbook neoclassical model views hours as a choice made by workers who are paid what they produce in a competitive spot market, there is substantial evidence that firms play an important role in setting workers' hours (Altonji and Paxson [1992], Goldin [2014], Bick et al. [2022]). However, this literature on "hours constraints" typically views hours as a fixed feature of a job and has little to say about the variability of hours and earnings within a job. Implicit (or long-term) contracts provide an alternative framework to the spot market and hours constraints models (Harris and Holmstrom [1982], Thomas and Worrall [1988]), and previous research has found empirical evidence supporting the predictions of implicit contracts for hours (Beaudry and DiNardo [1995], Ham and Reilly [2002]). Still, less is known quantitatively about how these contracts influence workers' outcomes and their implications for government labor market policies.

In this paper, I aim to answer these questions with four contributions. First, I document that workers commonly report changes in their hours within a job, but the elasticity of earnings with respect to hours differs across workers based on their *explicit* employment contract. By explicit employment contract, I refer to whether the worker is paid by the hour or not. Second, I develop a frictional labor market model where firms and workers agree to *implicit* employment contracts motivated by risk-sharing and constrained by two-sided limited commitment. In the model, changes in firm labor productivity and worker leisure preferences generate a motive to vary hours, and cooperatively negotiated implicit contracts determine the pass-through of these shocks to earnings and hours. Third, I estimate the model to match the empirical dynamics of earnings, hours, and job mobility. Although the model does not have explicit hourly and non-hourly contracts, its implicit contracts generate a larger elasticity of earnings with respect to hours for workers with low earnings and when workers are more likely to leave their jobs as in the data. Thus, I argue that the distinction between *explicit* hourly and non-hourly contracts partially represents a distinction in the degree of risk-sharing in *implicit* contracts. Finally, I use the estimated model to consider

the implications of employment contracts for government policies that regulate hours and provide transfers to the non-employed.

To begin, I use the Survey of Income and Program Participation (SIPP) to document that both hourly and non-hourly workers commonly report changes in their usual hours of work per week across surveys even when employed continuously at the same firm. The average absolute value of the change in usual hours of work per week is 2.4 and 3.2 hours per week for hourly and non-hourly workers, respectively. Although hourly workers report smaller changes in hours, they also tend to work fewer hours. The absolute value of the change in the logarithm of hours is approximately 8 log points for both sets of workers, meaning that the relative changes in their hours are of similar magnitude. These changes are also not generated by a handful of outliers because the change in usual hours is greater than or equal to five in absolute value for 20% and 30% of hourly and non-hourly workers, respectively. One concern with these patterns comes from the well-documented measurement error inherent in survey data ([Bound et al. \[2001\]](#)). However, I show that changes in hours are persistent across four surveys for both hourly and non-hourly workers, which means that they cannot be entirely explained by classical measurement error. Recent work using firms' administrative records has documented that changes in hours are common for workers who are paid by the hour ([Bound et al. \[1994\]](#), [Lachowska et al. \[2023\]](#), [Ganong et al. \[2024\]](#)). Here, I document that non-hourly workers report hours changes of similar magnitude to hourly workers in survey data that cannot be easily explained by measurement error.

Next, I show that although changes in hours are common within a job for both hourly and non-hourly workers, the elasticity of earnings with respect to hours is larger for hourly workers. Across surveys, a one percent change in hours is associated with a 0.4% change in earnings for hourly workers but only a 0.1% change in earnings for non-hourly workers. Measurement error in hours will lead to a downward bias in these estimates, and temporary changes in hours may have a differential effect on earnings compared to persistent changes. To account for this, I use information about changes in hours across four consecutive surveys to disentangle the relationship between persistent changes in hours from temporary changes such as classical measurement error. For persistent changes, hourly workers still experience a larger elasticity of earnings with respect to hours. A persistent one percent change in hours is associated with a one percent change in earnings for hourly workers but only a 0.4% change in earnings for non-hourly workers. The fact that hourly workers' earnings are less stable in the SIPP compared to non-hourly workers' is consistent with studies analyzing firm payroll records ([Grigsby et al. \[2021\]](#), [Ganong et al. \[2024\]](#)). However, both types of workers in the SIPP report similar changes in hours, which suggests that their employment contracts influence the relationship between changes in hours and earnings.

In order to understand why different workers receive different employment contracts from firms, I develop a frictional labor market model with on-the-job search where risk-neutral firms and risk-averse workers cooperatively negotiate implicit contracts for earnings and hours. Within a match, changes in the firm’s labor productivity and the worker’s leisure preferences generate a motive to adjust hours within a job. The implicit contract agreed upon by the firm and worker specifies how shocks transmit to the worker’s earnings and hours while also responding to outside offers that the worker receives via on-the-job search. Relative to recent papers studying how implicit contracts motivated by risk-sharing influence the transmission of labor productivity shocks to earnings or hourly wages (Rudanko [2011], Balke and Lamadon [2022], Souchier [2022]), this model additionally incorporates an hours margin of adjustment. Previous papers have studied hours within an implicit contract and found reduced-form empirical support for the predictions of a contracting model (Abowd and Card [1987], Beaudry and DiNardo [1995], Ham and Reilly [2002]). I augment these studies by introducing leisure preference shocks and search frictions.

Using the methods of Marcet and Marimon [2019], I derive the optimal history-contingent contract decisions for earnings and hours that reveal how a firm and worker optimally share risk. Relative to a model where workers set their own hours, the implicit contract *amplifies* the responsiveness of hours to productivity and preference shocks. The worker is willing to accept this amplification of hours variability because earnings are *insured* against the resulting output variation and are less variable with implicit contracts. However, if firms and workers lack commitment and can walk away from the contract as in Thomas and Worrall [1988], the extent to which the contract can amplify hours variations and insure the worker’s earnings will be reduced. When commitment constraints rarely bind, the optimal contract approximates one with full commitment where the worker receives smooth earnings payments and hours vary in response to changes in labor productivity or leisure preferences. If they frequently bind, then the worker’s earnings will vary in tandem with hours in order to satisfy the commitment constraints. This generates heterogeneity in the elasticity of earnings with respect to hours within a job based on the extent to which limited commitment constrains risk-sharing. While previous literature has considered differing job tasks as a reason for the distinction between hourly and non-hourly workers (Fama [1991], Haber and Goldfarb [1995], Hamermesh [2002]), different contracts arise in this model as a result of different levels of risk-sharing. Because hourly workers’ earnings are more correlated with their hours than non-hourly workers, this suggests that they receive less insurance from firms in implicit employment contracts.

Using the simulated method of moments, I estimate the model to match the dynamics of earnings, hours, and job mobility observed in the SIPP. The labor productivity shock

process and leisure preference shock process are separately identified based on the variability of earnings and hours. Although both shocks generate a motive to vary hours, labor productivity shocks will have a larger impact on workers' earnings. The estimated model is able to match well both the cross-section distribution of earnings and hours, the dynamics of earnings and hours, and the relationship between changes in earnings and changes in hours. To validate the model, I show that the model is able to understand two empirical facts. First, the model generates that workers with low earnings have a higher elasticity of earnings with respect to hours, which is also true in the data. In the data, this is because these workers are more likely to be paid by the hour. In the model, it is because the outside option of non-employment is relatively more attractive for workers with low earnings, and this increases the likelihood that commitment constraints bind for these workers. Second, I show that the elasticity of earnings with respect to hours is increasing in both the job finding rate for employed workers and the exogenous job destruction rate. In the data, hourly workers are more likely to leave their jobs by switching to a new firm or by exiting to non-employment. In the model, an increased probability of contacting a new firm reduces the ability for the contract to insure workers' earnings against changes in output because commitment constraints are more likely to bind. The ability of the model to match these facts provides some evidence that the distinction between hourly and non-hourly workers partially reflects different levels of risk-sharing between firms and workers.

In the estimated model, I find that 26% of the variance of hours is generated by job-specific labor productivity shocks, and 13% is generated by worker-specific leisure preference shocks. This suggests that labor productivity shocks are the main driver of changes in hours within a job rather than workers' leisure preferences. Most of the remaining variance in hours is accounted for by fixed heterogeneity in worker types. Additionally, hours play an important role in the contract to amplify the effect of labor productivity shocks on match output. If hours remained fixed, then a one percent increase in match productivity would be associated with a one percent higher match output. However, workers with one percent higher match productivity have 1.2% higher output as a result of working 0.2% more hours on average. Furthermore, I find that workers' earnings are well insured against changes in output resulting from changes in their leisure preference and labor productivity shocks. Workers with one percent higher labor productivity shock have 1.2% higher output but only 0.173% higher earnings, implying that firms absorb about 85% of differences in output associated with changes in productivity. Similarly, workers with one percent higher leisure preference shocks have 0.239% lower output but only 0.023% lower earnings, implying that firms absorb 90% of output differences associated with changes in leisure preferences.

In the final part of the paper, I use the model to consider the implications of implicit

contracts for government policies. First, I consider how workers' outcomes change when hours are exogenously set as a function of workers preferences and cannot adjust to changes in labor productivity shocks. When hours cannot adjust to changes in labor productivity shocks, output per worker declines in steady state by 4.4%, and workers are worse off by a consumption equivalence of 2.1% on average. Although the negative impact of restricting hours in an optimal contract is expected, these results emphasize that the variability of hours play an important role in the implicit contract to increase workers total expected output and earnings. It also provides caution to policymakers considering constraints on the variability of hours such as overtime premium, maximum hours of work, and predictive scheduling laws. However, these policies may also have benefits such as combatting monopsony power or work sharing that are not considered in this model, and the costs of restricting hours from the perspective of implicit contracts must be weighed against these benefits. Currently, policies regulating hours typically target specific groups of workers for whom the benefits of implicit contracting are likely to be smaller. For example, managers, professionals, and high income workers are excluded from overtime requirements, and workers in these occupations tend to have longer tenure on their jobs. Similarly, predictive scheduling laws target industries including retail and hospitality where tenure is low and turnover is high. When workers have longer tenure, the benefits from risk-sharing in implicit contracts are likely to be larger, and this can rationalize exempting these workers from certain labor market restrictions. Future policy discussions could consider tenure of workers and turnover when choosing how to regulate the labor market.

In addition to restricting hours, I also consider how government transfers to the non-employed impact risk-sharing between firms and workers within implicit contracts. A large literature starting with [Jacobson et al. \[1993\]](#) has shown that job loss has large and persistent impacts on workers' earnings, and government policies such as unemployment benefits aim to mitigate these impacts. However, these policies also crowd out risk-sharing in implicit contracts by reducing hours variability and increasing earnings variability in response to shocks. This crowd out occurs because the value of non-employment is increased by the transfer, increasing the extent to which workers' commitment constraints bind. Similarly, these transfers improve workers' bargaining position and reduce firm flow profits, which increases the extent to which firms' commitment constraints bind. I find that for the median worker a \$50 weekly transfer (7.3% of average weekly earnings) to the non-employed would increase the elasticity of earnings with respect to productivity shocks by 0.1, while reducing the elasticity of hours with respect to productivity shocks by 0.02. Additionally, the elasticity of earnings with respect to preference shocks would increase by 0.02 and the elasticity of hours with respect to preference shocks would decrease by 0.01. Previous work by [Burdett](#)

and Wright [1989] has shown that transfers to the non-employed reduces risk-sharing between firms and workers on the extensive margin by increasing the probability that workers are laid off from their jobs. Here, I additionally show that these transfers can reduce risk-sharing on the intensive margin by distorting the pass-through of shocks to workers' earnings and hours.

Related Literature Starting with Baily [1974] and Azariadis [1975], many papers consider how risk-neutral firms provide insurance to their risk-averse workers against changes in productivity in an implicit (or long-term) contract. The goal of these original papers was to understand the sizeable fluctuations in employment over the aggregate business cycle despite limited changes in wage compensation. Building on this work, Harris and Holmstrom [1982] analyze wage growth when workers cannot commit to the contract, and Thomas and Worrall [1988] consider how wages fluctuate when neither firms nor workers can commit. Several papers have extended these frameworks to allow for an hours margin of adjustment (Sigouin [2004], Thomas and Worrall [2007]), and reduced form evidence supports predictions of the contracting model (Abowd and Card [1987], Beaudry and DiNardo [1991], Beaudry and DiNardo [1995], Ham and Reilly [2002], Lagakos and Ordonez [2011], Bellou and Kaymak [2012]). I build on this work by considering leisure preference shocks in addition to labor productivity shocks as a source of risk faced by workers and study heterogeneity in the amount of insurance firms provide to different workers. Additionally, I argue consider implicit employment contracts as the motivation for the distinction between explicit hourly and non-hourly contracts.

This paper also relates to the literature on the determinants of labor supply emphasizing the role of firms. Several papers in this literature consider or argue that hours are a rigid feature of a job, and workers who wish to change their hours must seek employment at a new firm (Kahn and Lang [1992], Altonji and Paxson [1992], Dickens and Lundberg [1993], Bloemen [2008], Chetty et al. [2011]). However, I highlight in the SIPP that reported changes in hours happen within jobs across a wide range of worker characteristics, and that these changes in hours are persistent. Furthermore, several recent papers have studied the empirical relationship between earnings and hours (Yurdagul [2017], Bick et al. [2022], Labanca and Pozzoli [2022], Shao et al. [2023]). They find that there is a weak or negative relationship between earnings and hours, particularly at longer hours of work, and view this as a result of the underlying returns to hours in production. My work emphasizes the dynamic relationship between changes in earnings and hours, and considers how risk-sharing between firms and workers can generate influence the relationship between earnings and hours observed in the data.

Moreover, this paper contributes to the literature studying frictional labor market models. A large part of this literature building on the work of [Postel-Vinay and Robin \[2002\]](#), [Dey and Flinn \[2005\]](#), [Cahuc et al. \[2006\]](#) consider both workers and firms to be risk-neutral, while my framework incorporates risk-averse workers and implicit contracts. While several recent papers have considered implicit contracts in a frictional labor market ([Rudanko \[2011\]](#), [Balke and Lamadon \[2022\]](#), [Souchier \[2022\]](#)), they abstract from an hours margin of adjustment. An exception is [Sigouin \[2004\]](#) who considers hours and aggregate productivity shocks in a frictional labor market; however, he does not consider leisure preference shocks or on-the-job search. My work is also related to [Postel-Vinay and Turon \[2010\]](#) and [Lise et al. \[2016\]](#), which use empirical dynamics of earnings to understand latent dynamics of match productivity in equilibrium search models. I additionally incorporate the dynamics of hours within jobs and leisure preference shocks influencing these hours.

Outline The rest of this paper is organized as follows. Section 2 provides an overview of the data facts regarding earnings, hours, and employment contracts. Section 3 presents the structural model of implicit contracts. Section 4 details the estimation, Section 5 discusses the analysis of the estimated model and policy implications. Section 6 concludes.

2 Empirical Dynamics of Earnings and Hours

This section documents three key data patterns regarding the dynamics of earnings, hours, and job mobility: (1) workers commonly report changes in their hours within a job and these changes are persistent, (2) the elasticity of earnings with respect to hours differs based on whether they are paid by the hour or not, and (3) hourly workers have shorter tenure and higher turnover than observably similar non-hourly workers.

The main data source is the Survey of Income and Program Participation (SIPP) from 1990 to 2013.¹ Each household in the SIPP is surveyed once each four months for 32 to 48 months. Studying hours for both hourly and non-hourly workers necessitates the use of survey data because administrative records either contain no information about hours or

¹I build on the sample construction codes of [Gertler et al. \[2020\]](#) when constructing my sample.

accurate information only for workers who are paid by the hour.² While self-reported hours in survey data contain measurement error (Bound et al. [2001]), I later discuss how repeated observations in the SIPP can help to account for classical measurement error that is serially uncorrelated.

To avoid dynamics in earnings and hours generated by education and retirement that are beyond the scope of this paper, I restrict the sample to individuals between the ages of 25 and 59. This paper focuses on how firms design employment contracts, so I further exclude observations for the self-employed. For individuals with multiple jobs, I use information only about their main job, which is defined as the job with greater monthly earnings. Table 1 shows summary statistics about workers in the sample. In each SIPP survey, employed individuals are asked about their usual hours of work on their job: “How many hours per week did you usually work at all activities at this job?”. Respondents were told that if they have variable hours, they should report the “approximate average” of their actual hours per week for the weeks that they worked. In addition to hours, individuals are asked if they are paid by the hour and how much they were paid in each month during the survey.³ Although information about earnings is available for all months during the survey, the “seam phenomenon” causes the majority of changes in monthly earnings to happen across surveys rather than within surveys as discussed in the SIPP Users’ Guide (U.S. Census Bureau, 2001). Following Gottschalk and Huynh [2010] and Gertler et al. [2020], I use only the information about earnings in the last month of the survey, which I divide by weeks worked in the last month to arrive at a measure of weekly earnings. I deflate earnings to May 2001 dollars using monthly Personal Consumption Expenditures (PCE) price index.

2.1 Workers commonly report changes in hours within a job.

How common are changes in hours within a job? Table 2 shows that across surveys, workers who stay employed at the same firm commonly report changes in their usual hours of work per week. This is true for both hourly and non-hourly workers. On average, the absolute

²Relative to other surveys that interview households annually or biennially such as the National Longitudinal Survey of Youth and Panel Study of Income Dynamics, the SIPP between 1990 and 2013 allows for accurate measurement of employment dynamics at a higher frequency. Starting in 2014, the SIPP transitioned to an annual frequency. The Current Population Survey interviews households each month and asks about hours of work in every survey, but questions on labor earnings are only asked in the outgoing rotation surveys and March ASEC supplements that happen one year apart. Across outgoing rotation surveys and Annual Social and Economic supplements, it is also not possible to identify for most workers if their employer changed. The CPS primarily serves as an employment survey, and the lack of detailed information on income motivated the creation of the SIPP as its name suggests.

³Unfortunately, more detailed questions about how workers are paid is not included. However, the PSID includes a more detailed set of options from which workers can report their payment scheme. In Appendix A.1, I show that the vast majority of workers not paid by the hour report that they are paid fixed salaries.

Table 1: Summary Statistics

Contract Type	(1) Hourly	(2) Not Hourly
Avg. Earnings/week (2001 \$)	\$519.30 (360.77)	\$942.81 (617.98)
Avg. Hours/week	38.2 (9.0)	43.3 (9.6)
Avg. Age	40.3 (9.6)	41.4 (9.3)
Fraction Female	0.502	0.450
Fraction with Bachelor's Degree	0.127	0.498
Fraction with New Employer Next Survey	0.062	0.044
Fraction Non-employed Next Survey	0.055	0.028
Observations	459,629	410,164

Note: This table reports summary information about the sample of workers in the SIPP for years 1990 to 2013. Observations are weighted using longitudinal weights. Standard deviations are in parentheses.

value of the change in usual hours of work per week is 2.4 for hourly workers and 3.3 for non-hourly workers. Although hourly workers report smaller changes in hours on average, they also tend to work fewer hours. To account for differences in the typical level of hours, I also report the average absolute value of the change in the logarithm of hours. This statistic is 0.075 for hourly workers and 0.077 for non-hourly workers, so the absolute value of the change in hours is approximately 7 to 8% for both sets of workers. Furthermore, these large average changes in hours are not generated solely by outliers; 21.6% of hourly workers and 31.5% of non-hourly workers report a change in their usual hours of at least five in absolute value. Lastly, these changes in hours are not driven by particular subgroups of workers. In Appendix A.3, I show that workers commonly report changes in their usual hours of work when staying employed at the same firm regardless of their age, education, sex, industry, occupation, calendar month, or survey year.

Once concern may be that these changes are largely driven by measurement error, as

Table 2: Changes in Hours within a Job

Contract Type	(1) Hourly	(2) Not Hourly
Mean $ \Delta \text{ Usual Hours per Week} $	2.4 (5.19)	3.2 (5.94)
Mean $ \Delta \log(\text{Usual Hours per Week}) $	0.075 (0.203)	0.077 (0.189)
Fraction with $ \Delta \text{ Usual Hours per Week} \geq 5$	0.218	0.310
Fraction with $ \Delta \text{ Usual Hours per Week} \geq 10$	0.096	0.153
Observations	393,801	364,797

Note: This table reports summary information about changes in hours across surveys for the sample of workers employed at the same firm in two consecutive surveys. Observations are weighted using longitudinal weights. Standard deviations are in parentheses.

validation studies have found substantial measurement error in survey-reported hours ([Bound et al. \[2001\]](#)). Additionally, these changes could largely be transitory rather than persistent. Using four repeated observations of the same individual at the same job, however, it is possible to test whether changes in hours are persistent. Formally, suppose reported hours h_{it} for individual i at time t contain two components that are additively separable in logs:

$$\log h_{it} = p_{it} + m_{it}. \quad (1)$$

Here, p_{it} is a persistent component of reported hours with $\text{cov}(p_{it}, p_{it+k}) > 0$, and m_{it} is a transitory component that is serially uncorrelated and uncorrelated with the persistent component p_{it} . If there was classical measurement error in hours, then this would be captured by the transitory component m_{it} . However, m_{it} could also contain true temporary changes in hours. Across two surveys, it is not possible to know whether an observed change was caused by the persistent component p_{it} or the transitory component m_{it} .

However, using four consecutive surveys we can test whether there are any persistent changes. I will refer to the change in hours from periods t to $t + 3$ as the outer change in hours, and the change in hours from periods $t + 1$ to $t + 2$ as the inner change in hours. First, note that the covariance between the inner and outer change in hours is equal to the

covariance of the inner and outer persistent change in hours:

$$\begin{aligned}
& \text{cov}(\log h_{it+3} - \log h_{it}, \log h_{it+2} - \log h_{it+1}) \\
&= \text{cov}(m_{it+3} - m_{it}, m_{it+2} - m_{it+1}) + \text{cov}(p_{it+3} - p_{it}, m_{it+2} - m_{it+1}) \\
&\quad + \text{cov}(m_{it+3} - m_{it}, p_{it+2} - p_{it+1}) + \text{cov}(p_{it+3} - p_{it}, p_{it+2} - p_{it+1}) \\
&= \text{cov}(p_{it+3} - p_{it}, p_{it+2} - p_{it+1}). \quad (2)
\end{aligned}$$

This is because the measurement error is serially uncorrelated and uncorrelated with the persistent changes in hours, so the first three terms of the expand covariance are zero. Suppose that there are no persistent changes in hours, so $p_{it} = p_i$ is constant across time for each individual. Then the covariance of the inner and outer changes in hours would be zero by equation 2.

To test this hypothesis, we can regress the change in hours from $t + 1$ to $t + 2$ on the change in hours from t to $t + 3$ for the sample of workers who are employed at the same firm in four consecutive surveys:

$$\log h_{it+2} - \log h_{it+1} = \beta (\log h_{it+3} - \log h_{it}) + \gamma + \epsilon_{it}. \quad (3)$$

If there are in fact no persistent changes in hours and the covariance between these two variables is zero, then the resulting regression coefficient β would be zero. However, as shown in Table 3, the coefficient β is positive and statistically significant at any reasonable threshold for both hourly and non-hourly workers. Overall, workers with a one percent increase in hours from periods t to $t + 3$ on average have a 0.11% increase in hours from periods $t + 1$ to $t + 2$. The persistence of changes in hours is slightly larger for hourly workers than for non-hourly workers. This means that reported changes in hours are persistent across time and cannot entirely be explained by transitory factors such as classical measurement error.

Previous work using firms' administrative records has documented that changes in hours within a job are common for hourly workers. This was originally noted in the validation study of the PSID, which examined the administrative records of a single large manufacturing company: "Company records for hourly workers also showed surprising variability in work hours and earnings from one pay period to the next" ([Bound et al., 1994, p. 347]). Additionally, Lachowska et al. [2023] analyze the hours reported in administrative records from Washington state and report: "(M)uch of the variation in hours appears to be within a job over time, as opposed to resulting from fixed employer and worker effects" (p. 17-18). Finally, Ganong et al. [2024] find in a payroll processing company's records that: "in one

Table 3: Relationship between Inner and Outer Change in Hours

	(1)	(2)	(3)
	$\Delta \log(\text{hours})_{t+1,t+2}$	$\Delta \log(\text{hours})_{t+1,t+2}$	$\Delta \log(\text{hours})_{t+1,t+2}$
$\Delta \log(\text{hours})_{t,t+3}$	0.110 (0.002)	0.122 (0.002)	0.097 (0.002)
Contract Type	All	Hourly	Not Hourly
Observations	345,714	173,877	171,837

Note: This table reports the regression coefficients from equation 2 using the sample of SIPP workers who are employed at the same firm in four consecutive surveys. Standard errors are presented in parentheses. Observations are weighted using longitudinal weights.

quarter of months earnings change by at least 21%... Virtually all of this earnings volatility is driven by fluctuations in hours.” (p. 2).⁴ Thus, it should not be surprising that hourly workers in survey data like the SIPP also report changes in their hours. In administrative records of hours, though, it is not possible to observe accurate information about the hours for workers who are not paid by the hour. A contribution of this paper is to document that non-hourly workers report changes in their hours in surveys of similar magnitude to hourly workers.

2.2 The hours elasticity of earnings differs by contract type.

Both hourly and non-hourly workers commonly report changes in their hours within a job, but what is the elasticity of their earnings with respect to hours? To answer this question, I regress the change in the logarithm of workers’ earnings e_{it} from periods $t + 1$ to $t + 2$ on the change in the logarithm of workers’ hours $t + 1$ to $t + 2$ for individuals employed at the same firm in four consecutive surveys t to $t + 3$:

$$\log e_{it+2} - \log e_{it+1} = \beta(\log h_{it+2} - \log h_{it+1}) + \gamma + \epsilon_t \quad (4)$$

Here, β is the elasticity of earnings with respect to hours, meaning that a one percent change in hours would be associated with on average a β percent change in earnings. When estimated by ordinary least squares, the coefficient β measures this elasticity for a typical change in hours that may either be transitory or persistent. Results of estimating this regression by ordinary least squares are shown in the first two columns of Table 4. For hourly workers, a

⁴This is more volatile than the changes in hours for hourly workers in the SIPP. For hourly workers in the SIPP, in one quarter of observations, hours change by at least 9%.

one percent increase in hours is associated with a 0.393% increase in earnings, while for non-hourly workers this elasticity is only 0.117. This estimate of the elasticity will measure an average of the relationship between persistent and transitory changes in hours and earnings. If transitory changes in hours are largely measurement error, then the estimated elasticity will be biased toward zero.

Table 4: Elasticity of Earnings w.r.t. Hours by Payment Scheme

Contract	(1) Hourly	(2) Not Hourly	(3) Hourly	(4) Not Hourly
$\log(\text{hours})_{t+2} - \log(\text{hours})_{t+1}$	0.393 (0.005)	0.117 (0.005)	1.054 (0.039)	0.423 (0.047)
Estimation	OLS	OLS	IV	IV
First Stage F-Stat			3,001	1,831
Observations	173,877	171,837	173,877	171,837

Note: This table presents regression coefficients from equation 4 estimated by ordinary least squares (OLS) and instrument variable (IV). The instrument for the inner change in hours $\log(\text{hours})_{t+2} - \log(\text{hours})_{t+1}$ is the outer change in hours $\log(\text{hours})_{t+3} - \log(\text{hours})_t$. The sample includes workers who are employed at the same firm for four consecutive surveys t to $t + 3$. Observations are weighted using longitudinal weights.

To estimate the elasticity of earnings with respect to persistent changes in hours, we can use the outer change in hours $\log h_{it+3} - \log h_{it}$ as an instrument for the inner change in hours $\log h_{it+2} - \log h_{it+1}$ for the sample of workers employed at the same firm for four consecutive surveys. The outer change in hours will be assumed to be uncorrelated with the inner change in the transitory component of hours:

$$\text{cov}(\log h_{it+3} - \log h_{it}, m_{it+2} - m_{it+1}) = 0, \quad (5)$$

so the outer change satisfies the exogeneity condition for a valid instrument. Additionally, it will be correlated with the inner change in the persistent component of hours:

$$\text{cov}(\log h_{it+3} - \log h_{it}, p_{it+2} - p_{it+1}) > 0. \quad (6)$$

As shown in Table 3, this is a relevant instrument with an F-statistic sufficiently large for valid statistical inference (Lee et al. [2022]). As shown in columns three and four of Table 4, the elasticity of earnings with respect to hours is larger for persistent changes in hours. Hourly workers with a one percent persistent increase in hours have on average a 1.054%

increase in earnings, while non-hourly workers have on average a 0.432% increase in earnings. If transitory changes in hours are entirely classical measurement error and have no effect on earnings, then these estimates would suggest that 62% and 72% of the variance for the changes in hours are generated by measurement error for hourly and non-hourly workers, respectively. However, if transitory changes in hours are partially real and have a true effect on earnings, then this will over-state the importance of measurement error.⁵

Thus, whether measured by ordinary least squares or by an the instrument, hourly workers' changes in earnings are more correlated with changes in their hours on their jobs. This elasticity is over three times larger when estimated by ordinary least squares, and about two and a half times larger when estimated using the instrument. The elasticity for hourly workers is nearly one as would be expected for hourly workers below forty hours per week. Thus, although hourly and non-hourly workers experience changes in hours that are similar in magnitude, the relationship between changes in earnings and changes hours is much stronger for hourly workers.

One concern is that changes in earnings and hours are mechanically more correlated for hourly workers by design of the survey. In the SIPP, earnings are measured at the monthly level. However, workers are allowed to report their earnings to the survey as paychecks, yearly, monthly, or weekly amount and have these converted to a monthly amount. Additionally, workers can choose to report an hourly wage and hours and have their monthly earnings calculated accordingly. Hourly workers presumably would be more likely to choose the hourly calculation, while non-hourly workers would likely choose a different way of reporting earnings. However, the reason the survey is designed this way is to reduce measurement error in earnings by having all respondents report a monthly amount. Thus, these measured elasticities likely provide relevant information about how changes in hours correlate with changes in earnings. As shown in [Ganong et al. \[2024\]](#), hourly workers do have month-to-month earnings variability that is highly correlated with hours changes, while non-hourly workers largely have stable earnings month-to-month. Another concern is that non-hourly workers are more likely to receive bonuses than hourly workers. Although changes in non-hourly workers' earnings have less of an effect on their earnings today, it may have a larger effect on their earnings when bonuses are paid at the end of the year. However, [Grigsby et al. \[2021\]](#) reported that bonuses account for at least 10% of earnings for less than 10% of workers. Thus, although the coefficients for non-hourly workers are likely to be downward biased as a result of bonuses, the fact that relatively few workers receive substantial bonuses suggests that this would not lead to large changes.

⁵[Duncan and Hill \[1985\]](#) report that the measurement error of annual changes in hours has a variance that is 80% of the variance of true annual changes in hours.

2.3 Hourly workers have shorter tenure and higher turnover

I compare the tenure and turnover of workers who are and aren't paid hourly in the following regression:

$$y_{it} = \beta \text{Hourly}_{it} + \gamma X_{it} + \epsilon_{it}. \quad (7)$$

Here, y_{it} is the outcome of interest, which is either the tenure of the worker at her job measured in years, an indicator equal to one if she switches to a new firm at the next survey, or an indicator equal to one if she is non-employed next survey. The vector X_{it} is a set of observable worker characteristics including education, age, sex, occupation, industry, the logarithm of earnings, the logarithm of usual hours per week, indicators for the survey year, and indicators for the survey month. The coefficient β measures the average difference in the outcome variable for hourly workers relative to observably similar workers who are not paid by the hour.

Results from the estimation of equation 7 are presented in Table 5. Even after controlling for a rich set of observable worker characteristics, hourly workers have on average about three-fourths fewer years of tenure on their jobs, which is approximately 10% of the average tenure of the sample. Additionally, they are 0.6 percentage points and 0.4 percentage points more likely to transition to a new firm or non-employment at the next survey, respectively. Together, this means that hourly workers are about 10% more likely to leave their current firm than the average worker in the sample. This echoes one message from [Ganong et al. \[2024\]](#) that workers with more variable earnings who are typically paid by the hour are more likely to leave their jobs and motivates thinking about the joint dynamics of earnings and hours in a frictional labor market model.

3 Contracting Model

To understand the empirical dynamics of earnings, hours, and job mobility, this section develops a model where firms offer implicit contracts and compete for workers in a frictional labor market. The implicit contracting framework builds on [Thomas and Worrall \[1988\]](#) by adding an intensive hours margin of adjustment, while the frictional labor market builds on [Dey and Flinn \[2005\]](#) by allowing firms to deliver values via implicit contracts. There are three key ingredients of the model to match the three empirical facts. First, a worker's hours will vary at her job as a result of shocks to either her leisure preferences or her firm's labor productivity. Second, her earnings will not necessarily vary in tandem with her hours or production as the result of risk-sharing in an implicit contract with her employer. Finally, two-sided limited commitment will constrain risk-sharing in implicit contracts and generate

Table 5: Differences in Tenure and Turnover for Hourly and Non-Hourly Workers

Outcome	(1) Tenure (Years)	(2) Switch Firm Next Survey	(3) Non-emp. Next Survey
Hourly	-0.744 (0.019)	0.006 (0.001)	0.005 (0.001)
Outcome Mean	7.622	0.053	0.045
Observations	836,842	836,842	836,842

Note: This table presents regression coefficients on the indicator for hourly pay scheme from the regression in equation 7 using the sample of workers in the SIPP observed in two consecutive periods. Standard errors are in parentheses. The regression includes controls for age, sex, the logarithm of earnings, the logarithm of hours, occupation, industry, education, year, and month. Observations are weighted using longitudinal weights.

dynamics in earnings and hours that differ across workers. In particular, the elasticity of earnings with respect to hours will be higher for workers who are more likely to leave their jobs.

3.1 Agents and Environment

The labor market is frictional and in a steady state equilibrium. On one side of the market, there is a unit mass of workers who are heterogeneous in their average labor productivity type ψ_i and average leisure preference type θ_i jointly distributed according to $F_{\psi\theta}$. On the other side of the market, there is a continuum of ex-ante identical firms who produce a homogenous good. Time t is discrete and runs forever. Both firms and workers live forever and discount the future with a common factor $\beta \in [0, 1)$. The probabilities that non-employed and employed workers contact a job at another firm are given by λ_n and λ_e , respectively.

3.2 Production and Preferences

Production is constant returns to scale across workers within a firm and across firms within the economy. Thus, a firm may consider the production of each of its workers independently of other workers' production. Output from a matched worker i and job j each period depends on the worker's productivity type ψ_i , a job-specific labor productivity shock x_{jt} ,

and the worker's hours h_{it} . The production function is:

$$y_i(h_{it}|x_{jt}) = \psi_i x_{jt} h_{it}^\alpha. \quad (8)$$

Labor productivity shocks x_{jt} follow a Markov process $f_x(x'|x)$, and the initial value of the labor productivity shock at the start of a job is drawn from a distribution F_0 . These shocks are job-specific and uncorrelated with shocks at other firms and to other workers. The parameter $\alpha \in (0, 1]$ measures the elasticity of production with respect to hours. If there are diminishing returns to hours in production (i.e. $\alpha < 1$), output at a fixed labor productivity shock x_{jt} would be maximized by smoothing hours across periods. When the labor productivity shock varies over time, however, the total expected production from the worker can be increased by shifting hours from low productivity periods to high productivity periods.

The flow utility to the worker each period depends upon her consumption c_{it} , hours h_{it} , preference type θ_i , and worker-specific leisure preference shock ϕ_{it} . Preferences are additively separable in consumption and hours and are represented by the utility function:

$$u_i(c_{it}, h_{it}|\phi_{it}) = \frac{c_{it}^{1-\tau} - 1}{1-\tau} - \theta_i \phi_{it} \frac{h_{it}^{1+\gamma}}{1+\gamma}. \quad (9)$$

Leisure preference shocks follow a Markov process $f_\phi(\phi'|\phi)$. These shocks are specific to a worker and will follow her across firms and into non-employment. The parameter $\gamma > 0$ captures the increasing marginal disutility from additional hours of work at a fixed leisure preference level ϕ_{it} . Although the worker would prefer to smooth her hours at a fixed ϕ_{it} , her total expected value from the job will increase if hours of work are shifted from high leisure preference shock periods to low leisure preference shock periods.

The parameter $\tau > 0$ measures the worker's desire to smooth her consumption across time. I assume that the worker lacks access to any financial instruments such as savings and borrowing, so the worker will be hand-to-mouth and consume her labor earnings e_{it} when employed.⁶ When non-employed, the worker has zero hours of work and receives consumption b from home production that is common to all workers. Risk-aversion plus a lack of financial markets means that the worker would accept a reduction in her total expected earnings for a sufficiently large reduction in the variability of her earnings. In contrast to the worker, firms are risk-neutral and desire only to maximize their total expected profits from the match with

⁶Adding savings to the model substantially complicates the solution. With incomplete asset markets, workers will still demand to receive some insurance from their firms against shocks in addition to self-insuring themselves against changes in their earnings. Recent work by [Souchier \[2022\]](#) finds that self-insurance through asset markets partially crowds out insurance provided by firms in implicit contracts.

the worker. Risk-neutrality implies that the firm would accept an increase in profit variability within the match in exchange for an increase in total expected profits from the match. Thus, there is an opportunity for mutually beneficial trade under an implicit contract.

3.3 Implicit Contracts and Limited Commitment

Consider a worker i starting a job j at a time normalized to zero. In what follows, I drop the i and j subscripts for readability. The worker's leisure preference shock ϕ_t and the job's labor productivity shock x_t are observed by both the firm and worker each period prior to the choice of earnings and hours. Additionally, if the worker successfully contacts a new firm by searching in the frictional labor market, the labor productivity shock that she draws at this new firm \hat{x}_t is observed by both herself and the current firm prior to decisions. If the worker is unsuccessful in search, then $\hat{x}_t = \emptyset$ and her only outside option is non-employment. Let $\eta_t = \{\phi_t, x_t, \hat{x}_t\}$ be the current state variables, and let $\eta^t = \{\eta_0, \dots, \eta_t\}$ be the history of shocks up through period t . Because the state of the world η_t is observed by both the firm and worker, it is possible to write an implicit contract \mathcal{C} where labor earnings $e_t(\eta^t)$, hours of work $h_t(\eta^t)$, flow profits $\pi_t(\eta^t)$, and dissolution $d_t(\eta^t)$ are time-specific functions of the history of states η^t :

$$\mathcal{C} = \{e_t(\eta^t), h_t(\eta^t), \pi_t(\eta^t), d_t(\eta^t)\}_{t=0}^{\infty}. \quad (10)$$

For readability in what follows, I omit the functional argument for the decision variables.

Both the firm and worker can each unilaterally dissolve the contract at any time for an outside option. The firm's outside option is to fire the worker and receive a terminal value of zero from the job. Define $W_i^*(\phi, x)$ to be the highest value that a firm can offer a worker i with leisure preference shock ϕ and labor productivity shock is x while the firm earns non-negative total expected profits. The worker's outside option each period depends on whether she contacts a new firm in the frictional labor market and the labor productivity shock \hat{x} that she draws at this new firm. Define $\hat{W}(\phi, \hat{x})$ to be the value of the worker's best outside option:

$$\hat{W}_i(\phi, \hat{x}) = \max\{N_i(\phi), W_i^*(\phi, \hat{x})\}. \quad (11)$$

Here, $N_i(\phi)$ is the value of non-employment to the worker with leisure preference shock ϕ , and $W^*(\phi, \hat{x})$ is the maximum value that the new firm would be willing to offer the worker. When the worker does not contact a new firm in search so $\hat{x} = \emptyset$, then the maximum value that she can receive from an outside option firm $W^*(\phi, \emptyset) = \emptyset$. Because the firm and worker can unilaterally dissolve the contract, it will be constrained by limited commitment and must be self-enforcing as in [Thomas and Worrall \[1988\]](#). If either the firm or worker decides to dissolve the contract, they lose contact and cannot form a new match with each other in

future periods.⁷ The ability of the firm to freely dissolve the contract is consistent with at will employment laws in all of the United States except Montana. For the worker, the freedom to dissolve the contract for an outside option firm is consistent with a lack of cumbersome non-compete clauses. When the match is dissolved by either party, the firm receives its outside option value of zero. In contrast, the worker either receives the non-employment value or bargains a new contract with her new firm. Define $\mathcal{B}^W(\phi, x, \hat{x})$ to be the value that the worker can bargain with her new firm if the match is dissolved as described in the next section.

3.4 Contract Negotiation and a Recursive Formulation

The firm and worker cooperatively bargain the implicit contract \mathcal{C} in order to maximize the product of their surplus values (Nash [1953]). Define $W(\mathcal{C}, \eta_0)$ and $J(\mathcal{C}, \eta_0)$ to be the values that worker and firm receive from contract \mathcal{C} . The cooperatively bargained contract solves:

$$\max_{\mathcal{C}} \left(W(\mathcal{C}, \eta_0) - \hat{W}_0 \right) J(\mathcal{C}, \eta_0), \quad (12)$$

subject to

1. Budget constraint:

$$e_t + \pi_t = y(h_t | x_t). \quad (13)$$

2. Firm's commitment constraint:

$$(1 - d_t) \left(\pi_t + \mathbf{E} \left[\sum_{k=1}^{\infty} \beta^k (1 - D_{t+k}) (1 - d_{t+k}) \pi_{t+k} \mid \eta^t \right] \right) \geq 0. \quad (14)$$

3. Worker's commitment constraint:

$$(1 - d_t) \left(u(e_t, h_t | \phi_t) + \mathbf{E} \left[\sum_{k=1}^{\infty} \beta^k \{ (1 - D_{t+k}) (1 - d_{t+k}) u(e_{t+k}, h_{t+k} | \phi_{t+k}) + (1 - D_{t+k}) d_{t+k} \mathcal{B}_{t+k}^W \} \mid \eta^t \right] \right) \geq (1 - d_t) \hat{W}_t. \quad (15)$$

Here, $D_t = \max\{d_k\}_{k=0}^{t-1}$ tracks whether either the firm or worker dissolves the contract prior to period t . Earnings for the worker will certainly be positive because of the functional form assumption for utility, but the flow profits to the firm π_t could be negative as long as the

⁷Empirically, however, Fujita and Moscarini [2017] show that recall is in fact common for the unemployed in the SIPP, where 40% of unemployment spells end in a recall to the previous employer. Most of these recalls are not for workers who report being on temporary layoff.

total expected profits in future periods are sufficiently positive as captured by the firm's commitment constraint. Similarly, the worker must receive a total expected value at each point in time that is weakly greater than her outside option value \hat{W}_t .

Although the optimal contract consists of an infinitely large set of functions that each depends on a set of arguments that grows ever larger over time, it is possible to recursively solve for the optimal contract decisions using the ideas of [Marcet and Marimon \[2019\]](#). As described in the following proposition, the optimal contract problem can be written as a recursive saddle point problem where decisions in period t depend not on the full history of states η^t but only the current state η_t and the previous periods earnings e_{t-1} .

Proposition 1. In any Pareto efficient contract, the following conditions are satisfied:

1. For all states of the world $\eta_t = (\phi_t, x_t, \hat{x}_t)$, there exists a lower bound on earnings $e_{\min}(\eta_t)$ and upper bound on earnings $e_{\max}(\eta_t)$.
2. The optimal decision in period t are:
 - (a) The match dissolves if $e_{\max}(\eta_t) < e_{\min}(\eta_t)$:

$$d_t = \begin{cases} 1 & \text{if } e_{\max}(\eta_t) < e_{\min}(\eta_t), \\ 0 & \text{if } e_{\max}(\eta_t) \geq e_{\min}(\eta_t). \end{cases} \quad (16)$$

- (b) For all $t > 0$ when $d_t = 0$, earnings e_t are set according to:

$$e_t = \begin{cases} e_{\min}(\eta_t) & \text{if } e_{t-1} < e_{\min}(\eta_t), \\ e_{t-1} & \text{if } e_{\max}(\eta_t) \geq e_{t-1} \geq e_{\min}(\eta_t), \\ e_{\max}(\eta_t) & \text{if } e_{\max}(\eta_t) < e_{t-1}. \end{cases} \quad (17)$$

- (c) For all $t \geq 0$ when $d_t = 0$, hours h_t are set according to:

$$h_t = \left(e_t^{-\tau} \alpha \frac{\psi_i x_t}{\theta_i \phi_t} \right)^{\frac{1}{1-\alpha+\gamma}}. \quad (18)$$

Proof: Appendix

In this proposition, the lower bound on earnings $e_{\min}(\eta_t)$ represents the lowest earnings that the contract must promise the worker in order to provide her value \hat{W}_t . Similarly, the upper bound on earnings $e_{\max}(\eta_t)$ represents the highest earnings that the contract can provide the worker while the firm receives non-negative total expected profits. If the

lower bound on earnings is greater than the upper bound on earnings for a given state η_t , the firm's and worker's commitment constraints cannot be satisfied simultaneously, so they must separate; this is captured in equation 16. Otherwise, the contract will attempt to pay the worker the same earnings as the prior period; this is because the worker is risk-averse while the firm is risk-neutral, so an optimal risk-sharing agreement provides smooth earnings payments to the worker. When a change in state variables causes a binding commitment constraint at the previous earnings level, however, the contract adjusts the worker's earnings by as little as possible to satisfy the constraint. This adjustment impacts the worker's earnings not only today but also in future periods so long as commitment constraints do not bind. Although earnings for the worker will be smoothed across time, hours will adjust in response to shocks to labor productivity x_t and leisure preference shocks ϕ_t . This is because correlating hours with productivity shocks increases the total expected output from the match, and correlating hours with leisure preference shocks increases the total expected value of the worker. When a commitment constraint binds, however, the contract optimally adjusts the worker's hours as well as her earnings to satisfy the constraint; this is captured by hours in period t depending upon earnings e_t in period t .

This proposition provides a recursive formulation of the values provided by the contract at all histories depending on earnings in the previous period and the current state of the world. We can define $J(e_{-1}, \phi, x, \hat{x})$ and $W(e, \phi, x, \hat{x})$ to be value functions for the firm and the worker based on the previous earnings e_{-1} and current state of the world:

$$J(e_{-1}, \phi, x, \hat{x}) = (1 - d) \left(\pi + \beta \int_{x'} \int_{\phi'} (1 - \lambda_e) J(e, \phi', x') \right. \\ \left. + \lambda_e \left(\int_{\hat{x}'} J(e, \phi', x', \hat{x}') dF_0(\hat{x}') \right) dF_x(x'|x) dF_\phi(\phi'|\phi) \right), \quad (19)$$

$$W(e_{-1}, \phi, x, \hat{x}) = (1 - d) \left(u(e, h|\phi) + \beta \int_{x'} \int_{\phi'} (1 - \lambda_e) W(e, \phi', x') \right. \\ \left. + \lambda_e \left(\int_{\hat{x}'} W(e, \phi', x', \hat{x}') dF_0(\hat{x}') \right) dF_x(x'|x) dF_\phi(\phi'|\phi) \right) + d\mathcal{B}^W(\phi, x, \hat{x}). \quad (20)$$

Here, decisions for dissolution d , earnings e , and hours h depend on the current leisure preference and labor productivity shocks $\{\phi, x, \hat{x}\}$ as well as the previous period's earnings e_{-1} as given in the Proposition 1.

Because the chosen contract maximizes the product of the firm and worker surplus, they

will certainly agree to a contract that is Pareto efficient. This means that there are no feasible contracts that can make the firm better off without making the worker worse off and vice versa. The above proposition casts the Pareto frontier in terms of the worker's initial earnings e_0 , which will be decided to maximize the product of the firm's and worker's surplus:

$$e_0(\phi, x, \hat{x}) = \arg \max_e \left(W(e, \phi, x, \hat{x}) - \hat{W}(\phi, \hat{x}) \right) J(e, \phi, x, \hat{x}) \quad (21)$$

Thus, solving for the optimal contract amounts to solving for the initial earnings level e_0 that maximizes the product of the surplus values received by the firm and worker. The value that the worker receives from unemployment with leisure preference shock ϕ is then given by:

$$N(\phi) = u(b, 0|\phi) + \beta \int_{\phi'} \left\{ \lambda_n \left(\int_{x'} W(e_0, \phi', x', \emptyset) dF_0(x') \right) + (1 - \lambda_n) N(\phi') \right\} dF_\phi(\phi'|\phi) \quad (22)$$

Here, the earnings e_0 that the worker receives when finding a job next period depends on the labor productivity shock x' that she draws from F_0 as well her leisure preference shock ϕ' and is determined by the problem in equation 21.

Finally, the value that the worker receives when the match dissolves \mathcal{B}^W is given by:

$$\mathcal{B}^W(\phi, x, \hat{x}) = \max\{N(\phi), \quad W(e_0(\phi, \hat{x}, \emptyset), \hat{x}, \emptyset), \quad W(e_0(\phi, \hat{x}, x), \hat{x}, x)\} \quad (23)$$

The first term in the maximization set represents the scenario when either the worker does not meet a new firm in the frictional labor market so $\hat{x} = \emptyset$ or the labor productivity shock at the new firm \hat{x} is so low that the worker would prefer non-employment. The second term represents the scenario when the worker meets a new firm in the labor market that is superior to non-employment, but the labor productivity shock at her current firm x is so low that the worker would prefer non-employment. In this case, it is optimal for the worker to bargain against non-employment as her outside option. The final case represents the scenario where she meets a new firm and both the labor productivity shock at her current firm x and the labor productivity shock at the new firm \hat{x} are sufficiently high that the worker would prefer each firm to non-employment. In this case, the worker will use her current firm's labor productivity shock x when bargaining with the new firm with labor productivity shock \hat{x} .

3.5 Characterizing Risk-Sharing and Limited Commitment

The worker's hours are optimally set each period such that the worker's marginal rate of substitution of earnings for hours is equal to the marginal rate of transformation of hours

into production:

$$\frac{u_e(e, h|\phi)}{u_h(e, h|\phi)} = y_h(h|x) \quad (24)$$

The marginal rate of transformation can also be thought of as the firm's marginal rate of substitution of earnings for hours where the firm's utility function is defined based on the budget constraint $\pi = y - e$. Note that the specific functional equations for utility and production are not necessary in order for an optimal implicit contract to exist. They are necessary, however, to easily characterize how hours respond to shocks in the equation.

To understand how risk-sharing and limited commitment influence the variation in earnings and hours, it is useful to consider two extreme cases: fully enforceable contracts and spot markets. With enforceable implicit contracts, the optimal contract does not need to adjust based on the firm's and worker's commitment constraints. It needs only to consider the worker's outside option value in the initial period \hat{W}_0 when setting earnings and hours as shown in the following proposition.

Proposition 2. If employment contracts were fully enforceable, then earnings are constant at all points in time in the match ($e_t(\eta^t) = e_0$), and hours are set as:

$$h_t = \left(e_0^{-\tau} \alpha \frac{\psi_i x_t}{\theta_i \phi_t} \right)^{\frac{1}{1-\alpha+\gamma}}. \quad (25)$$

Proof: Appendix.

Fully enforceable contracts mean that the contract can ignore binding commitment constraints in future periods. Earnings are set in the initial period to maximize the product of the firm's and worker's surplus values and remain constant throughout the match because the worker is risk-averse. Hours each period optimally respond to shocks to labor productivity and leisure preferences. The elasticity of the worker's hours in response to shocks in fact does not depend at all upon her risk-averse level τ but only on the elasticity of production with respect to hours α and the inverse Frisch elasticity of labor supply γ .

In the other extreme, suppose the employment contracts behave like spot market contracts where the worker chooses her own hours and was paid exactly what she produced. This would be the case if worker's outside option was always another firm with an identical labor productivity shock as her current firm. In this case, the worker would set her hours such that the marginal benefit of additional consumption from additional production was equal to marginal cost of additional hours so that:

$$h_t = \left(\alpha \frac{\psi_i^{1-\tau} x_t^{1-\tau}}{\theta_i \phi_t} \right)^{\frac{1}{1-\alpha(1-\tau)+\gamma}}, \quad \text{and} \quad e_t = \psi_i x_t h_t^\alpha. \quad (26)$$

Here, we see that the elasticity of hours with respect to shocks is smaller when workers set their own hours and consume their production compared to the implicit contracting model because $\tau > 0$. Because hours variation will affect her consumption, the risk-averse worker attenuates the variability of her hours in response to shocks.

The variability of earnings and hours under implicit contracts constrained by limited commitment sits somewhere between these two extremes depending on the quality of the worker’s outside option. If the worker has a better outside option, then it will be more likely that the firm’s and worker’s commitment constraints will bind and require a change in earnings to maintain the match. Figure 1 shows how the contract behaves in response to an increase in the job’s labor productivity shock. If the contract was fully enforceable, then the contract increases the worker’s hours without any increase in her earnings. Although the worker is worse off during the high productivity period because she receives no compensation for her additional hours, the firm benefits by taking the additional production as additional profits. The converse would happen in response to a negative labor productivity shock. Although either the firm or worker is worse off ex-post, they both benefit ex-ante from the risk-sharing agreement. However, if the worker had a better outside option, then she could threaten to separate from the firm because her hours are too high and earnings too low. Wanting to retain its worker, the firm increases the worker’s earnings and reduces her hours to match her outside option value. Because the worker is risk-averse and has increasing marginal disutility of hours, the firm adjusts her earnings and hours not only during the period with high productivity but also in future periods to smooth these changes over time. These future promises allow the firm to optimally take advantage of the variation in productivity while providing value to the worker.

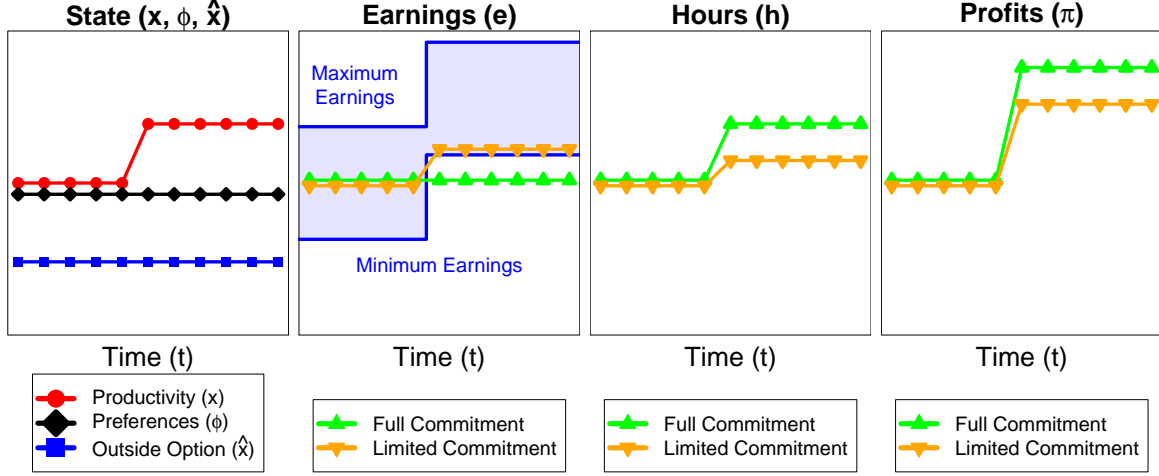
4 Estimation

In order to understand the sources of hours variation and create an environment for counterfactual analysis, this section estimates the model to match the dynamics of earnings, hours, and job mobility in the SIPP.

4.1 Externally Set Parameters

The length of a period is assumed to be four months as in the SIPP. I set workers’ relative risk-aversion in consumption τ to approach one, so they have logarithmic utility in consumption. This is on the lower end of estimates in the literature for risk-aversion (Layard et al. [2008]). However, because I do not allow workers to save, their desire to smooth earnings across

Figure 1: Impulse Response Functions



Note: This figure shows how earnings, hours, and profits respond in the model to an increase in labor productivity under full and limited commitment.

periods will be lower than if workers were able to save. I set the inverse of the Frisch elasticity γ equal to 4 based on the meta-analysis conducted by [Elminejad et al. \[2023\]](#), and I set the discount rate $\beta = 0.99$ for the four-month period, which implies an annual interest rate of 3.1%.

Table 6: Externally Set Parameters

	Value
Discrete Period Length	Four Months
Coefficient of Relative Risk-Aversion (τ)	$\rightarrow 1$
Inverse Frisch Elasticity (γ)	4.0
Discount Factor (β)	0.99

Note: This table shows the values of the parameters set outside of estimation as described in Section 4.1.

4.2 Parameterization and Identification

The model allows for permanent differences in individuals' productivity ψ_i and preferences for leisure θ_i that are jointly distributed according to $F_{\psi\theta}$. Because the model must be solved separately for each worker type i , I assume there are only nine types of workers in the economy for computational reasons. The distribution $F_{\psi\theta}$ is assumed to be a nine-point

Gauss-Hermite approximation of a joint log-normal distribution.⁸

$$\begin{bmatrix} \log(\psi_i) \\ \log(\theta_i) \end{bmatrix} \sim \mathcal{N} \left(\begin{bmatrix} \mu_\psi \\ \mu_\theta \end{bmatrix}, \begin{bmatrix} \sigma_\psi^2 & \rho_{\psi\theta}\sigma_\psi\sigma_\theta \\ \rho_{\psi\theta}\sigma_\psi\sigma_\theta & \sigma_\theta^2 \end{bmatrix} \right) \quad (27)$$

This yields five parameters to be estimated underlying the distribution of worker types $(\mu_\psi, \mu_\theta, \sigma_\psi, \sigma_\theta, \rho_{\psi\theta})$. Because I use only nine-points, this will not be a good approximation of the joint normal distribution. However, it allows for permanent differences in worker types to influence the distribution of earnings and hours. In order to estimate these parameters, I target the first and second order moments from the cross-sectional distribution of earnings and hours.

The Markov processes for preferences f_ϕ and job-specific labor productivity f_x are assumed to follow a logarithmic autoregressive process of order one with a normally distributed stochastic term:

$$x_{t+1} = \rho_x x_t + \epsilon_{x,t} \quad \epsilon_{x,t} \sim \mathcal{N}(0, \sigma_x^2), \quad (28)$$

$$\phi_{t+1} = \rho_\phi \phi_t + \epsilon_{\phi,t} \quad \epsilon_{\phi,t} \sim \mathcal{N}(0, \sigma_\phi^2). \quad (29)$$

Computationally, I approximate these distributions as a discrete Markov process with five states using the method proposed by [Rouwenhorst \[1995\]](#). Relative to other methods, Rouwenhorst's method is more accurate in approximating an autoregressive process even when the persistence parameters are relatively high ([Kopecky and Suen \[2010\]](#)). In order to estimate the parameters $(\rho_x, \sigma_x, \rho_\phi, \sigma_\phi)$, I target the variability and persistence of changes in earnings and hours.

As shown in Proposition 1, when either productivity or preferences change, the optimal implicit contract will adjust the worker's hours in response. Thus, separately identifying the shock processes is challenging. However, I argue that productivity shocks should have a larger impact on the variability of worker's earnings than preference shocks.⁹ This is because a preference shock impacts output only via a change in hours, while a productivity shock will impact output both through changes in hours and through the change in productivity. Be-

⁸This is the same as how [Fan et al. \[2024\]](#) model individual heterogeneity in ability to learn and tastes for leisure.

⁹A formal proof of identification could proceed similarly to the proof in [Balke and Lamadon \[2022\]](#). In their model of earnings dynamics in implicit contracts, workers experience changes in labor productivity that affect only their own output, and firms experience changes in labor productivity that affect the output of all workers at the firm. They show that five periods of data on a worker's earnings and her co-worker's earnings can non-parametrically identify the latent Markov process in firm and worker labor productivity. In my model, workers experience changes in their match specific labor productivity and their leisure preferences, and five periods of data on earnings and hours provide two variables to identify the two shocks. I leave a more formal proof for future work.

cause productivity shocks have a larger effect on output, it should be more difficult for firms to provide insurance against them as a result of limited commitment. Thus, productivity shocks should lead to more earnings volatility. Additionally, workers can escape bad job-specific labor productivity shocks by switching firms or switching to non-employment, so the job-specific labor productivity shock only affects the value of the current match. However, a leisure preference shock follows the worker into non-employment and to other firms, so it will impact both the current match and the worker's outside option values in similar ways. This allows for the contract to provide more insurance against preference shocks compared to productivity shocks, so preference shocks should cause less earnings variability compared to productivity shocks.

The probabilities that workers contact new firms when non-employed or employed in the model are given by λ_n and λ_e , respectively. In order to estimate these parameters, I target the fraction of employed workers who switch to a new firm (EE-rate) and the fraction of non-employed workers who become employed in the following period (NE-rate). In order to match the fraction of employed workers who become non-employed (NE-rate), I additionally include a probability δ that job-specific labor productivity enters an absorbing state of zero. When this happens, the firm and worker will certainly separate because the match will never be productive again. However, workers may transition to non-employment because of a high leisure preference shock or low labor productivity shock as well.

When workers contact a new firm when searching in the labor market, they draw an initial job-specific labor productivity \hat{x} from a distribution F_x . Computationally, the job-specific labor productivity can only take a finite number of values from the Rouwenhorst approximation with $N_x = 5$ points. I assume that the index of initial labor productivity is drawn from a truncated geometric distribution with probability p_x :

$$\mathbf{P}(\text{index}(\hat{x}) = j) = \frac{p_x(1 - p_x)^j}{1 - (1 - p_x)^{N_x}}. \quad (30)$$

The probability p_x determines the leftward shift in the distribution of initial labor productivity. In the limit as p_x approaches one, then the worker will start at the lowest level of labor productivity with probability one. As p_x decreases, then the worker is more likely to start at a higher level of labor productivity. If $p_x = 0$, then the distribution of initial labor productivity is evenly distributed across the N_x productivity states. In order to estimate this parameter, I target average difference of earnings for workers who enter into non-employment next period compared to workers who just exited non-employment. For higher values of p_x , workers will have more match productivity growth over an employment spell, and thus have more earnings growth over a typical employment spell.

The final two parameters in the contracting model are the value of home production b that workers consume when non-employed and the returns to hours in production α . A larger value of home production b will result in a larger value of non-employment, and thus will lead to workers being able to bargain for higher earnings when they exit non-employment. If b is lower, then workers will exit non-employment with lower earnings. If b is higher, workers will exit non-employment with higher earnings. Thus, I target the difference between the average earnings of workers who just exited non-employment compared to average earnings of all workers. Returns to hours in production α measures how changes in hours affect changes in output, and should be closely related to the elasticity of earnings with respect to hours. Thus, I target the covariance of changes in earnings and hours empirically.

In addition to the parameters in the structural model, I also allow for earnings and hours reported in the SIPP to contain measurement error ξ that is classical in logs with respect to true earnings and hours:

$$\log(\text{earnings}_{it}^{\text{report}}) = \log(\text{earnings}_{it}^{\text{true}}) + \xi_{iet}, \quad (31)$$

$$\log(\text{hours}_{it}^{\text{report}}) = \log(\text{hours}_{it}^{\text{true}}) + \xi_{iht}. \quad (32)$$

The measurement errors (ξ_{iet}, ξ_{iht}) each have mean zero, variances of $(\sigma_{\xi_e}^2, \sigma_{\xi_h}^2)$, and are uncorrelated with the true values of earnings and hours. Additionally, they are serially uncorrelated across time and with each other. In order to estimate these parameters, I target the auto-covariance of earnings and hours across four periods. As I show in Appendix C.1, it is necessary to target the auto-covariance over four periods to identify a permanent, persistent, and transitory component of an observed stochastic process. Additionally, I target the covariance of the change in earnings experienced over four periods t to $t + 3$ with the change in hours experienced over the inner two periods $t + 1$ to $t + 2$. As explained in Section 2.1, this covariance should not be impacted by transitory changes such as measurement error, so should help disentangle transitory measurement error from true changes in earnings and hours.

4.3 Estimation Procedure and Results

There are 17 parameters χ to be estimated:

$$\chi = \{\mu_\psi, \sigma_\psi, \mu_\theta, \sigma_\theta, \rho_{\psi\theta}, \quad \rho_x, \sigma_x, \quad \rho_\phi, \sigma_\phi, \quad \lambda_n, \lambda_e, \delta, p_x \quad b, \alpha \quad \sigma_{\xi_e}, \sigma_{\xi_h}, \}. \quad (33)$$

I estimate the model by simulated method of moments to select the parameters χ to minimize the distance between moments simulated by the model M_{sim} and corresponding moments

measured in the data M_{data} with a weight matrix W :

$$\chi^* = \arg \min_{\chi} (M_{\text{sim}}(\chi) - M_{\text{data}})'W(M_{\text{sim}}(\chi) - M_{\text{data}}). \quad (34)$$

I set the weight matrix to have diagonal terms equal to the absolute value of the inverse of the data moments and to have off-diagonal terms equal to zero. The optimization proceeds by differential evolution ([Storn and Price \[1997\]](#)).

Table 7: Estimation Results

Parameter	Estimate
1. Mean Productivity Type (μ_{ψ})	1.880
2. S.D. Productivity Type (σ_{ψ})	0.860
3. Mean Preference Type (μ_{θ})	-17.989
4. S.D. Preference Type (σ_{θ})	1.469
5. Corr. Productivity and Preference Type ($\rho_{\psi\theta}$)	0.589
6. Auto-Corr. Productivity Shock (ρ_x)	0.237
7. S.D. Productivity Shock (σ_x)	0.216
8. Auto-Corr. Preference Shock (ρ_{ϕ})	0.007
9. S.D. Preference Shock (σ_{ϕ})	0.432
10. Non-employed Job Finding Rate (λ_n)	0.982
11. Employed Job Finding Rate (λ_e)	0.250
12. Exogenous Job Destruction Rate (δ_x)	0.028
13. Distribution of Initial Labor Productivity (p_x)	0.317
14. Non-employed home production ($\log b$)	5.260
15. Production Returns to Hours (α)	0.983
16. S.D. Meas. Error for Earnings (σ_{ξ_e})	0.272
17. S.D. Meas. Error for Hours (σ_{ξ_h})	0.009

Note: This table shows the parameters estimated by simulated method of moments as described in [Section 4.2](#).

Results of the estimation are shown in [Table 7](#), and the model fit is shown in [Table 8](#). The model is broadly able to match the first and second moments of the cross-sectional distribution of earnings and hours relatively well even with only nine individual types. While the model matches the EE- and EN-rates relatively well, it underestimates the NE-rate by 0.041 p.p. This leads the non-employment rate in the model economy (0.724) to be 6.4 percentage points higher than in the data (0.788). However, the estimated probability that workers are able to contact a firm λ_n is estimated to be near one, so there is little room for

Table 8: Model Fit

	Moment	Model	Data
1.	$\mathbf{E}[\log e_{it}]$	6.284	6.276
2.	$\mathbf{E}[\log h_{it}]$	3.626	3.665
3.	$\text{var}(\log e_{it})$	0.650	0.642
4.	$\text{var}(\log h_{it})$	0.089	0.100
5.	$\text{cov}(\log e_{it}, \log h_{it})$	0.118	0.125
6.	EE Rate	0.054	0.052
7.	EN Rate	0.048	0.045
8.	NE Rate	0.126	0.167
9.	$\text{var}(\Delta \log e_{it})$	0.191	0.198
10.	$\text{cov}(\Delta \log e_{it}, \Delta \log e_{it+1})$	-0.084	-0.074
11.	$\text{var}(\Delta \log h_{it})$	0.068	0.050
12.	$\text{cov}(\Delta \log h_{it}, \Delta \log h_{it+1})$	-0.030	-0.019
13.	$\text{cov}(\Delta \log e_{it}, \Delta \log h_{it})$	0.019	0.019
14.	$\text{cov}(\log e_{it}, \log e_{it+3})$	0.545	0.463
15.	$\text{cov}(\log h_{it}, \log h_{it+3})$	0.047	0.048
16.	$\text{cov}(\log e_{it+3} - \log e_{it}, \log h_{it+2} - \log h_{it+1})$	0.006	0.004
17.	$\mathbf{E}[\log e_{it} \text{NE}] - \mathbf{E}[\log e_{it}]$	-0.342	-0.609
18.	$\mathbf{E}[\log e_{it} \text{EN}] - \mathbf{E}[\log e_{it} \text{NE}]$	0.095	0.098

Note: This table shows the value of the parameters estimated by simulated method of moments as described in section 4.2. The variable h_{it} is the usual hours of work per week for individual i at time t , and e_{it} is weekly earnings in dollars adjusted to 2001 levels using the PCE.

increasing this parameter to increase the NE-rate. Although non-employed workers almost always have an option to work at a firm, the labor productivity that they draw at these firms are low enough that non-employment is preferable to the highest value firms would be willing to offer. Increasing the NE-rate would require workers to draw higher initial labor productivity when contacting firms. However, this would lead to higher earnings for workers exiting non-employment, which are already relatively high in the estimated model compared to the data. Thus, there is a tension between the accurately matching the NE-rate and the earnings for workers exiting non-employment. This is possibly because of the coarse five-point grid assumed for the distribution of labor productivity as well as the functional form assumption for the initial labor productivity draws in equation 30. In future work, I hope

to improve upon these estimates by considering different distributions for the initial labor productivity draws.

Although the NE-rate in the data and the estimated model is about 4.5%, the exogenous job destruction rate δ is only 2.8%. Thus, about 40% of separation to non-employment happen endogenously as a result of the labor productivity shocks x and the leisure preference shocks ϕ .

The variability and persistence of changes in earnings and hours in the model and the data match well. Interestingly, the estimate for the job-specific labor productivity shock process of 0.237 is low relative to most estimates in the literature. This is likely because of the high volatility of earnings observed in the SIPP from across surveys that is highly correlated with hours. In order to rationalize this volatility, the model requires a volatile productivity shock process. [Balke and Lamadon \[2022\]](#) and [Souchier \[2022\]](#) estimate persistence of productivity to be greater than 0.9. However, a greater persistence in productivity would lead to a lower volatility of earnings in the model than observed in the SIPP data.

The non-employed home production b is roughly 40% of average earnings for workers. This is consistent with estimates from previous literature looking at the change in earnings for workers entering non-employment in the SIPP and PSID ([Rothstein and Valletta \[2017\]](#), [Braxton et al. \[2024\]](#)). The returns to hours in production α is estimated to be close to 0.983, which is much higher than previous estimates using data on relationship between earnings and hours ([Yurdagul \[2017\]](#), [Bick et al. \[2022\]](#), [Shao et al. \[2023\]](#)). In the model, the observed relationship between earnings and hours is less than the underlying relationship between output and hours as a result of insurance in the implicit employment contract. When shocks to productivity or preferences lead to an increase in hours, the optimal risk-sharing agreement will provide smooth earnings payments to the worker while leading to a lower elasticity of earnings with respect to hours compared to the elasticity of output with respect to hours.

The estimates for the measurement error suggest that roughly 11.4% of variance of earnings is measurement error, while less than one percent of the variance of hours is measurement error. Empirically, there is much variability for earnings that is uncorrelated with changes in hours, and the model partly interprets this as measurement error. When linking SIPP earnings records to tax records, [Gottschalk and Huynh \[2010\]](#) finds that the variance of measurement error to be 27% of the total variance of earnings. However, they also report that much of the measurement error in the SIPP is mean reverting, and the variance of earnings in the SIPP is in fact lower than the variance of earnings in tax records. Similarly, [Bound et al. \[2001\]](#) report that much of the measurement error in survey data is mean reverting. Because the model does not allow for mean reverting measurement error, it likely understates

the true importance of measurement error. Future work should consider how incorporating a mean reverting component to measurement error impacts the results of the estimation.

4.4 Elasticity of Earnings with Respect to Hours by Earnings

In addition to matching the overall dynamics of earnings and hours in the data as shown in Table 8, the model is also able to match how the elasticity of earnings with respect to hours differs for low and high earning workers as shown in Table 9. Low earners are defined to be workers with below average logarithmic earnings, while high earners have above average logarithmic earnings. In the data, low earners have a higher elasticity of earnings with respect to hours of 0.382 compared to high earners, whose elasticity is only 0.160. This reflects the fact that low earners are more likely to be paid by the hour compared to high earners. 72.1% of low earners are paid by the hour, while only 36.3% of high earners are paid by the hour.

In the estimated model, low earners also have a higher elasticity of earnings with respect to hours of 0.326 compared to high earners, whose elasticity is 0.212. While the estimated model does not have a concept of hourly and non-hourly jobs, the model is able to understand this difference in the elasticity across the earnings distribution as a result of differences in risk-sharing under limited commitment. Workers with higher permanent labor productivity types ψ_i or lower permanent leisure preference types θ_i will tend to be in the higher earnings group. Additionally, they view the option of non-employment as relatively less valuable compared to workers with lower permanent labor productivity types or higher permanent leisure preference types because all workers receive the same home production consumption b . Thus, they are less likely to hit their commitment constraint as a result of increases in hours in response to a shock, so their earnings remain more stable. Similarly, firms earn higher profits from these high permanent productivity type or low permanent leisure preference type workers, so they are less likely to hit their commitment constraint as a result of decreases in hours in response to a shock. This can be seen from the fact in Table 9 that low earners are more likely to transition to non-employment next period.¹⁰ This shows that implicit contracts under limited commitment can generate differences in the elasticity of earnings with respect to hours across the earnings distribution similar to that in the data even without having explicit hourly and non-hourly jobs.

¹⁰However, the model generates a significantly higher probability of transitioning to non-employment compared to the data for low earners. This could arise from the relatively coarse nine-point discrete distribution of permanent types in the model. A more flexible distribution of permanent types could help match the differential in the probability of transitioning to non-employment.

Table 9: Statistics from Model and Data by Earnings Level

	(1) Low Earners Model	(2) Data	(3) High Earners Model	(4) Data
Elasticity of Earnings w.r.t. Hours	0.326	0.382	0.212	0.160
Probability of New Job Next Period	0.051	0.066	0.054	0.040
Probability of Non-employed Next Period	0.165	0.062	0.030	0.023
Paid by the Hour	–	0.721	–	0.363

Note: This table shows the elasticity of earnings with respect to hours for firm stayers, the probability of moving to a new job next period, the probability of being non-employed next period, and the fraction of workers paid by the hour in the simulated model and the SIPP data. Workers are split into groups based on whether they have above average or below average earnings. Observations in the SIPP data are weighted using longitudinal weights.

4.5 The Elasticity of Earnings with respect to Hours and Turnover

In the data, workers who are paid by the hour have higher probabilities of leaving their jobs either to move to a new firm or to move to non-employment as shown in Table 5. In the model, I show that when increasing the probability that workers leave their jobs, the elasticity of earnings with respect to hours increases. To do this, I separately adjust the probability employed workers contact a new firm λ_e and the probability that workers are exogenously sent to non-employment δ while holding all other parameters fixed. Then I solve for the optimal contract choices with the adjusted parameter and simulate a new steady state distribution of workers. The average elasticity of earnings with respect to hours for changes in λ_e and δ are shown in Figure 2. For higher values of λ_e or δ workers will be more likely to leave their jobs. This also leads to a higher probability that commitment constrains risk-sharing in the contract. For higher values of λ_e , workers are more likely to have good options at other firms and threaten to quit their jobs if their hours are increased without increases in earnings. Additionally, as workers are more likely to leave their jobs when λ_e or δ increase, firms are less willing to take on negative flow profits today because they are less likely to recoup these losses in future periods. Thus, firms are more likely to threaten to fire workers when hours are reduced without a reduction in earnings. This increase in the extent to which commitment constraints bind leads to less risk-sharing in employment contracts and a higher elasticity of earnings with respect to hours. Thus, the model with implicit contracts and limited commitment is able to understand why workers with higher

turnover rates have higher elasticities of earnings with respect to hours.

5 Analysis

In this section, I use the estimated model to analyze the extent to which changes in labor productivity and leisure preferences pass through to worker's earnings, hours, and output as well as the implications of implicit contracts constrained by limited commitment for government policies.

5.1 Pass-through of Productivity and Preference Shocks

As shown in proposition 2, if both firms and workers could fully commit to the implicit contract, earnings would be constant e_{i0} for each worker i and hours h_{it} would be set as:

$$\log h_{it} = \frac{1}{1 - \alpha + \gamma} \left(\log x_{jt} + \log \phi_{it} - \tau \log e_{i0} + \log \left(\frac{\psi_i}{\theta_i} \right) + \log \alpha \right). \quad (35)$$

Here, ψ_i and θ_i are the permanent labor productivity and leisure preference types of worker i , while x_{jt} and ϕ_{it} are the job-specific labor productivity and leisure preference shocks. In the estimated model, the inverse Frisch elasticity of labor supply is set equal to 4 and the return to hours in production α is set equal to 0.983. Thus, the elasticity of hours with respect to both productivity and preference shocks under full commitment would be 0.249, and the elasticity of earnings with respect to both shocks would be zero.

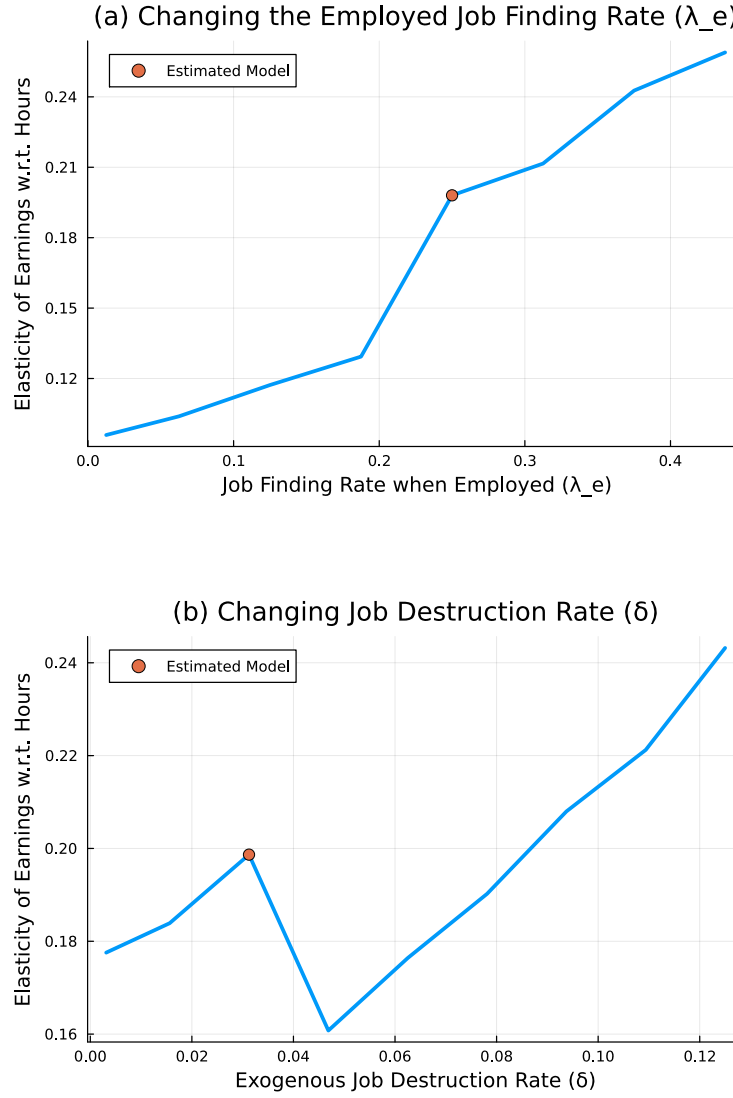
In the other extreme, if workers were able to set their own hours and were paid according to what they produced, then they would set their own hours as:

$$\log h_{it} = \frac{1}{1 - (1 - \tau)\alpha + \gamma} \left((1 - \tau) \log x_{jt} + \log \phi_{it} - \tau \log e_{i0} + \log \left(\frac{\psi_i}{\theta_i} \right) + \log \alpha \right). \quad (36)$$

Because the worker is risk-averse with coefficient of relative risk-aversion $\tau > 0$, the elasticity of hours with respect to shocks is smaller. In the estimated model, the coefficient of relative risk-aversion τ is set to one, so the elasticity of hours with respect to job-specific productivity shocks would be zero, and the elasticity of hours with respect to leisure preference shocks would be 0.333.

In the estimated model with implicit contracts constrained by limited commitment, the elasticity of hours and earnings with respect to the shocks will be somewhere between these two extremes as a result of limited commitment. The implicit contract will attempt smooth

Figure 2: Changing Search Frictions and Hours Elasticity of Earnings



Note: This figure shows how the elasticity of earnings with respect to hours within a job changes for workers when the probability of contacting a new firm λ_e or the probability of being exogenously sent to non-employment δ changes. The jagged decline for plot (b) is due to the discrete approximation of the type distribution. Once δ is high enough, the worker with the lowest permanent labor productivity and highest leisure preference type does work at low job-specific labor productivity shocks.

the workers earnings e_{it} across time and set hours h_{it} as:

$$\log h_{it} = \frac{1}{1 - \alpha + \gamma} \left(\log x_{jt} + \log \phi_{it} - \tau \log e_{it} + \log \left(\frac{\psi_i}{\theta_i} \right) + \log \alpha \right). \quad (37)$$

However, earnings will vary in response to binding commitment constraints, and this will attenuate the elasticity of hours with respect to shocks. For instance, in response to a one percent positive productivity shock, the optimal risk-sharing agreement would increase workers hours by 0.249%, while keeping their earning held constant. However, workers may threaten to quit their job if hours are now so high that they would prefer to move to their outside option. As a result of this binding commitment constraint, the worker's earnings must be increased to keep them from leaving the match, and this will result in a reduction in the worker's hours relative to the optimal risk-sharing agreement.

To understand the actual pass-through of shocks in the estimated model, I run the following regression on workers simulated from the estimated model:

$$\log(z_{it}) = \beta_i + \beta_x \log(x_{jt}) + \beta_\phi \log(\phi_{it}) + \epsilon_{it}. \quad (38)$$

Here, the outcome z_{it} is either hours, output, or earnings for worker i at time t , and β_i is a fixed effect for individual type. The estimated coefficients β_x and β_ϕ measure the elasticity of the outcome with respect to labor productivity. Results are shown in Table 10.

Workers with a one percent higher preference shock have 0.243% lower hours, 0.239% lower output, and 0.023% lower earnings. This suggests that the insurance that workers receive from firms against changes in their preferences is quite close to the case of full commitment, where a one percent change in preferences would lead to a 0.249% change in hours, a 0.245% change in output, and no change in earnings. There are several factors why firms are able to provide substantial insurance against preference shocks in the model. First, preference shocks are worker specific and will follow workers to non-employment and to other firms. This means that they impact both the value of the worker's current match and the value of the worker's outside option similarly. Thus, a preference shock is less likely to lead to a binding commitment constraint from the worker side. Additionally, the estimated persistence of preference shocks is low at 0.007. This means that for any preference shock value experienced in the current periods, workers' preferences are likely to revert to their mean value in the next period, so a change in preferences today has limited impact on the total expected production of the worker going forward. Even if the worker works less today because of high leisure preferences, it is possible that they will be willing to work longer hours next period.

Compared to preference shocks, limited commitment has a larger impact on the pass-through of job-specific productivity shocks to outcomes. Under full commitment, workers with a one percent higher job-specific labor productivity shock should have 0.249% higher hours, 1.245% higher output, and no change in earnings. However, in the estimated model as shown in Table 10, workers with a one percent higher productivity shock have 0.206% higher hours, 1.203% higher output, and 0.173% higher earnings. This suggests that the implicit contract under limited commitment is able to provide substantial insurance against productivity shocks, but not as much as against preference shocks. This is because productivity shocks do not affect the worker’s outside option value. When job-specific productivity is high, the contract must increase the worker’s earnings to respond to outside offers. Additionally, the estimated persistence of productivity shocks is 0.237, which is higher than the persistence of preference shocks. This means that a change in productivity today will have a larger impact on the total expected production of the worker going forward.

Table 10: Pass-through of Shocks to Outcomes with Limited Commitment

	(1)	(2)	(3)
Productivity Shock $\log(x)$	0.206	1.203	0.173
Preference Shock $\log(\phi)$	-0.243	-0.239	-0.023
Outcome	$\log(\text{hours})$	$\log(\text{output})$	$\log(\text{earnings})$

Note: This table show how outcomes differ for workers with different shocks to preferences and productivity in simulations of the estimated model by estimating regression coefficients for equation 38.

5.2 Variance Decomposition

The results of the previous section show how changes in shocks pass-through to workers outcomes, but they do not provide an understanding of the importance of these shocks for explaining different outcomes across workers. To understand the underlying sources of differences in earnings, hours, and output across workers, I perform a variance decomposition exercise in data simulated from the estimated model. To do this, I calculate for the regression in equation 38 the partial R-squared value for each explanatory variable: labor productivity shock x , leisure preference shock ϕ , and individual type i . The partial R-squared measures the fraction of the variance of the outcome that cannot be explained when that explanatory variable is removed from the regression. Results are shown in Table 11.

For all three outcomes, individual type i explains the largest portion of the variance. This is not surprising, because earnings and hours in the data are highly correlated across time for each individual. However, individual type explains substantially more of the variance in earnings compared to hours or output. The difference in the variance decomposition for earnings compared to output and hours arises in the model as a result of the risk-sharing in the implicit contract. Changes in labor productivity and leisure preferences result in changes in hours, but the firm insures the worker’s earnings against the resulting changes in output. Relative to leisure preference shocks, job-specific labor productivity shocks explain a larger fraction of the variance for all three outcomes. This is because the AR(1) process for job-specific labor productivity shocks is estimated to have a high variance of 0.216 and persistence of 0.237. This generates sizeable difference across in the job-specific labor productivity level.

Table 11: Partial R-Squared Variance Decomposition

	(1)	(2)	(3)
Individual Type i	0.448	0.869	0.394
Productivity Shock $\log x$	0.266	0.075	0.644
Preference Shock $\log \theta$	0.134	0.048	0.010
Outcome	$\log(\text{hours})$	$\log(\text{earnings})$	$\log(\text{output})$

Note: This table shows the partial R-squared for each outcome variable and explanatory variable in the estimated model. The partial R-squared for an explanatory variable measures the fraction of the variance for the outcome variable that cannot be explained by the other explanatory variables. The sum of partial R-squared values for a given outcome may sum to greater than 1 as a result of correlation between the explanatory variables. 4.2.

5.3 Restrictions on Hours within Contracts

In the implicit contract, hours play an important role to increase workers’ total expected output by varying hours in tandem with labor productivity shocks. To quantify the importance of this mechanism, I restrict workers hours to depend only on their own leisure preferences as in equation 26 with the coefficient of relative risk-aversion τ set to one as in the estimated model:

$$h_{it} = \left(\frac{\alpha}{\phi_{it}\theta_i} \right)^{\frac{1}{1+\gamma}}. \quad (39)$$

As part of the implicit contract, firms and workers can now only negotiate the path of earnings in response to the history of shocks and outside offers. In Table 12, I show how

workers' outcomes in steady state equilibrium of the model change when hours are restricted in this way at the estimated parameters. Although this restriction reduces the variability of workers hours by 50%, the reduction in total expected output from matches is 4.4% and the reduction in workers' average consumption is 5.2%. This drop in average consumption is large enough that workers are worse off in the hours restriction scenario. To make workers indifferent between the baseline and the hours restriction scenario, a transfer of \$12.62 per week in 2001 dollars would need to be made to all workers in each period of the hours restriction scenario. This transfer is equivalent to 2.1% of average earnings in the baseline scenario, emphasizing that hours variability in response to changes in labor productivity plays a quantitatively important role.

These results suggest that policymakers should be cautious to restrict the variability of hours in settings where firms and workers agree to implicit contracts. This is because the implicit contract optimally sets the variability of workers' hours to maximize the product of firms' total expected profits and workers' total expected values. When hours are restricted, the implicit contract is unable to optimally set hours in response to shocks, and this leads to a reduction in workers' welfare. Current government policies regulating hours such as overtime policies and maximum hours restrictions often exempt certain classes of workers, and these workers are more likely to be in implicit contracts with their firms. In the United States, for example, workers whose job duties can be classified as executive, administrative, or professional are exempt from overtime pay requirements. The median manager in the SIPP data has 6.3 years of tenure at their current firm, and the median professional has 5.4 years of tenure. For workers who are not managers or professionals, median tenure is only 4.3 years. These differences in tenure suggest that managers and professionals are more likely to be in implicit contracts with their firms and that exempting them from government policies regarding hours restrictions is beneficial. Similarly, recent predictive scheduling and fair workweek laws typically target only the hospitality and leisure industry, where median tenure in the SIPP is only 2.7 years. In all other industries, median tenure for workers is 5.1 years.

5.4 Transfers to Non-employed

In addition to government restrictions on hours, I additionally consider how government transfer to the non-employed impact risk-sharing in implicit contracts. By providing transfers to the non-employed, the government raises the value of non-employment as an outside option and increases the extent to which limited commitment constrains risk-sharing in implicit contracts. Figure 3 shows how the pass-through of shocks to workers' earnings and hours

Table 12: Impact of Restrictions on Hours within Contracts

	(1) Baseline	(2) Hours Restrictions	(3) % Change
Hours Variability ($\text{std}(\Delta \log(h))$)	0.260	0.122	-53.0%
Employment Rate	0.723	0.689	-4.7%
Output per person	614.96	588.43	-4.4%
Consumption per person	606.73	575.43	-5.2%
Profits per person	8.23	13.00	58.0%
Consumption equivalence per person	—	12.62	—

Note: This table shows how workers' outcomes in the model change when hours are restricted to depend only on workers' preferences as discussed in Section 5.3. Consumption equivalence is defined as the transfer to all workers in each period of the hours restriction scenario that makes them indifferent on average with the baseline.

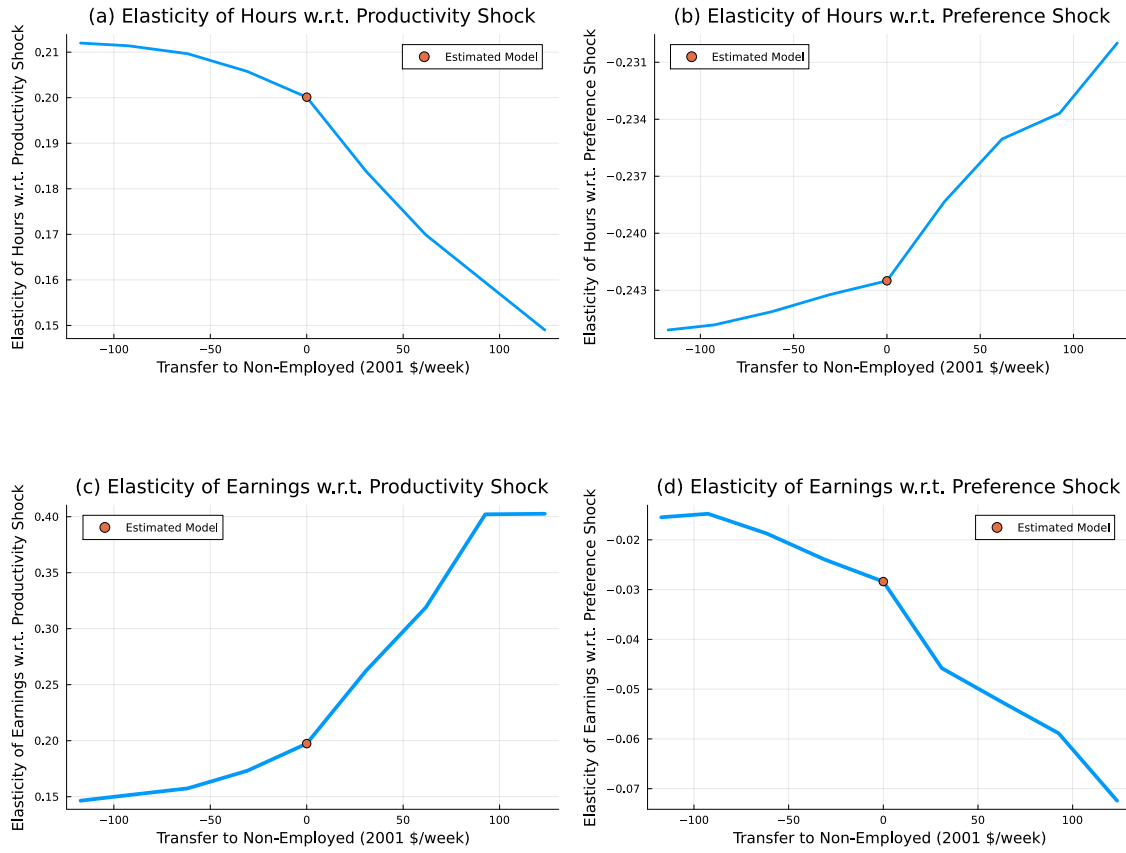
changes in response to changes in government transfers to the non-employed in the estimated model. As government transfers to the non-employed increase, the pass-through of shocks to workers' hours decreases and the pass-through to earnings increases.

6 Conclusion

This paper documents empirically that changes in hours within a job are common, but the elasticity of earnings with respect to hours is larger for hourly workers compared to non-hourly workers. Using data from four consecutive surveys, I show that these patterns cannot easily be explained by classical measurement error. Instead, I find that the heterogeneity in the elasticity of earnings with respect to hours is consistent with a model of implicit contracts constrained by two-sided limited commitment. In an estimated model, firms provide substantial insurance to workers' earnings against shocks to labor productivity and leisure preferences, and hours play a quantitatively important role in amplifying labor productivity shocks to increase total expected output of workers. From the perspective of optimal implicit contracts, restrictions on hours reduce total expected output and welfare for workers. For workers with higher tenure or lower turnover, the benefits of implicit contracting and thus the costs of government regulations on hours are likely greater. Additionally, transfers to the non-employed reduce risk-sharing on the intensive margin in implicit contracts by increasing the extent to which commitment constraints bind.

In the future, this work could be built upon in several dimensions. Empirically, improved data on earnings and hours for workers beyond survey data would provide a more accurate

Figure 3: Changing Transfer to Non-employed and Pass-through of Shocks



Note: This figure shows how the pass-through of shocks to workers earnings and hours changes in response to changes in government transfers to the non-employed.

measurement of their joint dynamics. For earnings, it would be possible to relax the use of survey data from the Synthetic SIPP, a Census Bureau project that matches administrative income data with SIPP questions including hours worked. For hours, collecting and analyzing more accurate information for workers who are not paid by the hour is an important area for future work. The growing use of software such as Microsoft Teams and Slack to coordinate work and schedule meetings for office workers may be fruitful for this purpose. Theoretically, the model could be extended to incorporate savings and coordinated production across workers. However, this coordination results in a non-concave production technology for hours that make solving for the optimal implicit contract theoretically challenging.

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A Data Appendix

A.1 How are non-hourly workers paid?

The SIPP unfortunately only reports whether workers are paid by the hour or not. Non-hourly workers do not report the type of contract that they receive from their employer. However, a similar question in the Panel Survey of Income Dynamics (PSID) gives workers

Table 13: Contract Types in the PSID

	Share of Answers
Salaried	0.400
Salary and Commissions	0.016
Paid by the Hour	0.523
Hourly and Tips	0.009
Hourly and Commissions	0.004
Other	0.047
Observations	5,269

Note: This table shows response to questions regarding payment scheme in the 2019 PSID for the main job heads of households and their spouses who are not self-employed. Observations are weighted using individual cross-section weights.

the option to choose fixed salary, hourly, commissions, and tips. I restrict the PSID sample to heads of households and their spouses in 2019 who are not self-employed. Additionally, I include only heads of households who are linked to an original PSID family. Table 13 shows that hourly and salary contracts alone account for 92.3% of all employment contracts. For the set of workers who choose that they are not paid by the hour, 86.3% report that they are paid a salary alone.

A.2 SIPP Subjective Question about Hours Changes

To understand the factors generating this variation in work hours within a job, I use two sets of subjective questions in the SIPP shown in Tables 14 and 15. First, workers in the SIPP are asked if they worked part-time (1-34 hours) in any weeks (Sunday to Saturday) during the survey. Those who responded affirmatively are further asked to choose a reason for working part-time from a menu of options. For workers who usually worked full-time, this is a reduction in their hours of work. Second, the SIPP asks workers if they were absent from their jobs without pay for any weeks (Sunday to Saturday) during the survey, and if yes, why. For all workers regardless of their usual hours, this represents a reduction

Table 14: Why worked less than 35 hours in a week?

	Share of Answers
<i>Worked any part-time weeks this wave?</i>	
Yes	0.117
<i>If yes, why?</i>	
Could not find full-time job	0.019
Wanted to work part time	0.022
Injury	0.018
Illness	0.090
Chronic Health Condition	0.010
Taking Care of Family	0.035
Full-time work week less than 35 hours	0.026
Slack work or material shortage	0.126
Job sharing arrangement	0.001
On vacation	0.471
In school	0.009
Other	0.173
Sample	Usually Full-time Hours
Observations	486,160

Note:

This table shows hours variation is caused by both demand and supply-side facts. The sample includes individuals usually working full-time, and their answers to if and why they worked part-time for at least one week during the survey wave. Observations are weighted using SIPP weights.

in their working time. Together, the answers to reasons for part-time work and unpaid absences reveal that both demand-side factors (layoffs, business conditions, and slack work) and supply-side factors (illness and family care) are important sources of variations in hours within a job.

Table 15: Why absent from work without pay?

	Share of Answers
<i>Any full week absences without pay this wave?</i>	
Yes	0.046
<i>If yes, why?</i>	
On layoff	0.109
Slack work or business conditions	0.196
Own injury	0.030
Own illness	0.107
Pregnancy/childbirth	0.034
Taking care of children	0.021
On vacation/personal days	0.272
Bad weather	0.024
Labor dispute	0.004
New job to begin within 30 days	0.028
Job-sharing arrangement	0.002
Other	0.175
Sample	All workers
Observations	575,280

Note:

This table shows hours variation is caused by both demand and supply-side facts. The sample includes individuals with a job during wave, and their answers to if and why they were absent from their job without pay. Observations are weighted using SIPP weights.

A.3 Changes in Hours by Subgroups

Table 16: Changes in Hours within a Job by Sex

	Mean $ \Delta h $	Mean $ \Delta \log(h) $	% $ \Delta h \geq 5$	% $ \Delta h \geq 10$	Observations
Female	2.48	0.08	23.1	10.0	375,338
Male	3.12	0.07	29.2	14.6	388,944

Note:

Sample includes individuals employed at same firm in two consecutive surveys. Observations are weighted using SIPP weights.

Table 17: Changes in Hours within a Job by Education Group

	Mean $ \Delta h $	Mean $ \Delta \log(h) $	% $ \Delta h \geq 5$	% $ \Delta h \geq 10$	Observations
1. No High School	3.03	0.09	26.2	13.3	62,636
2. High School	2.59	0.07	23.4	10.8	233,176
3. Some College	2.61	0.07	24.1	11.1	227,691
4. College	2.98	0.08	29.4	13.8	158,239
5. College Plus	3.59	0.09	35.1	17.6	82,540

Note:

Sample includes individuals employed at same firm in two consecutive surveys. Observations are weighted using SIPP weights.

Table 18: Changes in Hours within a Job by Age

	Mean $ \Delta h $	Mean $ \Delta \log(h) $	% $ \Delta h \geq 5$	% $ \Delta h \geq 10$	Observations
Age 25-29	2.99	0.09	28.0	13.0	93,668
Age 30-34	2.96	0.08	27.6	13.2	116,874
Age 35-39	2.88	0.08	26.9	12.7	128,378
Age 40-44	2.80	0.08	26.1	12.4	129,333
Age 45-49	2.74	0.07	25.6	12.0	118,428
Age 50-54	2.68	0.07	25.1	11.8	101,521

Note:

Sample includes individuals employed at same firm in two consecutive surveys. Observations are weighted using SIPP weights.

Table 19: Changes in Hours within a Job by Survey Month

	Mean $ \Delta h $	Mean $ \Delta \log(h) $	% $ \Delta h \geq 5$	% $ \Delta h \geq 10$	Observations
1. January	2.81	0.08	26.3	12.4	68,617
2. February	2.85	0.08	26.5	12.4	68,215
3. March	2.87	0.08	26.6	12.6	69,949
4. April	2.89	0.08	26.8	12.8	69,635
5. May	2.82	0.08	26.4	12.4	64,333
6. June	2.81	0.08	26.3	12.3	66,550
7. July	2.79	0.08	25.9	12.4	64,833
8. August	2.81	0.08	26.2	12.4	65,891
9. September	2.78	0.08	26.0	12.1	58,566
10. October	2.82	0.08	26.5	12.4	58,914
11. November	2.80	0.08	26.1	12.5	54,806
12. December	2.73	0.07	25.9	11.9	53,973

Note:

Sample includes individuals employed at same firm in two consecutive surveys. Observations are weighted using SIPP weights.

Table 20: Changes in Hours within a Job by Survey Year

	Mean $ \Delta h $	Mean $ \Delta \log(h) $	% $ \Delta h \geq 5$	% $ \Delta h \geq 10$	Observations
1990	2.97	0.08	26.4	12.3	29,805
1991	2.82	0.07	25.5	12.0	49,725
1992	2.88	0.08	26.2	12.4	57,611
1993	2.96	0.08	26.8	12.6	61,528
1994	2.85	0.08	26.0	12.3	44,997
1995	2.73	0.07	25.4	11.6	17,830
1996	3.35	0.09	30.7	14.3	35,740
1997	3.07	0.09	28.1	13.4	43,392
1998	2.90	0.08	27.3	12.8	43,667
1999	2.79	0.08	26.4	12.5	36,423
2001	3.23	0.09	30.2	14.3	38,990
2002	2.91	0.08	26.8	13.0	38,797
2003	2.71	0.08	25.8	12.2	25,870
2004	2.92	0.08	27.8	13.1	18,778
2005	2.78	0.08	26.1	12.5	18,869
2006	2.57	0.07	24.7	11.5	18,925
2007	2.44	0.07	23.3	11.0	12,180
2008	3.19	0.09	30.1	14.1	16,701
2009	2.86	0.08	26.8	12.8	38,939
2010	2.58	0.07	23.9	11.6	37,856
2011	2.40	0.07	23.0	10.6	33,680
2012	2.33	0.07	22.3	10.6	30,027
2013	2.11	0.06	20.9	9.1	13,952

Note:

Sample includes individuals employed at same firm in two consecutive surveys.
Observations are weighted using SIPP weights.

Table 21: Changes in Hours within a Job by Industry

	Mean $ \Delta h $	Mean $ \Delta \log(h) $	% $ \Delta h \geq 5$	% $ \Delta h \geq 10$	Observations
Agriculture	5.45	0.13	42.3	26.2	6,242
Army	6.04	0.12	45.1	29.2	3,993
Construction	3.06	0.08	28.5	15.3	36,834
Education	2.71	0.08	24.4	11.5	177,820
Finance	2.40	0.06	24.2	10.8	54,538
Government	1.83	0.05	16.1	8.0	53,148
Information	2.63	0.07	26.8	12.2	36,406
Leisure	3.57	0.11	33.5	14.9	37,210
Manufacturing	2.58	0.06	25.4	11.2	132,735
Mining	5.06	0.10	36.1	22.1	4,633
Other	3.30	0.10	30.0	14.3	24,151
Professional	3.02	0.08	28.5	13.9	54,051
Trade	2.94	0.08	28.3	12.6	100,019
Transportation	3.26	0.08	28.0	14.6	42,502

Note:

Sample includes individuals employed at same firm in two consecutive surveys. Observations are weighted using SIPP weights.

Table 22: Changes in Hours within a Job by Occupation

	Mean $ \Delta h $	Mean $ \Delta \log(h) $	% $ \Delta h \geq 5$	% $ \Delta h \geq 10$	Observations
Admin. Support	1.82	0.06	16.8	6.8	112,096
Army	5.92	0.12	44.0	28.4	3,948
Construction	2.97	0.08	26.3	14.5	31,663
Farming	5.33	0.13	41.4	25.8	4,058
Installation	2.55	0.06	23.5	11.2	31,183
Management	3.28	0.08	33.0	15.6	120,859
Production	2.41	0.06	22.5	9.7	73,975
Professional	2.86	0.08	27.4	12.9	204,065
Sales	3.15	0.09	30.8	14.1	46,402
Service	2.93	0.10	25.5	11.8	90,442
Transportation	3.60	0.09	30.4	16.3	45,591

Note:

Sample includes individuals employed at same firm in two consecutive surveys. Observations are weighted using SIPP weights.

A.4 Payment Schemes and Worker Characteristics Across Time

Why are some workers paid by the hour and other workers paid fixed salaries? As pointed out by Hamermesh ((2002)), there has been surprisingly little attempt to explain these differences in contract types either empirically or theoretically. The few papers that do consider the distinction between hourly and salaried jobs consider it to reflect the tasks of the job (Fama ((1991)), Haber and Goldfarb ((1995))). Conversely, highly skilled, non-routine, and professional jobs will be paid fixed salaries because hours are difficult to monitor and may not have a large impact on production.

However, Hamermesh ((2002)) argues that these theories provide only a partial understanding of the underlying differences between hourly and salaried jobs based on time series in job characteristics and payment schemes.¹¹ Using data Current Population Survey for years 1978 to 1997, he shows that the realized fraction of workers paid by the hour was largely stable and in fact grew slightly as shown in Figure 4. Extending the analysis to 2023, the fraction of workers paid by the hour again remained stable until the Covid-19 pandemic in 2020. This stability of the fraction of workers paid by the hour is surprising given changes in characteristics of US workers. Over the last several decades, US workers have become more educated, more experienced, and work in industries and occupations that typically were more likely to be paid by the hour.¹²

To show this formally, Hamermesh ((2002)) uses data for workers in base year $b = 1978$ to predict the probability that they are paid by the hour based on their observable characteristics in a linear probability model:

$$\text{Hourly}_{ib} = \beta_b X_{ib} + \epsilon_{ib} \quad (40)$$

¹¹Hamermesh ((2002)) uses data from the CPS starting in the year 1978. However, CPS data in IPUMS only includes the variable for whether workers are paid by the hour starting in 1982, so I conduct my analysis using $b = 1982$ as the base year. The overall message of the Hamermesh ((2002)) is largely unaffected by this difference in base year.

¹²Atalay et al. ((2020)) additionally show that job tasks have changed over time within occupations, so the observable changes in industries and occupations understates the true change in tasks done by workers.

Here, Hourly_{it} is an indicator equal to 1 if the worker is paid by the hour, and X_{ib} is a set of observable characteristics in the base year including workers including age, education, race, region, sex, industry, and occupation. Using the estimated regression coefficients $\hat{\beta}_b$ from equation 40, Hamermesh ((2002)) then predicts the fraction of workers that should be paid by the hour in year t as:

$$\overline{\text{Hourly}}_t^* = \hat{\beta}_b \overline{X}_t. \quad (41)$$

Here, \overline{X}_{it} is the average observable characteristics of workers in year t , and $\overline{\text{Hourly}}_t^*$ is the predicted fraction of workers paid by hour in year t .

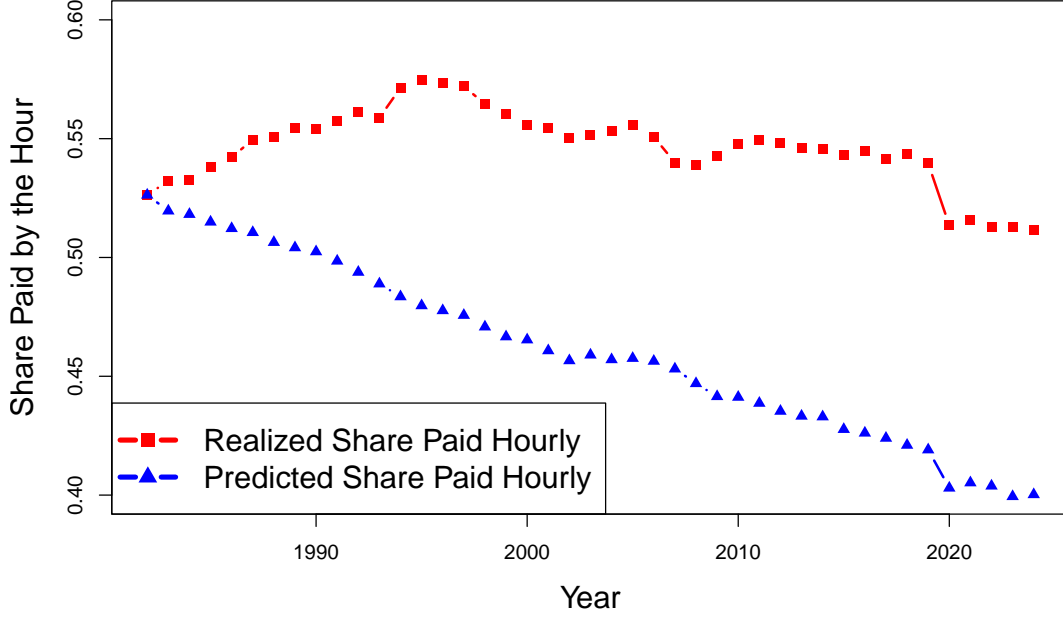
Results from this prediction are shown in Figure 4. Because of the changing characteristics of US workers, there should have been a decline in the number of workers paid by the hour. At the turn of the century, the fraction paid by the hour should have decline by about 7 percentage points, and by 2019 there should have been an additional 3 percentage point decline. However, as shown in the figure the realized fraction of workers paid by the hours has remained roughly constant and even grown slightly. This led Hamermesh ((2002)) to proclaim that there were “12 Million Salaried Workers are Missing” as the title of his paper in 2002 (p. 649). In 2024, that number has grown to over 17 million.

B Model Appendix

B.1 The Optimal Implicit Contract

Following Marcet and Marimon ((2019)), we can rewrite the contracting problem in equation 12 recursively with two additional state variables: Pareto weights on the worker and firm utility. I then show that we must only keep track of only the worker’s earnings in the preceding period. Suppose that W^* is the initial value that the worker receives from the cooperative negotiation and consider how the firm would decide to optimally deliver this

Figure 4: Predicted and Realized Share of Workers Paid by the Hour



Note: This figure replicates and extends Hamermesh ((2002)). The red line with squares presents the realized fraction of workers paid by the hour in the Current Population Survey. The blue line with triangles presents the predicted fraction of workers that are paid by the hour as described in equations 40 and 41. Observations are weighted using longitudinal weights.

value to the worker in an implicit contract.¹³ The firm's problem is:

$$\max_c (1 - d_t) \left(\pi_0 + \mathbf{E} \left[\sum_{t=1}^{\infty} \beta^t (1 - D_t) (1 - d_t) \pi_t \mid \eta^0 \right] \right), \quad (42)$$

subject to

1. Budget constraint at all histories η^t :

$$e_t + \pi_t = y(h_t | x_t). \quad (43)$$

2. Firm's commitment constraint at all histories η^t :

$$(1 - d_t) \left(\pi_t + \mathbf{E} \left[\sum_{k=1}^{\infty} \beta^k (1 - D_{t+k}) (1 - d_{t+k}) \pi_{t+k} \mid \eta^t \right] \right) \geq 0. \quad (44)$$

¹³It would alternatively be equivalent to define J^* to be the value that the firm receives from the cooperative negotiation and consider how the worker would deliver that value to the firm.

3. Worker's commitment constraint at all histories η^t :

$$(1 - d_t) \left(u(e_t, h_t | \phi_t) + \mathbf{E} \left[\sum_{k=1}^{\infty} \beta^k \{ (1 - D_{t+k})(1 - d_{t+k}) u(e_{t+k}, h_{t+k} | \phi_{t+k}) \right. \right. \\ \left. \left. + (1 - D_{t+k}) d_{t+k} \mathcal{B}_{t+k}^W \} \mid \eta^t \right] \right) \geq (1 - d_t) \hat{W}_t. \quad (45)$$

4. Worker receives cooperative negotiation value:

$$(1 - d_0) \left(u(e_0, h_0 | \phi_0) + \mathbf{E} \left[\sum_{t=1}^{\infty} \beta^t \{ (1 - D_t)(1 - d_t) u(e_t, h_t | \phi_t) \right. \right. \\ \left. \left. + (1 - D_t) d_t \mathcal{B}_t^W \} \mid \eta^0 \right] \right) \geq W^*. \quad (46)$$

This problem has the same set of constraints as the cooperative negotiation problem, so the solution to this problem will also be feasible for the cooperative negotiation game. The solution to this problem also will provide the value of the cooperative bargaining game to the worker, so it must also provide the value of the cooperative bargaining game to the firm. To see this, note that the contract that solves the cooperative negotiation game is feasible for this problem, so the firm must at least be better off here than they were in the cooperatively negotiated contract. However, if the firm was strictly better off here, then the cooperatively negotiated contract would not have been optimal. Thus, the contract solving the above problem is equivalent to the contract solving the cooperative negotiation game.

Let $\kappa_t^F(\eta^t)$ and $\kappa_t^W(\eta^t)$ be the Lagrange multipliers on the firm's and worker's commitment constraints at history η^t , respectively. Let μ be the Lagrange multiplier on the constraint that the worker initially receives a value W^* from the contract. Incorporating the constraints

and Lagrange multipliers into the objective function, the firm's problem becomes:

$$\begin{aligned} \max_c \quad & (1 - d_0) \left(\pi_0 + \mu(u(e_0, h_0) - W^*) \right. \\ & + \mathbf{E} \left[\sum_{t=1}^{\infty} \beta^t \left\{ (1 - D_t)(1 - d_t) (K_t^F \pi_t + K_t^W u(e_t, h_t) - \kappa_t^W \hat{W}_t) \right. \right. \\ & \left. \left. + (1 - D_t) d_t K_{t-1}^W \mathcal{B}^W(\eta_t) \right\} \middle| \eta^0 \right] \right), \quad (47) \end{aligned}$$

such that for all histories η^t where the match has not yet been dissolved ($D_t = 0$), the budget constraint is satisfied:

$$e_t + \pi_t = y(x_t, \psi, h_t), \quad (48)$$

and the Pareto weights for the worker and firm update according to:

$$K_t^W = K_{t-1}^W + \kappa_t^W, \quad (49)$$

$$K_t^F = K_{t-1}^F + \kappa_t^F. \quad (50)$$

Here, K_t^F and K_t^W are the promised Pareto weights for the firm and worker in each period. Over time, the Pareto weights increase for a party whenever they have a binding commitment constraint. The term κ_t^P for party $P \in \{F, W\}$ determining this update is the Lagrange multiplier on the party's commitment constraint. If the constraint is not binding, then this will be zero and the Pareto weight will not update. When the constraint binds, this will be the minimum positive number that is needed to satisfy the constraint. The initial condition is that the worker must receive the value from the cooperative negotiation game. Therefore, the worker's Pareto weight in the first period will be equal to the Lagrange multiplier on this constraint ($K_0^W = \mu$). The firm's initial Pareto weight is one from the objective function, so $K_0^F = 1$.

With this recursive reformulation of the contracting problem in hand, we can characterize

the optimal contract as a function of the promised Pareto weights. First, I show how to write the problem recursively with one additional state variable: the relative Pareto weight on the firm $K_t = K_t^F / (K_t^F + K_t^W)$. The firm's recursive problem with two additional state variables is:

$$V(\eta, K^F, K^W) = \max_c K_{new}^F \pi + K_{new}^W u(c, h) + \beta \mathbf{E}[V(\eta', K_{new}^F, K_{new}^W) | \eta] - \kappa^W \hat{W} \quad (51)$$

subject to the same constraints as before. Note that we can define a new value function as

$$\tilde{V}(\eta, K) = V(\eta, K^F, K^W) / (K^F + K^W), \quad (52)$$

where $K = K^F / (K^F + K^W)$ is the relative Pareto weight on the firm. Dividing equation 51 by $K^F + K^W$ and substituting in 52, we arrive at:

$$\tilde{V}(\eta, K) = \max_c (1 + \tilde{\kappa}^F + \tilde{\kappa}^W)(K' \pi + (1 - K')u(c, h) + \beta \mathbf{E}[V(\eta', K') | \eta]) - \tilde{\kappa}^W \hat{W} \quad (53)$$

subject to the same constraints as before. Here, $\tilde{\kappa}^P = \kappa^P / (K^F + K^W + \kappa^F + \kappa^W)$ for $P \in \{F, W\}$, and $K' = (K + \kappa^F) / (1 + \kappa^F + \kappa^W)$.

From the first order conditions of this problem, we can characterize the optimal decisions in the contract:

$$e = \left(\frac{K'}{1 - K'} \right)^{-\frac{1}{\tau}}, \quad (54)$$

and

$$h = \left(\alpha \frac{\psi_i}{\theta_i} \frac{x}{\phi} \frac{K'}{1 - K'} \right)^{\frac{1}{1 - \alpha + \gamma}} \quad (55)$$

Here, we see that decisions depend on both the promised relative Pareto weight and the shocks to productivity in the match. Consumption depends only on the relative Pareto weight. When neither firm nor worker commitment constraint bind, consumption is constant within a match. Consumption will increase in response to a worker's binding commitment

constraint, while the opposite is true when the firm's constraint binds. Hours depend both on the Pareto weight and the productivity shock. A perfect correlation exists between hours and productivity when neither constraint binds. Binding commitment constraints for the worker decrease hours, and binding commitment constraints for firms increase hours. The optimal contract decision rules highlight why productivity shocks and two-sided limited commitment can generate hours variation in the data that is not proportional to earnings variation.

From here, we can prove Proposition 1. Equation 54 shows that there is a one-to-one mapping between the relative Pareto weights K' and the worker's earnings e . For each state $\eta = \{\phi, x, \hat{x}\}$, the worker has an outside option value of \hat{W} . There exists a relative Pareto weight K at which the worker's earnings and hours are set such that she is indifferent between staying in the contract and going to her outside option. This maps to the minimum earnings $e_{\min}(\eta)$ that the worker must be paid. Similarly, the firm's outside option value in each period is to receive total expected profits of zero. There exists a relative Pareto weight K at which point the firm receives total expected value from staying in the contract of zero. This maps to the maximum earnings that the contract is willing to pay the worker.

Because the outside option for the worker \hat{x} is observed before decisions are made, the contract will only dissolve if there is no Pareto weight K where the firm and worker's commitment constraints are satisfied simultaneously. This will be the case when the relative Pareto weight K that makes the worker indifferent between staying in the match is smaller than the relative Pareto weight that makes the firm indifferent between staying in the match. This would imply that the minimum earnings that the worker needs to receive is larger than the maximum earnings that firm is willing to pay. In cases where the match does not dissolve, the relative Pareto weight will adjust by as little as possible in order to satisfy the binding commitment constraint. In the case where the worker's commitment constraint binds, this means that the worker will receive the minimum earnings level. In cases where the firm's commitment constraint binds, this means that the worker will receive the maximum earnings level. When commitment constraints do not bind for either party, then the relative Pareto

weight K will not update, so the earnings for the worker today will be the same as earnings for the worker in the previous period. When the match does not dissolve, hours are also set according to equation 55.

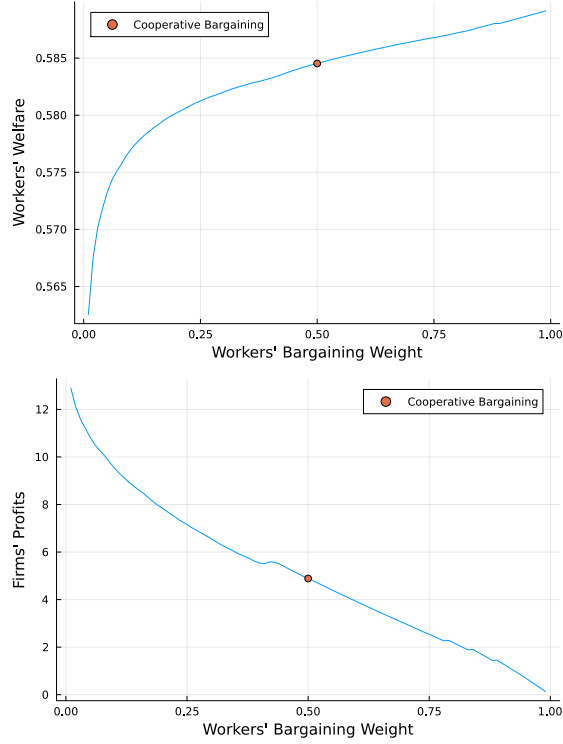
For the case where there is full commitment in Proposition 2, decisions in the optimal contract can be solved for similarly except there is no commitment constraints 44 and 45. The contract problem is only constrained by the budget constraint in equations 43 and that the worker receives the cooperatively negotiated value in equation 46. Thus, the Lagrange multipliers κ_t^F and κ_t^W will be zero in every period. The relative Pareto weight throughout all periods of the match where the contract does not dissolve would be $K = 1/(1 + \mu)$, where μ is the Lagrange multiplier that the worker receives the cooperatively negotiated value in equation 46. Thus, earnings will be constant through the match from equation 54 and hours will be set optimally as in 55.

B.2 Varying the Worker's Bargaining Weight

In the model, the firm and workers' bargaining weight are assumed to be the same as in a cooperative bargaining game (Nash ((1953))). The resulting contract is bilaterally efficient given the outside offers that the worker can negotiate when they meet other firms. However, this equal bargaining weight for the worker may maximize their welfare, and the worker may not the worker may actually want to have a lower bargaining weight. A lower bargaining weight on the worker would reduce the share of the maximum value that they can negotiate with their current firm. However, it reduces the extent to which the worker and firm commitment constraints will bind, which will increase the maximum value that the firm is willing to offer the worker. To understand the extent to which the worker would like to vary their bargaining weight, I solve the model at the estimated parameters for a range of bargaining weights and calculate total worker welfare. Results are shown in Figure 5.

At the estimated parameters, worker welfare is always increasing in the bargaining weight, meaning that they would not want to take on a lower bargaining weight in order to get more

Figure 5: Varying Workers' Bargaining Weight



insurance from firms in long-term employment contracts.

C Estimation Appendix

C.1 Identification in a Simpler Model

In order to provide some intuition for the identification of the contracting model, I derive point identification in a model where workers set their own hours and are paid according to what they produce. Here, it is possible to identify the processes governing the dynamics of earnings and hours using four periods of data.

Consider a large number of workers indexed by i whose earnings e_{it} and hours h_{it} are observed over four periods $t, t+1, t+2, t+3$. The data set is then $\{(e_{it}, h_{it})_{s=t}^{t+3}\}_{i=1}^{N_i}$. Workers'

preferences for consumption and hours are given by:

$$u_i(c_{it}, h_{it} | \phi_{it}) = \log(c_{it}) - \theta_i \frac{h_{it}^{1+\gamma}}{1+\gamma}, \quad (56)$$

and their production is:

$$y_{it} = \psi_i x_{it} h_{it}^\alpha. \quad (57)$$

Here, θ_i and ψ_i are permanent shocks (types) for the workers' preferences and production that are jointly log-normal:

$$\begin{bmatrix} \log \theta_i \\ \log \psi_i \end{bmatrix} \sim \mathcal{N} \left(\begin{bmatrix} \mu_\theta \\ \mu_\psi \end{bmatrix}, \begin{bmatrix} \sigma_\theta^2 & \sigma_{\theta\psi}^2 \\ \sigma_{\theta\psi}^2 & \sigma_\psi^2 \end{bmatrix} \right). \quad (58)$$

The preference shock ϕ_{it} and productivity shock x_{it} processes follow an AR(1) process with a normally distributed innovation term:

$$\phi_{it+1} = \rho_\phi \phi_{it} + \epsilon_{it}^\phi \quad \epsilon_{it}^\phi \sim \mathcal{N}(0, \sigma_\phi^2) \quad (59)$$

$$x_{it+1} = \rho_x x_{it} + \epsilon_{it}^x \quad \epsilon_{it}^x \sim \mathcal{N}(0, \sigma_x^2) \quad (60)$$

These shocks are independent of each other and independent of the permanent types. Additionally, I assume that these shocks have reached a stationary distribution across workers, so their expectations and variances are:

$$\mathbf{E}[\phi_{it}] = 0, \quad (61)$$

$$\mathbf{E}[x_{it}] = 0, \quad (62)$$

$$\text{var}(\phi_{it}) = \frac{\sigma_\phi^2}{1 - \rho_\phi^2}, \quad (63)$$

$$\text{var}(x_{it}) = \frac{\sigma_x^2}{1 - \rho_x^2}, \quad (64)$$

Suppose workers set their own hours, are paid according to what they produce ($e_{it} = y_{it}$), and consume their earnings ($c_{it} = e_{it}$). The first order condition for the optimal choice of hours yields the following equation for hours:

$$\log(h_{it}) = \frac{1}{1 + \gamma} \log \theta_i + \frac{1}{1 + \gamma} \log \phi_{it} + \frac{1}{1 + \gamma} \log \alpha. \quad (65)$$

The budget constraint yields the following equation for earnings:

$$\log(e_{it}) = \log \psi_i + \log x_{it} + \alpha \log h_{it}. \quad (66)$$

Moreover, earnings \tilde{e}_{it} and hours \tilde{h}_{it} as observed by the econometrician contain classical measurement error that is serially uncorrelated:

$$\log \tilde{e}_{it} = \log e_{it} + m_{it}^e \quad m_{it}^e \sim \mathcal{N}(0, \sigma_{me}^2), \quad (67)$$

$$\log \tilde{h}_{it} = \log(h_{it}) + m_{it}^h \quad m_{it}^h \sim \mathcal{N}(0, \sigma_{mh}^2). \quad (68)$$

I assume that γ is known, so there are twelve parameters to be estimated.

$$\{\mu_\psi, \mu_\theta, \sigma_\psi^2, \sigma_\theta^2, \sigma_{\psi\theta}^2, \rho_x, \sigma_x^2, \rho_\phi, \sigma_\phi^2, \sigma_{me}^2, \sigma_{mh}^2, \alpha\}. \quad (69)$$

These parameters can be estimated using a method of moment estimator derive from the four observations of earnings and hours.

First, consider the auto-covariance of hours over the four periods:

$$\text{cov}(\log \tilde{h}_{it}, \log \tilde{h}_{it+1}) = \frac{1}{(1 + \gamma)^2} \sigma_\theta^2 + \frac{\rho_\phi}{(1 + \gamma)^2} \frac{\sigma_\phi^2}{1 - \rho_\phi^2} \quad (70)$$

$$\text{cov}(\log \tilde{h}_{it}, \log \tilde{h}_{it+2}) = \frac{1}{(1+\gamma)^2} \sigma_\theta^2 + \frac{\rho_\phi^2}{(1+\gamma)^2} \frac{\sigma_\phi^2}{1-\rho_\phi^2} \quad (71)$$

$$\text{cov}(\log \tilde{h}_{it}, \log \tilde{h}_{it+3}) = \frac{1}{(1+\gamma)^2} \sigma_\theta^2 + \frac{\rho_\phi^3}{(1+\gamma)^2} \frac{\sigma_\phi^2}{1-\rho_\phi^2} \quad (72)$$

Using these three equations, we can sequentially solve for ρ_ϕ , σ_θ^2 , and σ_ϕ^2 as:

$$\rho_\phi = \frac{\text{cov}(\log \tilde{h}_{it}, \log \tilde{h}_{it+3}) - \text{cov}(\log \tilde{h}_{it}, \log \tilde{h}_{it+2})}{\text{cov}(\log \tilde{h}_{it}, \log \tilde{h}_{it+2}) - \text{cov}(\log \tilde{h}_{it}, \log \tilde{h}_{it+1})}, \quad (73)$$

$$\sigma_\theta^2 = \frac{\text{cov}(\log \tilde{h}_{it}, \log \tilde{h}_{it+2}) - \rho_\phi \text{cov}(\log \tilde{h}_{it}, \log \tilde{h}_{it+1})}{1 - \rho_\phi}, \quad (74)$$

$$\sigma_\phi^2 = \frac{1 - \rho_\phi^2}{\rho_\phi} \left((1+\gamma)^2 \text{cov}(\log \tilde{h}_{it}, \log \tilde{h}_{it+1}) - \sigma_\theta^2 \right). \quad (75)$$

With these values in hand, we can use the equation for the variance of observed hours:

$$\text{var}(\log \tilde{h}_{it}) = \frac{1}{(1+\gamma)^2} \sigma_\theta^2 + \frac{1}{(1+\gamma)^2} \frac{\sigma_\phi^2}{1-\rho_\phi^2} + \sigma_{mh}^2 \quad (76)$$

to solve for the variance of the measurement error in hours as:

$$\sigma_{mh}^2 = \text{var}(\log \tilde{h}_{it}) - \frac{1}{(1+\gamma)^2} \sigma_\theta^2 - \frac{1}{(1+\gamma)^2} \frac{\sigma_\phi^2}{1-\rho_\phi^2}. \quad (77)$$

Next, the covariance between changes in earnings and hours can be used to estimate the returns to hours in production.

$$\text{cov}(\Delta \log \tilde{e}_{it}, \Delta \log \tilde{h}_{it}) = \alpha \text{var}(\Delta \log h_{it}). \quad (78)$$

This implies:

$$\alpha = \frac{\text{cov}(\Delta \log \tilde{e}_{it}, \Delta \log \tilde{h}_{it})}{\text{var}(\Delta \log h_{it}) - 2\sigma_{mh}^2}. \quad (79)$$

Then, we can solve for the average leisure preference level μ_θ using the average hours in the

economy:

$$\mathbf{E}[\log \tilde{h}_{it}] = \frac{1}{1 + \gamma}(\mu_\theta + \log(\alpha)). \quad (80)$$

Before pinning down the random processes underlying labor productivity, we first need to pin down the covariance of the permanent leisure preference type θ_i and permanent labor productivity type ψ_i . This can be accomplished using the covariance of observed earnings and hours:

$$\text{cov}(\log \tilde{e}_{it}, \log \tilde{h}_{it}) = \frac{1}{1 + \gamma} \sigma_{\psi\theta}^2 + \alpha \text{var}(\log h_{it}), \quad (81)$$

This yields:

$$\sigma_{\psi\theta}^2 = (1 + \gamma)(\text{cov}(\log \tilde{e}_{it}, \log \tilde{h}_{it}) - \alpha \text{var}(\log h_{it})). \quad (82)$$

Now, consider the auto-covariance structure of earnings:

$$\text{cov}(\log \tilde{e}_{it}, \log \tilde{e}_{it+1}) = \sigma_\psi^2 + \rho_x \frac{\sigma_x^2}{1 - \rho_x} + \alpha^2 \text{cov}(\log \tilde{h}_{it}, \log \tilde{h}_{it+1}) + \alpha \sigma_{\psi\theta}^2 \quad (83)$$

$$\text{cov}(\log \tilde{e}_{it}, \log \tilde{e}_{it+2}) = \sigma_\psi^2 + \rho_x^2 \frac{\sigma_x^2}{1 - \rho_x} + \alpha^2 \text{cov}(\log \tilde{h}_{it}, \log \tilde{h}_{it+2}) + \alpha \sigma_{\psi\theta}^2 \quad (84)$$

$$\text{cov}(\log \tilde{e}_{it}, \log \tilde{e}_{it+3}) = \sigma_\psi^2 + \rho_x^3 \frac{\sigma_x^2}{1 - \rho_x} + \alpha^2 \text{cov}(\log \tilde{h}_{it}, \log \tilde{h}_{it+3}) + \alpha \sigma_{\psi\theta}^2 \quad (85)$$

Using these three equations, we can sequentially solve for ρ_x , σ_ψ^2 , and σ_x^2 as:

$$\rho_x = \frac{\frac{\text{cov}(\log \tilde{e}_{it}, \log \tilde{e}_{it+3})}{\text{cov}(\log \tilde{e}_{it}, \log \tilde{e}_{it+2})} - \alpha^2 \frac{\text{cov}(\log \tilde{h}_{it}, \log \tilde{h}_{it+3}) - \text{cov}(\log \tilde{h}_{it}, \log \tilde{h}_{it+2})}{\text{cov}(\log \tilde{e}_{it}, \log \tilde{e}_{it+2})}}{1 - \frac{\text{cov}(\log \tilde{e}_{it}, \log \tilde{e}_{it+1})}{\text{cov}(\log \tilde{e}_{it}, \log \tilde{e}_{it+2})} - \alpha^2 \frac{\text{cov}(\log \tilde{h}_{it}, \log \tilde{h}_{it+2}) - \text{cov}(\log \tilde{h}_{it}, \log \tilde{h}_{it+1})}{\text{cov}(\log \tilde{e}_{it}, \log \tilde{e}_{it+2})}}, \quad (86)$$

$$\sigma_\psi^2 = \frac{1}{1 - \rho_x} \left(\text{cov}(\log \tilde{e}_{it}, \log \tilde{e}_{it+2}) - \alpha^2 \text{cov}(\log \tilde{h}_{it}, \log \tilde{h}_{it+2}) - \alpha \sigma_{\psi\theta}^2 - \rho_x (\text{cov}(\log \tilde{e}_{it}, \log \tilde{e}_{it+1}) - \alpha^2 \text{cov}(\log \tilde{h}_{it}, \log \tilde{h}_{it+1}) - \alpha \sigma_{\psi\theta}^2) \right), \quad (87)$$

$$\sigma_x^2 = \frac{1 - \rho_x^2}{\rho_x} \left(\text{cov}(\log \tilde{e}_{it}, \log \tilde{e}_{it+1}) - \alpha^2 \text{cov}(\log \tilde{h}_{it}, \log \tilde{h}_{it+2}) - \alpha \sigma_{\psi\theta}^2 - \sigma_\psi^2 \right). \quad (88)$$

With these values in hand, we can use the equation for the variance of observed earnings:

$$\text{var}(\log \tilde{e}_{it}) = \sigma_\psi^2 + \frac{\sigma_x^2}{1 - \rho_x^2} + \alpha^2 (\text{var}(\log \tilde{h}_{it}) - \sigma_{mh}^2) + \alpha \sigma_{\psi\theta}^2 + \sigma_{me}^2 \quad (89)$$

to solve for the variance of the measurement error in earnings as:

$$\sigma_{me}^2 = \text{var}(\log \tilde{e}_{it}) - \sigma_\psi^2 - \frac{\sigma_x^2}{1 - \rho_x^2} - \alpha^2 (\text{var}(\log \tilde{h}_{it}) - \sigma_{mh}^2) - \alpha \sigma_{\psi\theta}^2. \quad (90)$$

Finally, the average labor productivity type μ_ψ can be solved from average earnings:

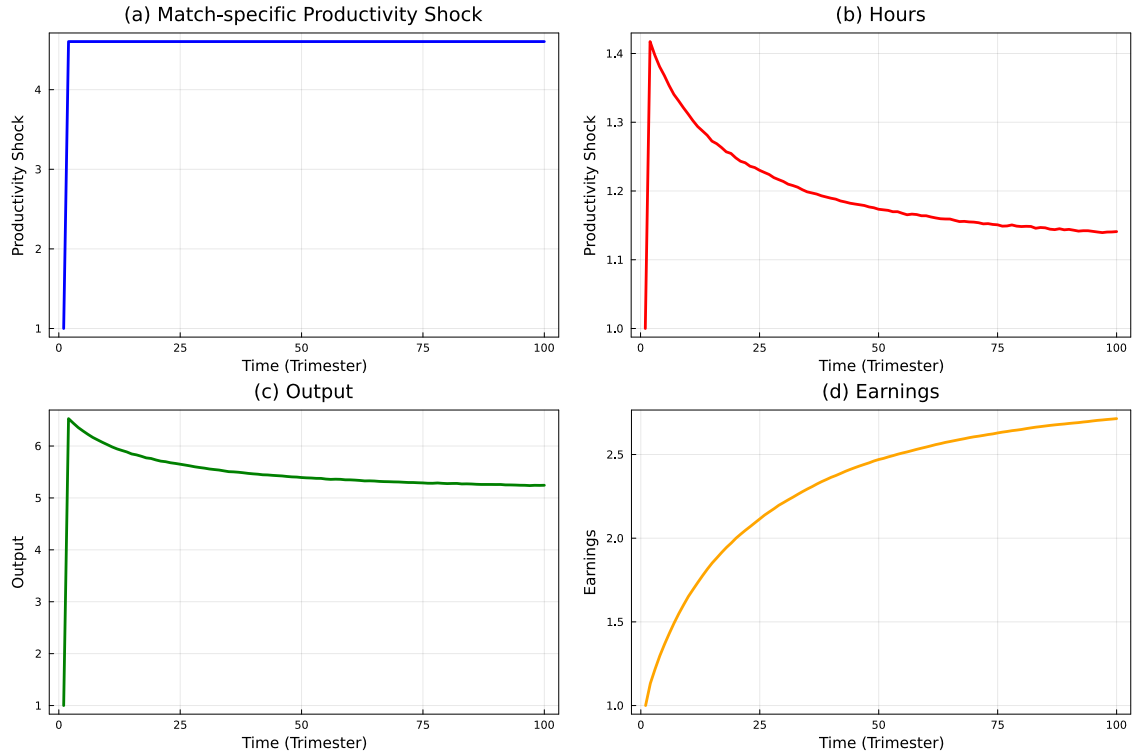
$$\mathbf{E}[\log \tilde{e}_{it}] = \mu_\psi + \alpha \log \tilde{h}_{it}. \quad (91)$$

In the model estimated in the paper, earnings and hours will further be affected by the risk-sharing between firms and workers within the implicit contract. However, by estimating the contact rates for meeting firms when non-employed λ_n and employed λ_e as well as the exogenous job destruction rate δ by matching the empirical employment transition rates, we can hopefully infer how much risk-sharing firms and workers can do within the contract, and then back out the random processes underlying productivity and preferences.

D Analysis Appendix

In addition to the regression coefficients shown in Table 10, I also show how a positive shock to productivity and a negative shock to preferences pass through to outcomes over time in Figures 6 and 7. Initially, the shocks lead to an increase in hours and output. However, worker's earnings remain relatively unchanged as a result of the risk-sharing in the implicit contract. Instead, the additional output is passed on to the firms' profits. Over time, however, the worker receives better outside offers from other firms in the economy, and their

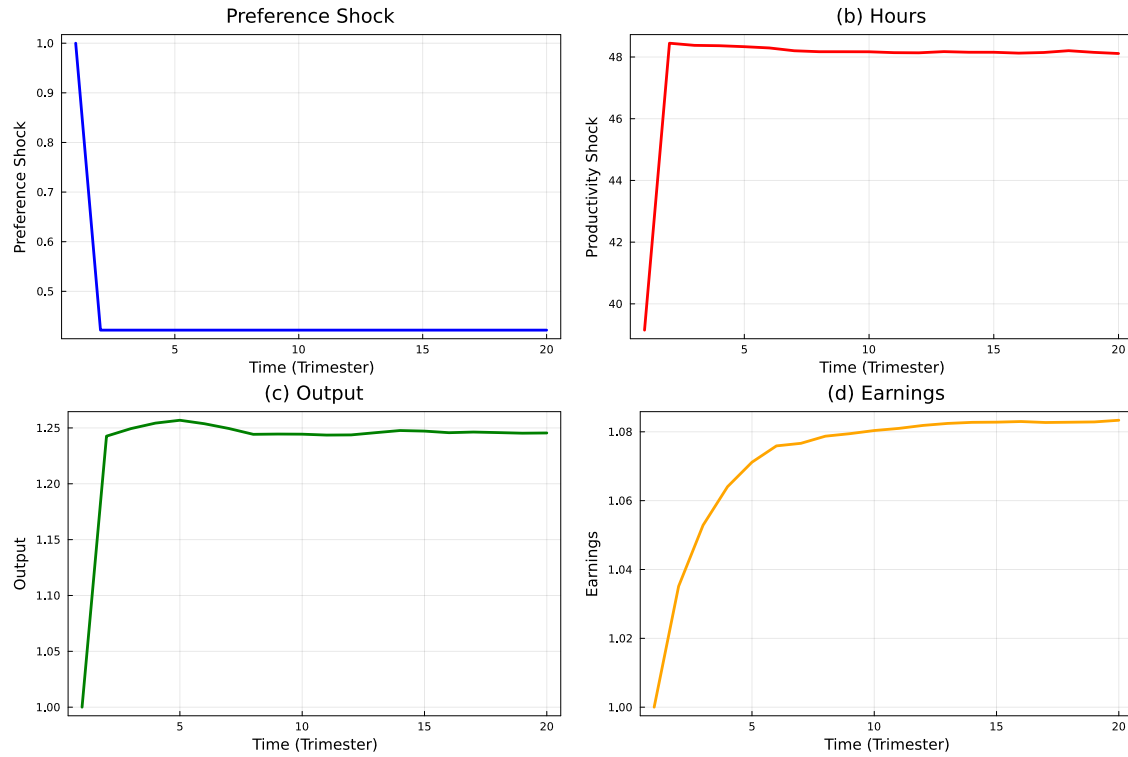
Figure 6: Average Response to Positive Productivity Shock



Note: This figure shows how hours, output, and earnings respond to a positive productivity shock in the estimated model. The job-specific productivity exogenously shifts from the median level of 1 to the highest level of 4.604. The path of hours, output, and earnings is shown for the next 100 periods. Transitions to non-employment are ruled out.

participation constraint binds. This leads to decreases in the workers' hours and output, but increases in workers' earnings.

Figure 7: Average Response to Negative Preference Shock



Note: This figure shows how hours, output, and earnings respond to a negative leisure preference shock in the estimated model. The preference shock exogenously shifts from the median level of 1 to the lowest level of 0.422. The path of hours, output, and earnings is shown for the next 100 periods. Transitions to non-employment are ruled out.